

# Quiz on Section 1 Results for SevdanurGenc

❗ Correct answers are hidden.

Score for this attempt: **11.5** out of 12

Submitted Jun 17 at 11:16pm

This attempt took 10 minutes.

## Question 1

1 / 1 pts

Given that  $x_1 + x_2 + x_3 + x_4 + x_5 \leq 5$  should hold, select the penalty term corresponding to this constraint.

☐

$(x_1 + x_2 + x_3 + x_4 + x_5 + 5)^2 = 0$  where  $s$  is a non-negative slack variable.

☒

$(x_1 + x_2 + x_3 + x_4 + x_5 + s - 5)^2 = 0$  where  $s$  is a non-negative slack variable.

☐

$(x_1 + x_2 + x_3 + x_4 + x_5 - 5)^2$

☐

$(x_1 + x_2 + x_3 + x_4 + x_5 - s - 5)^2 = 0$  where  $s$  is a non-negative slack variable.

## Question 2

1 / 1 pts

Select the penalty terms that correspond to the constraint  $x = y$ .

☒

$(x - y)^2$

☐

$xy - x - y$

☒

$x + y - 2xy$

☐

$xy$

**Question 3**

1 / 1 pts

What is the objective value we can obtain for a feasible solution of the graph coloring problem?

- ☐ 10
- ☒ 0
- ☐ -5
- ☐ Not enough information

**Question 4**

1 / 1 pts

Suppose that  $Q$  is the QUBO matrix representing a graph coloring problem with two nodes and two colors.

$$Q = \begin{pmatrix} -1 & 2 & 1 & 0 & 1 & 0 \\ 0 & -1 & 0 & 1 & 0 & 1 \\ 0 & 0 & -1 & 2 & 1 & 0 \\ 0 & 0 & 0 & -1 & 0 & 1 \\ 0 & 0 & 0 & 0 & -1 & 2 \\ 0 & 0 & 0 & 0 & 0 & -1 \end{pmatrix}$$

Find out if the vector  $x = (0, 1, 1, 1, 0, 1)$  provides a feasible solution to the graph coloring problem or not.

- ☒ The vector provides an infeasible solution.
- ☐ The vector provides a feasible solution.

**Question 5**

1 / 1 pts

Greedy approach can always find an optimal solution to a graph colouring problem.

☐ True☒ False**Question 6**

1 / 1 pts

A path through a graph that visits each vertex exactly once is called a Hamiltonian path.

☒ True☐ False**Question 7**

1 / 1 pts

Variables in a QUBO problem must always be

☐ Integer☐ Continuous☒ Binary

## Question 8

1 / 1 pts

Find the right QUBO matrix representation for the following objective function

$$f(x_1, x_2, x_3) = -10x_1 - 2x_2 + 5x_3 + 3x_1x_2 + x_1x_3 + 2x_2x_3$$

☒ 
$$\begin{bmatrix} -10 & 3 & 1 \\ 0 & -2 & 2 \\ 0 & 0 & 5 \end{bmatrix}$$

☐ 
$$\begin{bmatrix} -10 & 3 & 1 \\ 0 & -2 & 2 \\ 0 & 0 & 10 \end{bmatrix}$$

☐ 
$$\begin{bmatrix} -5 & 4 & 8 \\ 0 & -3 & 2 \\ 0 & 0 & -8 \end{bmatrix}$$

☐ 
$$\begin{bmatrix} -1 & 3 & 1 \\ 0 & 0 & 2 \\ 0 & 0 & 5 \end{bmatrix}$$

## Question 9

1 / 1 pts

The objective function of the max-cut problem is

$$\min \sum_{(i,j) \in E} x_i + x_j - 2x_i x_j$$

☐ True

☒ False

## Question 10

1 / 1 pts

The maximum cut of a bipartite graph is equal to the total number of edges in the graph.

☒ True

☐ False

### Question 11

1 / 1 pts

Suppose we have the penalty term  $P \sum_{i=0}^5 \left( \sum_{t=0}^5 x_{i,t} - 1 \right)^2$  in our objective function and  $P = 5$ .

Given that the following binary variables are equal to 1 in the solution, what can you conclude about the penalty included in the objective value due to the above term?

$$x_{2,0} = 1, x_{3,1} = 1, x_{5,2} = 1, x_{5,3} = 1, x_{4,4} = 1, x_{1,5} = 1$$

☐ -5

☐ 0

☒ 10

☐ 5

Partial

### Question 12

0.5 / 1 pts

Suppose that  $Q$  is the QUBO matrix representing a TSP instance with 4 cities and the penalty coefficient is set to  $P = 4$ . Suppose for a given  $x$ , the value of  $x^T Q x$  is -20. Which one of the followings can you conclude with certainty?

- ☐ The found route is feasible.
- ☐ Optimal solution has a cost less than or equal to 12.
- ☐ Optimal route has cost 12.
- ☒ The cost of the found route is 12.
- ☐ The found route is optimal.

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