MNIST Decision Tree

July 15, 2019

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In [1]: import time
        import mnist
        from sklearn.metrics import confusion matrix
        from sklearn.tree import DecisionTreeClassifier
        from sklearn.metrics import accuracy_score
        from sklearn.tree import export_graphviz
        from sklearn.externals.six import StringIO
        from IPython.display import Image
        import pydotplus
        import numpy as np
In [2]: # getting data
        train = mnist.train_images()
        label_train = mnist.train_labels()
        test = mnist.test_images()
        label_test = mnist.test_labels()
In [3]: # reshaping the data for the decision tree
        nsamples, nx, ny = train.shape
        train = train.reshape((nsamples,nx*ny))
        nsamples, nx, ny = test.shape
        test = test.reshape((nsamples,nx*ny))
In [4]: from sklearn.tree._tree import TREE_LEAF
        def prune_index(inner_tree, index, threshold):
            if inner_tree.value[index].min() < threshold:</pre>
                # turn node into a leaf by "unlinking" its children
                inner_tree.children_left[index] = TREE_LEAF
                inner_tree.children_right[index] = TREE_LEAF
            # if there are shildren, visit them as well
            if inner_tree.children_left[index] != TREE_LEAF:
                prune_index(inner_tree, inner_tree.children_left[index], threshold)
                prune_index(inner_tree, inner_tree.children_right[index], threshold)
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In [5]: # building the decision tree of depth 10
        start = time.time()
        dt = DecisionTreeClassifier(max_depth = 10, random_state = 1)
        dt.fit(train, label train)
        prune_index(dt.tree_, 0, 1)
        end = time.time()
In [6]: # predicting
        pred = dt.predict(test)
In [7]: # function to calculate the metrics
        def metrics(cm, cls, size):
            cm = np.array(cm)
            tp = cm[cls][cls]
            fp = sum(cm[x, cls] for x in range(10))-cm[cls][cls]
            fn = sum(cm[cls, x] for x in range(10))-cm[cls][cls]
            tn = size - tp - fp - fn
            precision = tp/(tp+fp)
            recall = tp/(tp+fn)
            fmeasure = 2*(precision*recall)/(precision + recall)
            accuracy = (tp + tn)/size
            return precision, recall, fmeasure, accuracy
In [8]: # Rows: Actual
        # Cols: Predicted
        cm = confusion_matrix(label_test, pred)
        print("Confusion Matrix:\n ")
        print(cm)
Confusion Matrix:
[[ 839
               3
                    4
                             55
                                   18
                                         4
                                             24
                                                  31]
                         1
 1 1043
              43
                   15
                         3
                              9
                                    3
                                         1
                                             17
                                                   0]
   12
         62
             760
                    8
                        19
                             20
                                   52
                                        21
                                             57
                                                  21]
 Γ
   16
         16
              53
                  714
                         8
                             63
                                   12
                                        12
                                             93
                                                  231
 Γ
                       705
                             23
                                        28
                                             42 145]
     4
          9
               5
                    1
                                   20
 Γ
   29
         9
               7
                   60
                        13
                            630
                                   45
                                        47
                                             33
                                                 197
 Γ
   27
         20
               9
                    1
                        19
                             34
                                 766
                                         3
                                             26
                                                  53]
 2
                                    1 830
     2
         37
              50
                         9
                             10
                                             28
                                                  59]
 Г
     6
         25
                   25
                                   62
                                         5 712
              28
                         8
                             46
                                                  57]
 Γ
     6
         12
               4
                   25
                        29
                             37
                                    9
                                        37
                                             60 790]]
In [9]: # Class 0
        precision0, recall0, f0, acc0 = metrics(cm, 0, len(test))
                       Precision Recall F-measure Accuracy")
        print("
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print("Class 0: ", round(precision0, 3), " ", round(recall0, 3), \
             " ", round(f0, 3), " ", round(acc0,3))
       Precision Recall F-measure Accuracy
Class 0: 0.891
                  0.856
                          0.873
                                   0.976
In [10]: # Class 1
        precision1, recall1, f1, acc1 = metrics(cm, 1, len(test))
                     Precision Recall F-measure Accuracy")
        print("Class 1: ", round(precision1, 3), " ", round(recall1, 3), \
              " ", round(f1, 3), " ", round(acc1,3))
       Precision Recall F-measure Accuracy
Class 1: 0.845
                0.919
                         0.881
                                    0.972
In [11]: # Class 2
        precision2, recall2, f2, acc2 = metrics(cm, 2, len(test))
                     Precision Recall F-measure Accuracy")
        print("Class 2: ", round(precision2, 3), " ", round(recall2, 3), \
              " ", round(f2, 3), " ", round(acc2,3))
       Precision Recall F-measure Accuracy
Class 2: 0.79
               0.736 0.762
                                 0.953
In [12]: # Class 3
        precision3, recall3, f3, acc3 = metrics(cm, 3, len(test))
                     Precision Recall F-measure Accuracy")
        print("Class 3: ", round(precision3, 3), " ", round(recall3, 3), \
              " ", round(f3, 3), " ", round(acc3,3))
       Precision Recall F-measure Accuracy
Class 3: 0.835 0.707 0.766
                                   0.956
In [13]: # Class 4
        precision4, recall4, f4, acc4 = metrics(cm, 4, len(test))
                      Precision Recall F-measure Accuracy")
        print("Class 4: ", round(precision4, 3), " ", round(recall4, 3), \
              " ", round(f4, 3), " ", round(acc4,3))
       Precision Recall F-measure Accuracy
Class 4: 0.866 0.718 0.785
                                   0.961
In [14]: # Class 5
        precision5, recall5, f5, acc5 = metrics(cm, 5, len(test))
                      Precision Recall F-measure Accuracy")
        print("Class 5: ", round(precision5, 3), " ", round(recall5, 3), \
              " ", round(f5, 3), " ", round(acc5,3))
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Precision Recall F-measure Accuracy
Class 5: 0.68
                 0.706
                        0.693
                                   0.944
In [15]: # Class 6
        precision6, recall6, f6, acc6 = metrics(cm, 6, len(test))
                     Precision Recall F-measure Accuracy")
        print("Class 6: ", round(precision6, 3), " ", round(recall6, 3), \
              " ", round(f6, 3), " ", round(acc6,3))
       Precision Recall F-measure Accuracy
Class 6: 0.775 0.8 0.787
In [16]: # Class 7
        precision7, recall7, f7, acc7 = metrics(cm, 7, len(test))
                      Precision Recall F-measure Accuracy")
        print("Class 7: ", round(precision0, 3), " ", round(recall7, 3), \
              " ", round(f7, 3), " ", round(acc7,3))
       Precision Recall F-measure Accuracy
Class 7: 0.891 0.807
                         0.823
                                   0.964
In [17]: # Class 8
        precision8, recall8, f8, acc8 = metrics(cm, 8, len(test))
                      Precision Recall F-measure Accuracy")
        print("Class 8: ", round(precision8, 3), " ", round(recall8, 3), \
              " ", round(f8, 3), " ", round(acc8,3))
       Precision Recall F-measure Accuracy
Class 8: 0.652
                0.731
                          0.689
                                    0.936
In [18]: # Class 9
        precision9, recall9, f9, acc9 = metrics(cm, 9, len(test))
        print(" Precision Recall F-measure Accuracy")
        print("Class 9: ", round(precision9, 3), " ", round(recall9, 3), \
              " ", round(f9, 3), " ", round(acc9,3))
       Precision Recall F-measure Accuracy
Class 9: 0.659
                  0.783
                          0.716
                                   0.937
In [19]: # number of instances classified correctly
        acc_score = accuracy_score(pred, label_test)
        print("Accuracy_score: ", round(acc_score, 5))
Accuracy_score: 0.7789
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