

2x2 Confusion Matrix

Predicted	Actual	
	Positive	Negative
Positive	TP = 10	FP = 3
Negative	FN = 1	TN = 6

Accuracy = $\frac{\text{No of Correct Predictions}}{\text{Total No of Predictions}}$

$$= \frac{TP + TN}{TP + TN + FP + FN}$$

$$\text{Accuracy} = \frac{10 + 6}{10 + 6 + 3 + 1} = \frac{16}{20} = 0.8$$

$$= 0.8 \times 100$$

$$\text{Accuracy} = 80\%$$

Class - 1 (Positive) :-

$$\text{Recall} = \frac{TP}{TP + FN}$$

$$= \frac{10}{10 + 1} = \frac{10}{11} = 0.91$$

$$\text{Precision} = \frac{TP}{TP + FP}$$

$$= \frac{10}{10 + 3} = \frac{10}{13} = 0.77$$

$$\text{F1 Score} = 2 \times \frac{\text{Precision} \times \text{Recall}}{\text{Precision} + \text{Recall}}$$

$$= 2 \times \frac{0.77 \times 0.91}{0.77 + 0.91}$$

$$= 2 \times 0.417$$

$$\text{F1 Score} = 0.83$$

Class - 2 (Negative) :-

$$\text{Recall} = \frac{\text{TN}}{\text{FP} + \text{TN}}$$

$$= \frac{6}{3 + 6} = \frac{6}{9} = 0.67$$

$$\text{Precision} = \frac{\text{TN}}{\text{FN} + \text{TN}}$$

$$= \frac{6}{1 + 6} = \frac{6}{7} = 0.86$$

$$\text{F1 Score} = \frac{2 \times \text{Precision} \times \text{Recall}}{\text{Precision} + \text{Recall}}$$

$$= \frac{2 \times 0.86 \times 0.67}{0.86 + 0.67}$$

$$\text{F1 Score} = 2 \times 0.376 = 0.75$$

Weighted Average Precision:-

= Actual class-1 (Positive) instances * precision of class-1 (positive) +
Actual class-2 (Negative) instances * precision of class-2 (Negative)

$$= \frac{TP+FN}{100} * 0.77 + \frac{FP+TN}{100} * 0.86$$

$$= \frac{10+1}{100} * 0.77 + \frac{3+6}{100} * 0.86$$

$$= 0.0847 + 0.0774$$

$$= 0.1621$$

Weighted Average Recall :-

= Actual class-1 (Positive) instances * Recall
of class-1 (Positive) +

Actual class-2 (Negative) instances * Recall
of class-2 (Negative)

$$= \frac{TP + FN}{100} * 0.91 + \frac{FP + TN}{100} * 0.67$$

$$= \frac{10 + 1}{100} * 0.91 + \frac{3 + 6}{100} * 0.67$$

$$= 0.1001 + 0.0603$$

$$= 0.1604$$

3x3 Confusion Matrix

		Actual		
		Positive	Negative	Neutral
Predicted	Positive	TP = 10	FP = 1	FP = 2
	Negative	FN = 0	TN = 6	FN = 4
	Neutral	FNeutral = 1	FNeutral = 2	TNeutral = 4

$$\text{Accuracy} = \frac{\text{No of Correct Predictions}}{\text{Total no of Predictions}}$$

$$= \frac{TP + TN + TNeutral}{TP + TN + FP + FN + TNeutral + FNeutral}$$

$$= \frac{10 + 6 + 4}{10 + 6 + 3 + 4 + 4 + 3}$$

$$= \frac{20}{30}$$

$$= 0.6667$$

$$= 0.6667$$

$$= 0.6667 \times 100$$

$$\text{Accuracy} = 66.67\%$$

Class - 1 (Positive) :-

$$\text{Recall} = \frac{TP}{TP + FN + F\text{Neutral}}$$

$$= \frac{10}{10 + 0 + 1} = \frac{10}{11} = 0.91$$

$$\text{Precision} = \frac{TP}{TP + FP + FN}$$

$$= \frac{10}{10 + 1 + 2} = \frac{10}{13} = 0.77$$

$$F1 \text{ Score} = 2 \times \frac{\text{Precision} \times \text{Recall}}{\text{Precision} + \text{Recall}}$$

$$= 2 \times \frac{0.77 \times 0.91}{0.77 + 0.91}$$

$$= 2 \times 0.417$$

$$F1 \text{ Score} = 0.83$$

Class-2 (Negative) :-

$$\begin{aligned}\text{Recall} &= \frac{TN}{TN + FP + F\text{Neutral}} \\ &= \frac{6}{6 + 1 + 2}\end{aligned}$$

$$\text{Recall} = \frac{6}{9} = 0.67$$

$$\begin{aligned}\text{Precision} &= \frac{TN}{TN + FN + FN} \\ &= \frac{6}{6 + 0 + 4} = \frac{6}{10}\end{aligned}$$

$$\text{Precision} = 0.60$$

$$F1 \text{ Score} = 2 \times \frac{\text{Precision} \times \text{Recall}}{\text{Precision} + \text{Recall}}$$

$$= 2 \times \frac{0.60 \times 0.67}{0.60 + 0.67}$$

$$= 2 \times 0.316$$

$$F1 \text{ Score} = 0.63$$

Class - 3 (Neutral)

$$\begin{aligned}\text{Recall} &= \frac{\text{TNeutral}}{\text{TNeutral} + \text{FP} + \text{FN}} \\ &= \frac{4}{4 + 2 + 4}\end{aligned}$$

$$\text{Recall} = \frac{4}{10} = 0.40$$

$$\begin{aligned}\text{Precision} &= \frac{\text{TNeutral}}{\text{TNeutral} + \text{FNeutral} + \text{FNNeutral}} \\ &= \frac{4}{4 + 1 + 2}\end{aligned}$$

$$= \frac{4}{7}$$

$$\text{Precision} = 0.57$$

$$F1 \text{ Score} = 2 \times \frac{\text{Precision} \times \text{Recall}}{\text{Precision} + \text{Recall}}$$

$$= 2 \times \frac{0.57 \times 0.40}{0.57 + 0.40}$$

$$= 2 \times 0.235$$

$$F1 \text{ Score} = 0.47$$

Weighted Average Precision:-

= Actual Class-1 (Positive) instances * precision of class-1 (Positive) +

Actual class-2 (Negative) instances * precision of class-2 (Negative) +

Actual Class-3 (Neutral) instances * precision of class-3 (Neutral)

$$= \frac{TP+FN+F_{Neutral}}{100} \times 0.77 + \frac{FP+TN+F_{Neutral}}{100} \times 0.60$$

$$+ \frac{FP+FN+T_{Neutral}}{100} \times 0.57$$

$$= \frac{10+0+1}{100} \times 0.77 + \frac{1+6+2}{100} \times 0.60 + \frac{2+4+4}{100} \times 0.57$$

$$= \frac{11}{100} \times 0.77 + \frac{9}{100} \times 0.60 + \frac{10}{100} \times 0.57$$

$$= 0.0847 + 0.054 + 0.057$$

$$= 0.1957$$

Weighted Average Recall

= Actual class-1 (Positive) instances * Recall
of class-1 (Positive) +

Actual class-2 (Negative) instances * Recall
of class-2 (Negative) +

Actual class-3 (Neutral) instances * Recall
of class-3 (Neutral)

$$= \frac{TP + FN + F_{Neutral}}{100} * 0.91 + \frac{FP + TN + F_{Neutral}}{100} * 0.67$$

$$+ \frac{FP + FN + T_{Neutral}}{100} * 0.40$$

$$= \frac{10 + 0 + 1}{100} * 0.91 + \frac{1 + 6 + 2}{100} * 0.67 + \frac{2 + 4 + 4}{100} * 0.40$$

$$= \frac{11}{100} * 0.91 + \frac{9}{100} * 0.67 + \frac{10}{100} * 0.40$$

$$= 0.1001 + 0.0603 + 0.04$$

$$= 0.2004$$