



COM S-342

Recitation 10/29/18 – 10/31/18



Today

- Lambda Calculus (what computation this lambda expression represents?)
- Reflang programming

Lambda Encoding

- Functions
 - $f1 = (\lambda (m) (\lambda (n) (\lambda (f) (\lambda (x) (m\ f\ (n\ f\ x))))))$
 - $((f1\ two)\ one) = ???$
 - $f2 = (\lambda (m) (\lambda (n) (\lambda (f) (\lambda (x) (m\ (n\ f)\ x))))$
 - $(f2\ two)\ one) = ???$
 - $(f2\ two)\ three) = ???$

Lambda Encoding

- `((f1 two) one)`
 - `((((λ (m) (λ (n) (λ(f) (λ(x) (m f (n f x))))) two) one)`
 - `((λ (n) (λ(f) (λ(x) (two f (n f x))))) one)`
 - `(λ(f) (λ(x) (two f (one f x)) // remember ((two g) w)?`

Lambda Encoding

- $((f1\ two)\ one)$
 - $((((\lambda\ (m)\ (\lambda\ (n)\ (\lambda\ (f)\ (\lambda\ (x)\ (m\ f\ (n\ f\ x))))))\ two)\ one)$
 - $((\lambda\ (n)\ (\lambda\ (f)\ (\lambda\ (x)\ (two\ f\ (n\ f\ x))))))\ one)$
 - $(\lambda\ (f)\ (\lambda\ (x)\ (two\ f\ (one\ f\ x)))\ //\ remember\ ((two\ g)\ w)?$
 - $(\lambda\ (f)\ (\lambda\ (x)\ (two\ f\ (f\ x)))\ //\ remember\ ((two\ g)\ w)?$
 - $(\lambda\ (f)\ (\lambda\ (x)\ (f\ (f\ (f\ x))))$
 - $= ???$

Lambda Encoding

- $((f1\ two)\ one)$
 - $((((\lambda\ (m)\ (\lambda\ (n)\ (\lambda\ (f)\ (\lambda\ (x)\ (m\ f\ (n\ f\ x))))))\ two)\ one)$
 - $((\lambda\ (n)\ (\lambda\ (f)\ (\lambda\ (x)\ (two\ f\ (n\ f\ x)))))\ one)$
 - $(\lambda\ (f)\ (\lambda\ (x)\ (two\ f\ (one\ f\ x)))\ //\ remember\ ((two\ g)\ w)?$
 - $(\lambda\ (f)\ (\lambda\ (x)\ (two\ f\ (f\ x)))\ //\ remember\ ((two\ g)\ w)?$
 - $(\lambda\ (f)\ (\lambda\ (x)\ (f\ (f\ (f\ x))))$
 - $=\ three$
- $((f1\ three)\ two) = ???$



Lambda Encoding

- $(f2\ two)\ one) = ???$
- $(f2\ two)\ three) = ???$



Lambda Encoding

- $f1 = (\text{plus } m \ n)$
- $f2 = (\text{mult } m \ n)$

Lambda Encoding

- You can encode
 - If conditions (e.g. `ite`)
 - Boolean functions (e.g. `or` asked in hw)
 - Etc.
- When we ask what computation this represents, is just what computation does this encode?



RefLang

- We add extensions to our language to support side effects
- These extensions focus on reading and writing memory locations
- We need two concepts and definitions
 - Heap: memory reserved for dynamic alloc
 - References: locations in the heap

Reference Expressions

- Represent malloc expressions
- (ref 1): stores the value 1 in a fresh location
- (free (ref 1)): deallocate the location for (ref 1)
- (deref (ref 1)): dereference a previously allocated memory location
 - \$ (define loc (ref 3))
 - \$ (deref loc)
 - \$ 3

Reference Expressions

- (set! loc v): mutates the value of location *loc*, assigning value *v*
 - *\$ (define loc (ref 5))*
 - *\$ (deref loc)*
 - *\$ 5*
 - *\$ (set! loc 10)*
 - *\$ (deref loc)*
 - *\$ 10*

Examples RefLang

- \$ (define loc (ref 5))
- \$ (deref loc)
- \$ 5
- \$ (free loc)
- \$ (deref loc)
- \$ Error: null

Examples RefLang

- `$ (define l1 (ref 10))`
- `$ (define l2 (ref 20))`
- `$ l2`
- `$??`
- `$ (free l2)`
- `$ (l2)`
- `$??`
- `$ (set! l2 20)`
- `$ 20`
- `$ (deref l2)`
- `$??`
- `$ (define l2 (ref 30))`
- `$ l2`
- `$??`

Examples RefLang

- `$ (define l1 (ref 10))`
- `$ (define l2 (ref 20))`
- `$ l2`
- `$ 1`
- `$ (free l2)`
- `$ (l2)`
- `$ Error: null`
- `$ (set! l2 20)`
- `$ 20`
- `$ (deref l2)`
- `$ 20`
- `$ (define l2 (ref 30))`
- `$ l2`
- `$ 30`