## ComS 342 Recitation 2, 10:00 Tuesday Homework 6

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1a)
(( 
$$(\lambda(x)(x x)) (\lambda(y)(y x)) ) z$$
)
((  $(x x) [x \to \lambda(y)(y x)] ) z$ )

((  $(\lambda(y)(y x) \lambda(y)(y x)) ) z$ )
((  $(y x) [y \to \lambda(y)(y x)] ) z$ )

((  $(\lambda(y)(y x) x) ) z$ )
((  $(x x) [y \to x]) z$ )

((  $(x x) [y \to x]) z$ )

((  $(x x) [y \to x]) z$ )

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((  $(x x) [y \to x]) z$ )

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1c)
(((\lambda(x)(x x))(\lambda(y) y))(\lambda(y) y))
(((x x) [x \rightarrow \lambda(y) y]) (\lambda(y) y))
(((\lambda(y) y) (\lambda(y) y)) (\lambda(y) y))
((y [y \rightarrow (\lambda(y) y)]) (\lambda(y) y))
((\lambda(y) y) (\lambda(y) y))
(y [y \rightarrow (\lambda(y) y)])
(\lambda(y) y)
2a)
((\lambda(x) p) ((\lambda(y)(y y)) (\lambda(z)(z z)))
( (p) [x \rightarrow ( (\lambda(y)(y y)) (\lambda(z)(z z)) ) ] )
(p)
2b)
((\lambda(x) p) ((\lambda(y)(y y)) (\lambda(z)(z z)))
((\lambda(x) p) ((y y) [y \rightarrow (\lambda(z)(z z))]))
((\lambda(x) p) (((\lambda(z)(z z)) (\lambda(z)(z z))))
( (\lambda(x) p) ( (z z) [z \rightarrow (\lambda(z)(z z))] ) )
((\lambda(x) p) (((\lambda(z)(z z)) (\lambda(z)(z z))))
((\lambda(x) p) (((z z) [z \rightarrow (\lambda(z)(z z))])))
((\lambda(x) p) ((\lambda(z)(z z)) (\lambda(z)(z z)))
( (p) [x \rightarrow ((\lambda(z)(z z))(\lambda(z)(z z)))])
(p)
3) and = (\lambda(a)(\lambda(b)) ite a b false))
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4a)
((\lambda(z)((two f) z)) (succ zero))
((\lambda(z)((two f) z)) 1)
(((two f) z) [z \rightarrow 1])
((two f) 1)
(f(f(1)))
This function applies f to the successor of 0 (1) two times.
4b) zero = \lambda(f)(\lambda(x)x), one = \lambda(f)(\lambda(x) f(x)), two = \lambda(f)(\lambda(x) f(f(x)))
i. (g zero)
((\lambda(n)((n \text{ unknown}) \text{ false})) \text{ zero})
((zero unknown) false)
(((\lambda(f)(\lambda(x)x))) unknown) false)
(false)
ii. (g one)
((\lambda(n)((n \text{ unknown}) \text{ false})) \text{ one})
((one unknown) false)
(((\lambda(f)(\lambda(x) f(x)))) unknown) false)
(unknown (false))
((\lambda(x)(\lambda(y)(\lambda(z) y))) \text{ (false)})
(\lambda(y)(\lambda(z) y))
(true)
iii. (g two)
((\lambda(n)((n \text{ unknown}) \text{ false})) \text{ two})
((two unknown) false)
(((\lambda(f)(\lambda(x) f(f(x)))) \text{ unknown}) \text{ false})
(unknown (unknown (false)))
(unknown ((\lambda(x)(\lambda(y)(\lambda(z) y))) (false)))
(unknown (\lambda(y)(\lambda(z) y)))
(unknown (true))
((\lambda(x)(\lambda(y)(\lambda(z) y))) \text{ (true)})
((\lambda(y)(\lambda(z) y)))
(true)
    iv. (n != 0)
```

Algorithm 1	$oldsymbol{U}$ :	gev
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Boof