

## Bernoulli Distribution

$X$  = obtaining a “success” in experiment with only 2 outcomes (“success”, “failure”).  $P(\text{Success}) = p$ .

$$X \sim \text{Bern}(p)$$

- Probability Mass Function (PMF)

$$p_X(x) = p^x(1-p)^{1-x} \quad \text{for } x = 0, 1$$

- Cumulative Distribution Function (CDF)

$$F_X(t) = P(X \leq t) = \begin{cases} 0 & \text{for } t < 0 \\ 1-p & \text{for } 0 \leq t < 1 \\ 1 & \text{for } t \geq 1 \end{cases}$$

- Expected Value:  $E(X) = p$
- Variance:  $\text{Var}(X) = p(1-p)$

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## Binomial Distribution

$X$  = # of “successes” in  $n$  trials, where each trial has only 2 outcomes (“success”, “failure”).  $P(\text{Success}) = p$ .

$$X \sim \text{Bin}(n, p)$$

- Probability Mass Function (PMF)

$$p_X(x) = \binom{n}{x} p^x (1-p)^{n-x} \quad \text{for } x = 0, 1, 2, \dots, n$$

- Cumulative Distribution Function (CDF)

$$F_X(t) = P(X \leq t) = \sum_{x=0}^{\lfloor t \rfloor} \binom{n}{x} p^x (1-p)^{n-x}$$

- Expected Value:  $E(X) = np$
- Variance:  $\text{Var}(X) = np(1-p)$

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## Geometric Distribution

$X$  = # of trials until 1<sup>st</sup> success where each trial has only 2 outcomes (“success”, “failure”).  $P(\text{Success}) = p$ .

$$X \sim \text{Geo}(p)$$

- Probability Mass Function (PMF)

$$p_X(x) = P(X = x) = (1-p)^{x-1}p \quad \text{for } x = 1, 2, 3, \dots$$

- Cumulative Distribution Function (CDF)

$$F_X(t) = P(X \leq t) = \begin{cases} 0 & \text{for } t < 1 \\ 1 - (1-p)^{\lfloor t \rfloor} & \text{for } t \geq 1 \end{cases}$$

- Expected Value:  $E(X) = \frac{1}{p}$
- Variance:  $\text{Var}(X) = \frac{1-p}{p^2}$

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## Poisson Distribution

$X$  = # of events occurring during an interval.  $\lambda$  is the “rate”.

$$X \sim \text{Pois}(\lambda)$$

- Probability Mass Function (PMF)

$$p_X(x) = \frac{e^{-\lambda} \lambda^x}{x!} \quad \text{for } x = 0, 1, 2, 3, \dots$$

where  $\lambda > 0$  is the rate parameter.

- Cumulative Distribution Function (CDF)

$$F_X(x) = P(X \leq t) = \sum_{x=0}^{\lfloor t \rfloor} p_X(x)$$

- Expected Value:  $E(X) = \lambda$
- Variance:  $\text{Var}(X) = \lambda$

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