MNIST Neural Shrub-Leaves

July 15, 2019

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In [3]: import time
        import mnist
        import numpy as np
        from sklearn.tree import DecisionTreeClassifier
        from sklearn.tree import export_graphviz
        from sklearn.externals.six import StringIO
        from IPython.display import Image
        import pydotplus
        from keras.utils import np_utils
        from keras import Sequential
        from keras import layers
In [4]: # gets the data
        def get_data():
            test = mnist.test_images()
            label_test = mnist.test_labels()
            train = mnist.train_images()
            label_train = mnist.train_labels()
            nsamples, nx, ny = train.shape
            train = train.reshape((nsamples,nx*ny))
            nsamples, nx, ny = test.shape
            test = test.reshape((nsamples,nx*ny))
            return train, label_train, test, label_test
In [5]: from sklearn.tree._tree import TREE_LEAF
        def prune_index(inner_tree, index, threshold):
            if inner_tree.value[index].min() < threshold:</pre>
                # turn node into a leaf by "unlinking" its children
                inner_tree.children_left[index] = TREE_LEAF
                inner_tree.children_right[index] = TREE_LEAF
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# if there are shildren, visit them as well
            if inner_tree.children_left[index] != TREE_LEAF:
                prune_index(inner_tree, inner_tree.children_left[index], threshold)
                prune_index(inner_tree, inner_tree.children_right[index], threshold)
In [6]: # builds the decision tree of depth 10
        def decision_tree(train, label):
            dt = DecisionTreeClassifier(max_depth = 10, random_state = 1)
            dt.fit(train, label)
            prune index(dt.tree , 0, 1)
            return dt
In [7]: # building the neural network
        def neural_network(class_data):
            num train = []
            num_label = []
            for x in class_data:
                num_train.append(x[0])
                num_label.append(x[1])
            n_{classes} = 10
            num_train = np.matrix(num_train).astype('float32')/255
            num_label = np.array(num_label)
            num_label = np_utils.to_categorical(num_label, n_classes)
            model = Sequential()
            model.add(layers.Dense(512, activation = 'relu', input_shape=(784,)))
            model.add(layers.Dense(512, activation = 'relu'))
            model.add(layers.Dense(10, activation = 'softmax'))
            model.compile(loss='categorical_crossentropy', metrics=['accuracy'], \
                          optimizer='adam')
            model.fit(num_train, num_label, batch_size=128, epochs=10)
            return model
In [8]: # builds the neural shrub
        def neural_shrubs(tree, train, label):
            train = np.array(train)
            label = np.array(label)
            # leave id: index of the leaf that cantains the instance
            leave_id = tree.apply(train)
            classes = dict()
            for x in range(len(train)):
                leaf = leave_id[x]
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#.value: contains value of all the tree nodes
                #.value[leaf]: returns the value of the leaf
                #idx = tree.tree_.value[leaf][0][0]
                # insert the instance into the class
                if leaf in classes.keys():
                    classes[leaf].append([train[x], label[x]])
                else:
                    classes[leaf] = [[train[x], label[x]]]
            # stores the neural network for each class
            nn_models = dict()
            #stores the max time taken to build a neural network
            max_time = 0;
            for key in classes.keys():
                start = time.time()
                model = neural_network(classes[key])
                end = time.time()
                time_taken = end - start
                if max_time < time_taken:</pre>
                    max_time = time_taken
                nn_models[key] = model
            # returns a neural network for each class and the max
            # time taken to build the neural network
            return nn_models, max_time
In [9]: # The algorithm to build the neural shrub
        train, train_label, test, test_label = get_data()
        dt_start = time.time()
        tree = decision_tree(train, train_label)
        dot_data = StringIO()
        export_graphviz(tree, out_file=dot_data)
        graph = pydotplus.graph_from_dot_data(dot_data.getvalue())
        Image(graph.create_png())
        dt_end = time.time()
In [10]: shrubs, max_time = neural_shrubs(tree, train, train_label)
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Gets the class for each leaf

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89/89 [============= ] - Os 351us/step - loss: 0.4429 - acc: 0.8764
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89/89 [============ ] - Os 153us/step - loss: 0.1496 - acc: 0.9326
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200/200 [============= ] - Os 232us/step - loss: 0.0770 - acc: 0.9800
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8/8 [============= ] - Os 2ms/step - loss: 0.0547 - acc: 1.0000
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100/100 [============= ] - Os 178us/step - loss: 0.3994 - acc: 0.9200
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17/17 [============] - Os 835us/step - loss: 0.1079 - acc: 1.0000
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66/66 [=============] - Os 290us/step - loss: 0.8468 - acc: 0.7424
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66/66 [============== ] - Os 209us/step - loss: 0.2102 - acc: 0.9545
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88/88 [============== ] - Os 173us/step - loss: 0.4630 - acc: 0.8523
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75/75 [===========] - Os 228us/step - loss: 0.8772 - acc: 0.7600
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75/75 [===========] - Os 221us/step - loss: 0.8499 - acc: 0.7600
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75/75 [============= ] - Os 203us/step - loss: 0.5883 - acc: 0.8667
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66/66 [============== ] - Os 262us/step - loss: 0.4026 - acc: 0.8636
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66/66 [=============] - Os 224us/step - loss: 0.3096 - acc: 0.9242
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77/77 [===========] - Os 232us/step - loss: 0.3219 - acc: 0.8961
Epoch 9/10
77/77 [===========] - Os 244us/step - loss: 0.2449 - acc: 0.9481
Epoch 10/10
77/77 [===========] - Os 231us/step - loss: 0.1858 - acc: 0.9870
Epoch 1/10
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55/55 [============] - Os 317us/step - loss: 0.1440 - acc: 0.9636
Epoch 8/10
Epoch 9/10
55/55 [============] - Os 352us/step - loss: 0.1279 - acc: 0.9636
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7/7 [==========] - Os 2ms/step - loss: 0.0012 - acc: 1.0000
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93/93 [============= ] - Os 253us/step - loss: 0.6017 - acc: 0.8065
Epoch 7/10
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70/70 [============] - Os 236us/step - loss: 0.4421 - acc: 0.9143
Epoch 8/10
Epoch 9/10
70/70 [============= ] - Os 306us/step - loss: 0.2153 - acc: 0.9857
Epoch 10/10
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In [11]: # predicts using the neural shrub
  def neural_shrub_predict(tree, nn_model, test, label):
   label_test = np.array(label)
   test = np.array(test)
   #row - actual; col - pred
   confusion_matrix = np.zeros((10,10), dtype=np.int)
```

```
correct = 0
             for i in range(len(test)):
                 x = test[i]
                 pred_class = tree.apply([x])
                 x = np.array([x])
                 nn_model_class = nn_model[pred_class[0]]
                 pred = np.argmax(nn_model_class.predict(x))
                 confusion_matrix[label[i]][pred] = \
                     confusion_matrix[label[i]][pred] + 1
                 if pred == label[i]: correct = correct + 1
             acc_score = correct/len(test)
             return confusion_matrix, acc_score
In [12]: # function to calculate the metrics
         def metrics(cm, cls, size):
             cm = np.array(cm)
             tp = cm[cls][cls]
             fp = sum(cm[x, cls] for x in range(10))-cm[cls][cls]
             fn = sum(cm[cls, x] for x in range(10))-cm[cls][cls]
             tn = size - tp - fp - fn
             precision = tp/(tp+fp)
             recall = tp/(tp+fn)
             fmeasure = 2*(precision*recall)/(precision + recall)
             accuracy = (tp + tn)/size
             return precision, recall, fmeasure, accuracy
In [13]: # Predicting
         cm, acc_score = neural_shrub_predict(tree, shrubs, test, test_label)
         print("Confusion Matrix:\n\n", cm)
Confusion Matrix:
 [[ 960
                     0
                          1
                               5
                                    4
                                         1
                                                    1]
               4
                    4
                                              5
                                                   0]
     0 1117
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    1
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                                         3 904
 4
          2
               3
                   10
                        19
                                              7 940]]
                             11
                                    0
                                        13
```

```
In [14]: # Class 0
        precision0, recall0, f0, acc0 = metrics(cm, 0, len(test))
                      Precision Recall F-measure Accuracy")
        print("Class 0: ", round(precision0, 3), " ", round(recall0, 3), \
              " ", round(f0, 3), " ", round(acc0,3))
       Precision Recall F-measure Accuracy
Class 0: 0.961
               0.98
                       0.97
                                 0.994
In [15]: # Class 1
        precision1, recall1, f1, acc1 = metrics(cm, 1, len(test))
        print(" Precision Recall F-measure Accuracy")
        print("Class 1: ", round(precision1, 3), " ", round(recall1, 3), \
              " ", round(f1, 3), " ", round(acc1,3))
       Precision Recall F-measure Accuracy
Class 1: 0.985 0.984
                         0.985
In [16]: # Class 2
        precision2, recall2, f2, acc2 = metrics(cm, 2, len(test))
                     Precision Recall F-measure Accuracy")
        print("Class 2: ", round(precision2, 3), " ", round(recall2, 3), \
              " ", round(f2, 3), " ", round(acc2,3))
       Precision Recall F-measure Accuracy
Class 2: 0.94 0.94 0.94
                                0.988
In [17]: # Class 3
        precision3, recall3, f3, acc3 = metrics(cm, 3, len(test))
                  Precision Recall F-measure Accuracy")
        print("Class 3: ", round(precision3, 3), " ", round(recall3, 3), \
              " ", round(f3, 3), " ", round(acc3,3))
       Precision Recall F-measure Accuracy
Class 3: 0.932
                0.932
                         0.932
                                   0.986
In [18]: # Class 4
        precision4, recall4, f4, acc4 = metrics(cm, 4, len(test))
                     Precision Recall F-measure Accuracy")
        print("
        print("Class 4: ", round(precision4, 3), " ", round(recall4, 3), \
              " ", round(f4, 3), " ", round(acc4,3))
       Precision Recall F-measure Accuracy
Class 4: 0.955
                0.937
                         0.946
                                   0.99
```

```
In [19]: # Class 5
        precision5, recall5, f5, acc5 = metrics(cm, 5, len(test))
                      Precision Recall F-measure Accuracy")
        print("Class 5: ", round(precision5, 3), " ", round(recall5, 3), \
              " ", round(f5, 3), " ", round(acc5,3))
       Precision Recall F-measure Accuracy
Class 5: 0.915
                0.913 0.914
                                   0.985
In [20]: # Class 5
        precision5, recall5, f5, acc5 = metrics(cm, 5, len(test))
        print(" Precision Recall F-measure Accuracy")
        print("Class 5: ", round(precision5, 3), " ", round(recall5, 3), \
              " ", round(f5, 3), " ", round(acc5,3))
       Precision Recall F-measure Accuracy
Class 5: 0.915 0.913 0.914
In [21]: # Class 6
        precision6, recall6, f6, acc6 = metrics(cm, 6, len(test))
                     Precision Recall F-measure Accuracy")
        print("Class 6: ", round(precision6, 3), " ", round(recall6, 3), \
              " ", round(f6, 3), " ", round(acc6,3))
       Precision Recall F-measure Accuracy
Class 6: 0.952
               0.955 0.954
                                   0.991
In [22]: # Class 7
        precision7, recall7, f7, acc7 = metrics(cm, 7, len(test))
                  Precision Recall F-measure Accuracy")
        print("Class 7: ", round(precision0, 3), " ", round(recall7, 3), \
              " ", round(f7, 3), " ", round(acc7,3))
       Precision Recall F-measure Accuracy
Class 7: 0.961 0.953
                         0.958
                                   0.991
In [23]: # Class 8
        precision8, recall8, f8, acc8 = metrics(cm, 8, len(test))
        print(" Precision Recall F-measure Accuracy")
        print("Class 8: ", round(precision8, 3), " ", round(recall8, 3), \
              " ", round(f8, 3), " ", round(acc8,3))
       Precision Recall F-measure Accuracy
Class 8: 0.91
                0.928
                       0.919
                                  0.984
```

```
In [24]: # Class 9
        precision9, recall9, f9, acc9 = metrics(cm, 9, len(test))
                       Precision Recall F-measure Accuracy")
        print("Class 9: ", round(precision9, 3), " ", round(recall9, 3), \
              " ", round(f9, 3), " ", round(acc9,3))
       Precision Recall F-measure Accuracy
Class 9: 0.94
               0.932
                        0.936
                                  0.987
In [25]: # number of instances classified correctly
        print("Accuracy_score: ", round(acc_score, 5))
Accuracy_score: 0.9461
In [26]: # training time
        total_time_taken = dt_end - dt_start + max_time
        print("Training Time: %s sec" % round(total_time_taken, 5))
Training Time: 23.32264 sec
```