Cpr E 489 Spring 2020

Homework #2

Due Date: 2/13/2020 (Thu) by 11:00 AM Type your answers and submit on Canvas

1. (40 points)

Consider the 2-out-of-5 error detection code. In this code, each codeword is 5-bit long; 2 out of 5 bits are "1"s and the others are "0"s. For example, 11000 is a valid codeword, but 01110 is not.

- a. (10 points) List all the valid codewords.
- b. (15 points) What fraction of errors is undetectable by this code, i.e., what is the FUE of this code? Justify your answer.
- c. (15 points) What fraction of *4-bit errors* is undetectable by this code, i.e., what is the FUE(M=4) of this code? Justify your answer.

2. (60 points)

Consider a CRC code with a generator polynomial of $g(x) = x^4 + x^3 + 1$.

- a. (20 points) Show step by step (using the longhand division) how to find the codeword that corresponds to information bits of 1101.
- b. (20 points) Show the shift-register circuit that implements this CRC code.
- c. Suppose the codeword length is 8. Answer the following questions, with proper justifications.
 - i. (10 points) Give an example of undetectable error burst of length 6;
 - ii. (10 points) Give an example of undetectable 6-bit error;