



Course Name: **Engineering Calculus**

Course Code: **EMAT101L**

Academic Year: 2024-25

Semester: Odd

Date: August 24, 2024

Type: 3-1-0

Tutorial Sheet: **2**

**CO-mapping:**

	CO1	CO2	CO3	CO4	CO5	CO6
Q1	✓					
Q2	✓					
Q3	✓					
Q4	✓					
Q5	✓					

**Objectives:** Students will be able to understand and apply the different methods of convergence and divergence of a sequence.

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1. Show that the sequence  $\langle S_n \rangle$ , defined by the recursion formula

$$S_{n+1} = \sqrt{3S_n} \quad S_1 = 1$$

converges to 3.

2. Examine if the following sequences converge, diverge or oscillate. The  $n^{th}$  term of the sequence are given by:

(a)  $a_n = n \cdot (-1)^{n+3}$

(b)  $a_n = \frac{n^3}{n+1}$

(c)  $a_n = \frac{\cos^2 n}{n}$

3. Show that the following sequences, whose  $n^{th}$  terms are given below, are the convergent sequences.

(a)  $a_n = \left(1 + \frac{1}{n}\right)^n$

(b) For any real number  $x$ ,  $a_n = \frac{x^n}{n!}$

(c)  $a_n = \left( \frac{1}{\sqrt{n^2+1}} + \frac{1}{\sqrt{n^2+2}} + \frac{1}{\sqrt{n^2+3}} + \cdots + \frac{1}{\sqrt{n^2+n}} \right)$

4. Use Sandwich theorem to prove that

(a)  $\lim_{n \rightarrow \infty} \frac{1}{n} \sin^2 n = 0$ .

(b)  $\lim_{n \rightarrow \infty} \left[ \frac{n}{n^3+1} + \frac{2n}{n^3+2} + \cdots + \frac{n^2}{n^3+n} \right] = \frac{1}{2}$ .

5. Use Monotone convergence theorem to prove that

$$\{x_n\} = \left\{ \frac{1}{n+1} + \frac{1}{n+2} + \cdots + \frac{1}{n+n} \right\}$$

is convergent.

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“Constantly think about how you could be doing things better. Keep questioning yourself.” — Elon Musk

