Show all of your work, and *please* staple your assignment if you use more than one sheet. Write your name, the course number and the section on every sheet. Problems marked with \* will be graded and one additional randomly chosen problem will be graded.

- 1. \* A coin is tossed three times, and the sequence of heads and tails is recorded.
  - (a) Determine the sample space,  $\Omega$ .
  - (b) List the elements that make up the following events: i. A = exactly two tails, ii. B = at least two tails, iii. C = the last two tosses are heads

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- (c) List the elements of the following events: i.  $\overline{A}$ , ii.  $A \cup B$ , iii.  $A \cap B$ , iv.  $A \cap C$
- 2. Let a sample space  $\Omega = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$ . Let  $A = \{1, 3, 5\}$  and  $B = \{1, 5, 10\}$  be two events. Verify DeMorgan's Laws on events A and B by showing the events on both sides of the = sign contain the same outcomes.
  - (a)  $\overline{A \cap B} = \overline{A} \cup \overline{B}$
  - (b)  $\overline{A \cup B} = \overline{A} \cap \overline{B}$
- 3. Suppose a six sided die is rolled and the probability of each number occurring is proportional to itself, i.e.  $\mathbb{P}(1) = 1k, \mathbb{P}(2) = 2k...$  Give the probabilities for each number being rolled so that the axioms of probability are satisfied.
- 4. Two fair dice are tossed and the number on each die is recorded, e.g. (3,2) indicates the first die had a 3 and the second die had a 2.
  - (a) Write down the sample space (Hint: there are 36 outcomes.).

    Assume all outcomes in the sample space are equally likely for the next problems
  - (b) What is the probability that the sum of the two numbers is 7?
  - (c) What is the probability that the sum of the two numbers is 7 or 11?
  - (d) What is the probability of getting an even on the first die or a total of 11?
- 5. Suppose that after 10 years of service, 35% of computers have problems with motherboards (MB), 30% have problems with hard drive (HD), and 20% have problems with both MB and HD.
  - (a) What is the probability that a 10-year old computer has a problem with MB or HD?
  - (b) What is the probability that a 10-year old computer still has a fully functioning MB and HD?
- 6. \* The probability that a visit to a physician's office results in neither lab work nor referral to a specialist is 50%. Also, suppose in visits to a physician's office, 30% are referred to specialists and 40% require lab work.
  - (a) Calculate the probability that a visit to a physician's office results in both lab work and referral to a specialist.
  - (b) Calculate the probability that a visit results in lab work or referral to a specialist.
  - (c) Calculate the probability that a visit results in only one of the actions (lab work and no referral or no lab work and referral).