Discrete Fast Fourier Transform

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# Motivation

Fast Fourier Transforms are useful in a variety of applications, most notably signal processing. If signal processing must occur as fast as possible or with a very large input size, parallelization of a Fast Fourier Transform algorithm can reap large benefits in required processing time.   
In this project, a Fast Fourier Transform algorithm is implemented. Initially it is implemented as a single threaded, serially-executing program. This implementation is analyzed for candidates for parallelization which are then moved to an OpenCL kernel.  
These two implementations are compared both in theoretical complexity as a function of input size, as well as real world execution speed.

# How-to

Import the FFT project into eclipse.  
After running the program, the results of the algorithm should be printed.

The number of elements in the input and the input is printed.  
The FFT CPU results are printed.  
The FFT GPU results are printed.  
These results are automatically compared and checked for errors.  
The speed test for the algorithm is run and the results are printed.  
  
The input file is included in the deliverable. This file is named “input.txt”. This can be modified to provide different inputs, as long as the format of the example is maintained.  
  
The speed test input cannot be changed, it’s purpose is solely to test the performance of the implementation with various input sizes. The results of these FFT executions are not returned. For the speed test, only the execution times are printed, both to the consoles and to “output.txt”.

# Program structure

For this Fast Fourier Transform implementation, the Cooley-Tukey Algorithm was chosen. This algorithm works in stages in which two independent indices of the input array interact. The results of these interactions are placed back into the array and the algorithm is run in a chained manner, in which the results of previous stages are used in the current stage. Each interaction involves two indices and a computed root of unity. Additionally, the initial input must be placed in a specific order.  
As such, our implementation could be broken down into three sub problems, each with their unique challenges.  
1. Reordering of the input

2. Mapping and implementation of interactions

3. Computation and mapping of roots of unity

Each of these is visible in the diagram of an example input size of 8 below.  
The reordering of the input is visible on the input nodes at the left of the diagram. The interacting index pairs, or stages, are shown as arrows. The boxes shown indicate the computations performed involving the roots of unity and the two inputs.

C:\Users\Sev\AppData\Local\Microsoft\Windows\INetCache\Content.Word\drawing.emf

## Reordering of the input

Inputs need to be reordered before the algorithm can be run. Unfortunately, because this reordering does not operate on independent indices, this portion of the FFT implementation was not a candidate for parallelization. Instead, this was implemented as a recursive function that executes prior to any FFT execution.

|  |
| --- |
| std::vector<doublec> reorder\_input(std::vector<doublec> input)  {  //check base case  if (input.size() <= 2)  return input;  //create even and odd index reorder vectors  std::vector<doublec> even(input.size()/2);  std::vector<doublec> odd(input.size()/2);  //split even and odd indices  for (unsigned int i = 0; i < even.size(); i++)  {  even.at(i) = input.at(i \* 2);  odd.at(i) = input.at((i \* 2) + 1);  }  //recursive call to reorder even and odd index vectors  even = reorder\_input(even);  odd = reorder\_input(odd);  //regroup returned vectors and return  std::vector<doublec> result;  result.reserve(input.size());  result.insert(result.end(), even.begin(), even.end());  result.insert(result.end(), odd.begin(), odd.end());  return result;  } |

## Mapping and implementation of interactions

The number of interactions occurring at each stage is half that of the input size. For example, in the given diagram, the sample size is 8. The left column of arrows, however, always shows two pairs of nodes interacting, creating a total of four interactions in that stage. Similarly, stages 2 and 4 also have 4 interacting pairs. As such, the number of threads spawned is half of the input size.

### Thread mapping

One major challenge to this approach was finding the corresponding mapping from the thread number to the nodes it operates on, in a specific stage.

As an example, the diagram shows thread 0 mapped to index 0 and index 1 of the input array. Similarly, thread 0 is mapped to index 0 and 2 and index 0 and 4 at stages 2 and 4, respectively.  
By analyzing the pattern, the following mapping was found to output an index, given the thread number and the current stage.

|  |
| --- |
| unsigned int thread\_index\_map(unsigned int thread\_id, unsigned int stage)  {  return (stage \* 2 \* (thread\_id / stage)) + thread\_id % stage;  } |

Finally, after retrieving the one thread to index mapping, the other interacting index can be found simply by adding the current stage to the returned mapping.

### Interaction implementation

Once the correct mapping is found, the two data items at those indices interact with each other, as well as an additional root of unity.

This interaction is defined as:

result[home\_index] = result[home\_index] + (result[target\_index] \* root)  
result[target\_index] = result[home\_index] – (result[target\_index] \* root)

Of interest is the fact that the root for a particular interaction remains constant. As such, the (target\_index\*root) may be computed only once, further optimizing for execution speed.

This is implemented in the code below:

|  |
| --- |
| cl\_float2 pq = floatc\_mul(result.at(target\_index), roots.at(home\_root));  cl\_float2 top = floatc\_add(pq, result.at(home\_index));  cl\_float2 bottom = floatc\_sub(result.at(home\_index), pq);  result.at(home\_index) = top;  result.at(target\_index) = bottom; |

## Computation and mapping of roots of unity

The required degree of the roots of unity for this FFT implementation is directly related to the size of the input. For instance, an input of size 8 will require 8 roots of unity. As such, instead of computing the necessary root for that particular stage and thread, the required roots are computed at the beginning of the algorithm and are simply referenced later via an additional mapping function.  
Additionally, because roots are symmetric around the unit circle, more time was saved by simply computing half of them. For example, an input size of 8 will only require 4 roots to be computed. Coincidentally, since 4 threads are spawned for the same input size, each thread is tasked with computing one root.   
This computation is shown below:

|  |
| --- |
| for (unsigned int i = 0; i < roots.capacity(); i++)  {  double arg = (2 \* pi \* (double)i) / ((double)result.capacity());  roots.at(i).real = cos(arg);  roots.at(i).imag = -1 \* sin(arg);  } |

Like the thread to index mapping function, threads need a mapping function to find the correct root to use, as shown below:

|  |
| --- |
| unsigned int thread\_root\_map(unsigned int thread\_id, unsigned int estage, unsigned int istage)  {  return istage \* (thread\_id % estage);  } |

In this function, estage counts up (1, 2, 4, 8, …) while istage counts in reverse (…, 8, 4, 2, 1).

# Parallelization and expected results

Examination of the diagram of the FFT algorithm reveals that the number of stages of the algorithm is logarithmically related to the size of the input. Similarly, the number of operations performed within each stage is linearly related to the size of the input. Additionally, the non-recurring cost of computing the roots is also linearly related to the size of the input.  
Thus, the runtime complexity of the serially executing algorithm is O(n+n\*log(n)) where n is the size of the input. This reduces to just O(n\*log(n)).  
Analysis of the algorithm reveals two primary candidates for optimization:

1. Root computation

2. FFT algorithm

## Parallelization

### Root computation

Parallelizing the root computation simply maps one root computation to each thread. Thus, the runtime complexity for this portion reduces from O(n) to O(1).

FFT algorithm  
The stages of the algorithm cannot be parallelized, as they rely on previous stages’ results. However, the interactions within each stage are easily parallelized by mapping each interaction to its own thread. Thus, the runtime complexity for this portion reduces from O(n\*log(n)) to O(log(n)).  
  
Overall this results in a runtime complexity reduction from O(n\*log(n) to O(log(n)).

## Expected Results

Timing results from the implementation are expected to roughly follow these complexities.  
However, there is an overhead cost associated with moving data to the OpenCL device as well as an associated cost in starting up the computation on the device. This introduces a relatively constant overhead and causes a breakeven point in the total run time. This means that for dataset inputs below a certain size, the OpenCL overhead would cause the theoretically faster OpenCL implementation to be slower than the serial CPU implementation.

# Results

## Execution speed

The implementation was executed 5 times over a large range of input sizes. The timing results were averaged with each other to minimize spurious results.

This graph clearly shows the breakeven point. This point is located at the intersections of the CPU and GPU lines. Thus, any dataset with a size of around 2048 or larger should be run on the GPU implementation as the execution time cost is lower. Sizes below this should not be run on the GPU as the GPU overhead destroys its parallelized execution improvements.

This graph more clearly shows the overhead cost of executing on a GPU. The long, negative slope line from 2 to about 32768 relates well to the increasing size of the input. This indicates that most of the execution time on the GPU seen in this range is the overhead. From 32768 to the end of the graph, this overhead appears to amortize and we see the true execution time per element.

## Potential improvements

Since this implementation only computes the roots once at the beginning of the algorithm, the effects of the sine and cosine functions are negligible. However, in a different implementation where the roots are computed again when needed, using native\_sin and native\_cos functions may result in significant performance increases. The implementation used for this project assumed that a memory access of the stored roots would be faster than a repeated computation of each required root.  
  
Additionally, as the size of the input and the required memory increases, the GPU may be starved due to insufficient memory bandwidth. Without reducing the input size, increasing cache size, or compressing the individual elements, there is no easy way to solve this.

# Sources

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# Appendix

## FFT.cpp

|  |
| --- |
| #include <stdio.h>  #include <Core/Assert.hpp>  #include <Core/Time.hpp>  #include <OpenCL/cl-patched.hpp>  #include <OpenCL/Program.hpp>  #include <OpenCL/Event.hpp>  #include <OpenCL/Device.hpp>  #include <fstream>  #include <sstream>  #include <iostream>  #include <cmath>  #include "floatc.hpp"  using namespace Core;  using namespace std;  #define pi 3.14159265359f  int read\_input(std::vector<cl\_float2>\* input, string filename);  void print\_vector(std::vector<cl\_float2>\* input);  std::vector<cl\_float2> reorder\_input(std::vector<cl\_float2> input);  unsigned int thread\_index\_map(unsigned int thread\_id, unsigned int stage);  unsigned int thread\_root\_map(unsigned int thread\_id, unsigned int estage, unsigned int istage);  void print\_vector(std::vector<cl\_float2>\* input)  {  cout << endl;  for (unsigned int i = 0; i < input->size(); i++)  {  cout << floatc\_to\_string(input->at(i)) << endl;  }  }  int read\_input(std::vector<cl\_float2>\* input, string filename)  {  input->clear();  //read file  ifstream inputFile;  inputFile.open(filename.c\_str(), ifstream::in); //input.csv  //verify that file is open  if (inputFile.is\_open())  {  //log success  }  else  {  //log fail  return -1;  }  string inputLine;  //count number of lines (samples) in file  while (getline(inputFile, inputLine))  {  cl\_float2 sample;  sample.y = 0;  try  {  float line = ::atof(inputLine.c\_str());  sample.x = line;  }  catch (...)  {  return -1;  }  input->push\_back(sample);  }  //check sample size for usability  //TODO  if (input->size() < 2)  {  return -1;  }  unsigned int powertwo = 2;  //find smallest power of two larger than the input vector  while (powertwo < input->size())  powertwo = powertwo \* 2;  //pad input vector with 0s until it's a power of two size  while (input->size() != powertwo)  {  cl\_float2 sample;  sample.x = 0;  sample.y = 0;  input->push\_back(sample);  }  return true;  }  std::vector<cl\_float2> reorder\_input(std::vector<cl\_float2> input)  {  //check base case  if (input.size() <= 2)  return input;  //create even and odd index reorder vectors  std::vector<cl\_float2> even(input.size()/2);  std::vector<cl\_float2> odd(input.size()/2);  //split even and odd indices  for (unsigned int i = 0; i < even.size(); i++)  {  even.at(i) = input.at(i \* 2);  odd.at(i) = input.at((i \* 2) + 1);  }  //recursive call to reorder even and odd index vectors  even = reorder\_input(even);  odd = reorder\_input(odd);  //regroup returned vectors and return  std::vector<cl\_float2> result;  result.reserve(input.size());  result.insert(result.end(), even.begin(), even.end());  result.insert(result.end(), odd.begin(), odd.end());  return result;  }  std::vector<cl\_float2> fft\_cpu(std::vector<cl\_float2> input)  {  std::vector<cl\_float2> result(input);  std::vector<cl\_float2> roots;  roots.reserve(input.size()/2);  //populate root vector with empty complex numbers  for (unsigned int i = 0; i < roots.capacity(); i++)  {  cl\_float2 root;  root.x = 0;  root.y = 0;  roots.push\_back(root);  }  //calculate half of the roots  //we do this to match the number of threads (size/2) that run on the OpenCL implementation  for (unsigned int i = 0; i < roots.capacity(); i++)  {  float arg = (2 \* pi \* (float)i) / ((float)result.capacity());  roots.at(i).x = cos(arg);  roots.at(i).y = -1 \* sin(arg);  }  #ifdef DEBUG  cout << "unity roots";  print\_vector(&roots);  cout << endl;  #endif  //threads always operate on pairs of indices in each stage  //so we start half as many threads as the input size  unsigned int num\_of\_threads = (unsigned int)(result.size() / 2);  //we maintain a power of two up counter and a power of two down counter to avoid exp or log functions  //here we loop through the stages which has a runtime complexity of log(n)  unsigned int istage = num\_of\_threads;  for (unsigned int estage = 1; estage <= num\_of\_threads; estage = estage \* 2)  {  #ifdef DEBUG  cout << "STAGE " << estage << endl;  #endif  //the inner loops simply executes our "threads".  //this will be parallelized in the opencl implementation  //runtime for this is n  //total for fft serial execution is nlogn  for (unsigned int thread\_id = 0; thread\_id < num\_of\_threads; thread\_id++)  {  //we query for our home and target indeces  //as well as our home and target root indeces  unsigned int home\_index = thread\_index\_map(thread\_id, estage);  unsigned int target\_index = home\_index + estage;  unsigned int home\_root = thread\_root\_map(thread\_id, estage, istage);  #ifdef DEBUG  cout << "t" << thread\_id << ": " << "hi" << home\_index << ", ti" << target\_index << endl;  cout << "t" << thread\_id << ": " << "hr" << home\_root << endl;  #endif  cl\_float2 pq = floatc\_mul(result.at(target\_index), roots.at(home\_root));  cl\_float2 top = floatc\_add(pq, result.at(home\_index));  cl\_float2 bottom = floatc\_sub(result.at(home\_index), pq);  result.at(home\_index) = top;  result.at(target\_index) = bottom;  }  #ifdef DEBUG  cout << endl;  #endif  istage = istage / 2;  }  return result;  }  unsigned int thread\_index\_map(unsigned int thread\_id, unsigned int stage)  {  return (stage \* 2 \* (thread\_id / stage)) + thread\_id % stage;  }  unsigned int thread\_root\_map(unsigned int thread\_id, unsigned int estage, unsigned int istage)  {  return istage \* (thread\_id % estage);  }  float round(float x){  float y = ceilf(x\*100)/100;  return y;  }  unsigned int error\_calculator(std::vector<cl\_float2> fromCPU, std::vector<cl\_float2> fromGPU)  {  unsigned int errorCount = 0;  for(size\_t i = 0; i < fromCPU.size(); i++){  float xdif = abs(fromCPU[i].x - fromGPU[i].x);  float ydif = abs(fromCPU[i].y - fromGPU[i].y);  if(xdif > 0.0001 || ydif > 0.0001)  errorCount++;  }  return errorCount;  }  std::vector<cl\_float2> opencl(std::vector<cl\_float2> input, Core::TimeSpan \*gpuTime)  {  std::vector<cl\_float2> output;  // Create a context  //cl::Context context(CL\_DEVICE\_TYPE\_GPU)  std::vector<cl::Platform> platforms;  cl::Platform::get(&platforms);  if (platforms.size() == 0) {  std::cerr << "No platforms found" << std::endl;  return output;  }  int platformId = 0;  for (size\_t i = 0; i < platforms.size(); i++) {  //cout << platforms[i].getInfo<CL\_PLATFORM\_NAME>() << endl;  platformId = i;  }  cl\_context\_properties prop[4] = { CL\_CONTEXT\_PLATFORM, (cl\_context\_properties)platforms[platformId](), 0, 0 };  //std::cout << "Using platform '" << platforms[platformId].getInfo<CL\_PLATFORM\_NAME>() << "' from '" << platforms[platformId].getInfo<CL\_PLATFORM\_VENDOR>() << "'" << std::endl;  cl::Context context(CL\_DEVICE\_TYPE\_GPU, prop);  // Get a device of the context  //std::cout << "Context has " << context.getInfo<CL\_CONTEXT\_DEVICES>().size() << " devices" << std::endl;  cl::Device device = context.getInfo<CL\_CONTEXT\_DEVICES>()[0];  std::vector<cl::Device> devices;  devices.push\_back(device);  // Create a command queue  cl::CommandQueue queue(context, device, CL\_QUEUE\_PROFILING\_ENABLE);  // Load the source code  cl::Program program = OpenCL::loadProgramSource(context, "src/FFT.cl");  // Compile the source code. This is similar to program.build(devices) but will print more detailed error messages  OpenCL::buildProgram(program, devices);  std::size\_t data\_size = input.size()\*sizeof(cl\_float2);  cl::Buffer d\_data(context, CL\_MEM\_READ\_WRITE, data\_size);  cl::Buffer d\_roots(context, CL\_MEM\_READ\_WRITE, (input.size()/2) \* sizeof(cl\_float2));  cl::Event copytoGPU;  queue.enqueueWriteBuffer(d\_data, true, 0 , data\_size, input.data(), NULL, &copytoGPU);  cl::Event event;  // Create a kernel object  cl::Kernel kernel1(program, "fftKernel");  kernel1.setArg(0, d\_data);  kernel1.setArg(1, d\_roots);  unsigned int WG\_size = input.size()/2;  if(WG\_size > 256)  WG\_size = 256;  queue.enqueueNDRangeKernel(kernel1, 0, input.size()/2, WG\_size, 0, &event);  cl::Event copytoCPU;  queue.enqueueReadBuffer(d\_data, true, 0, data\_size, input.data(), NULL, &copytoCPU);  queue.finish();  Core::TimeSpan gpuExecTime = OpenCL::getElapsedTime(event);  Core::TimeSpan copyTime = OpenCL::getElapsedTime(copytoGPU) + OpenCL::getElapsedTime(copytoCPU);  \*gpuTime = gpuExecTime + copyTime;  //cout << "Total time in GPU is " << gpuTime << endl;  return input;  }  void speed\_test(unsigned int size)  {  ofstream myfile;  myfile.open ("output.txt");  unsigned vector\_size = 1;  for(unsigned int i = 0; i <= size; i ++)  {  vector\_size = vector\_size \* 2;  std::vector<cl\_float2> test;  for(unsigned int j = 0; j < vector\_size; j++)  {  cl\_float2 sample;  sample.y = 0;  sample.x = (float)(j+1);  test.push\_back(sample);  }  //CPU  Core::TimeSpan cpuStart = Core::getCurrentTime();  vector<cl\_float2> result = fft\_cpu(test);  Core::TimeSpan cpuEnd = Core::getCurrentTime();  Core::TimeSpan cpuTime = cpuEnd - cpuStart;  cout << "CPU, " << vector\_size << ", " << cpuTime << endl;  //GPU  Core::TimeSpan gpuTime = Core::getCurrentTime();  vector<cl\_float2> resultgpu = opencl(test, &gpuTime);  cout << "GPU, " << vector\_size << ", " << gpuTime << endl;  myfile << "CPU, " << vector\_size << ", " << cpuTime << ", GPU, " << vector\_size << ", " << gpuTime << endl;  }  myfile.close();  }  int main()  {  std::vector<cl\_float2> h\_input;  if (read\_input(&h\_input, "input.txt"))  {  cout << "Input has " << h\_input.size() << " samples." << endl;  }  else  {  cout << "Input invalid" << endl;  return 1;  }  cout << "raw input";  print\_vector(&h\_input);  cout << endl;  h\_input = reorder\_input(h\_input);  #ifdef DEBUG  cout << "reordered input";  print\_vector(&h\_input);  cout << endl;  #endif  Core::TimeSpan cpuStart = Core::getCurrentTime();  vector<cl\_float2> result = fft\_cpu(h\_input);  Core::TimeSpan cpuEnd = Core::getCurrentTime();  Core::TimeSpan cpuTime = cpuEnd - cpuStart;  cout << "fft result";  print\_vector(&result);  cout << endl;  Core::TimeSpan gpuTime = Core::getCurrentTime();  vector<cl\_float2> resultgpu = opencl(h\_input, &gpuTime);  cout << "opencl result";  print\_vector(&resultgpu);  cout << endl;  cout << "Found errors in " << error\_calculator(result,resultgpu) << " values" << endl;  cout << "Total time in CPU is " << cpuTime << endl;  cout << "Total time in GPU is " << gpuTime << endl;  speed\_test(20);  } |

## FFT.cl

|  |
| --- |
| #ifndef \_\_OPENCL\_VERSION\_\_  #include <OpenCL/OpenCLKernel.hpp> // Hack to make syntax highlighting in Eclipse work  #endif  #define pi 3.14159265359f  unsigned int thread\_index\_map(unsigned int thread\_id, unsigned int stage)  {  return (stage \* 2 \* (thread\_id / stage)) + thread\_id % stage;  }  unsigned int thread\_root\_map(unsigned int thread\_id, unsigned int estage, unsigned int istage)  {  return istage \* (thread\_id % estage);  }  float2 floatc\_add(float2 a, float2 b)  {  float2 c;  c.x = a.x + b.x;  c.y = a.y + b.y;  return c;  }  float2 floatc\_sub(float2 a, float2 b)  {  float2 c;  c.x = a.x - b.x;  c.y = a.y - b.y;  return c;  }  float2 floatc\_mul(float2 a, float2 b)  {  float2 c;  c.x = a.x\*b.x - a.y\*b.y;  c.y = a.y\*b.x + a.x\*b.y;  return c;  }  \_\_kernel void fftKernel(\_\_global float2\* d\_input, \_\_global float2\* d\_roots) {  size\_t i = get\_global\_id(0);  size\_t count = get\_global\_size(0);  //populate root array  float arg = (2 \* pi \* (float)i) / ((float)count \* 2);  d\_roots[i].x = cos(arg);  d\_roots[i].y = -1 \* sin(arg);  barrier(CLK\_GLOBAL\_MEM\_FENCE);  unsigned int istage = count;  for (unsigned int estage = 1; estage <= count; estage = estage \* 2)  {  //we query for our home and target indeces  //as well as our home and target root indeces  unsigned int home\_index = thread\_index\_map(i, estage);  unsigned int target\_index = home\_index + estage;  unsigned int home\_root = thread\_root\_map(i, estage, istage);  float2 pq = floatc\_mul(d\_input[target\_index], d\_roots[home\_root]);  float2 top = floatc\_add(pq, d\_input[home\_index]);  float2 bottom = floatc\_sub(d\_input[home\_index], pq);  d\_input[home\_index] = top;  d\_input[target\_index] = bottom;  istage = istage / 2;  barrier(CLK\_GLOBAL\_MEM\_FENCE);  }  } |

## floatc.hpp

|  |
| --- |
| #ifndef FLOATC\_H  #define FLOAT\_H  #include <iostream>  using namespace std;  cl\_float2 floatc\_add(cl\_float2 a, cl\_float2 b)  {  cl\_float2 c;  c.x = a.x + b.x;  c.y = a.y + b.y;  return c;  }  cl\_float2 floatc\_sub(cl\_float2 a, cl\_float2 b)  {  cl\_float2 c;  c.x = a.x - b.x;  c.y = a.y - b.y;  return c;  }  cl\_float2 floatc\_mul(cl\_float2 a, cl\_float2 b)  {  cl\_float2 c;  c.x = a.x\*b.x - a.y\*b.y;  c.y = a.y\*b.x + a.x\*b.y;  return c;  }  string floatc\_to\_string(cl\_float2 a)  {  stringstream ss;  ss << a.x << " + " << a.y << "i";  return ss.str();  }  #endif |