

## Master's Thesis Proposal

# Mechanized Consistency Models for Distributed Database Transactions

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## Introduction

Cloud database systems use transactions for synchronization. Depending on the desired scalability and availability, different systems provide different transactional consistency guarantees, aka. consistency models in the literature. Prevalent consistency models include read atomic (RA) [BFG<sup>+</sup>16], causal consistency (CC) [LFKA11], parallel snapshot isolation (PSI) [SPAL11], snapshot isolation (SI) [BBG<sup>+</sup>95], and serializability (SER) [Pap79]. Different concurrency control mechanisms have been proposed that implement these consistency notions. For example, RAMP [BFG<sup>+</sup>16] satisfies RA, COPS [DBC<sup>+</sup>00] and Eiger-PORT [LSL20] satisfy CC, and Two-Phase Locking implements SER.

## Motivation

The complex concurrent behaviors of these protocols call for formal verification that they satisfy the desired consistency model. Moreover, a formal analysis of transactional client programs is also desirable. Different types of formal semantics have been studied for these models.

*Declarative semantics* have been previously introduced for these models, using dependency graphs [AL99] and abstract executions [CBG15]. This type of semantics is quite concise, but also quite abstract. While it is possible to use abstract executions to prove that a concurrency control protocols implementing its intended consistency model, the complete lack of state information seems to make this type of model unsuitable for proving properties of client programs.

Xiong et al. in [XCRG20] define an *operational semantics* for representing different consistency models in a unified way. This model is a centralized one: the database is represented as a single, multi-versioned key-value store. In reality, the database may be sharded and

replicated and each client may have a different view on its current content. These *client views* are explicitly represented in the centralized model as subsets of versions of each key that a given client sees. Transactions are executed atomically and the desired notion of consistency is specified as a so-called execution test, which consists of a condition that must be satisfied for a commit to take place and a constraint on the possible updates of the committing client's view on the database. The commit condition is formulated in terms of the Write-Read (WR) and Write-Write (WW) dependency relations and the Read-Write (RW) anti-dependency relation, first introduced in Adya's PhD thesis [AL99]. This model can be used both for verifying that concurrency control protocols implement their claimed notion of consistency and for analysing client programs' robustness under different consistency models.

## Objectives

The main objective of this thesis is to set up a framework for studying the correctness of concurrency control protocols and of client programs using databases based on these protocols. Concretely, we will

- formalize the operational framework for consistency models proposed in [XCRG20] and
- use it to model and prove the correctness of a concurrency control protocol in Isabelle/HOL.

Such a correctness proof must establish that at the time of committing a transaction, the protocol state can be related to an abstract state of the centralized model, which satisfies the execution test of the desired notion of consistency. We will put particular attention on the proof technique for establishing the correctness of such protocols. While the centralized model executes transactions atomically, the concrete protocol executes the constituting read and write operations one-by-one. It is not a priori clear whether standard simulation proof techniques can relate such concrete and abstract executions. We will investigate whether more advanced techniques such as non-atomic refinement [DW03] or vertical implementation [RG01] better suit this purpose.

We propose the following candidate protocols for such a verification effort:

1. The RAMP algorithms [BFG<sup>+</sup>16], which provide RA (Read Atomicity) and the RYW (Read Your Writes) session guarantee [TDP<sup>+</sup>94].
2. The Eiger-PORT protocol [LSL20], which satisfies CC (Causal Consistency). This is a recent and novel algorithm published at a top conference.

Both RAMP and Eiger-PORT are state-of-the-art representative implementations of their respective consistency models in the literature.

To our knowledge, this will be the first formalization of a general framework of consistency models and the first general and fully mechanized correctness proof of a concurrency control protocol in such a framework. Depending on our investigation, we might also be able to contribute novel proof techniques for establishing the correctness of such protocols.

## Tasks

Our development will be done in Isabelle/HOL, based on definitions, data consistency models, and execution test infrastructure of the ECOOP paper [XCRG20].

1. Study the definitions and semantics as described in [XCRG20], in particular the semantics of transactional and sequential commands and programs, consistency models, and execution tests.
2. Formalize key-value stores, client views, and the semantics of transactional commands and programs in Isabelle/HOL.
3. Formalize the execution tests of the most widely used consistency models for further usage in the formal verification of database concurrency control protocols.
4. Formalize a candidate state-of-the-art protocol and establish its correctness with respect to the corresponding centralized consistency model.
5. **(optional)** Establish the correctness of some instances of the centralized model of [XCRG20] with respect to the corresponding notion of abstract execution, showing that these model instances indeed correctly reflect the intended notion of data consistency.
6. **(optional)** Investigate whether it is possible to refine the centralized model of [XCRG20] into a generic distributed model (similar to [CBG15]) that could be used to simplify the correctness proofs of concrete concurrency control protocols.

## Deliverables

**Final report** The final report must be written in English and should include an introduction, an analysis of related work, and a detailed report of formalizations and proofs.

**Isabelle theories** for the case study.

**Presentation** At the end of the thesis a presentation of 30 minutes must be given during an Information Security group seminar. It should give an overview as well as the most important details of the work.

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