

III) 0/1 Knapsack problem

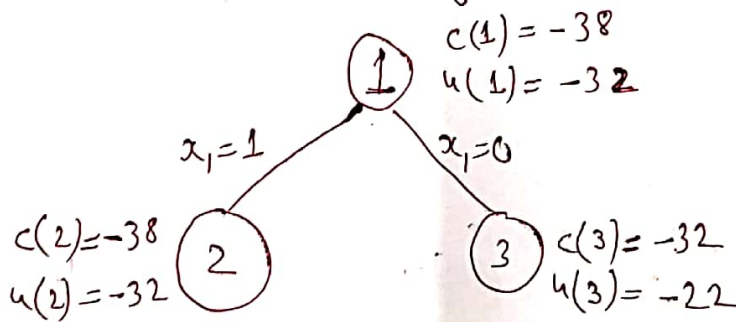
$n = 4$ items
 $W = 15$ kg

| i | 1 | 2 | 3 | 4 |
|---|----|----|----|----|
| P | 10 | 10 | 12 | 18 |
| w | 2 | 4 | 6 | 9 |

We want to maximize profit in the knapsack of capacity (15 kg)

Sol:- Branch-and-Bound technique is applicable to "Minimization problems". So, here we'll solve this problem (of maximization) by converting it into Minimization problem.

C (cost) \rightarrow with fractional
 u (upper bound) \rightarrow without fractional



(Explore the Least-Cost Node)

$c(3)$ [Fractional]

$$\Downarrow$$

$$i \Rightarrow 2, 3, \frac{5}{9}(4)$$

$$P \Rightarrow 10 + 12 + \frac{5}{9}(18)$$

$$= -32$$

$u(3)$ [without fractional]

$$i \Rightarrow 2, 3$$

$$P \Rightarrow 10 + 12 = -22$$

$c(1)$ [fractional]

$$\Downarrow$$

$$i \Rightarrow 1, 2, 3, \frac{3}{9}(4)$$

$$P \Rightarrow 10 + 10 + 12 + \frac{3}{9}(18)$$

$$= 10 + 10 + 12 + 6$$

$$= -38$$

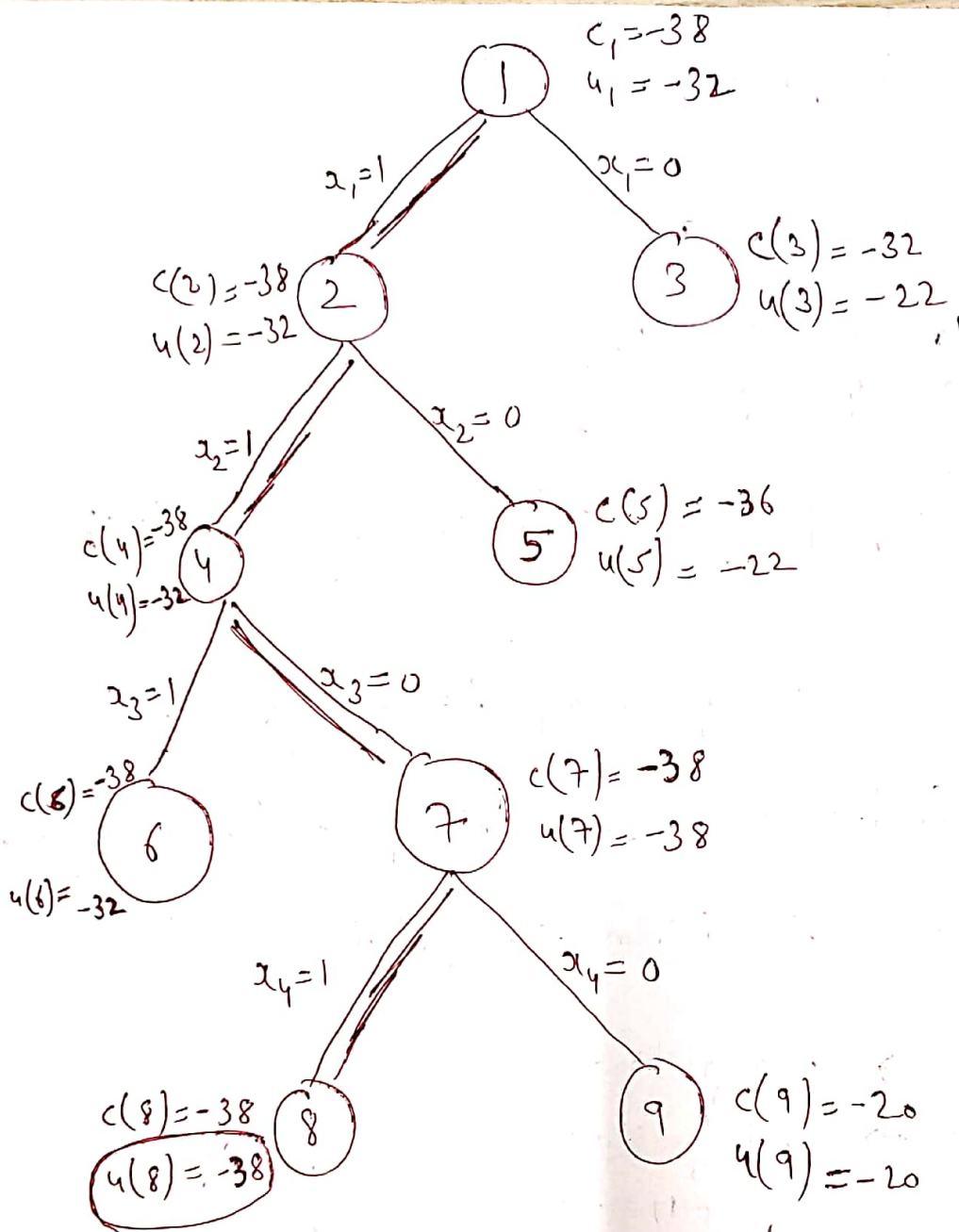
$u(1)$ [without fractional]

$$\Downarrow$$

$$i \Rightarrow 1, 2, 3$$

$$P \Rightarrow 10 + 10 + 12$$

$$= -32$$



$$\begin{aligned}
 & c(5) \\
 & \Downarrow \\
 & i \Rightarrow 1, 3, 4\left(\frac{7}{9}\right) \\
 & P \Rightarrow 10 + 12 + \frac{7}{9}(18) \\
 & = \underline{\underline{-36}} \\
 & u(5) \\
 & \Downarrow \\
 & i \Rightarrow 1, 3 \\
 & P \Rightarrow 10 + 12 \\
 & = \underline{\underline{-22}}
 \end{aligned}$$

Profit = 38 units.

Selection = $\{1, 1, 0, 1\}$ [Items:- 1, 2 and 4]

Q-2

$n = 4$ items

$W = \underline{\underline{16 \text{ kg}}}$

| i | 1 | 2 | 3 | 4 |
|---|----|----|----|----|
| P | 45 | 30 | 45 | 10 |
| w | 3 | 5 | 9 | 5 |