



# Project Related Discussion

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- Code Structure
- CPU parallelization
- Code Transformations
  - Reasoning About Parallelism: Privatization & Array Expansion
  - Creating CUDA Kernels via Loop Distribution
  - Various Optimizations, e.g., Coalesced Memory
- Project Code: A Bit More Complex Due to a Seq Loop



#### Datasets

- Small: OUTER=16, NUM\_X=32, NUM\_Y=256, NUM\_T=90
- Medium: OUTER=32, NUM\_X=47, NUM\_Y=181, NUM\_T=93
- Large: OUTER=128, NUM\_X=256, NUM\_Y=256, NUM\_T=128

The goal is to parallelize all three parallel dimensions, i.e., TRIDAG can be re-written based on segmented scans. Also optimize such that all accesses to global memory are coalesced.

Target primarily the *small* dataset, which, otherwise, does not has enough parallelism to fully utilize the hardware.



#### **Code Structure**

```
Code Entry Point
                                                value( ... ) {
                                         REAL
                                           initGrid(s0,alpha,nu,t,
                                                    numX.numY.numT.
                                                    globs);
     run_OrigCPU(...) {
void
                                           initOperator(globs.mvX,
  REAL strike;
                                                        globs.myDxx);
  PrivGlobs globs(numX,numY,numT);
                                           initOperator(globs.myY,
  for(int i=0; i<outer; ++ i) {</pre>
                                                        globs.myDyy);
    strike = 0.001*i:
                                           setPayoff(strike, globs);
    res[i] = value( globs, s0, strike, t,
                                           for(int i=numT-2;i>=0;--i){
                    alpha, nu, beta,
                                             updateParams(i,alpha,beta,
                    numX, numY, numT);
                                                          nu,globs);
                                             rollback(i, globs);
                                           return globs.myResult[globs.myXindex]
                                                                 [globs.myYindex]
```

#### **Loop Nests**

#### Loop Nests

```
rollback( ... ) {
 vector<vector<REAL> > u(numY, vector<REAL>(numX)); // [numY] [numX]
 vector<vector<REAL> > v(numX, vector<REAL>(numY)); // [numX] [numY]
 vector<REAL> a(numZ), b(numZ), c(numZ), y(numZ); // [max(numX,numY)]
 vector<REAL> yv(numZ); // temporary used in tridag // [max(numX,numY)]
 for(i=0;i<numX;i++) {</pre>
   for(j=0;j<numY;j++) {</pre>
     u[j][i] = dtInv*globs.myResult[i][j];
 } } ......
 // implicit y
 for(i=0;i<numX;i++) {
   for(j=0;j<numY;j++) { // here a, b, c should have size [numY]</pre>
      a[j] = -0.5*(0.5*globs.myVarY[i][j]*globs.myDyy[j][0]);
     b[j] = dtInv - 0.5*(0.5*globs.myVarY[i][j]*globs.myDyy[j][1]);
      c[j] = -0.5*(0.5*globs.myVarY[i][j]*globs.myDyy[j][2]);
   for(j=0;j<numY;j++)
     y[j] = dtInv*u[j][i] - 0.5*v[i][j];
    // here yy should have size [numY]
    tridag(a,b,c,y,numY,globs.myResult[i],yy);
```

#### How To Parallelize

- summarize accesses inter-procedurally. For each loop what does it write and what does it read?
- Within each loop: are all reads covered by writes executed within the same iteration? If so then privatization solves those dependencies!
- For CUDA: do array expansion instead of privatization.
- Decide for each loop whether it can or cannot be parallelize.
- Use loop distribution to create perfect nests, which will become later your CUDA kernels.
- Use loop interchange and/or matrix transposition to obtain coalesced access to global memory.



- 1 Code Structure
- 2 CPU parallelization
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#### **CPU Parallelization**

In function run\_OrigCPU move the declaration of strike and globs inside the loop, and parallelize the loop via an OPENMP pragma:

```
Parallelizing the Outermost Loop Via OpenMP
```

#### Explain why this is safe in the report!

(For example if you do NOT move the declarations inside the loop and still parallelize the loop, the execution will NOT validate).



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- CPU parallelization
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  - Various Optimizations, e.g., Coalesced Memory
- 4 Project Code: A Bit More Complex Due to a Seq Loop



### Reasoning About Parallelism: Privatization

#### Parallelizing the Outermost Loop Via Privatization

```
float A[N];
                                            for(int i=0;i<M;i++){ //par
for(int i=0;i<M;i++){ //seq
                                              float A[N];
  for(int j=0; j<N; j++) {
                                              for(int j=0;j<N;j++){
    A[j] = \dots
                                                A[j] = \dots
  for(int j=0; j<N; j++){
                                              for(int j=0;j<N;j++){
    \dots = A[j]
                                                 \dots = A[j]
```

- The outermost loop of index i is NOT parallel as it is, because all its iterations write and read all indices of array A.
- However, the iteration reads (is covered by) what was written in the same iteration, a.k.a., array A can be privatized.
- Privatization can be achieved by moving the declaration of a inside the outermost loop (each iteration works with its own private version of A).

## **Array Expansion**

#### Semantically Equivalent: Privatized vs Expanded A

- In CUDA it is preferable that all memory is allocated before the kernel starts, hence making array A local would not work.
- Instead, expand array A with an extra (outermost) dimension, whose size is the count of the outermost loop.
- Now iteration i has exclusive access, i.e., writes to and reads from, row i of expanded array A.
- The two versions of code below are semantically equivalently

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- 2 CPU parallelization
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### Create CUDA Kernels via Loop Distribution

- Theorem: A parallel loop can be distributed across its statements (guaranteed that its dependency graph does not have cycles).
- CUDA kernels are obtained by distributing the outer loop around the inner loops (in order to improve the degree of parallelism).

```
Degree of parallelism M
                               VS.
                                        Degree of parallelism: M*N
                                          float A[M, N];
                                          for(int i=0;i<M;i++){ //par</pre>
float A[M. N]:
for(int i=0;i<M;i++){ //par
                                            for(int j=0; j<N; j++){ //par
  for(int j=0; j<N; j++) {
                                              A[i,j] = ...; // 2D CUDA kernel
    A[i,j] = \dots
                                          for(int i=0;i<M;i++){ //par
  for(int j=0; j<N; j++){
    \dots = A[i,j]
                                          for(int i=0;i<M;i++){ //par
                                            for(int j=0;j<N;j++){ //par
                                               ... = A[i,j]; // 2D CUDA Kernel
                                           } }
```

# Inline Simple Expression vs Array Expansion

- Loop distribution requires array expansion of the local variables.
- If the local variable is a simple scalar expression it is better to inline that expression rather than creating an array for it.
- Use your better judgment when to distribute and when to inline, i.e., do not create too many arrays (tradeoff between redundant computation AND extra memory & global accesses)

```
Inline Scalar Variables
                               Rather Than
                                                   Array Expansion
float A[M, N];
                                      // Systematic distribution will create
for(int i=0;i<M;i++){ //par
                                      // Many Arrays, and Many access to Global
 int tmp = i*i;
                                      // Memory. (It might be cheaper to do some
 for(int j=0; j<N; j++){
                                      // ← redundant computation instead).
    A[i,j] = \dots * tmp;
                                      float tmps[M];
                                      float A[M, N];
       inline scalar exp ↓
                                      for(int i=0;i<M;i++) //par</pre>
float A[M, N];
                                        tmps[i] = (float)(i*i);
for(int i=0;i<M;i++) //par</pre>
                                      for(int i=0;i<M;i++) //par</pre>
 for(int j=0; j<N; j++){//par}
                                        for(int j=0; j<N; j++){//par
    A[i,j] = \dots * ((float)i*i);
                                          A[i,j] = \dots * tmps[i];
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```

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# Optimising CUDA Kernel (Memory Coalescing)

- After creating the CUDA Kernels, one might also want to optimise them, for example
- Coalesced Access to global memory may be obtained via loop interchange or (segmented) matrix transposition.

#### Coalesced Access via Loop Interchange or Matrix Transposition

```
float A[M, N];
                                         // Fixing uncoalesced accesses via
for(int j=0;j<N;j++){ //par</pre>
                                         // matrix transposition
  for(int i=0;i<M;i++){ //par</pre>
                                         float Atr[N, M];
    A[i,j] = ... // uncoalesced access
                                         for(int j=0;j<N;j++){ //par</pre>
for(int i=0;i<M;i++){ //par</pre>
                                              Atr[j,i] = ... // coalesced
for(int i=0;i<M;i++){ //par
  for(int j=0; j<N; j++){ //par
                                         float A[M,N];
    A[i,j] = ... // coalesced access
                                         A=transpose(Atr); //Atr[j,i] \( A \) A[i,j]
} }
```

Note that applying loop interchange may make some uncoalesced accesses coalesced, but it might also make other (originally) coalesced accesses uncoalesced. In those cases use TRANSPOSITION.

# You May Need Segmented Transpose

- Project uses three dimensional arrays, i.e., an array of matrices, and requires transposing each matrix (the two inermost dims).
- Nothing to be afraid of this corresponds to a three dimensional CUDA kernel in which you write the matrix-transposition code for the innermost two dimensions. Pseudocode below:

#### Segmented Transposition: Sequential and CUDA Kernel

```
__global__ void sgmMatTranspose( float* A,
                                        float* trA, int rowsA, int colsA) {
                                   __shared__ float tile[T][T+1];
                                   int gidz=blockIdx.z*blockDim.z*threadIdx.z;
                                   A+=gidz*rowsA*colsA; Atr+=gidz*rowsA*colsA;
float A[O, M, N];
                                   // follows code for matrix transp in x & y
for(int k=0; k<0; k++){ //par
                                   int tidx = threadIdx.x, tidy = threadIdx.y;
 for(int i=0;i<M;i++){ //par</pre>
                                   int j=blockIdx.x*T+tidx,i=blockIdx.y*T+tidy;
   for(int j=0;j<N;j++){ //par</pre>
                                   if( j < colsA && i < rowsA )
      Atr[k,j,i] = A[k,i,j];
                                     tile[tidy][tidx] = A[i*colsA+j];
                                   __syncthreads();
                                   i=blockIdx.y*T+tidx; j=blockIdx.x*T+tidy;
                                   if( j < colsA && i < rowsA )</pre>
```

trA[j\*rowsA+i] = tile[tidx][tidy]

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C. Oancea: Project Sept 2014 19 / 20

### Sequential Loop in Between Parallel Loops

- Loop of index t is sequential because it reads the array myResult[k,0:M-1,0:N-1] produced by previous iteration t-1!
- Distribute the outermost loop across the two loop nests, then interchange to get loop of index t in the outermost position:

```
Code after Array Expansion
                                            Get Seq Loop Outside
float myResult[Outer, M, N];
                                            float myResult[Outer, M, N];
for(int k=0;j<Outer;k++){ //par</pre>
                                            for(int k=0;j<Outer;k++){ //par</pre>
  for(int i=0; i<M; i++) //par</pre>
                                              for(int i=0; i<M; i++) //par</pre>
    for(int j=0; j<N; j++) //par</pre>
                                                for(int j=0; j<N; j++) //par
      myResult[k,i,j] = ...;
                                                   myResult[k,i,j] = ...;
  for(int t=0;tT;t++){ //seq
                                            for(int t=0;tT;t++){ //seq
    for(int i=0; i<M; i++) //par</pre>
                                              for(int k=0;j<Outer;k++){ //par</pre>
      for(int j=0; j<N; j++) //par</pre>
                                                for(int i=0; i<M; i++) //par
         \dots = \dots myResult[k,i,j] \dots;
                                                   for(int j=0; j<N; j++) //par
    for(int i=0; i<M; i++) //par</pre>
                                                     \dots = \dots myResult[k,i,j]
      for(int j=0; j<N; j++) //par</pre>
                                                for(int i=0; i<M; i++) //par
        myResult[k,i,j] = ...;
                                                   for(int j=0; j<N; j++) //par</pre>
                                                     myResult[k,i,j] = ...;
```

myResult[k,i,j] = ...;

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### Sequential Loop in Between Parallel Loops

• Finally, distribute again loop k against the two inner loop nests to create CUDA kernels! Then optimize coalescing, etc.!

```
After Distrib Kernels 2 & 3 are called inside a Sequential Loop
                                            float myResult[Outer, M, N];
float myResult[Outer, M, N];
                                            for(int k=0; j<Outer; k++){ //Kernel1</pre>
for(int k=0;j<Outer;k++){ //par</pre>
                                              for(int i=0; i<M; i++) //Kernel1</pre>
  for(int i=0; i<M; i++) //par</pre>
                                                for(int j=0; j<N; j++) //Kernel1</pre>
    for(int j=0; j<N; j++) //par</pre>
                                                   myResult[k,i,j] = ...;
      myResult[k,i,j] = ...;
                                            for(int t=0;tT;t++){ //seq
for(int t=0;t<T;t++)\{ //seq \}
                                              for(int k=0;j<Outer;k++){ //Kernel2</pre>
  for(int k=0;j<Outer;k++){ //par</pre>
                                                for(int i=0; i<M; i++) //Kernel2</pre>
    for(int i=0; i<M; i++) //par</pre>
                                                   for(int j=0; j<N; j++)//Kernel2</pre>
      for(int j=0; j<N; j++) //par</pre>
                                                     \dots = \dots myResult[k,i,j] \dots
         \dots = \dots myResult[k,i,j] \dots;
    for(int i=0; i<M; i++) //par</pre>
                                              for(int k=0;j<Outer;k++){ //Kernel3</pre>
                                                for(int i=0; i<M; i++) //Kernel3</pre>
      for(int j=0; j<N; j++) //par</pre>
         myResult[k,i,j] = ...;
                                                   for(int j=0; j<N; j++)//Kernel3
```