

# Homework #7 (Due: Mar. 9)

Total 400 points

Please write down your name on your homework.

Please submit your homework online through Canvas by Friday 10:00pm.

Late homework will be penalized.

Important: Your submission must be in .pdf format ONLY!

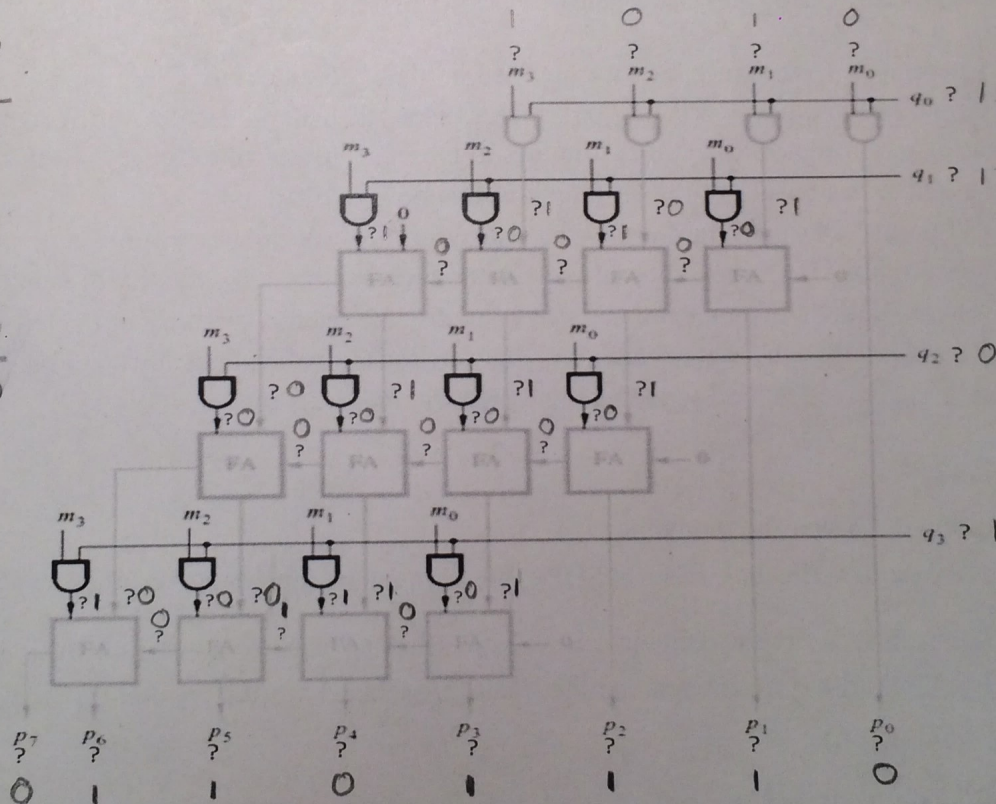
## Class 18 (80 points)

1. (80 points) You are given two unsigned 4-bit numbers  $M = 1010$  and  $Q = 1011$ .

- (50 points) Perform the multiplication  $M \times Q$  in binary in the same manner as Fig. 3.34 (b). Please keep track of the carry bits whenever addition is performed. The carry bits will be useful in part (b) below.
- (30 points) Annotate all 48 wires (each "?") in the 4 x 4 multiplier circuit as shown in Fig. 3.35 with 0 or 1 when  $M \times Q$  is performed. (Fig. 3.35 is also included below for your convenience.)

a)

$$\begin{array}{r}
 10101010 \\
 \times 1011 \\
 \hline
 10101010 \\
 +10101010 \\
 \hline
 11111111 \\
 +00000000 \\
 \hline
 01111111 \\
 +10101010 \\
 \hline
 11011110
 \end{array}$$



## Class 19 (70 points)

- (35 points) Represent the decimal number 15.625 in IEEE 754 single-precision (32 bit) floating-point format.  $01000001\ 0111010\ 00000000\ 00000000$
- (35 points) What is the decimal value of the following IEEE 754 single-precision floating-point number?  $1\ 10000001\ 011010000000000000000000$   $-5.625$

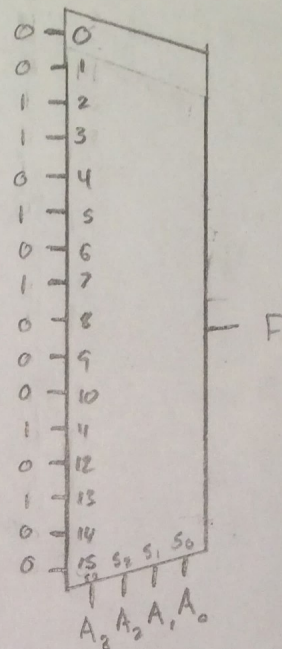


1)  $(A \cdot \bar{X}) + (B \cdot X)$

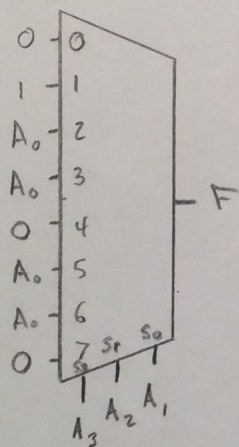
2) a)

$A_3$	$A_2$	$A_1$	$A_0$	$P$
0	0	0	0	0
0	0	0	1	0
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	1
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	1
1	0	1	1	1
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

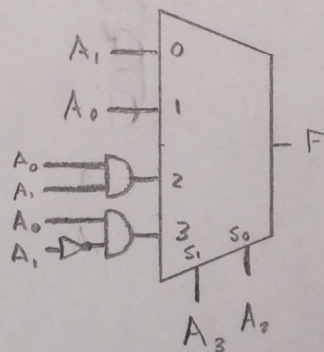
b)



c)



d)

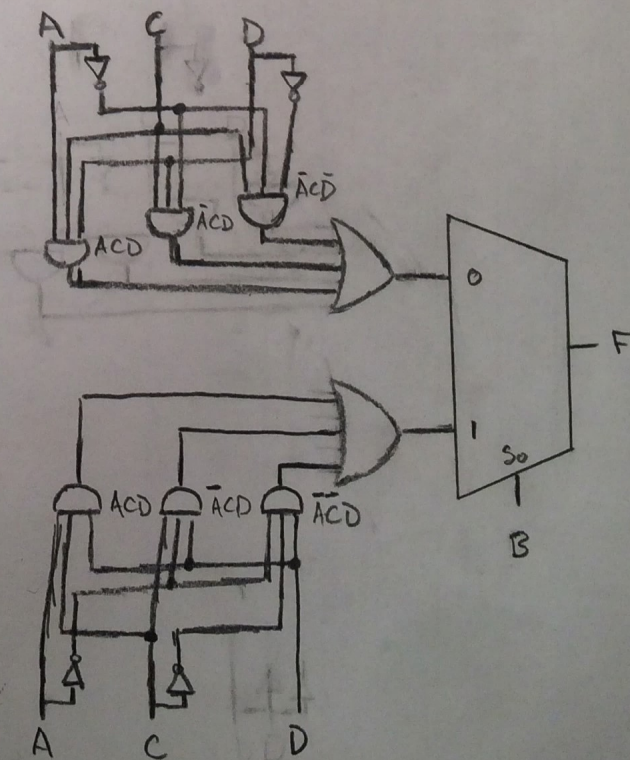


e)  $A_3 = A, A_2 = B, A_1 = C, A_0 = D$

$$F = \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D + A\bar{B}C\bar{D} + A\bar{B}CD$$

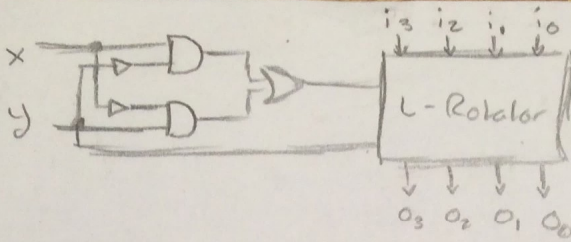
$$\Rightarrow \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + A\bar{B}\bar{C}\bar{D} + A\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + A\bar{B}C\bar{D} + A\bar{B}CD$$

$$\Rightarrow (\bar{A}\bar{C}\bar{D} + \bar{A}\bar{C}D + A\bar{C}\bar{D} + A\bar{C}D)\bar{B} + (\bar{A}\bar{C}\bar{D} + \bar{A}\bar{C}D + A\bar{C}\bar{D} + A\bar{C}D)B$$

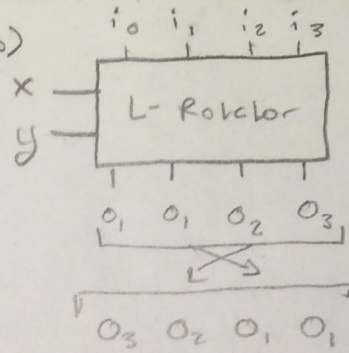




3) a)



b)



Sean Gordon

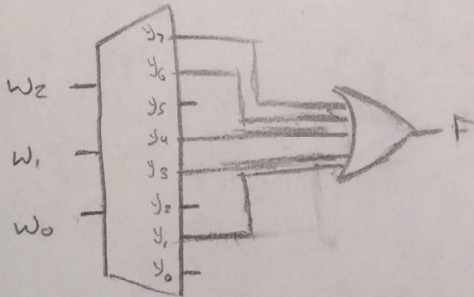
Class 22

1) a)  $\bar{w}_2 \bar{w}_1 w_0 + \bar{w}_2 w_1 w_0 + w_2 \bar{w}_1 \bar{w}_0 + w_2 w_1 \bar{w}_0 + w_2 w_1 w_0 = \bar{w}_2 w_0 + w_2 \bar{w}_0 + w_2 w_1$

b)  $|y_7 = w_2 w_1 w_0 \quad |y_6 = w_2 w_1 \bar{w}_0 \quad |y_5 = w_2 \bar{w}_1 w_0 \quad |y_4 = w_2 \bar{w}_1 \bar{w}_0 \quad |$

$|y_3 = \bar{w}_2 w_1 w_0 \quad |y_2 = \bar{w}_2 w_1 \bar{w}_0 \quad |y_1 = \bar{w}_2 \bar{w}_1 w_0 \quad |y_0 = \bar{w}_2 \bar{w}_1 \bar{w}_0 \quad |$

c)



2)

	$w_3$	$w_2$	$w_1$	$w_0$	$y_1$	$y_2$
0	0	0	0	0	0	0
1	0	0	0	1	0	0
2	0	0	1	0	0	1
3	0	0	1	1	0	1
4	0	1	0	0	1	0
5	0	1	0	1	1	0
6	0	1	1	0	1	0
7	0	1	1	1	1	0
8	1	0	0	0	1	1
9	1	0	0	1	1	1
10	1	0	1	0	1	1
11	1	0	1	1	1	1
12	1	1	0	0	1	1
13	1	1	0	1	1	1
14	1	1	1	0	1	1
15	1	1	1	1	1	1