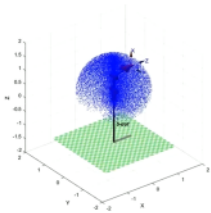


rtbdemo轨迹规划1

2024年12月8日 10:22

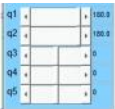
机器人工具箱 工作空间可视化

关节空间随机生成变量  $\xrightarrow{\text{fkine}}$  变换矩阵  $\xrightarrow{\text{transl}}$  三维坐标



rand函数:  
 $x = \text{rand}$  returns a single uniformly distributed random number in the interval (0,1).  
在[m,n]内随机生成一个数字:  
 $m + \text{rand} * (n - m)$   
随机关节空间变量:  
 $q = q_{\min} + \text{rand} * (q_{\max} - q_{\min})$

默认关节范围:



关节限制是Link类的一个属性: Link.qlim

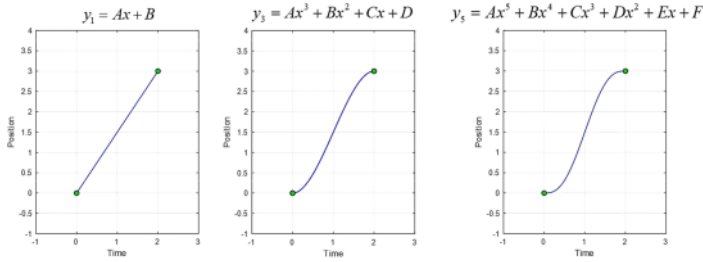
定义关节限制:  
`L(1).qlim = [-150, 150]/180*pi;`  
`L(2).qlim = [-100, 90]/180*pi;`  
`L(3).qlim = [-90, 90]/180*pi;`  
`L(4).qlim = [-100, 100]/180*pi;`  
`L(5).qlim = [-180, 180]/180*pi;`  
  
`L(1) = Link('revolute','d',0.216,'a',0,'alpha',pi/2, ...`  
`'qlim', [-150, 150]/180*pi);`  
`L(2) = Link('revolute','d',0,'a',0.5,'alpha',0,'offset',pi/2, ...`  
`'qlim', [-100, 90]/180*pi);`

然后你像查看相应的呃关节的一个关节限制的话

num = 30000; 然后num呢是迭代次数

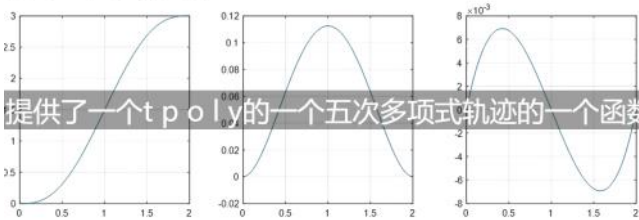
```
P = zeros(num, 3);  
  
for i=1:num  
    q1 = L(1).qlim(1) + rand * ( L(1).qlim(2) - L(1).qlim(1) );  
    q2 = L(2).qlim(1) + rand * ( L(2).qlim(2) - L(2).qlim(1) );  
    q3 = L(3).qlim(1) + rand * ( L(3).qlim(2) - L(3).qlim(1) );  
    q4 = L(4).qlim(1) + rand * ( L(4).qlim(2) - L(4).qlim(1) );  
    q5 = L(5).qlim(1) + rand * ( L(5).qlim(2) - L(5).qlim(1) );  
  
    q = [q1 q2 q3 q4 q5];  
  
    T = Five_dof.fkine(q);  
  
    P(i, :) = transl(T);  
end  
  
plot3(P(:,1), P(:,2), P(:,3), 'b.', 'markersize', 1);
```

轨迹: 时间、位置、速度、加速度  
给定时间 0—2s, 位置0—3



五次多项式轨迹 tpoly:

`t = linspace(0, 2, 51);`  
`[P, dP, ddP] = tpoly(0, 3, t);`

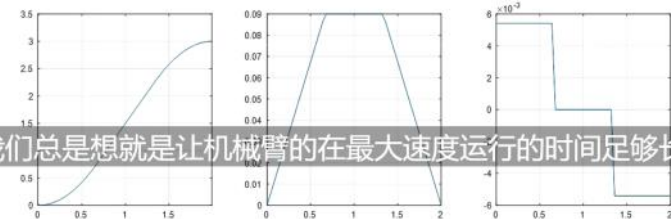


提供了一个tpoly的一个五次多项式轨迹的一个函数

指定初末速度: `[P, dP, ddP] = tpoly(0, 3, 51, 0.02, 0.01);`

混合曲线轨迹 lspb:

`t = linspace(0, 2, 51);`  
`[P, dP, ddP] = lspb(0, 3, t);`

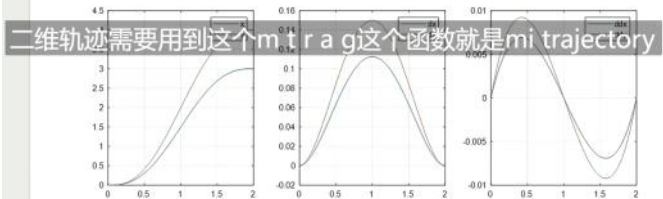


我们总是想就是让机械臂的在最大速度运行的时间足够长

指定最大速度: `[P, dP, ddP] = lspb(0, 3, 51, 0.1);`

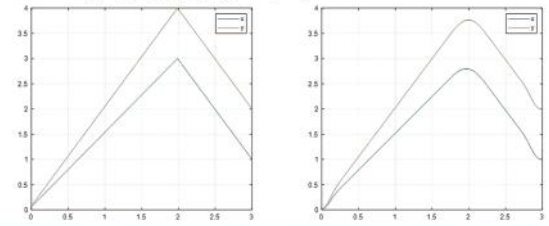
多维轨迹 mtraj: (0, 0) → (3, 4)

`t = linspace(0, 2, 51);`  
`[P, dP, ddP] = mtraj(@tpoly, [0, 0], [3, 4], t);`



二维轨迹需要用到这个mtraj这个函数就是mi trajectory

多维多段轨迹 `mstraj`:  $(0, 0) \xrightarrow{2s} (3, 4) \xrightarrow{1s} (1, 2)$   
`TRAJ = mstraj(WP, QDMAX, TSEG, Q0, DT, TACC, OPTIONS)`  
`wp = [0, 0; 3, 4; 1, 2];`  
`P1 = mstraj(wp, [ ], [2, 1], [ ], 0.04, 0);`  
`P2 = mstraj(wp, [ ], [2, 1], [ ], 0.04, 0.5);`



这时候就要用到多维多端轨迹 `mstraj` 这个函数咯

81.运动轨迹规划2

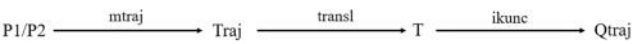
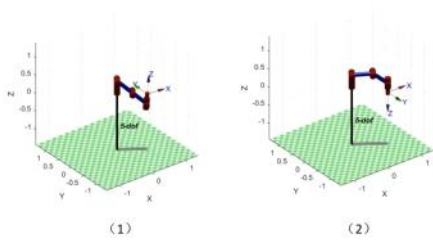
给定位置： (0.7, -0.5, 0) → (0.7, 0.5, 0.5)

```
T1 = transl(0.7, -0.5, 0);
T2 = transl(0.7, 0.5, 0.5);

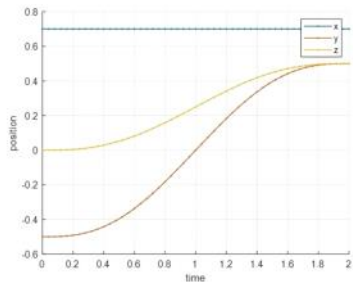
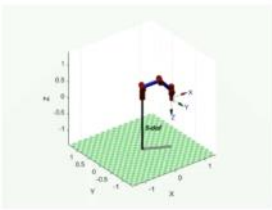
q1 = Five_dof.ikunc(T1);
q2 = Five_dof.ikunc(T2);

Five_dof.plot(q1);
pause;
Five_dof.plot(q2);
```

增加姿态： trotx(180)



轨迹： 'trail', 'b'  
保存动画： 'movie', 'trail.gif'



```
运行and保存一个动画
% Five_dof.plot(Qtraj, 'trail', 'b');
% Five_dof.plot(Qtraj, 'movie', 'trail.gif');I
```

```
%%绘制xyz的曲线图

hold on

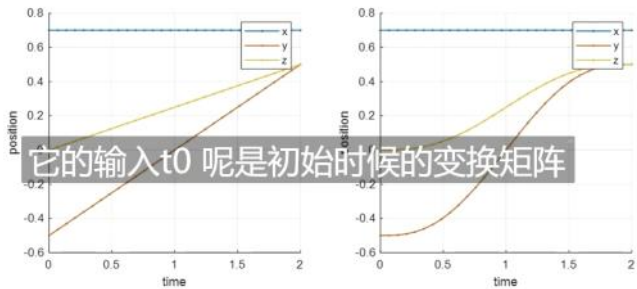
plot(t, Traj(:, 1), '-.', 'linewidth', 1);
plot(t, Traj(:, 2), '-.', 'linewidth', 1);
plot(t, Traj(:, 3), '-.', 'linewidth', 1);

grid on
legend('x', 'y', 'z');
xlabel('time');
ylabel('position')
```

位姿插值 trinterp:

trinterp(T0, T1, M) as above but M is a positive integer and return a sequence (4x4xM) of homogeneous transforms linearly interpolating between T0 and T1 in M steps.

```
T = trinterp(T1, T2, 51);
T = trinterp(T1, T2, tpoly(0, 2, 51) / 2);
```



线性差值

```
T_linear = trinterp(T1, T2, 51);
P_linear = transl(T_linear);
t1 = linspace(0, 2, 51);

subplot(1, 2, 1);
hold on
plot(t1, P_linear(:, 1), '-.', 'linewidth', 1);
plot(t1, P_linear(:, 2), '-.', 'linewidth', 1);
```

5次多项式差值

笛卡尔轨迹ctrqaj:

TC = ctraj(T0, T1, N) is a Cartesian trajectory (4x4xN) from pose T0 to T1 with N points that follow a trapezoidal velocity profile along the path. The Cartesian trajectory is a homogeneous transform sequence and the last subscript being the point index, that is, T(:, :, i) is the i'th point along the path.

```

t1 = linspace(0, 2, 51);

subplot(1, 2, 1);
hold on
plot(t1, P_inert(, 1), '-o', 'linewidth', 1);
plot(t1, P_inert(, 2), '-o', 'linewidth', 1);
plot(t1, P_inert(, 3), '-o', 'linewidth', 1);

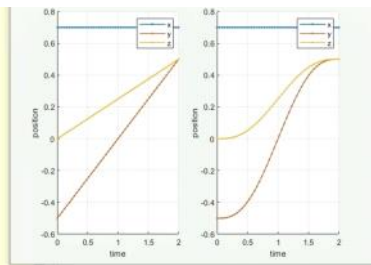
grid on
legend('x', 'y', 'z');
xlabel('time');
ylabel('position')

T_tpoly = trinterp(T1, T2, tpoly(0, 2, 50) / 2);
P_tpoly = trans(T_tpoly);
t2 = linspace(0, 2, 50);clc

subplot(1, 2, 2);
hold on
plot(t2, P_tpoly(, 1), '-o', 'linewidth', 1);
plot(t2, P_tpoly(, 2), '-o', 'linewidth', 1);
plot(t2, P_tpoly(, 3), '-o', 'linewidth', 1);

grid on

```



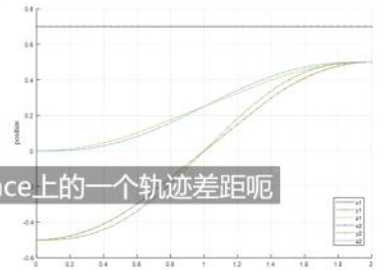
哎这时候就可以运行啊

$TC = \text{ctrjaj}(T0, T1, N)$  is a Cartesian trajectory ( $4 \times 4 \times N$ ) from pose  $T0$  to  $T1$  with  $N$  points that follow a trapezoidal velocity profile along the path. The Cartesian trajectory is a homogeneous transform sequence and the last subscript being the point index, that is,  $T(:, :, i)$  is the  $i$ 'th point along the path.

$T = \text{ctrjaj}(T1, T2, 51);$

$T = \text{ctrjaj}(T1, T2, \text{tpoly}(0, 2, 50) / 2);$

就表示在condition space上的一个轨迹差距呢



# rtbdemo轨迹规划3

2024年12月8日 10:51

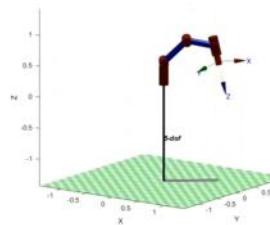
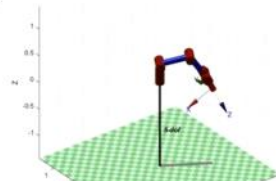
## 轨迹规划 (3)

给定位置和姿态:  $(0.7, -0.5, 0) * \text{troty}(150) \longrightarrow (0.7, 0.5, 0.5) * \text{trotx}(200)$

```
T1 = transl(0.7, -0.5, 0) * troty(150);
T2 = transl(0.7, 0.5, 0.5) * trotx(200);

q1 = Five_dof.ikunc(T1);
q2 = Five_dof.ikunc(T2);

Five_dof.plot(q1);
pause;
Five_dof.plot(q2);
```



运行程序呢跟之前差不多

%%

```
T1 = transl(0.7, -0.5, 0) * troty(150);
T2 = transl(0.7, 0.5, 0.5) * trotx(200);

q1 = Five_dof.ikunc(T1);
q2 = Five_dof.ikunc(T2);

Five_dof.plot(q1);
pause;
Five_dof.plot(q2);
```

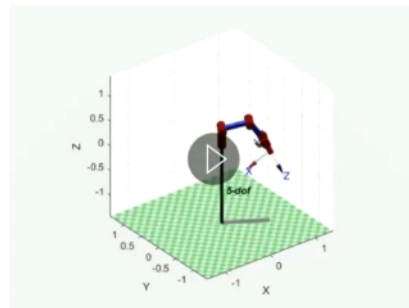
$T1, T2 \xrightarrow{\text{tr2rpy}} \text{rpy1}, \text{rpy2} \xrightarrow{\text{mtraj}} \text{rpy\_traj} \xrightarrow{\text{rpy2tr}} T\_traj\_rot$

```
rpy1 = tr2rpy(T1) / pi * 180;
rpy2 = tr2rpy(T2) / pi * 180;
```

```
t = linspace(0, 2, 51);
rpy_traj = mtraj(@tpoly, rpy1, rpy2, t);
T_traj_rot = rpy2tr(rpy_traj);
```

```
P1 = transl(T1);
P2 = transl(T2);
P_traj = mtraj(@tpoly, P1, P2, t);
T_traj_transl = transl(P_traj);
```

```
n = length(t);
T_traj = zeros(4, 4, n);
for i = 1:n
    T_traj(:, :, i) = T_traj_transl(:, :, i) * T_traj_rot(:, :, i);
end
```

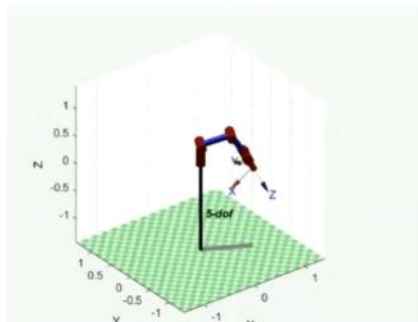


其实可以类比于之前位移的规划对吧

**trinterp:**

```
t = linspace(0, 2, 51);  
T_traj = trinterp(T1, T2, t/2);  
q = Five_dof.ikunc(T_traj);
```

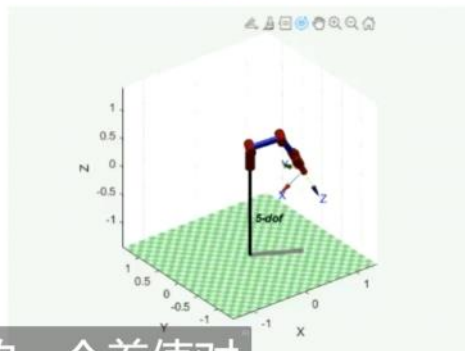
```
Five_dof.plot(q, 'trail', 'r')
```



**ctrjaj:**

```
t = linspace(0, 2, 51);  
T_traj = ctraj(T1, T2, t/2);  
q = Five_dof.ikunc(T_traj);
```

```
Five_dof.plot(q, 'trail', 'r')
```

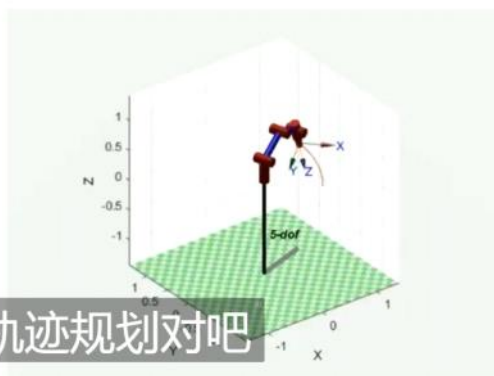


然后这个是梯形速度图像的一个差值对

$[Q, QD, QDD] = \text{jtraj}(Q0, QF, M)$  is a joint space trajectory  $Q$  ( $M \times N$ ) where the joint coordinates vary from  $Q0$  ( $1 \times N$ ) to  $QF$  ( $1 \times N$ ). A quintic (5th order) polynomial is used with default zero boundary conditions for velocity and acceleration. **最好用的一集** Time is assumed to vary from 0 to 1 in  $M$  steps. Joint velocity and acceleration can be optionally returned as  $QD$  ( $M \times N$ ) and  $QDD$  ( $M \times N$ ) respectively. The trajectory  $Q$ ,  $QD$  and  $QDD$  are  $M \times N$  matrices, with one row per time step, and one column per joint.

```
q1 = Five_dof.ikunc(T1);  
q2 = Five_dof.ikunc(T2);
```

```
t = linspace(0, 2, 51);  
q_traj = jtraj(q1, q2, t);
```



然后再对这个关节变量做轨迹规划对吧

$[Q, QD, QDD] = \text{jtraj}(Q0, QF, T, QD0, QDF)$  as above but specifies initial and final joint velocity for the trajectory and a time vector.



## 83.matlab三维mod

2024年12月8日 10:59

```

clear;
clc;

L(1)=Link('revolute','d',0.216,'a',0,'alpha',pi/2);
L(2)=Link('revolute','d',0,'a',0.5,'alpha',0,'offset',pi/2);
L(3)=Link('revolute','d',0,'a',sqrt(0.145^2+0.42746^2),'alpha',0,'offset',-atan(427.46/145));
L(4)=Link('revolute','d',0,'a',0,'alpha',pi/2,'offset',atan(427.46/145));
L(5)=Link('revolute','d',0.258,'a',0,'alpha',0);

Five_dof=SerialLink(L,'name','5-dof');
Five_dof.base=transl(0,0,0.28);

q0=[0 0 0 0 0];
v=[35 20];
w=[-1 1 -1 1 0 2];

Five_dof.plot3d(q0,'tilesize',0.1,'workspace',w,'path','E:\SW Data\Fdof','nowrist','view',v)

light('Position',[1 1 1],'color','w');
    
```

'path',P  
'workspace',W  
'floorlevel',L  
'delay',D

Override path to folder containing STL model files  
Size of robot 3D workspace, W = [xmn, xmx ymn, ymx zmn, zmx]  
Z-coordinate of floor (default = 1)  
Delay between frames for animation (s)

只能用于标准型的函数建模  
pass后面接的是包含stl模型文件



```

clear;
clc;

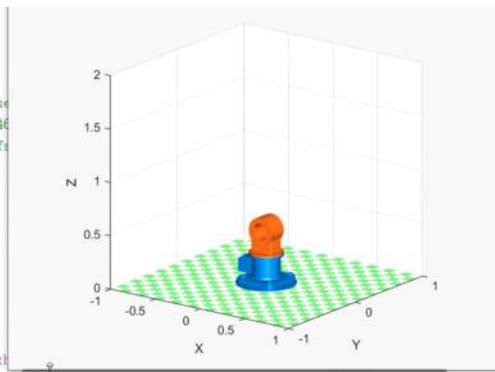
L(1)=Link('revolute','d',0.216,'a',0,'alpha',pi/2);
% L(2)=Link('revolute','d',0,'a',0.5,'alpha',0,'offset',pi/2);
% L(3)=Link('revolute','d',0,'a',sqrt(0.145^2+0.42746^2),'alpha',0,'offset',-atan(427.46/145));
% L(4)=Link('revolute','d',0,'a',0,'alpha',pi/2,'offset',atan(427.46/145));
% L(5)=Link('revolute','d',0.258,'a',0,'alpha',0);

Five_dof=SerialLink(L,'name','5-dof');
Five_dof.base=transl(0,0,0.28);

q0=[0 0 0 0 0];
v=[35 20];
w=[-1 1 -1 1 0 2];

Five_dof.plot3d(q0,'tilesize',0.1,'workspace',w,'path','E:\SW Data\Fdof','nowrist','view',v)

light('Position',[1 1 1],'color','w');
    
```

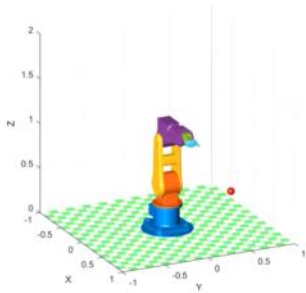


跟那个cd模型是吻合的对吧

## 搬运仿真

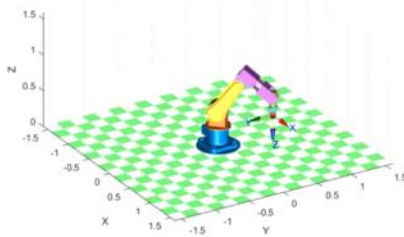
```
plot_sphere(position, radius, color)
```

```
position = [0.5 0.5 0.5]
```



ikunc jtraj plot3d

姿态  
 $T = \text{transl}(\text{position}) * \text{rpy2tr}(180, 0, 0)$



```
%% pick
```

```
Positon = [0.5 0.5 0.5];
```

```
r = 0.04;
```

```
plot_sphere(Positon, r, 'r');
```

```
Tl = transl(Positon) * rpy2tr(180, 0, 0);
```

```
q1 = Five_dof.ikunc(Tl);
```

```
q = jtraj(q0, q1, 60);
```

```
Five_dof.plot3d(q, 'view', v, 'fps', 60, 'nowrist');
```

## 搬运仿真

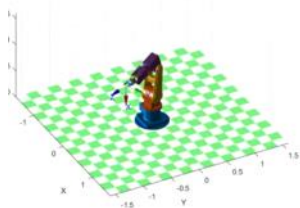
```
position2 = [0.5, -0.5, 1]
```

```
T2 = transl(position2) * rpy2tr(90, 90, 0)
```

```
q2 = Five_dof.ikunc(T2);
```

```
q = jtraj(q1, q2, 30);
```

```
plot3d ?
```



```
for i = 1:30
```

```
qi = q(i, :);
```

```
fkine
```

```
Ti
```

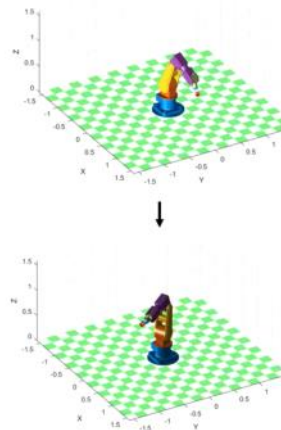
```
transl
```

```
Pi
```

```
plot_sphere
```

```
plot3d
```

```
end for
```



```
for i = 1:30
```

```
qi = q(i, :);
```

```
Ti = Five_dof.fkine(qi);
```

```
Pi = transl(Ti);
```

```
plot_sphere(Pi, r, 'r');
```

```
Five_dof.plot3d(qi, 'view', v, 'nowrist');
```

```
cla
```

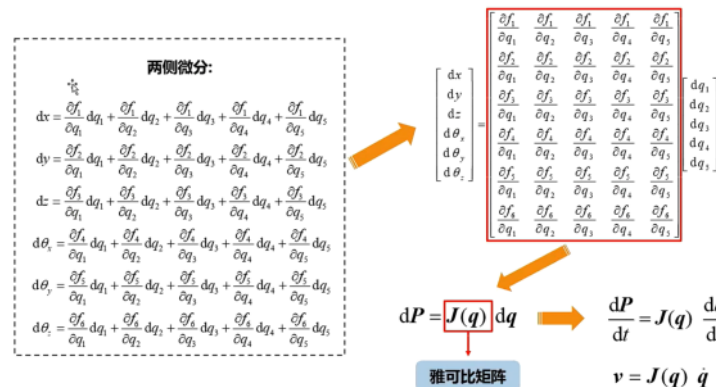
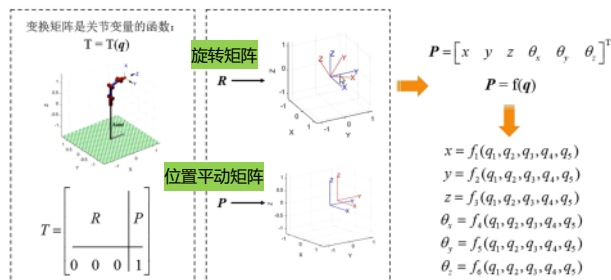
```
end
```



# 雅可比矩阵

2024年12月8日 11:18

## 雅可比矩阵



**Jacob0:**

`J0 = R.jacob0(Q, OPTIONS)` is the Jacobian matrix (6xN) for the robot in pose Q (1xN), and N is the number of robot joints. The manipulator Jacobian matrix maps joint velocity to end-effector spatial velocity  $V = J0*\dot{Q}$  expressed in the world-coordinate frame.

**Five\_dof . Jacob0(q0):**

-0.0000	-0.6450	-0.1450	0.0000	0
0.6855	0.0000	0.0000	0.0000	0
0.0000	0.6855	0.2580	0	0
-0.0000	0	0	0	1.0000
0.0000	-1.0000	-1.0000	-1.0000	-0.0000
1.0000	0.0000	0.0000	0.0000	-0.0000

这个返回的是世界坐标系下的雅可比矩阵

`J1 = R.jacob0(Q, options)` is the Jacobian matrix (6xN) for the robot in pose Q, and N is the number of robot joints. The manipulator Jacobian matrix maps joint velocity to end-effector spatial velocity  $V = J1*\dot{Q}$  in the end-effector frame.

**Five\_dof . Jacob1(q0):**

0.0000	0.6855	0.6855	0.2580	0
-0.6855	0.0000	0.0000	0	0
-0.0000	-0.6450	-0.1450	0	0
1.0000	0	0	0	0
0.0000	1.0000	1.0000	1.0000	0
-0.0000	0.0000	0.0000	0.0000	1.0000

一个是世界坐标系下的雅可比矩阵，then一个是执行器下的雅可比矩阵

那我们自己可以尝试着去把这两个雅可比矩阵联系起来呢

**Five\_dof . fline(q0):**

0	0	1	0.6855
0	-1	0	0
1	0	0	1.141

$R = \begin{bmatrix} R & R \end{bmatrix}$

$J_e = R J_0$

$J_0 = R^{-1} J_e$

**Five\_dof . Jacob0(q0, 'trans'):**

-0.0000	-0.6450	-0.1450	0.0000	0
0.6855	0.0000	0.0000	0.0000	0
-0.0000	0.6855	0.6855	0.2580	0

**Five\_dof . Jacob0(q0, 'rot'):**

-0.0000	0	0	0	1.0000
0.0000	-1.0000	-1.0000	-1.0000	-0.0000
1.0000	0.0000	0.0000	0.0000	-0.0000

%%

`q1 = [pi/2 0 0 0 0];`

`t = 0:0.05:2;`

`[Q, dQ, ddQ] = jtraj(q0, q1, t);`

`Five_dof.plot(Q);`

-0.0000	-0.6450
0.6855	-0.0000
0.0000	0.6855
-0.0000	0.0000
-0.0000	-1.0000
1.0000	-0.0000

这是他第一个关节从零转到90度啊