

We use Master Theorem when we have a recursive function in the form:  $T(n) = a.T(n/b) + f(n)$  and we want to express  $T(n) = \Theta(?)$

1. We check that  $a, b$  are constants and  $a \geq 1, b > 1, f(n)$  is non-negative function.

If any of these conditions does not hold, theorem is not applicable

We test the three cases:

CASE #1:  $f(n) = O(n^c)$  &  $c < \log_b(a)$   $\Rightarrow T(n) = \Theta(n^{\log_b a})$

CASE #2:  $f(n) = \Theta(n^c \cdot \log^k(n))$  &  $c = \log_b(a)$  &  $(k \geq 0)$   $\Rightarrow T(n) = \Theta(n^{\log_b a} \cdot \log^{k+1}(n))$

CASE #3:  $f(n) = \Omega(n^c)$  &  $c > \log_b(a)$  &  $a.f(n/b) \leq k.f(n)$  &  $k < 1 \Rightarrow T(n) = \Theta(f(n))$

If none of them holds then the BASIC form of Master theorem does not hold

For CASE #2 if all conditions hold except  $(k \geq 0)$  then the extended theorem holds.