

1. (a) Total sales (S) of a firm selling two products X and Y is given by $S=a+bX+cY$. Determine sales when 10 units of X and 20 units of Y are sold.

- **Approach:**

1. **Formulate Equations:** Set up three linear equations using the given sales data for three months to solve for constants a, b, and c.
2. **Solve using Determinants (Cramer's Rule):** Calculate determinants to find the values of a, b, and c.
3. **Calculate Sales:** Substitute the derived a, b, and c values into the sales equation with $X=10$ and $Y=20$.

OR

1. (a) Mr. Y invested ₹50,000 divided into three investments. Use matrix algebra to find the amount in each.

- **Approach:**

1. **Define Variables:** Represent the amounts invested in savings, bonds, and business as x, y, and z.
2. **Formulate System of Equations:** Create three linear equations based on total investment, net income, and the relationship between business and savings investments.
3. **Solve using Matrix Algebra:** Represent the system as $AX=B$ and calculate $X=A^{-1}B$.

1. (b) Input-Output Analysis: Given transaction matrix, final demand, and labour inputs.

- **Approach:**

- **(i) Technology Matrix & Simon-Hawkins:** Calculate the technology matrix (A) and test viability using Simon-Hawkins conditions on the $(I-A)$ matrix.
- **(ii) Gross Output for New Demand:** Use the Leontief Inverse model: $X=(I-A)^{-1}D_{\text{new}}$.
- **(iii) Feasibility with Labour:** Calculate total labour required for the new output and compare it with the available labour.
- **(iv) Value Added:** Determine value added for each sector (Total Output - Intermediate Consumption).
- **(v) Equilibrium Prices:** Use the price equation $P'=(I-A')^{-1}V'$ (value added per unit derived from labour cost).

OR

1. (b) Input-Output Analysis: Given transaction matrix.

- **Approach:**
 - **(i) Technology Matrix & Simon-Hawkins:** Similar to 1(b)(i) above.
 - **(ii) New Transaction Matrix for Increased Final Demand:** Calculate new gross outputs using the Leontief Inverse, then construct the new transaction matrix by applying the technology coefficients to the new gross outputs.
-

2. (a) EOQ and Inventory Cost: Given annual demand, unit cost, ordering cost, and storage cost.

- **Approach:**
 1. **Calculate EOQ:** Apply the Economic Order Quantity formula.
 2. **Calculate Minimum Total Cost:** Sum the purchasing, ordering, and holding costs at EOQ.
 3. **Evaluate Discount Offer:** Calculate total cost if the order size is 1000 units with the discount and compare it to the minimum total cost.

OR

2. (a) Demand Function: $5q=400-2p$.

- **Approach:**
 - **(i) Elasticity Regions:** Derive the elasticity of demand formula, then find price intervals for elastic, inelastic, and unit elasticity.
 - **(ii) Revenue Function Analysis:** Formulate the total revenue function ($R=pq$), find its derivative, set to zero to maximize revenue, and identify intervals of increase/decrease.

2. (b) Cable Service Operator: Maximize Total Revenue.

- **Approach:**
 1. **Define Variables:** Let 'x' be the number of price decreases.
 2. **Formulate Price and Quantity:** Express price and number of subscribers in terms of 'x'.

3. **Revenue Function:** Create the total revenue function $R=P \times Q$.
4. **Maximize Revenue:** Find the derivative of R with respect to x , set it to zero, and solve for x to determine the optimal decrease in service charge.

OR

2. (b) Engine Cost: Most Economical Speed.

- **Approach:**
 1. **Formulate Fuel Cost:** Establish the proportionality constant 'k' from the given data ($C_f = kv^2$).
 2. **Total Cost per km:** Formulate a total cost function that includes fuel cost and other costs, divided by speed, to get cost per kilometer.
 3. **Minimize Cost:** Differentiate the cost per km function with respect to speed (v), set to zero, and solve for v .
-

3. (a) Monopolist selling in two separate markets: Maximize Profit.

- **Approach:**
 1. **Revenue Functions:** Derive total revenue from each market.
 2. **Total Cost:** Express total cost as a function of total quantity.
 3. **Profit Function:** Formulate profit as Total Revenue - Total Cost.
 4. **Maximize Profit:** Find partial derivatives of profit with respect to quantities in each market, set to zero, and solve the system.

OR

3. (a) Production Function $Q=AL^{2/7}K^{2/7}$.

- **Approach:**
 - **(i) Returns to Scale:** Sum the exponents of L and K .
 - **(ii) Returns to Inputs:** Analyze individual exponents to determine if returns to individual factors are diminishing.
 - **(iii) Total Reward and Exhaustion of Product:** Calculate marginal products (MP_L , MP_K). Total reward is ($L \times MP_L$

$)+(K \times MPK)$. Compare to Q using Euler's theorem for homogeneous functions.

3. (b) Elasticity of Demand: Find Demand Function.

- **Approach:**

1. **Differential Equation:** Set up a differential equation using the elasticity formula $E_d = (dq/dp) \cdot (p/q)$.
2. **Integration:** Integrate the derived differential equation after partial fraction decomposition.
3. **Solve for Constant:** Use the given initial condition ($q=4$ at $p=3$) to find the integration constant and complete the demand function.

OR

3. (b) Demand and Supply Laws: Find Consumer and Producer Surplus.

- **Approach:**

1. **Equilibrium:** Solve for equilibrium quantity (x_0) and price (P_0) by setting demand equal to supply.
2. **Consumer Surplus (CS):** Calculate $\int_0^{x_0} P_d(x) dx - P_0 x_0$.
3. **Producer Surplus (PS):** Calculate $P_0 x_0 - \int_0^{x_0} P_s(x) dx$.

4. Attempt any three questions.

- (a) **Debt Repayment: Find Final Payment.**

1. **Principle of Equivalence:** Equate the present value of all debts to the present value of all payments.
2. **Calculate Present Values:** Discount all future obligations and known payments to the present.
3. **Solve for Final Payment:** Use the equivalence principle to set up an equation and solve for the unknown final payment.

- (b) **Machine Selection: Preferable Machine (NPV).**

1. **Calculate NPV:** For each machine, compute the Net Present Value as (PV of Annual Savings) - Initial Cost.
2. **PV of Annual Savings:** Use the present value of annuity formula.
3. **Compare:** Choose the machine with the higher NPV.

- (c) **Deferred Annuity: Find Amount of Annuity.**

1. **Future Value of Annuity:** Use the future value of an ordinary annuity formula, noting that the deferral period

doesn't affect the future value *at the end of the annuity term itself*.

- (d) **Machine Depreciation: Find Years Used.**
 1. **Depreciation Formula:** Use the reducing balance method formula: $\text{Salvage Value} = \text{Cost} \times (1 - \text{rate})^n$.
 2. **Solve for n:** Substitute the given values and solve for 'n' (number of years) using logarithms.
-

5. Linear Programming (Simplex Method): Complete and Analyze Simplex Table.

- **Approach:**
 - **(i) Complete and Test Optimality:** Calculate the Z_j and $C_j - Z_j$ rows. For maximization, optimality is achieved when all $C_j - Z_j \leq 0$.
 - **(ii) Optimal Product Mix and Profit:** Identify basic variables and their values from the 'Quantity' column to determine the optimal product mix and profit.
 - **(iii) Feasibility:** A solution is feasible if all basic variable values in the 'Quantity' column are non-negative.
 - **(iv) Alternative Solutions:** If any non-basic variable has a $C_j - Z_j = 0$ in the optimal table, an alternative solution exists.
 - **(v) Shadow Prices:** These are the $C_j - Z_j$ values for the slack variables in the optimal table.
 - **(vi) Priority for Expansion:** Prioritize the department with the highest positive shadow price.
 - **(vii) Producing 13 units of x3:** Substitute $x_3 = 13$ into the original constraints and analyze the impact on the other variables and feasibility.
 - **(viii) Price Increase for x3:** This relates to the allowable increase in x_3 's objective function coefficient, often derived from its $C_j - Z_j$ value in the optimal tableau.
 - **(ix) Degeneracy:** A solution is degenerate if any basic variable in the 'Quantity' column has a value of zero.