

Phy 112 Assignment 3.1

For inner cylinder:  $\sigma_1 = 18 \times 10^{-6} \text{ C/m}^2$   
 $R_1 = 0.4 \times 10^{-3} \text{ m}$

For ~~outer~~ outer cylinder:

$$\sigma_2 = ?$$

$$R_2 = 1.5 \times 10^{-3} \text{ m}$$

$$\textcircled{a} \quad \sigma (2\pi R_1 L) = -\sigma_2 (2\pi R_2 L)$$

$$\Rightarrow \sigma (R_1) = -\sigma_2 (R_2)$$

$$\Rightarrow \sigma_2 = \frac{-\sigma_1 R_1}{R_2} = \frac{-18 \times 10^{-6} \times 0.4 \times 10^{-3}}{1.5 \times 10^{-3}}$$

$$= -4.8 \times 10^{-6}$$

$\textcircled{b}$

→ curved surface

$$\int E dA \cos 0^\circ + \int E A \cos 90^\circ + \int E A \cos 90^\circ =$$

$$\frac{\sigma_1 (2\pi R_1 L)}{\epsilon_0}$$

↓  
upper circle

↓  
lower circle

$$E \int dA = \frac{Q \times 2\pi R_1 L}{\epsilon_0}$$

$$E (2\pi r l) = \frac{Q \times 2\pi R_1 L}{\epsilon_0}$$

$$E = \frac{Q_1 R_1}{\pi \epsilon_0}$$

$$= \frac{18 \times 10^{-6} \times 0.4 \times 10^{-3}}{0.76 \times 10^{-3} \times 8.854 \times 10^{-12}}$$

$$= 1069989.181$$

②

$$V = \int_{R_1}^{R_2} -E dr = \int_{R_1}^{R_2} \frac{Q_1 R_1}{\epsilon_0} \ln \left( \frac{R_2}{R_1} \right)$$

$$V = \frac{Q_1 R_1}{\epsilon_0} \int_{R_1}^{R_2} \frac{dr}{r} = \frac{Q_1 R_1}{\epsilon_0} \ln \left( \frac{R_2}{R_1} \right)$$

$$\therefore V = \frac{18 \times 10^{-6} \times 0.4 \times 10^{-3}}{8.854 \times 10^{-12}} \ln \left( \frac{1.5 \times 10^{-3}}{0.4 \times 10^{-3}} \right)$$

$$= 1074.8399 \text{ volts}$$



② Capacitance 'C' is given by  
( $L = 0.14 \text{ m}$ )

$$C = \frac{q}{V} = \frac{0_1 (2\pi R_1 L)}{1074.8399}$$

$$= \frac{18 \times 10^{-6} \times 2 \times 3.1416 \times 0.4 \times 10^3 \times 0.14}{1074.8399}$$

$$= 5.892 \times 10^{-12}$$

$$= 5.892 \times 10^{-12}$$

$$\underline{3.2}$$

$q = 5 \mu\text{C}$  charge at the origin

③ Electric field at  $r_1 = 2 \text{ m}$

$$EA = \frac{q}{\epsilon_0}$$

$$\Rightarrow E(4\pi r_1^2) = \frac{q}{\epsilon_0}$$

$$\Rightarrow E = \frac{1}{4\pi\epsilon_0} \frac{q}{r_1^2}$$

$$E = \frac{1}{4\pi\epsilon_0} \frac{5 \times 10^{-6}}{r^2}$$

$$[1 \mu\text{C} = 10^{-6} \text{C}]$$

$$= \frac{1}{4 \times 3.1416 \times 8.854 \times 10^{-12}} \times \frac{5 \times 10^{-6}}{49}$$

$$= 917.114$$

$$a = 1 \text{ m}$$

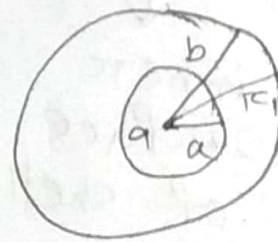
$$b = 4 \text{ m}$$

net charge

$$q_{\text{net}} = 0$$

SO, inner surface will have  $-q$  charge  
 " " " "  $+q$  "  
 outer " " " "

Net charge enclosed by sphere of  
 radius  $r_1$   $q_{\text{enc}} = q - q$   
 $= 0$





②

$$c = 21 \text{ m}$$

$$d = 35 \text{ m}$$

$$r_2 = 17.5 \text{ m}$$

net charged enclosed by  $r_2$

$$q_{\text{enc}} = q - q + q$$

at the center  $\leftarrow$   $\downarrow$   $\rightarrow$  outer surface of shell A

inner surface of shell A

$$\Rightarrow q_{\text{enc}} = q = 5 \times 10^{-6}$$

Electric field at  $r_2$

$$EA = \frac{q_{\text{enc}}}{\epsilon_0}$$

$$\Rightarrow E \cdot 4\pi r_2^2 = \frac{q}{\epsilon_0}$$

$$\Rightarrow E = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r_2^2}$$

$$= \frac{1}{4 \times 3.1416 \times 8.854 \times 10^{-12}} \times \frac{5 \times 10^{-6}}{(17.5)^2}$$

$$= 146.738$$

(d)

we know,

flux formula is  $= q/\epsilon_0$

$$= \frac{5 \times 10^{-6}}{8.854 \times 10^{-12}}$$

$$= 564716.5123$$

(e)

Potential at  $r = d$ ,  $V(d) = \frac{kq}{d}$

$$= \frac{k \times 5 \times 10^{-6}}{35}$$

$$= \frac{9 \times 10^9 \times 5 \times 10^{-6}}{35}$$

$$= 1285.714 \text{ V}$$

Potential at  $r = c$ ,  $V(c) = V(d)$

$$r = \frac{c+d}{2}, V\left(\frac{c+d}{2}\right) = V(d)$$

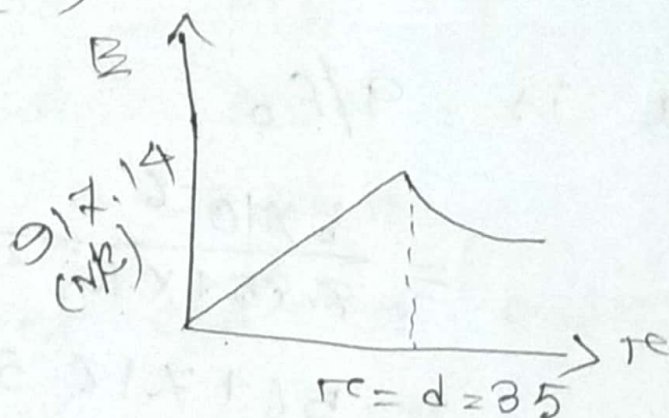
~~For~~  
~~For~~  
For,  
sphere  
 $V_{\text{inside}} =$   
 $V_{\text{sphere}}$

Since  $d$  is the outermost radius

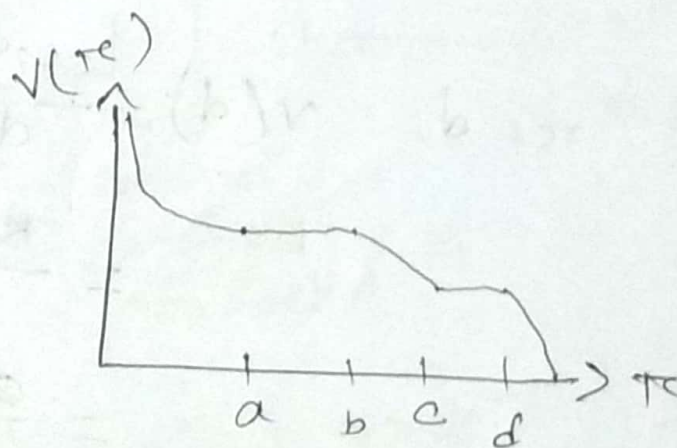
$$V(c) = V\left(\frac{c+d}{2}\right) = V(d) = 1285.714 \text{ V}$$



(f)



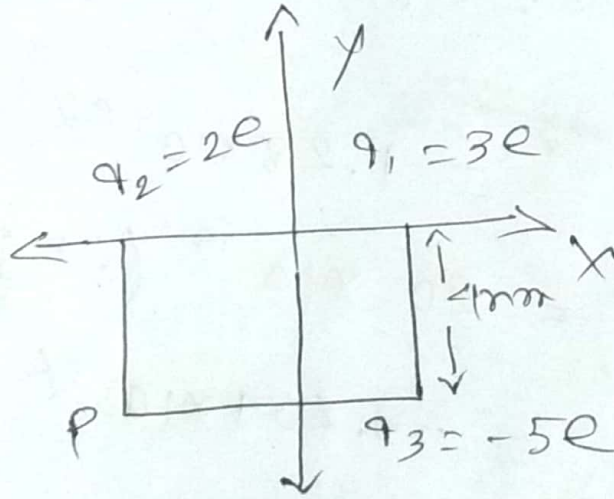
(g)



For plotting potential of  $r$ , we always take the largest value of  $r$  because we always assume  $V(\infty) = 0$

$$V(r) = \begin{cases} \frac{kq}{r} & ; r > d \\ \frac{kq}{d} & ; c < r < d \\ \frac{kq}{r} & ; b < r < c \\ \frac{kq}{b} & ; a < r < b \\ \frac{kq}{r} & ; r < a \end{cases}$$

3.3



① Dipole moment,

$$\vec{P} = \sum q_i \vec{r}_i$$

$$= q_1 \vec{r}_1 + q_2 \vec{r}_2 + q_3 \vec{r}_3$$

$$= (3e \times 2\hat{x}) + (2e \times -2\hat{x}) + (-5e) (2\hat{x} - 4\hat{y})$$



$$x \text{ component} = -8 \times 10^{-9} (-1.60 \times 10^{-19})$$

$$= 1.28 \times 10^{-27}$$

$$y \text{ component} = 20 \times 10^{-9} (-1.602 \times 10^{-19})$$

$$= -3.204 \times 10^{-27}$$

(b)

Electric Potential at 'P'

$$V = \sum \frac{1}{4\pi\epsilon_0} \cdot \frac{q_i}{r_{iP}}$$

$$\begin{aligned} r_{1P} &= 4\sqrt{2} \text{ nm} \\ r_{2P} &= 4 \text{ nm} \\ r_{3P} &= 4 \text{ nm} \end{aligned}$$

$$V = \frac{1}{4\pi\epsilon_0} \left[ \frac{q_1}{r_{1P}} + \frac{q_2}{r_{2P}} + \frac{q_3}{r_{3P}} \right]$$

$$= \frac{1}{4 \times 3.1416 \times 8.854 \times 10^{-12}} \left[ \frac{3 \times (-1.60 \times 10^{-19})}{4\sqrt{2}} + \frac{2 \times (-1.60 \times 10^{-19})}{4} + \frac{5 \times (-1.60 \times 10^{-19})}{4} \right] \times 10^9$$

$$= 3.158 \times 10^{-10} \times 10^9$$

$$= .3158$$

Part II

$$V(x, y) = 3xy(mx + n)$$

$$m = 1 \text{ N/C m}, \quad n = 1 \text{ N/C m}, \quad x = 2 \times 10^{-9} \text{ m}, \quad y = 4 \times 10^{-9} \text{ m}$$

③ Potential at Point 'p' due to  $V(-2, -4)$

$$V(-2, -4) = 3 \times (-2 \times 10^{-9}) \times (-4 \times 10^{-9}) [-2 \times 10^{-9} + 1]$$

$$= 2.399 \times 10^{-17}$$

④ Total Potential  $= V + V(-2, -4)$

$$= .3158 + (2.399 \times 10^{-17})$$

$$= .3158$$

If a proton is placed at P  
then potential energy

$$U = V_P \times e_P$$

$$= .3158 \times (1.602 \times 10^{-19})$$

$$= 5.05 \times 10^{-20}$$



(e)

Electric field due to dipole.

$$E_1 = \frac{kq_1}{(4\sqrt{2})^2} \left( -\sin 45^\circ \hat{i} - \cos 45^\circ \hat{j} \right)$$

$$= \frac{(8.987 \times 10^9) \times (3 \times (-1.602 \times 10^{-19}))}{(4\sqrt{2} \times 10^{-9})^2} \times \left( -\frac{1}{\sqrt{2}} \hat{i} - \frac{1}{\sqrt{2}} \hat{j} \right)$$

$$= -134923506.2 \left( -\frac{1}{\sqrt{2}} \hat{i} - \frac{1}{\sqrt{2}} \hat{j} \right)$$

$$= 95440681.5 \hat{i} + 95440681.5 \hat{j}$$

$$E_2 = \frac{kq_2}{(4 \times 10^{-9})^2} (-\hat{j})$$

$$= \frac{9 \times 10^9 \times 2 \times (-1.602 \times 10^{-19})}{(4 \times 10^{-9})^2} (-\hat{j})$$

$$= 180225000 \hat{j}$$

$$\begin{aligned}
 E_3 &= \frac{kq_3}{(4 \times 10^{-9})^2} (-\hat{i}) \\
 &= \frac{9 \times 10^9 \times 5 \times 1.602 \times 10^{-19}}{(4 \times 10^{-9})^2} (-\hat{i}) \\
 &= -450562500 \hat{i}
 \end{aligned}$$

Electric field due to continuous charge.

$$\vec{E}_4 = \frac{\partial V}{\partial x} \hat{i} - \frac{\partial V}{\partial y} \hat{j} \quad \left| \begin{array}{l} V = 3xy(x+y) \\ = 3x^2y + 3xy^2 \end{array} \right.$$

$$= -(6xy + 3y) \hat{i} - (3x^2 + 3y) \hat{j}$$

$$= -\cancel{6xy} - \cancel{3y}$$

$$= -\cancel{6xy}$$

$$= (-6x - 2x - 4 + 3x - 4) \hat{i} - 3(-2) \hat{j}$$

$$= -60 \hat{i} - 18 \hat{j}$$



value of  $E_4$  is very small compared to  $E_1, E_2, E_3$

x-component of  $E = (9.5441 \times 10^7 - 4.499 \times 10^8) \hat{i}$

$$= -354459000 \hat{i}$$

$$= -3.544 \times 10^8 \hat{i}$$

y-component of  $E = (9.5441 \times 10^7 + 180225000) \hat{j}$

$$= 275666000 \hat{j}$$

$$= 2.75 \times 10^8 \hat{j}$$

(f)

(i)  $\vec{F} = q\vec{E}$

$$\vec{F} = e_p \vec{E}$$

$$= (1.602 \times 10^{-19}) (-3.544 \times 10^8 \hat{i} + 2.75 \times 10^8 \hat{j})$$

$$= -5.67 \times 10^{-11} \hat{i} + 4.4055 \times 10^{-11} \hat{j}$$

$$(17) \quad a_z = \frac{|\vec{r}|}{r} = \frac{\sqrt{(-5.67 \times 10^{-11})^2 + (4.4 \times 10^{-11})^2}}{1.67 \times 10^{-27}}$$

$$= 4.29 \times 10^{16}$$

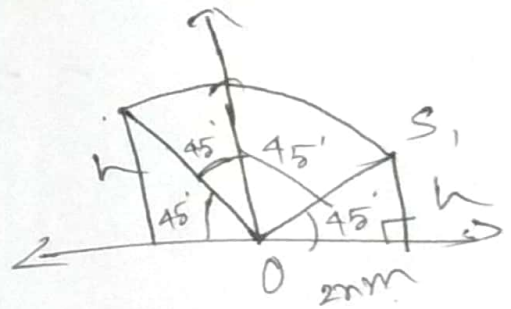
Part - III

$$\tan 45^\circ = \frac{\text{height}}{\text{base}}$$

$$\Rightarrow 1 = \frac{h}{(2 \times 10^{-9})}$$

$$\therefore h = 2 \times 10^{-9} \text{ m or } 2 \text{ nm}$$

$$\text{So, } S_1 = (2, 2) \text{ and } S_2 = (-2, -2) \text{ in nm}$$





(g)

$$V(x, y) = 3xy(x+1)$$

at  $S_1$ ,

$$V(2, 2) = 3(2 \times 10^{-9})(2 \times 10^{-9})(2 \times 10^{-9} + 1)$$

$$= 1.2 \times 10^{-17}$$

$$V(-2, 2) = 3(-2 \times 10^{-9})(-2 \times 10^{-9})(-2 \times 10^{-9} + 1)$$

$$= -1.2 \times 10^{-17}$$

(h)

Potential at  $S_1$ ,

$$V = \sum \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r_{i2}}$$

$$= \frac{1}{4\pi\epsilon_0} \left[ \frac{q_1}{r_{11}} + \frac{q_2}{r_{21}} + \frac{q_3}{r_{31}} \right]$$

$$= \frac{1}{4\pi\epsilon_0} \left[ \frac{3e}{2} + \frac{2e}{4.47} - \frac{5e}{6} \right] \times 10^9$$

$$= -1.6041$$

$$\begin{aligned} r_{11} &= 2 \text{ nm} \\ r_{31} &= 4 + 2 = 26 \text{ nm} \\ r_{21} &= \sqrt{4^2 + 2^2} \\ &= 4.47 \text{ nm} \end{aligned}$$

Potential at  $S_2$ ,

$$V = \sum \frac{1}{4\pi\epsilon_0} \cdot \frac{q_i}{r_{i2}}$$

$$= \frac{1}{4\pi\epsilon_0} \left[ \frac{q_1}{r_{12}} + \frac{q_2}{r_{22}} + \frac{q_3}{r_{32}} \right]$$

$$r_{12} = \sqrt{4^2 + 2^2} = 4.47 \text{ nm}$$

$$r_{22} = 2 \text{ nm}$$

$$r_{32} = \sqrt{6^2 + 4^2} = 7.21 \text{ nm}$$

$$= \frac{1}{4 \times 3.1416 \times 8.854 \times 10^{-12}} \left[ \frac{3e}{4.47} + \frac{2e}{2} - \frac{5e}{7.21} \right] \times 10^9$$

$$= -1.4078$$

i) Total potential at  $S_1 = V_{\text{ees}_1} + V_{\text{dipoles}_1}$

$$= (1.2 \times 10^{-17}) - (1.6039)$$

$$= -1.6039$$

Total potential at  $S_2 = V_{\text{ees}_2} + V_{\text{dipoles}_2}$

$$= (-1.2 \times 10^{-17}) - 1.4078$$

$$= -1.4078$$



(5)

$$V_{S2'} = \frac{kP}{r_{CS_2}}$$

$$= \frac{9 \times 10^9 \times 1.6 \times 10^{-19}}{4 \times 10^{-9}}$$

$$= 0.359 \text{ V}$$

$$V_{netS2'} = V_{netS2'} + V_{S2'}$$

$$= 0.359 - 1.407$$

$$= -1.048 \text{ V}$$

Potential Energy.

$$U = V_{netS2'} \times P$$

$$= -1.048 \times 1.6 \times 10^{-19}$$

$$= -1.676 \times 10^{-19}$$