- (a) Geometric Distribution.
- (b) Multinomial Distribution.
- (c) Rectangular Distribution
- (d) Gamma Distribution
- (e) Beta Distribution.
- (f) Exponential Distribution.
- (g) Weibull Distribution.
- (h) Logistic Distribution.
- (i) Cauchy Distribution.
- 7. Lack of memory property of Exponential Distribution.

Practical work to be conducted using electronic spreadsheet / EXCEL/ Statistical Software Package/ SPSS.

#### ESSENTIAL READINGS

- Gupta, S. C. and Kapoor, V. K. (2020). Fundamentals of Mathematical Statistics, Twelfth Edition, Sultan Chand and Sons, Delhi.
- Ross, Sheldon M. (2013): A First Course in Probability, Ninth Edition, Pearson.
- Miller, I. and Miller, M. (2006). John E. Freund's Mathematical Statistics with Applications, Eight Edition., Pearson Education, Asia.
- Mood, A.M. Graybill, F.A. and Boes, D.C. (2007). Introduction to the Theory of Statistics, Third Edition, (Reprint), Tata McGraw-Hill Pub. Co. Ltd.

## **SUGGESTED READINGS**

- Rohatgi, V. K and Saleh M. E. (2015). An Introduction to Probability and Statistics, Third Edition, John Wiley and Sons, Inc., New Jersey.
- Hogg, R.V., Tanis, E.A. and Rao, J.M. (2009). Probability and Statistical Inference, 7th Ed., Pearson Education, New Delhi.
- Ross, Sheldon M.(2009). Introduction to Probability and Statistics for Engineers and Scientists, Fourth Edition, Academic Press.

Note: Examination scheme and mode shall be as prescribed by the Examination Branch University of Delhi, from time to time.

## DISCIPLINE SPECIFIC CORE COURSE – 9: MATHEMATICAL ANALYSIS

# CREDIT DISTRIBUTION, ELIGIBILITY AND PRE-REQUISITES OF THE COURSE

Course title & Code	Credits	Credit distribution of the course			Eligibility	Pre-requisite of
		Lecture	Tutorial	Practical/ Practice	criteria	the course (if any)
Mathematical Analysis	4	3	0	1	Class XII with Mathematics	Nil

The learning objectives include:

- To study Real Analysis, which deals with the analytical properties of real functions and sequences.
- To study Numerical Analysis, which is the study of algorithms that use numerical approximation for the problems of mathematical analysis.

# **Learning Outcomes:**

After successful completion of this course, students should be able to:

- · Understand the fundamental properties of real numbers and real-valued functions.
- · Understand the Analytical properties of sequences.
- · Apply Infinite series, their properties and different tests.
- · Apply limits, continuity, differentiability, and mean value theorems.
- · Use the fundamentals of numerical analysis, interpolation, numerical integration and difference equation.

#### **SYLLABUS OF DSC-9**

# **Theory**

UNIT I (10 hours)

## **Set Theory and Sequences**

Completeness: The Completeness property of R; Archimedean property in R; Neighbourhood and limit points: Neighbourhood, Open Set, Closed Set, Supremum and Infimum, Limit Point of a Set; Sequences: Definition of a Sequence, Convergent Sequence, Divergent Sequence, Oscillatory Sequence, Cauchy Sequence, Monotone Sequence.

UNIT II (10 hours)

## **Series**

Infinite series, positive termed series and their convergence, Comparison test, D'Alembert's ratio test, Cauchy's n<sup>th</sup> root test, Raabe's test. Gauss test, Cauchy's condensation test and integral test (Statements and Examples only). Absolute convergence of series, Conditional convergence.

UNIT III (10 hours)

## **Limit and Continuity**

Review of limit, continuity and differentiability, uniform Continuity and boundedness of a function. Rolle's and Lagrange's Mean Value theorems. Taylor's theorem with Lagrange's and Cauchy's form of remainder (without proof). Taylor's and Maclaurin's series expansions of  $\sin(x)$ ,  $\cos(x)$ ,  $\log(1+x)$ .

UNIT IV (15 hours)

### **Numerical Methods**

Factorial, finite differences and interpolation. Operators, E and divided difference. Newton's forward, backward and divided differences interpolation formulae. Lagrange's interpolation formulae. Gauss and Stirling interpolation formulae. Numerical integration. Trapezoidal rule, Simpson's one-third rule, three-eights rule, Stirling's approximation to factorial n. Solution of difference equations of first order, Euler Maclaurin's summation formula.

## PRACTICAL/LAB WORK – (30 hours)

### **List of Practical:**

## Practicals based on:

- 1. Formation of difference table, fitting of polynomial and missing terms for equal interval of differencing.
- 2. Newton's Gregory forward difference interpolation formula.

- 3. Newton's backward difference interpolation formula.
- 4. Newton's divided difference and Lagrange's interpolation formula.
- 5. Gauss forward, Gauss backward central difference interpolation formula.
- 6. Stirling's central difference interpolation formula.
- 7. Lagrange's Inverse interpolation formula.
- 8. Method of successive approximation or iteration.
- 9. Method of reversion of series.
- 10. Trapezoidal Rule, Simpson's one-third rule, Simpson's three-eighth rule, Weddle's rule.
- 11. Euler-Maclaurin summation formula

Practical work to be conducted using electronic spreadsheet / EXCEL/ Statistical Software Package/ SPSS/ calculators.

## **ESSENTIAL READINGS**

- Appostol, T.M. (1987). Mathematical Analysis, 2nd Ed., Narosa Publishing House, New Delhi
- Ghorpade, S.R. and Limaye, B.V. (2006). A Course in Calculus and Real Analysis, Undergraduate Texts in Mathematics, Springer (SIE), Indian reprint.
- Sastry, S.S. (2000). Introductory Methods of Numerical Analysis, 3rd Ed., Prentice Hall of India Pvt. Ltd., New Delhi.

#### **SUGGESTIVE READINGS:**

- Bartle, R.G. and Sherbert, D.R. (2002). Introduction to Real Analysis, (3rd Ed.,), John Wiley and Sons (Asia) Pte. Ltd., Singapore.
- Jain, M.K., Iyengar, S.R.K. and Jain, R.K. (2003). Numerical methods for scientific and engineering computation, New age International Publisher, India.
- Malik, S.C. and Arora, S. (1994). Mathematical Analysis, Second Edition, Wiley Eastern Limited, New Age International Limited, New Delhi.
- Mukherjee, Kr. Kalyan (1990). Numerical Analysis. New Central Book Agency.
- Narayan, S. (1987). A course of Mathematical Analysis, 12th revised Ed., S. Chand &Co. (Pvt.) Ltd., New Delhi.
- Somasundram, D. and Chaudhary, B. (1987). A First Course in Mathematical Analysis, Narosa Publishing House, New Delhi.

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