

$$\psi^{(i)} = A_i^+ e^{ik_i x} + A_i^- e^{-ik_i x}$$

$$|\psi_i\rangle = \begin{pmatrix} A_i^+ \\ A_i^- \end{pmatrix}$$

$$\begin{pmatrix} A_i^+(d) \\ A_i^-(d) \end{pmatrix} = \begin{pmatrix} e^{ik_i d} & 0 \\ 0 & e^{-ik_i d} \end{pmatrix} \begin{pmatrix} A_i^+(0) \\ A_i^-(0) \end{pmatrix}$$

$$\begin{aligned} V_1 &= V_2 \\ \frac{k_1}{m_1} &= \frac{k_2}{m_2} \end{aligned}$$

$$\frac{\psi_1'}{m_1} = \frac{\psi_2'}{m_2}$$

$$\begin{pmatrix} A_2^+ \\ A_2^- \end{pmatrix} = T_{21}(E) \begin{pmatrix} A_1^+ \\ A_1^- \end{pmatrix}$$

$$T_{21}(E) = F_2^{-1} F_1$$

$$\psi, \quad \frac{\psi}{m} \propto \frac{k}{m}$$

$$k_{1,2} = \sqrt{2m_{1,2}(E - V_{1,2})}$$

$$\begin{pmatrix} \psi_i \\ \frac{\psi_i}{m} \end{pmatrix} \propto \begin{pmatrix} 1 & 1 \\ \frac{k_i}{m} & -\frac{k_i}{m} \end{pmatrix} \begin{pmatrix} A_i^+ \\ A_i^- \end{pmatrix}$$

$$F_i \equiv \begin{pmatrix} 1 & 1 \\ \frac{k_i}{m_i} & -\frac{k_i}{m_i} \end{pmatrix}$$

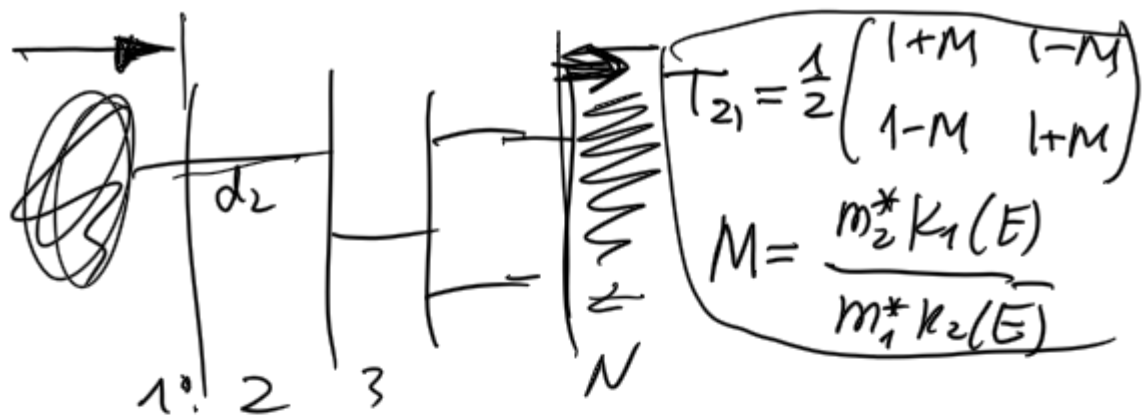
$$x=0 \quad \psi_i = A_i^+ + A_i^-$$

$$\frac{\psi_i'}{m} \propto \frac{k_i}{m_i} A_i^+ - \frac{k_i}{m_i} A_i^-$$

$$\begin{pmatrix} A_2^+ \\ A_2^- \end{pmatrix} = F_2^{-1} F_1 \begin{pmatrix} A_1^+ \\ A_1^- \end{pmatrix}$$

$$F_2^{-1} \begin{pmatrix} \psi_i \\ \frac{\psi_i}{m} \end{pmatrix} \propto F_i \begin{pmatrix} A_i^+ \\ A_i^- \end{pmatrix}$$

$$F_2^{-1} \begin{pmatrix} A_2^+ \\ A_2^- \end{pmatrix} = \begin{pmatrix} \psi_2 \\ \frac{\psi_2}{m_2} \end{pmatrix} = \begin{pmatrix} \psi_1 \\ \frac{\psi_1}{m_1} \end{pmatrix} = F_1 \begin{pmatrix} A_1^+ \\ A_1^- \end{pmatrix}$$



$$T_{N,N-1} \begin{pmatrix} T_{3,d_3} & T_{32} \end{pmatrix} \begin{pmatrix} T_{2,d_2} & T_{21} \end{pmatrix} \begin{pmatrix} A_1^+ \\ A_1^- \end{pmatrix} = \begin{pmatrix} A_N^+ \\ A_N^- \end{pmatrix}$$

$$\begin{pmatrix} A_N^+ \\ A_N^- \end{pmatrix} = T_{\text{tot}} \begin{pmatrix} A_1^+ \\ A_1^- \end{pmatrix} \begin{pmatrix} b \\ 0 \end{pmatrix} = T_{\text{tot}} \begin{pmatrix} 1 \\ r \end{pmatrix}$$

$$\begin{pmatrix} A_N^+ \\ A_N^- \end{pmatrix} \begin{pmatrix} b \\ 0 \end{pmatrix} \quad \begin{pmatrix} A_1^+ \\ A_1^- \end{pmatrix} \quad \begin{pmatrix} |A_1^+|^2 = 1 \\ |A_1^-|^2 = R \\ |t|^2 = T \\ |r|^2 = R \end{pmatrix}$$

$$\begin{pmatrix} A_N^+ \\ A_N^- \end{pmatrix} \neq 0 \quad \begin{pmatrix} A_1^+ \\ A_1^- \end{pmatrix} \quad \begin{pmatrix} |A_N^+|^2 = T \end{pmatrix}$$

$$\begin{pmatrix} t \\ 0 \end{pmatrix} = \begin{pmatrix} T_{11}(\epsilon) & T_{12}(\epsilon) \\ T_{21}(\epsilon) & T_{22}(\epsilon) \end{pmatrix} \begin{pmatrix} 1 \\ r \end{pmatrix}$$

$$0 = t_{21} + T_{22} \cdot r$$

$$r = - \frac{T_{21}}{T_{22}}$$

$$t = T_{11} + T_{12} \left(- \frac{T_{21}}{T_{22}} \right)$$

$$\boxed{t = \frac{\det T}{T_{22}}}$$



$$\psi(x+d) = e^{ikd} \psi(x)$$

$$\hat{T}_d \begin{pmatrix} A^+ \\ A^- \end{pmatrix} = e^{ikd} \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} A^+ \\ A^- \end{pmatrix}$$

$$R(E) \parallel |\psi\rangle$$

$$\left(\hat{T}_d - e^{ikd} \hat{1} \right) |\psi\rangle = 0$$

$$T_d(E, k)$$

$$R'(E) = \frac{R(E+\delta) - R(E)}{\delta}$$

$$R(E_0) |\psi_0\rangle = 0$$

$$|\psi\rangle \neq \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

$$E_0 = E + \Delta \quad \Delta \text{ near } 0$$

$$R(E_0) |0\rangle = R(E) |0\rangle + R'(0)$$

$$E_0 = E + \Delta$$



$$0 = R(E_0)|0\rangle = R(E)|0\rangle + R'(E)\Delta|0\rangle$$

$$[R']^{-1} | -R(E)|0\rangle = R'(E) \cdot \Delta |0\rangle$$

$$\boxed{A|0\rangle = \Delta|0\rangle}$$

$$A = -[R']^{-1} \cdot R$$

$$\Delta = \begin{pmatrix} \Delta_1 \\ \Delta_2 \end{pmatrix}$$

$$\tilde{\Delta} = \min_{\text{abs}}(\Delta_{1,2})$$

$$\tilde{\Delta}_1, \tilde{\Delta}_2, \dots, \tilde{\Delta}_N \xrightarrow{(\text{abs})} 0$$