

Tutorial No 2: Finite Automata

Q:1 In each case below, find a string of minimum length in $\{a, b\}^*$ not in the language corresponding to the given regular expression.

- $b^*(ab)^*a^*$
- $(a^*+b^*)(a^*+b^*)(a^*+b^*)$
- $a^*(baa^*)^*b^*$
- $b^*(a+ba)^*b^*$

Q:2 Consider the two regular expressions

$$r = a^* + b^*$$

$$s = ab^* + ba^* + b^*a + (a^*b)^*$$

- Find a string corresponding to r but not to s
- Find a string corresponding to s but not to r
- Find a string corresponding to both r and s
- Find a string in $\{a, b\}^*$ corresponding to neither r nor s

Q:3 Find the regular expression and finite automaton for following languages.

$$\Sigma = \{a, b\}$$

- The language of all strings containing exactly two a 's.
- The language of all strings containing at least two a 's.
- The language of all strings that do not end with ab
- The language of all strings that begin or end with aa or bb
- The language of all strings not containing the substring aa .

Q:4 Explain in brief any 3 applications of Finite State Machine.

Q:5 For the following sets, write the corresponding regular expression:

- $\{1, 12, 112, 1112, 11112, \dots\}$
- $\{0, 1\}$
- $\{a^2, a^4, a^6, a^8, a^{10}, \dots\}$
- $\{a^x \mid x \text{ is divisible by 3 or 5}\}$