Stat 330 Homework 10

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1)
(a) Mean = 56.9Median = 50.5Q1 = 44.5, Q3 = 58, IQR = 13.5Variance = 632.49, Stand. Dev. = 25.15

- (b) The only number outside of the range is 130.
- (c) Mean = 48.8Median = 50Q1 = 44, Q3 = 55, IQR = 11Variance = 43.01, Stand. Dev. = 6.56
- (d) An outlier will greatly skew the mean and standard deviation, but will not have much effect on the median or IQR.
- (a) The histogram is exponential, with the vast majority of diamonds in the lower price range, and a sloping decrease of the number of diamonds as the price increases.
 - (b) Exponential, as the decrease in diamond price follows an exponential curve.
 - (c) As diamond carat increases, the price increases linearly, and the variability increases as well.

3)
$$\frac{1}{n-1}(n\mathbb{E}(X^2) - n\mathbb{E}(\bar{X}^2)) = \frac{1}{n-1}n(\mathbb{E}(X^2) - \mathbb{E}(\bar{X}^2)) = \frac{1}{n-1}n(Var(x) + \mathbb{E}(X)^2 - Var(x) - \mathbb{E}(\bar{X})^2) = \frac{1}{n-1}n(\mathbb{E}(X)^2 - \mathbb{E}(\bar{X})^2) = \frac{1}{n-1}n(\mathbb{E}(X)^2 - \mathbb{E}(\bar{X})^2) = ? = \sigma^2$$

4)
(a)
$$E(\frac{X_1+X_2+X_3+X_4}{4}) = \frac{E(X_1)+E(X_2)+E(X_3)+E(X_4)}{4} = \frac{4\mu}{4} = \mu$$
 $E(\frac{X_1+2X_2+X_3}{4}) = \frac{E(X_1)+E(X_2)+E(X_2)+E(X_3)}{4} = \frac{4\mu}{4} = \mu$
(b) ?

5) (a)
$$E(Y)$$
 for $Pois(\lambda) = \lambda$.
 $\mu_1 = E(Y) = \bar{Y} = m_1 \implies \lambda = \bar{y} \implies \lambda_{MoM} = \bar{y}$

(b)
$$\prod_{i=1}^{n} \frac{e^{-\lambda} \lambda^{y_i}}{y_i!} = \frac{e^{-n\lambda} \lambda^{ny_i}}{\prod_{i=1}^{n} y_i!} \Rightarrow$$
$$l(\lambda) = (-n\lambda + ny \log(\lambda)) - \sum_{i=1}^{n} \log(y_i!)$$
$$dx * l(\lambda) = -n + \frac{ny}{\lambda} = 0 \Rightarrow \lambda_{MLE} = y$$

(c)
$$\bar{x} = \frac{7+6+7+2+4}{5} = 5.2 = \text{MoM}$$

6) (a)
$$\mu = E(X) = \int x f(x) dx \Rightarrow \int_0^1 x \theta x^{\theta - 1} dx = \frac{\theta}{\theta + 1} = \bar{x}$$

$$\frac{\theta}{\theta + 1} = \bar{x} \Rightarrow \theta = \frac{\bar{x}}{1 - \bar{x}} \Rightarrow \theta = \frac{.666}{1 - .666} = 2$$

(b) No idea

7)