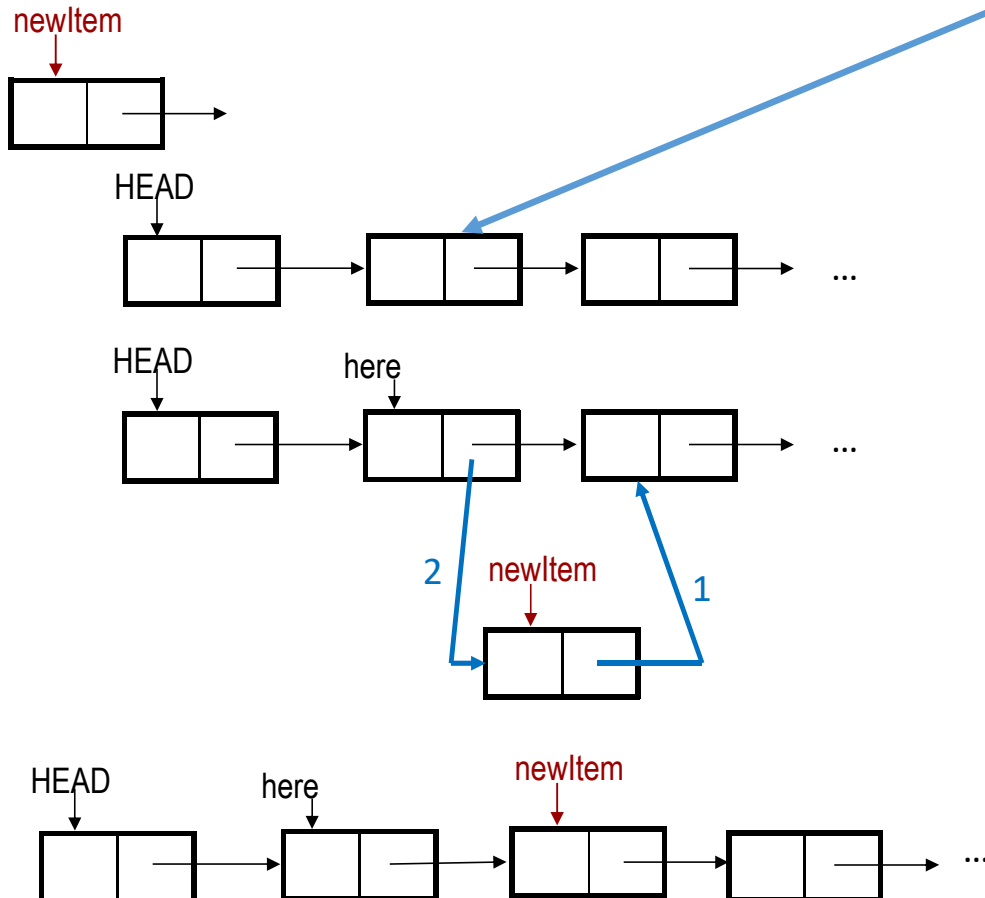


# CSE 105: Data Structures and Algorithms-I (Part 2)

Instructor  
Dr Md Monirul Islam

# Insert at Middle (after a desired node)

Review



```
newItem = //create it as before
if (newItem == NULL) //error handling
newItem ->data= //assign it ;
newItem ->next=here ->next;
here ->next= newItem;
```

Complexity?

# Insert a node after a given value

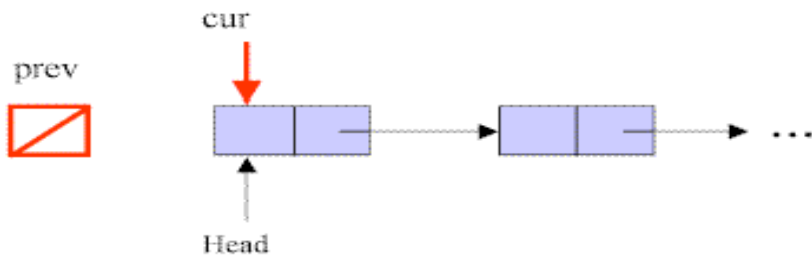
Review

//head is the start of list  
//value is the given value  
//newItem is the node to be inserted

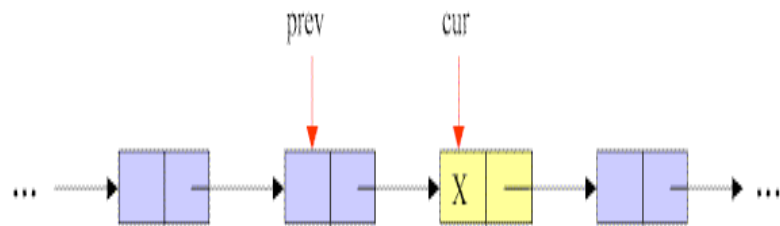
```
for (struct node *here = head; here != null; here = here->next {  
    if (here->data==value) {  
        newItem ->next=here ->next;  
        here ->next= newItem;  
        exit loop; //done  
    } // if  
} // for  
// Couldn't insert--do something reasonable!  
}
```

# Delete Any

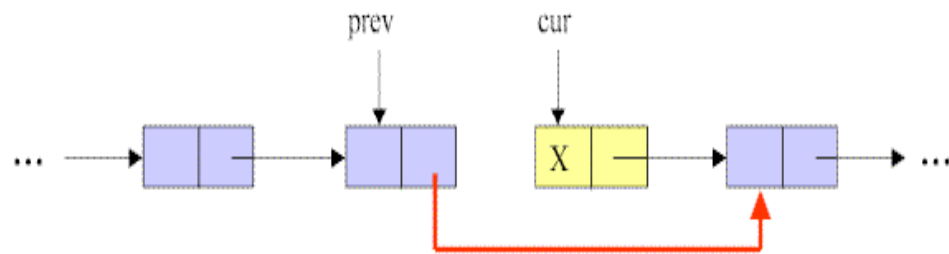
Review



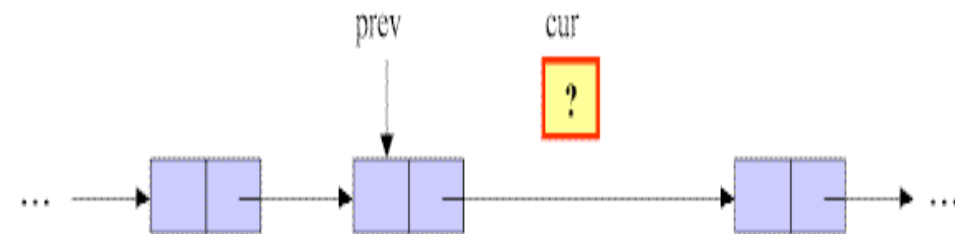
Step 1



Step 2



Step 3



Step 4

If head==NULL  
//error handling and return

```
cur = head;
prev = NULL;
while (cur)
    if curr->value == x
        break;
    prev = cur;
    cur = cur->next;
```

if (cur==NULL) //NOT Found, Return

If (prev) prev ->next=curr->next;  
else head= head->next;

free (cur);

# Comparison of Implementations

## Array-Based Lists:

- Insertion and deletion are  $\Theta(n)$ .
- Prev, next and direct access are  $\Theta(1)$ .
- Array must be **allocated in advance**.
- **No overhead** if all array positions are full.

## Linked Lists:

- Insertion and deletion are  $\Theta(1)$ .
- Prev and direct access are  $\Theta(n)$ .
- Space **grows dynamically**.
- Every element **requires overhead**.

# Space Comparison

When the array based implementation is better  
in space?

# Space Comparison

When the array based implementation is better  
in space?

n: The number of existing elements  
D: Maximum number of elements for array.  
E: Space for data value.  
P: Space for pointer.  
Array Based space:  $DE$   
LL based space:  $(E+P)*n$

# Space Comparison

When the array based implementation is better  
in space?

$$n(P + E) > DE \Rightarrow n > DE/(P+E)$$

n: The number of existing elements  
D: Maximum number of elements for array.

E: Space for data value.

P: Space for pointer.

Array Based space: DE

LL based space:  $(E+P)*n$



# Space Comparison

When the array based implementation is better  
in space?

$$n(P + E) > DE \Rightarrow n > DE/(P+E)$$

*If  $P=E$ , the point is at  $D/2$ .*

n: The number of existing elements  
D: Maximum number of elements for array.

E: Space for data value.

P: Space for pointer.

Array Based space:  $DE$

LL based space:  $(E+P)*n$

# Space Comparison

When the array based implementation is better  
in space?

$$n(P + E) > DE \Rightarrow n > DE/(P+E)$$

*If  $P=E$ , the point is at  $D/2$ .*

=> array-based implementation is more efficient if

- the **link field size** = the **element field size**, and
- the array is more than half full.

n: The number of existing elements  
D: Maximum number of elements for array.

E: Space for data value.

P: Space for pointer.

Array Based space:  $DE$

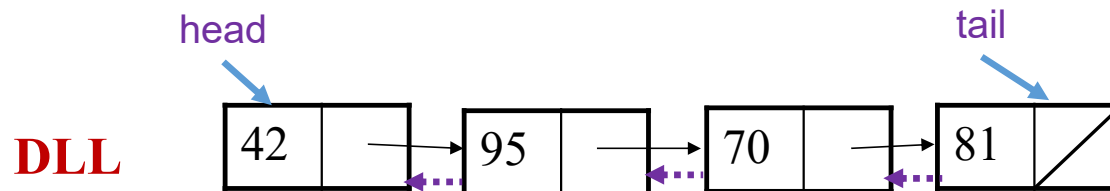
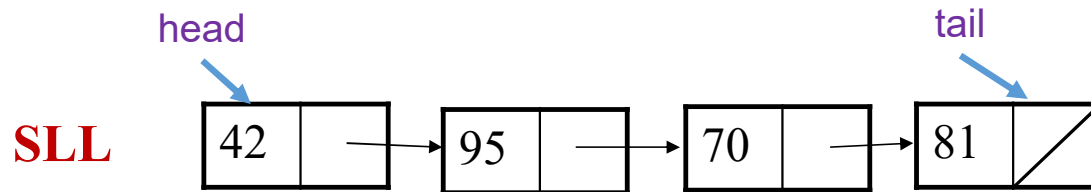
LL based space:  $(E+P)*n$

## Rule of Thumb

- **Linked list** is more space efficient when the number of elements varies widely or is **unknown**.
- **Array-based list** is generally more space efficient when we know approximately **how large the list** will become.

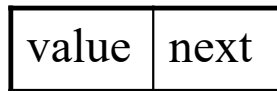
# Doubly Linked List (DLL)

- In **SLL**, we can only traverse in one direction.
- Often, we need to traverse an LL list in both directions

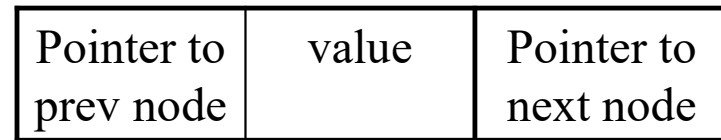


# Doubly linked list

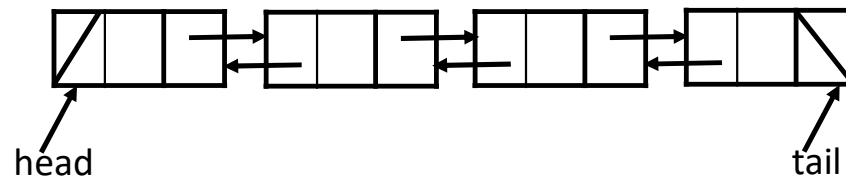
- Each node contains a **value**, a link to its **successor** (if any), and a link to its **predecessor** (if any)
- The header points to the first node in the list



An SLL node



A DLL node

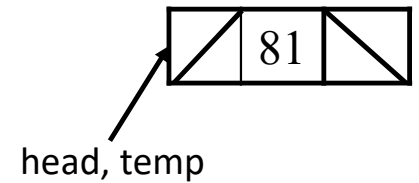


# DLL Creation

// linked list node in C

```
struct DLLnode {  
    int data;  
    struct node *next, *prev;  
}
```

```
struct DLLnode *head, *temp;  
temp = (struct DLLnode *) malloc (sizeof (struct DLLnode));  
if (temp==NULL) //error handling code  
temp->data=81;  
temp->next=temp->prev=NULL;  
head=temp;
```

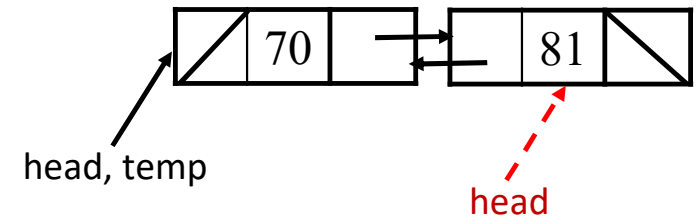


# DLL Creation

// linked list node in C

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struct DLLnode {  
    int data;  
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}
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struct DLLnode *head, *temp;  
temp = (struct DLLnode *) malloc (sizeof (struct DLLnode));  
if (temp==NULL) //error handling code  
temp->data=81;  
temp->next=temp->prev=NULL;  
head=temp;
```



```
temp = (struct DLLnode*) malloc (sizeof (struct DLLnode));  
if (temp==NULL) //error handling code  
temp->data=70;  
temp->next=temp->prev=NULL;  
temp->next=head;  
head->prev=temp;  
head=temp;
```

# DLL pros and cons

- Advantages:
  - Can be **traversed in either direction** (may be essential for some programs)
  - **Some operations**, such as deletion and inserting before a node, become **easier**
- Disadvantages:
  - Requires **more space**
  - List **manipulations** are **slower** (because more links must be changed)
  - **Greater** chance of having **bugs** (because more links must be manipulated)



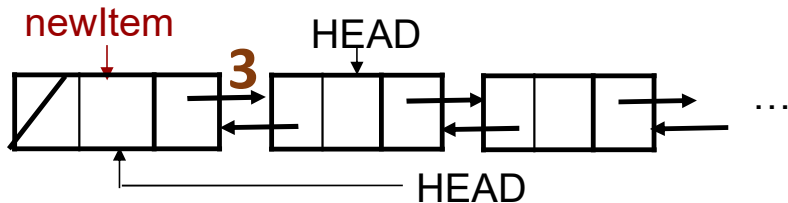
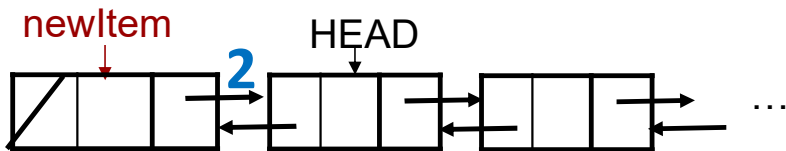
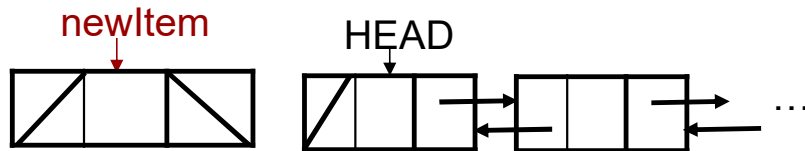
# Basic Operations of DLL

- **Insert:** Add a new node in the first, last or interior of the list.
- **Delete:** Delete a node from the first, last or interior of the list.
- **Search:** Search a node containing particular value in the linked list.

## Insert at the beginning of a DLL

Very similar to the SLL

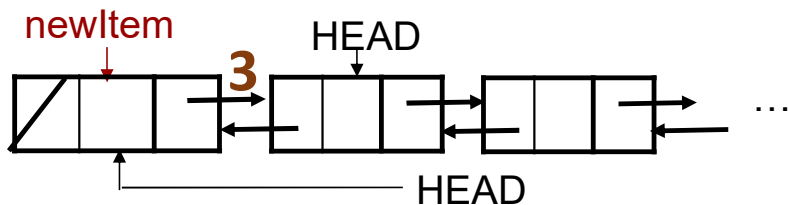
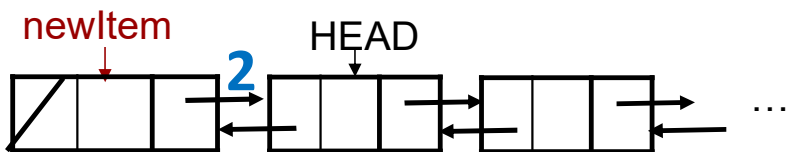
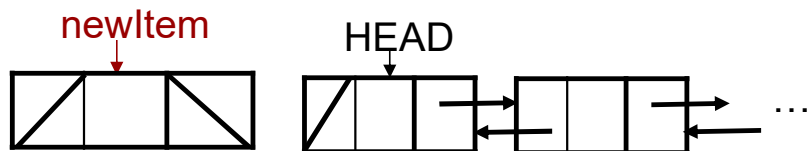
- Step 1. Create a new node, *newItem*.
- Step 2. *newItem* is linked to the first node of the DLL
- Step 3. Set the pointer *head* to *newItem*.



## Insert at the beginning of a DLL

Very similar to the SLL

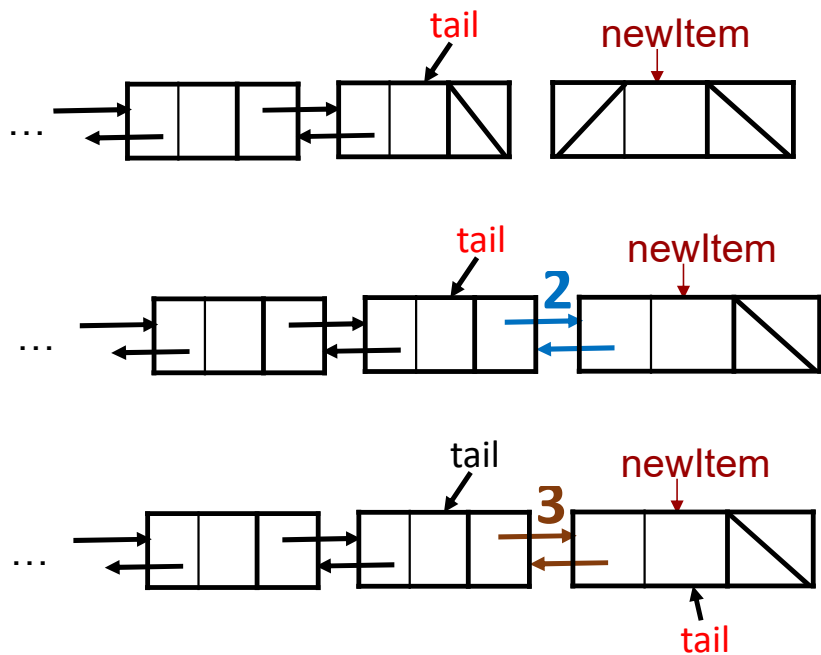
- Step 1. Create a new node, *newItem*.
- Step 2. *newItem* is linked to the first node of the DLL
- Step 3. Set the pointer *head* to *newItem*.



```
struct DLLnode *head, *temp;  
newItem = (struct DLLnode*) malloc (sizeof (struct DLLnode));  
if (newItem == NULL) //error handling code  
newItem ->next=temp->prev=NULL;  
newItem ->next=head;  
if (head !=NULL) head ->prev= newItem;  
  
head= newItem;
```

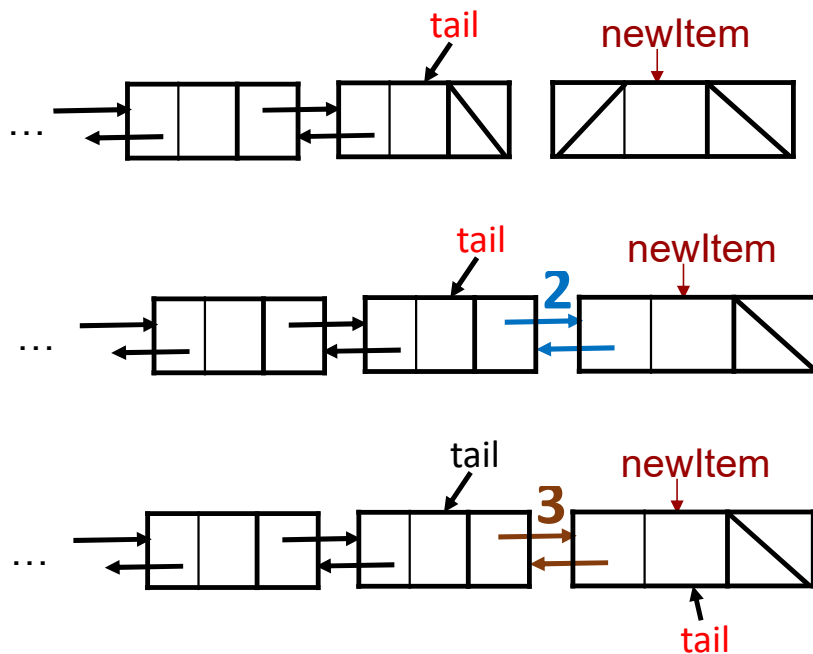
## Insert at the end of a DLL

- **Step 1.** Create a new node, *newItem*.
- **Step 2.** *newItem* is linked to the **tail** of the DLL
- **Step 3.** Set the pointer **tail** to *newItem*.



## Insert at the end of a DLL

- Step 1. Create a new node, *newItem*.
- Step 2. *newItem* is linked to the *tail* of the DLL
- Step 3. Set the pointer *tail* to *newItem*.



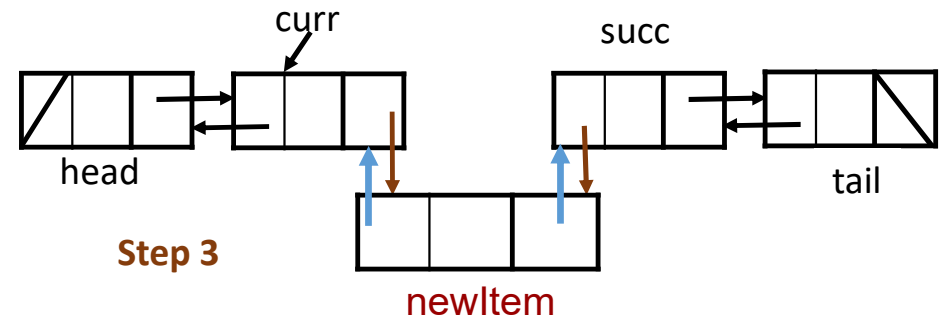
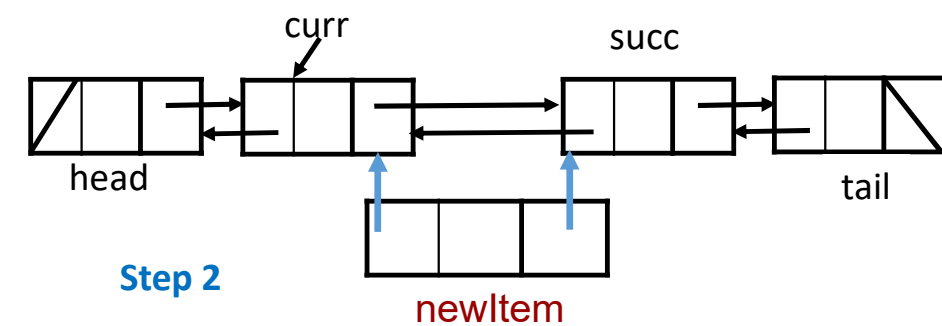
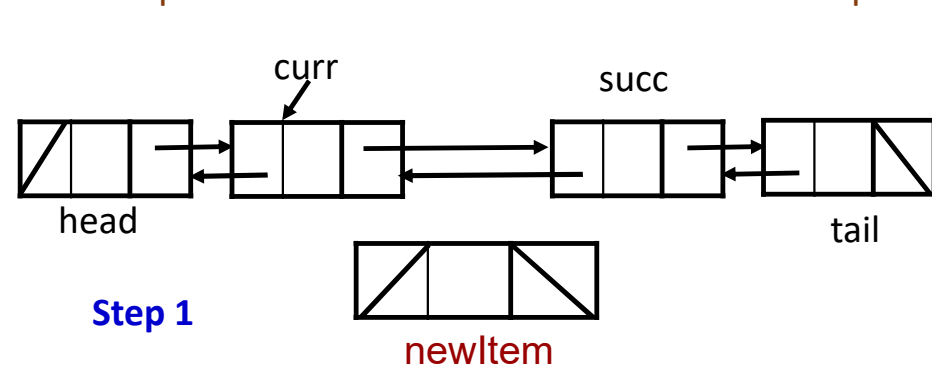
```
struct DLLnode *head, *temp;  
newItem = (struct DLLnode*) malloc (sizeof (struct DLLnode));  
if (newItem ==NULL) //error handling code  
newItem ->next=temp->prev=NULL;  
newItem ->prev=tail;  
if (tail !=NULL) tail->next= newItem;
```

```
tail= newItem;
```

## Insert interior of a DLL

Assume we will insert after **curr** AND **succ** is the next node of **curr**.

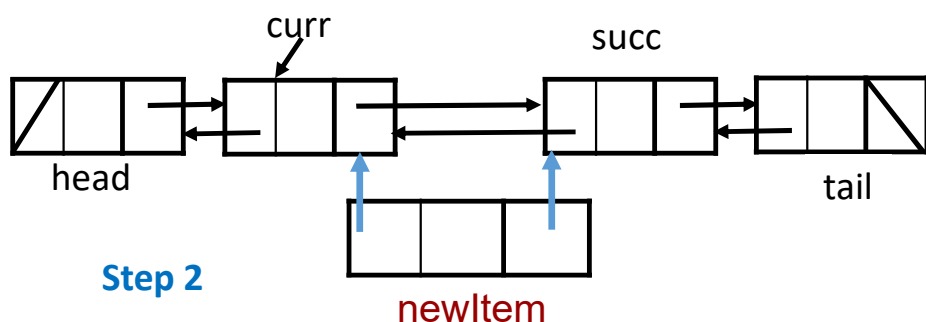
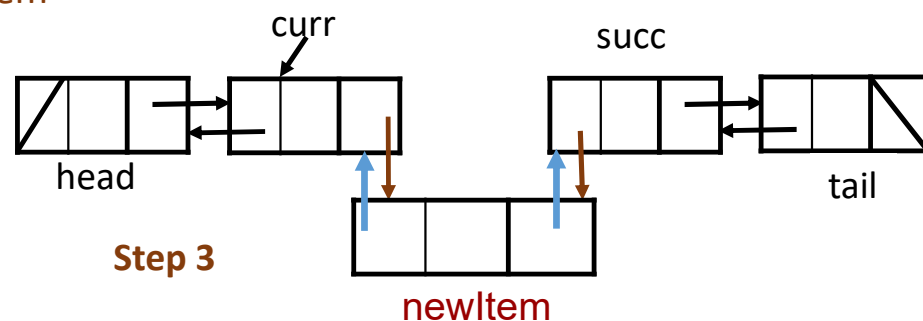
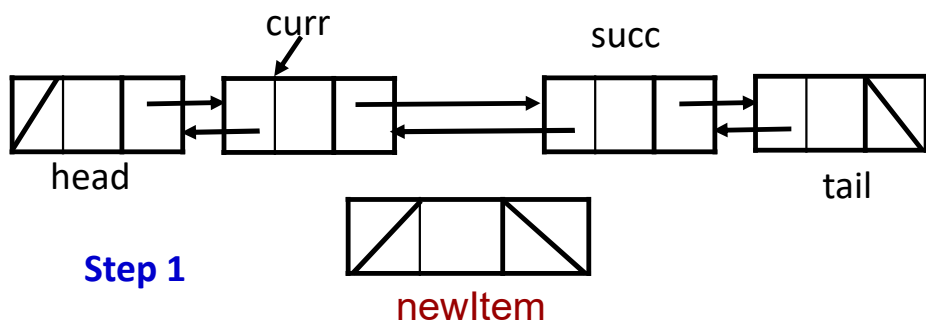
- Step 1. Create a new node, *newItem*.
- Step 2. *newItem->prev* is linked **curr** and *newItem->next* is linked to **succ**
- Step 3. Set **curr->next = newItem** and **succ->prev = newItem**



## Insert interior of a DLL

Assume we will insert after **curr** AND **succ** is the next node of curr.

- Step 1. Create a new node, **newItem**.
- Step 2. **newItem->prev** is linked **curr** and **newItem->next** is linked to **succ**
- Step 3. Set **curr->next = newItem** and **succ->prev = newItem**



```
newItem ->next=succ; //curr->next
newItem ->prev=curr;
if (succ) succ->prev=newItem;
if (curr) curr->next= newItem;
```

# Deletion of a node in DLL

- Deletion in DLL is **easier** than deletion in SLL
- In SLL, we have to **find the predecessor** of the discarded **node** in  $O(n)$
- In DLL, the predecessor and successor of a node are immediately known.

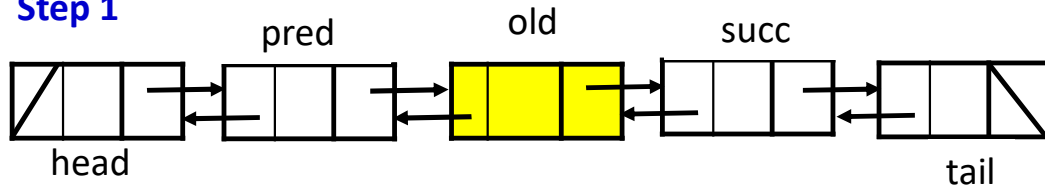


# Deletion of a node in DLL

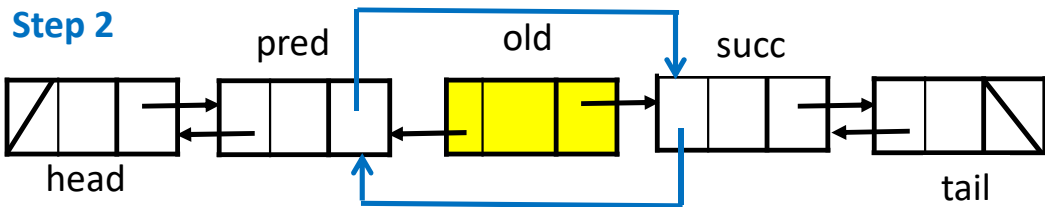
Assume **old** is to be deleted. **pred** and **succ** are its **previous** and **next** nodes

- **Step1.** Set pointer **pred = old->prev** and **succ = old->next**
- **Step2.** Set **pred->next = succ** and **succ->prev = pred**
- **Step3.** Discard the node pointed by **old**.

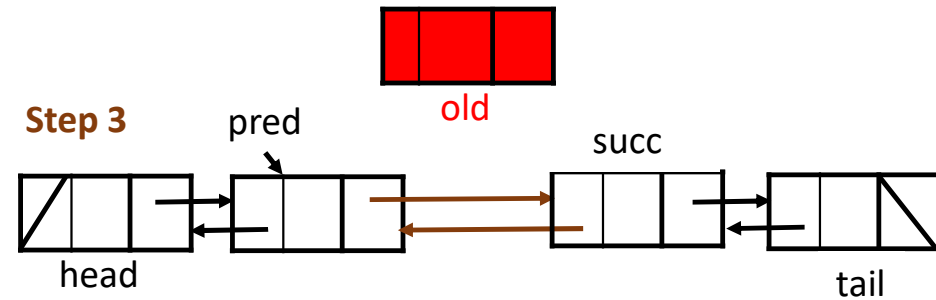
**Step 1**



**Step 2**



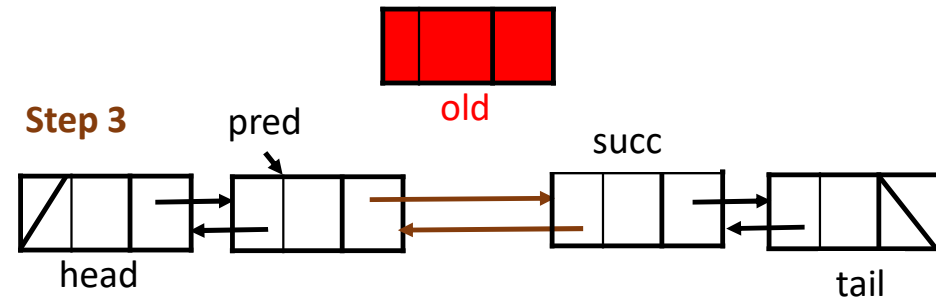
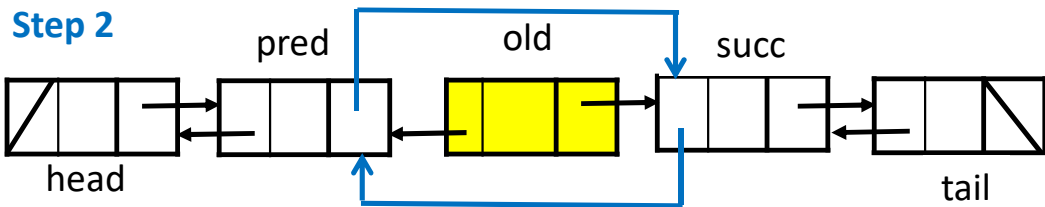
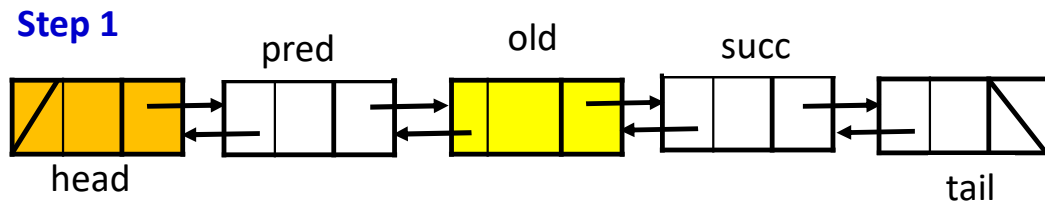
**Step 3**



# Deletion of a node in DLL (head being deleted)

Assume **old** is to be deleted. **pred** and **succ** are its **previous** and **next** nodes

- **Step1.** Set pointer **pred = old->prev** and **succ = old->next**
- **Step2.** Set **pred->next = succ** and **succ->prev = pred**
- **Step3.** Discard the node pointed by **old**.



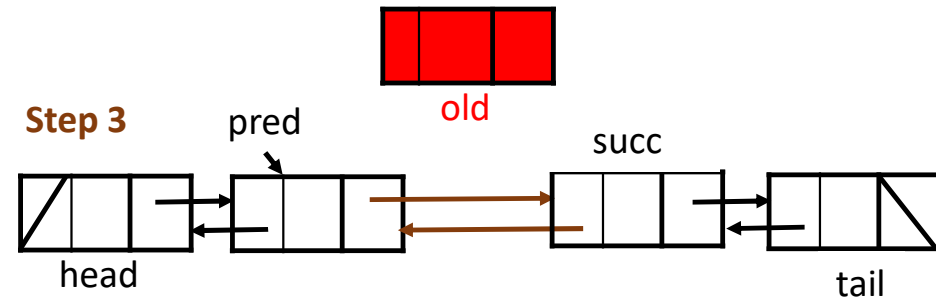
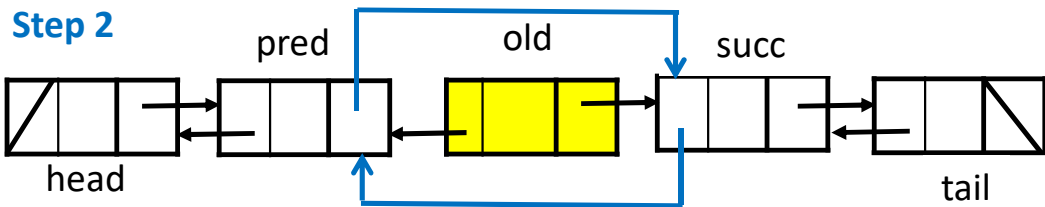
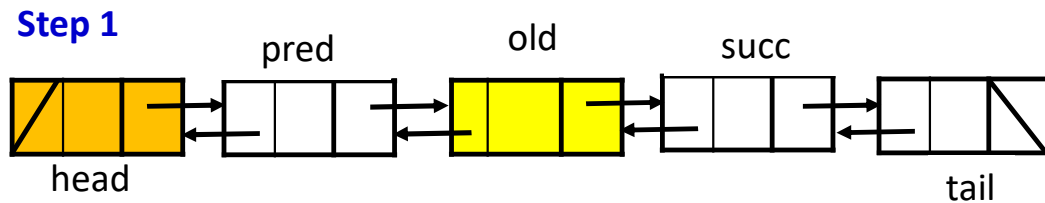
**Will it work?**

```
pred=old->prev;    succ=old->next;  
pred->next=succ;  
succ->prev=pred;  
free(old)
```

# Deletion of a node in DLL (head being deleted)

Assume **old** is to be deleted. **pred** and **succ** are its **previous** and **next** nodes

- **Step1.** Set pointer **pred = old->prev** and **succ = old->next**
- **Step2.** Set **pred->next = succ** and **succ->prev = pred**
- **Step3.** Discard the node pointed by **old**.



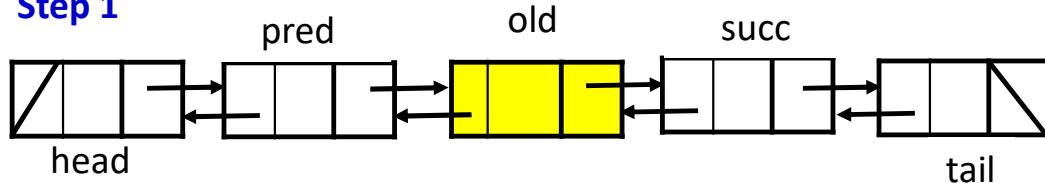
```
pred=old->prev;    succ=old->next;  
if (pred) pred->next=succ;  
else head=succ;  
succ->prev=pred;  
free(old)
```

# Deletion of a node in DLL (tail being deleted)

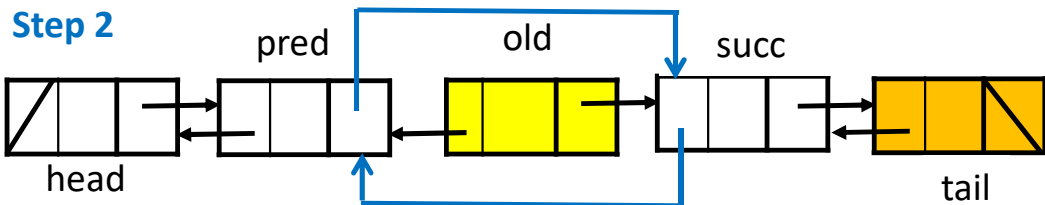
Assume **old** is to be deleted. **pred** and **succ** are its **previous** and **next** nodes

- **Step1.** Set pointer **pred = old->prev** and **succ = old->next**
- **Step2.** Set **pred->next = succ** and **succ->prev = pred**
- **Step3.** Discard the node pointed by **old**.

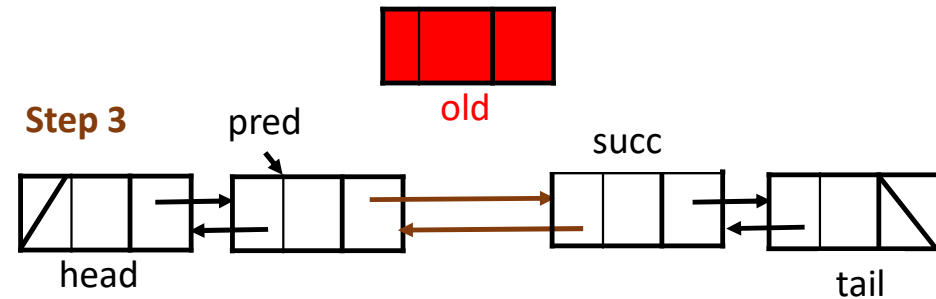
**Step 1**



**Step 2**



**Step 3**

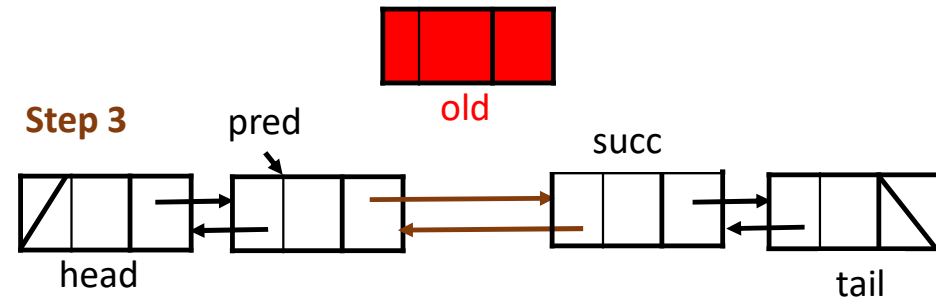
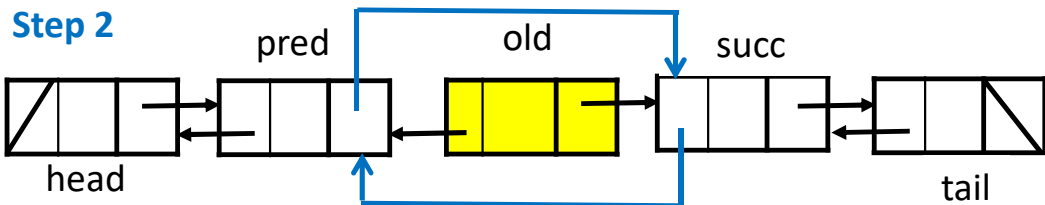
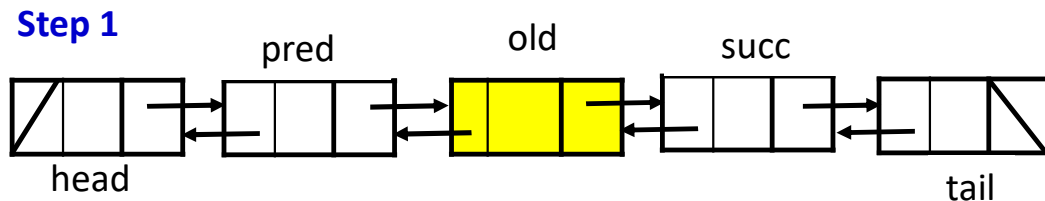


```
pred=old->prev;    succ=old->next;
if (pred) pred->next=succ;
else head=succ;
if (succ) succ->prev=pred;
else tail=pred;
free(old)
```

# Deletion of a node in DLL (tail being deleted)

Assume **old** is to be deleted. **pred** and **succ** are its **previous** and **next** nodes

- **Step1.** Set pointer **pred = old->prev** and **succ = old->next**
- **Step2.** Set **pred->next = succ** and **succ->prev = pred**
- **Step3.** Discard the node pointed by **old**.



**Will it work if old is the only node?**

```
pred=old->prev;    succ=old->next;
if (pred) pred->next=succ;
else head=succ;
if (succ) succ->prev=pred;
else tail=pred;
free(old)
```

# Singly linked list

|               | head        | <i>middle</i> | tail        |
|---------------|-------------|---------------|-------------|
| Find          | $\Theta(1)$ | $O(n)$        | $\Theta(1)$ |
| Insert Before | $\Theta(1)$ | $O(n)$        | $\Theta(n)$ |
| Insert After  | $\Theta(1)$ | $\Theta(1)^*$ | $\Theta(1)$ |
| Replace       | $\Theta(1)$ | $\Theta(1)^*$ | $\Theta(1)$ |
| Erase         | $\Theta(1)$ | $O(n)$        | $\Theta(n)$ |
| Next          | $\Theta(1)$ | $\Theta(1)^*$ | n/a         |
| Previous      | n/a         | $O(n)$        | $\Theta(n)$ |

\* These assume we have already accessed the middle node—an  $O(n)$  operation

# Doubly linked lists

|               | head        | <i>middle</i> | tail        |
|---------------|-------------|---------------|-------------|
| Find          | $\Theta(1)$ | $O(n)$        | $\Theta(1)$ |
| Insert Before | $\Theta(1)$ | $\Theta(1)^*$ | $\Theta(1)$ |
| Insert After  | $\Theta(1)$ | $\Theta(1)^*$ | $\Theta(1)$ |
| Replace       | $\Theta(1)$ | $\Theta(1)^*$ | $\Theta(1)$ |
| Erase         | $\Theta(1)$ | $\Theta(1)^*$ | $\Theta(1)$ |
| Next          | $\Theta(1)$ | $\Theta(1)^*$ | n/a         |
| Previous      | n/a         | $\Theta(1)^*$ | $\Theta(1)$ |

\* These assume we have already accessed the middle node—an  $O(n)$  operation