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This assignment is worth 10/60 ($\approx 9.5\%$) of Problem Assignment points

Name: _____

1. Convert the following as indicated: (2 points)

(a) 00101001_2 to a decimal integer,
~~346+21~~

$$1_{10} \times 2_{10}^5 + 1_{10} \times 2_{10}^3 + 1_{10} \times 2_{10}^0 = 32 + 8 + 1$$

Answer: 41₁₀

(b) 00101100_2 to a hexadecimal integer,

$\downarrow \quad \downarrow$
 $2_{16} \quad 12_{10}$
 \downarrow
 C_{16}

Answer: 2C₁₆

(c) B_{16} to an 8-bit unsigned binary integer, and

$B = 11$

Answer: 10110001₂

(d) 212_{10} to an 8-bit unsigned binary integer.

$$\begin{array}{r} 106 \text{ r } 0 \\ 2 \overline{) 212} \\ \underline{204} \\ 8 \\ 53 \text{ r } 0 \\ 2 \overline{) 106} \\ \underline{104} \\ 2 \\ 26 \text{ r } 1 \\ 2 \overline{) 53} \\ \underline{52} \\ 1 \\ 13 \text{ r } 0 \\ 2 \overline{) 26} \\ \underline{26} \\ 0 \\ 6 \text{ r } 1 \\ 2 \overline{) 13} \\ \underline{12} \\ 1 \\ 3 \text{ r } 0 \\ 2 \overline{) 6} \\ \underline{6} \\ 0 \\ 1 \text{ r } 1 \\ 2 \overline{) 3} \\ \underline{2} \\ 1 \\ 0 \text{ r } 1 \\ 2 \overline{) 1} \\ \underline{0} \\ 1 \end{array}$$

Answer: 1101 0100₂

Cont.

2. Compute the **4-bit binary** sum of the following 4-bit unsigned binary integers. Provide the base-10 result as well. Do allow values to overflow—that is do not add bits in excess of the 4 bits. Additionally, provide decimal(base₁₀) integer values ¹: (2 points)

(a) 0011 + 0111

$$\begin{array}{r} \downarrow \quad \downarrow \\ 3_{10} \quad 7_{10} \end{array}$$

$$\begin{array}{r} 0011 \\ + 0111 \\ \hline 1010 \end{array}$$

Answer: _____ 1010_2

Answer: _____ 10_{10}

(b) 1010 + 0111

$$\begin{array}{r} \downarrow \quad \downarrow \\ 10_{10} \quad 7_{10} \end{array}$$

$$\begin{array}{r} 1010 \\ + 0111 \\ \hline 0001 \end{array}$$

Answer: _____ 0001_2

Answer: _____ 1_{10}

¹Take into account overflow. Do not tell me that $15_{10} + 15_{10} = 30_{10}$. I know you know that. Due to overflow in 4-bit, $15_{10} + 15_{10} = 14_{10}$; i.e., at least 5-bits are necessary to count above 15.

3. Convert the following to **8-bit two's complement-encoded binary** integers and perform the indicated operations. You must show all conversions into and out of two's complement encoding. Provide your results in 8-bit two's complement binary and base-10 or base-16, based on problems' radii: (2 points)

(a) $27_{10} - 15_{10} = 27 + (-15)$

$-15_{10} = 0000\ 1111$

$$\begin{array}{r} 1111\ 1111 \\ 1111\ 0001 \\ 0000\ 1111 \\ \hline 0000\ 0000 \end{array}$$

$27_{10} = 0001\ 1011$

$$\begin{array}{r} 1111\ 1111 \\ 0001\ 1011 \\ 1111\ 0001 \\ \hline 0000\ 1100 \end{array}$$

Answer: _____

0000 1100₂

Answer: _____

12
10

0000 1100
8421

$$(b) -17_{16} - 1A_{16} = -17_{16} + (-1A_{16})$$

$$-1A_{16} = -00011010_2$$

$$-17_{16} = -00010111_2$$

$$\begin{array}{r} 111111 \\ 11100110 \\ \hline 00011010 \\ 00000000 \\ 11111111 \\ 11101001 \\ \hline 00010111 \\ 00000000 \end{array}$$

$$\begin{array}{r} 11 \\ 11100110 \\ 11101001 \\ \hline 11001111 \end{array}$$

$$\begin{array}{r} 0011|0001 \\ \swarrow \searrow \\ 3_{16} \quad 1_{16} \end{array}$$

$$\text{Answer: } \underline{11001111}_2$$

$$\text{Answer: } \underline{-31}_{16}$$

4. For each of the following, show their conversion to binary coded decimals (BCD) as 8421-code: (2 points)

(a) 572_{10}

572
 $\swarrow \downarrow \rightarrow 0010$
 $0101 \quad 0111$

Answer: 0101 0111 0010

(b) 213_4

$2 \cdot 4^2 + 1 \cdot 4^1 + 3 \cdot 4^0 = 32 + 4 + 3 = 39_{10}$
 $\swarrow \searrow$
 $0011 \quad 1001$

Answer: 0011 1001

5. Decode the two following 8-bit binary **strings** into ASCII characters²: (2 points)

(a) 01100011 01010011 01000011 01100101

0110 0011 0101 0011 0100 0011 0110 0101
c S C e

Answer: _____

cSce

(b) 01100011 01100011 00111110 01101010 01100001 01110110 01100001

c c > j a v a

Answer: _____

cc>java

²You may use the 7-bit ASCII from the book, but do keep in mind ASCII values, like all values in a computer, are at least 8-bits in size. Simply add a 0 as the most significant bit of each character from the book.