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Practical 5

Grades with Gaussian distribution

• **Definition :** Write a program which scans marks of n (scan n from the user) students in P & S. Assuming that the students are to be graded on 5 grade-scale (A, B, C, D, and F), display marks and grade of each student. Fit Gaussian distribution to the data. Repeat the exercise if students are to be graded on 7 grade-scale (A, B, C+, C, C-, D, F). Also display bar chart for both the cases.

• **Additional information :**

For more than 30 students in a course, the statistical method shall be used, with marginal adjustment for natural cut-off. The mean(\bar{X}) and the standard deviation(SD) of marks obtained of all the students in a course shall be calculated and grades shall be awarded to a student depending upon the marks and the standard deviation as per table given below:

- For 5 grade scale :

$$A > \bar{X} + 1.5SD$$

$$\bar{X} + 1.0SD < B \leq \bar{X} + 1.5SD$$

$$\bar{X} + 0.5SD < C \leq \bar{X} + 1.0SD$$

$$\bar{X} < D \leq \bar{X} + 0.5SD$$

$$\text{Other : F}$$

- For 7 grade scale :

$$A+ > \bar{X} + 1.5SD$$

$$\bar{X} + 1.0SD < A \leq \bar{X} + 1.5SD$$

$$\bar{X} + 0.5SD < B+ \leq \bar{X} + 1.0SD$$

$$\bar{X} < B \leq \bar{X} + 0.5SD$$

$$\bar{X} - 0.5SD < C \leq \bar{X}$$

$X - 1.0SD < D \leq X - 0.5SD$

Other : F

• Code :

```

1. import math
2. import random
3. import numpy as np
4. import matplotlib.pyplot as plt
5.
6. def gaussFunction(s, x, m):
7.     return (1 / (s * math.sqrt(2 * math.pi))) *
8.         math.exp((-1 / 2) * math.pow((x - m) / s, 2))
9.
10. def cal_grade_5scale(marks, mean, standard_deviation):
11.     if (marks > (mean + 1.5 * standard_deviation)):
12.         return 'A'
13.     elif (mean + standard_deviation < marks <= mean +
14.         1.5 * standard_deviation):
15.         return 'B'
16.     elif (mean + 0.5 * standard_deviation < marks <=
17.         mean + standard_deviation):
18.         return 'C'
19.     elif (mean < marks <= mean + 0.5 *
20.         standard_deviation):
21.         return 'D'
22.     else:
23.         return 'F'
24.
25. def cal_grade_7scale(marks, mean, standard_deviation):
26.     if (marks > (mean + 1.5 * standard_deviation)):
27.         return 'A+'
28.     elif (mean + standard_deviation < marks <= mean +
29.         1.5 * standard_deviation):
30.         return 'A'
31.     elif (mean + 0.5 * standard_deviation < marks <=
32.         mean + standard_deviation):
33.         return 'B+'
34.     elif (mean < marks <= mean + 0.5 *
35.         standard_deviation):
36.         return 'B'
37.
38. # Main Program
39. # Generating random marks
40. marks = np.random.normal(75, 10, 100)
41. # Calculating mean and standard deviation
42. mean = np.mean(marks)
43. standard_deviation = np.std(marks)
44. # Calculating grade for each student
45. grade = []
46. for i in range(100):
47.     grade.append(cal_grade_5scale(marks[i], mean, standard_deviation))
48. # Calculating grade for each student
49. grade = []
50. for i in range(100):
51.     grade.append(cal_grade_7scale(marks[i], mean, standard_deviation))
52. # Printing the grade for each student
53. for i in range(100):
54.     print(marks[i], grade[i])
55.
56. # Plotting the histogram of marks
57. plt.hist(marks, bins=10, color='blue', edgecolor='black')
58. plt.title('Histogram of Marks')
59. plt.xlabel('Marks')
60. plt.ylabel('Frequency')
61. plt.show()

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30. elif (mean - 0.5 * standard_deviation < marks <=
    mean + standard_deviation):
31.     return 'C'
32. elif (mean - standard_deviation < marks <= mean -
    0.5 * standard_deviation):
33.     return 'D'
34. else:
35.     return 'F'
36.
37. def cal_grade_custom(marks, z_score_ranges):
38.     grade = 'A'
39.     for grade_index in range(np.shape(z_score_ranges)
        [0]):
40.         if (z_score_ranges[grade_index][0] < marks <=
            z_score_ranges[grade_index][1]):
41.             return grade
42.         else:
43.             grade = chr(ord(grade) + 1)
44.             continue
45.     return 'F' #by default grade
46.
47. if __name__ == "__main__":
48.     n = int(input("Enter number of students : "))
49.     marks = [random.randint(0, 100) for i in range(n)]
        #generating random marks
50.
51.     mean = np.mean(marks)
52.     standard_deviation = np.std(marks)
53.
54.     grades5 = [cal_grade_5scale(mark, mean,
        standard_deviation) for mark in marks]
55.
56.     print("\n\nGRADES by 5-scale\nMARKS\tGRADES")
57.     for index in range(n):
58.         print(str(marks[index]).ljust(5), "
        ", grades5[index].ljust(5))
59.
60.     grades7 = [cal_grade_7scale(mark, mean,
        standard_deviation) for mark in marks]
61.
62.     print("\n\nGRADES by 7-scale\nMARKS\tGRADES")
63.     for index in range(n):

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64.         print(str(marks[index]).ljust(5), "
",grades7[index].ljust(5))
65.
66. total_grades = int(input("\nEnter total number of
grades : "))
67. print("Enter z-score range for each grade one by one
: ")
68. z_score_ranges = np.zeros(shape=(total_grades,2))
69.
70. for index in range(total_grades):
71.     z_score_ranges[index][0] = float(input("\nEnter
LOWER limit of z-score for GRADE {} :
".format(chr(index+65))))
72.     z_score_ranges[index][1] = float(input("\nEnter
UPPER limit of z-score for GRADE {} :
".format(chr(index+65))))
73.     print()
74.
75. z_score = [(mark - np.mean(marks)) / np.std(marks))
for mark in marks]
76.
77. grades_custom = [cal_grade_custom(z_score_ind,
z_score_ranges) for z_score_ind in z_score]
78. print(grades_custom)
79.
80. print("\n\nGRADES by CUSTOM\nMARKS\tGRADES")
81. for index in range(n):
82.     print(str(marks[index]).ljust(5), "
",grades_custom[index].ljust(5))
83.
84. count5 = []
85. count7 = []
86. counter = 0
87.
88. scale_5_grades = ['A','B','C','D','F']
89. scale_7_grades = ['A','A+','B+','B','C','D','F']
90.
91. for grade_main in scale_5_grades:
92.     counter = 0
93.     for grade_cal in grades5:
94.         if(grade_cal == grade_main):
95.             counter+=1
96.     count5.append(counter)

```

```
97.
98.  for grade_main in scale_7_grades:
99.      counter = 0
100.     for grade_cal in grades7:
101.         if(grade_cal == grade_main):
102.             counter+=1
103.     count7.append(counter)
104.

105. plt.subplot(1,3,1)
106. plt.plot(sorted(marks) ,
    [gaussFunction(standard_deviation, mark, mean) for mark
    in sorted(marks)])
107. plt.title("Gaussian Distribution")
108. plt.xlabel("Marks")
109. plt.ylabel("Probability Density Function")
110.
111. plt.subplot(1,3,2)
112. plt.bar(['A','B','C','D','F'],count5)
113. plt.title("GRADE by scale-5")
114. plt.xlabel("Grades")
115. plt.ylabel("Number of Students")
116.
117. plt.subplot(1,3,3)
118. plt.bar(['A+','A','B+','B','C','D','F'],count7)
119. plt.title("GRADE by scale-7")
120. plt.xlabel("Grades")
121. plt.ylabel("Number of Students")
122.
123. plt.show()
```

• **Sample I/O :**

```
Enter number of students : 500

GRADES by 5-scale
MARKS    GRADES
0        F
85       B
82       B
42       F
30       F
78       C
50       F
80       B
31       F
37       F
```

Running... CPU 0% Memory 789.2M cal_grade_7scale Tabs: 4 Line 59, Column 20

- Like this, it will show the randomly generated marks of all 500 students and corresponding grades assigned by calculation.
- The same will be applied for 7-grade scale as well.

```
GRADES by 7-scale
MARKS    GRADES
0        F
85       A
82       A
42       C
30       D
78       B+
50       C
80       A
31       D
37       C
12       F
57       B
```

Running... CPU 0% Memory 789.3M cal_grade_7scale Tabs: 4 Line 59, Column 20

Z-score values which are entered by user.

```

Enter total number of grades : 4
Enter z-score range for each grade one by one :
  Enter LOWER limit of z-score for GRADE A : -2

  Enter UPPER limit of z-score for GRADE A : -1

  Enter LOWER limit of z-score for GRADE B : -1
  Enter UPPER limit of z-score for GRADE B : 0

  Enter LOWER limit of z-score for GRADE C : 0
  Enter UPPER limit of z-score for GRADE C : 1

  Enter LOWER limit of z-score for GRADE D : 1
  Enter UPPER limit of z-score for GRADE D : 2

```

Running... CPU 0% Memory 789.3M cal_grade_7scale Tabs: 4 Line 59, Column 20

Graph generated :

