

# Quiz- QPE, Order finding, Shor Results for SevdanurGenc

❗ Correct answers are hidden.

Score for this attempt: **14.5** out of 20

Submitted Jun 15 at 8:35pm

This attempt took 20 minutes.

## Question 1

2 / 2 pts

**[D03-02]** Let  $U$  be the quantum operator such that  $U|\psi\rangle = e^{2\pi i\phi}|\psi\rangle$ . Let  $k > 0$  be an integer. We apply  $CU^k$  operator to the state. What is the resulting state.

- ☐  $\frac{1}{\sqrt{2}}(e^{2\pi i\phi}|0\rangle|\psi\rangle + e^{2\pi i\phi}|1\rangle|\psi\rangle)$
- ☐  $\frac{1}{\sqrt{2}}(|0\rangle|\psi\rangle - e^{2\pi ik\phi}|1\rangle|\psi\rangle)$
- ☐  $\frac{1}{\sqrt{2}}(e^{2\pi ik\phi}|0\rangle|\psi\rangle + |1\rangle|\psi\rangle)$
- ☒  $\frac{1}{\sqrt{2}}(|0\rangle|\psi\rangle + e^{2\pi ik\phi}|1\rangle|\psi\rangle)$

## Question 2

2 / 2 pts

**[D03-03]** Select the steps of the QPE algorithm.

- ☒ Apply inverse QFT to the first register.
- ☐ Initialize first register as the eigenvector of the operator  $U$ .
- ☐ Apply X gates to the all qubits in the first register.
- ☒ Apply Hadamard gate to the first register.
- ☒ Apply  $CU^k$  operator where the target is the second register.

**Question 3**

2 / 2 pts

**[D03-07]** Write the code to define i'th power of the operator CU and store inside the variable CUi.

```
phase = 2/7  
CU = CZPowGate(exponent=phase*2)  
CUi = ...
```

Incorrect

**Question 4**

0 / 2 pts

**[D03-06]** If  $\phi = 3/16$  and the first register contains 3 qubits, which states do you expect to observe more frequently?

☐  $|011\rangle$  and  $|100\rangle$ ☐  $|001\rangle$  and  $|010\rangle$ ☐  $|011\rangle$ ☒  $|011\rangle$  and  $|111\rangle$ **Question 5**

2 / 2 pts

**[D04-01]** Let  $x=4$  and  $N=81$ . What is  $r$  ? (You can compute in Python)

Partial

## Question 6

0.5 / 2 pts

[D04-02] Select the true statements.

☐ When  $s$  and  $r$  are not relatively prime, the algorithm needs to be repated.



We need continued fractions algorithm to extract  $r$  out of the estimate for  $s/r$ .



If  $U_x$  is the operator which maps  $U_x|y\rangle \rightarrow |xy \bmod N\rangle$  where  $x < N$  are relatively prime, its eigenvalues are of the form  $e^{\frac{2\pi is}{r}}$ .



The second register is initialized as  $|1\rangle$  in the order finding algorithm.



At the end of the order finding algorithm, we measure  $r$  in the first register.



Modular exponentiation is the name of the procedure in which the powers of the operator  $CU$  are computed.



Order finding has no use in practice since we don't know how to prepare the eigenvector.

## Question 7

2 / 2 pts

[D04-03] Given the continued fraction expression  $[1,4,2,1]$  write one of the convergents. (Do not leave any space e.g. write  $3/2$  instead of  $3 / 2$ )

## Question 8

2 / 2 pts

[D05-01] Select the true statements.



Shor's algorithm provides quadratic speedup compared to the best known classical algorithm.



If  $r$  is not even, then one should pick a new  $x$  and repeat the algorithm.



It is proven that no classical algorithm solves the factorization problem in polynomial time.



The main advantage of Shor's algorithm is the ability to compute  $r$  efficiently.

### Question 9

2 / 2 pts

**[D05-02]** If the quantum state before applying the inverse QFT is the the following state,

$$\frac{1}{\sqrt{2^9}} (|0\rangle|1\rangle + |1\rangle|3\rangle + |2\rangle|9\rangle + |3\rangle|7\rangle + |4\rangle|1\rangle + |5\rangle|3\rangle + |6\rangle|9\rangle + \dots + |2$$

what is  $r$  ?

4

Incorrect

### Question 10

0 / 2 pts

**[D06-01]** If at the end of the Shor's algorithm, the probability of observing state  $|k\rangle$  is given by  $\left| \frac{1}{\sqrt{85 \cdot 512}} \sum_{x=0}^{84} e^{-\frac{2\pi i(6x+2)k}{512}} \right|^2$ , write down a state (except 0 and 256) which is likely to be observed with high probability. (Write it as a decimal number, e.g. 34)

1/2

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