

Tutoring Lesson Notes: Lesson 1 (5/4)

Topics: Overview & introduction, Newton's Laws, inclined slope question, introduction to energy.

Scalars & Vectors:

- SCALAR - a magnitude

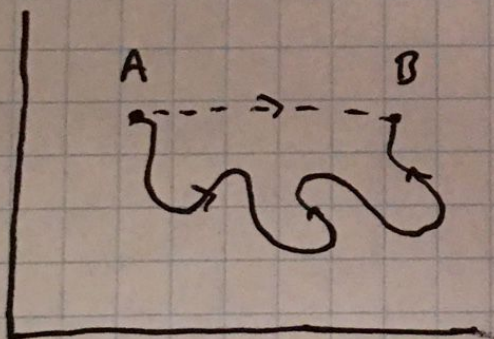
Examples: time, speed, mass

- VECTOR - a magnitude with a direction

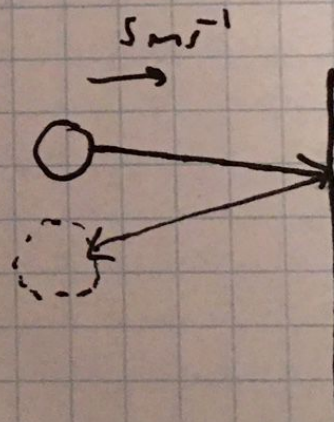
Examples: velocity, acceleration, force

velocity = speed with direction

displacement = distance with direction



Here my distance travelled is the squiggly line (say, 4 miles) while my displacement is 2 miles from A to B (the dotted line)



Here the ball starts with a velocity of 5 m s^{-1} to the right, but changes velocity (5 m s^{-1} to the left).

The speed is a constant, the velocity is not.

Relationship:

$$\text{speed} = \frac{\text{distance}}{\text{time}}$$

$$\text{velocity} = \frac{\text{displacement}}{\text{time}}$$

Focus on this equation!
More useful!

Ex 1. If a car moves at speed 30 miles per hour for 2 hours, what distance does the car move?

$$\text{Speed} = \frac{\text{distance}}{\text{time}} \Rightarrow s = \frac{d}{t} \Rightarrow d = st = 30 \times 2 = 60 \text{ miles}$$

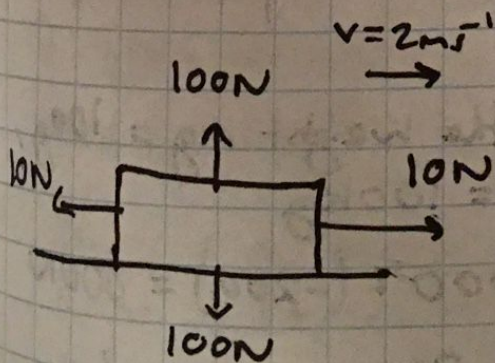
Make sure units are correct!

$$\text{acceleration} = \frac{\text{velocity}}{\text{time}}$$

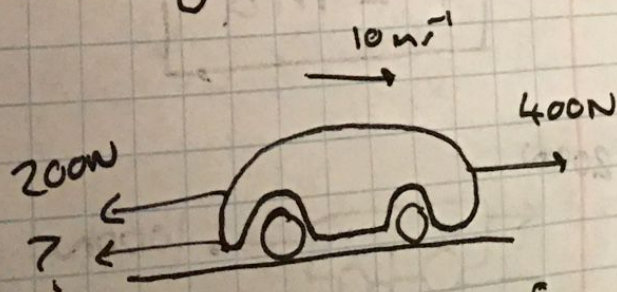
or in words: acceleration is the rate of change of velocity.

NEWTON'S LAWS:

- 1st Law - if the total forces acting on an object sum to zero, then the velocity is constant.

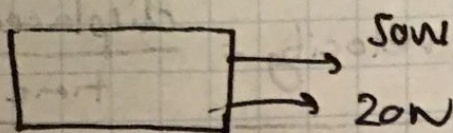


The forces are equal and cancel out = constant velocity (in this case, 2 m/s)

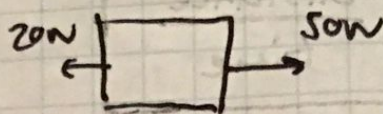


Constant velocity \Rightarrow forces sum to zero
 $\Rightarrow 400 + (-200) + (-?)$
 $\Rightarrow -200 \text{N} \Rightarrow 200 \text{N to the left.}$

Note how forces add:

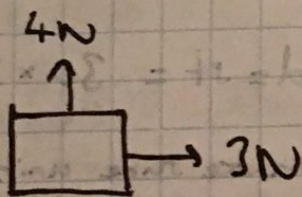


$$F = 50 + 20 = 70\text{N}$$

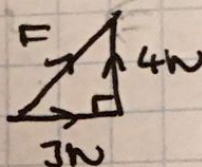


$$50\text{N} + (-20\text{N}) = 30\text{N}$$

here a force is positive if it goes to the right, negative if to the left

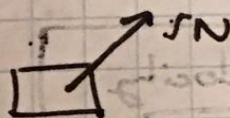


\Rightarrow



$$F = \sqrt{3^2 + 4^2} = 5\text{N}$$

\Rightarrow



We can look at this more next week!

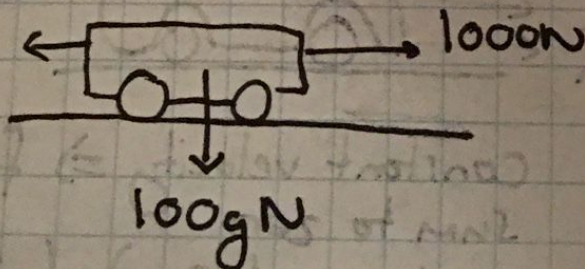
• 2nd Law - the opposite!

If the forces don't sum to zero, then the velocity is not constant! There is an acceleration:

$$F = ma$$

F is the overall force

200N



Here the weight $mg = 100\text{g}$,
so $m = 100\text{kg}$

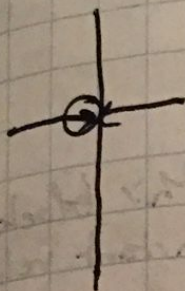
$$F = 1000 + (-200) = 800\text{N}$$

$$\Rightarrow a = \frac{800}{100} = 8\text{ m s}^{-2}$$

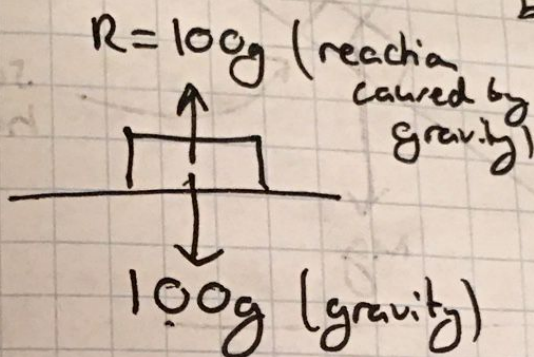
Quick note: Look at $F=ma$. If $F=0$, then $a=0$ (assuming $m>0$). Thus we have Newton's 1st Law!

3rd Law - every action has an EQUAL and OPPOSITE reaction.

Examples:



Force ball exerts on wall = -Force wall exerts on ball.



There are nuances here, but don't overthink this one. Just think of these examples.

Imagine that there must be a surface for this to hold if it helps (the only cave in the GAMMAT as far as I know where this will be useful).

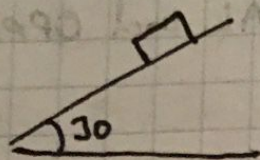
Questions:

1. If a car has a driving force $1000N$, air resistance $100N$ and friction $200N$, and a weight of $7000N$, what is its acceleration?
2. Suppose a block has two forces acting on it, $11N$ and $1N$. What values can the net force take?

[think about this one]

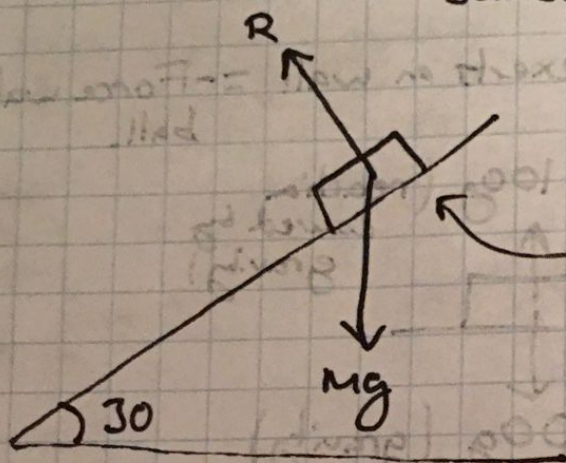
Inclined Slope!

Consider the following:



What are the forces?

- Gravity (straight down)
- Reaction (perpendicular to surface)
- Sometimes friction

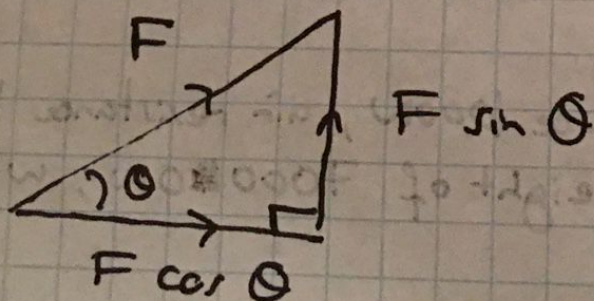


Suppose this block has a constant velocity

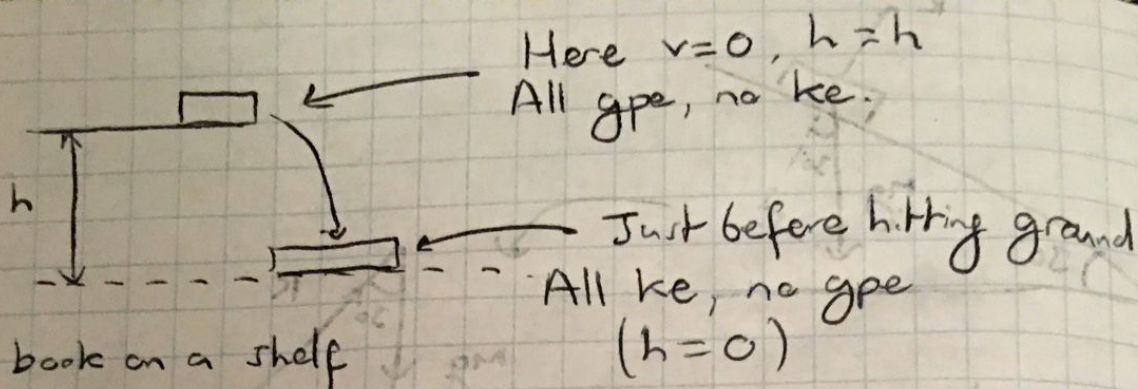
By Newton's 1st Law:

Forces up = Forces down.

To solve this, we need to resolve the reaction force R into its vertical and horizontal components. How? Here's a trick:



[Remember: Along the Corridor (\cos), Up the Stairs (\sin)]



Suppose a ^{2kg} ball is thrown vertically upwards at 10 m/s . What is its maximum height?

$h=?$

$$ke = \frac{1}{2} \cdot 2 \cdot 10^2 = 100\text{ J}$$

At max height, $v=0 \Rightarrow ke=0$

As energy conserved, then

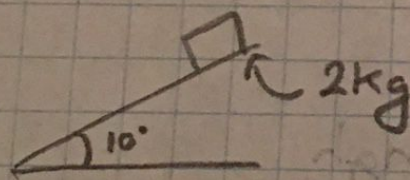
$$gpe = 100\text{ J}$$

$$\Rightarrow 100 = mgh$$

$$\Rightarrow 100 = 2 \cdot 10 \cdot h \rightarrow \underline{h = 5\text{ m}}$$

Questions (to ponder)

1.



Find R

2. A box sits on an inclined plane without sliding. As the angle of the plane increases, the normal force (the reaction force, R)

- Increases linearly
- Increases non-linearly
- Decreases linearly
- Decreases non-linearly
- No change

3. A book is at height 6m and is dropped. If the book is 2kg , what is the final speed of the book before it hits the ground?