

# Tutorial = 5

Ques = 1 Minimize the following FAs

1.  $\Rightarrow A, B, C, D, E, \emptyset$

Accepting states  
 $= A, B, C, D, E$

* B	2				
* C	3	2			
* D	3	2			
* E	3	2			
* $\emptyset$	1	1	1	1	1
	A	B	C	D	E

C, D, E

A

B

$\emptyset$

$$\delta(B, a) = \emptyset$$

$$\delta(A, a) = b$$

$$\delta(B, b) = \emptyset$$

$$\delta(A, b) = E$$

$$\delta(D, a) = E$$

$$\delta(\emptyset, a) = b$$

$$\delta(D, b) = D$$

$$\delta(A, b) = D$$

$$\delta(C, a) = E$$

$$\delta(B, a) = \emptyset$$

$$\delta(E, a) = E$$

$$\delta(B, a) = \emptyset$$

$$\delta(C, a) = E$$

$$\delta(A, a) = b$$

$$\delta(C, b) = D$$

$$\delta(A, b) = D$$

$$\delta(E, a) = E$$

$$\delta(A, a) = b$$

$$\delta(E, b) = D$$

$$\delta(A, b) = D$$

$$\delta(D, a) = E$$

$$\delta(B, a) = \emptyset$$

$$\delta(D, a) = E$$

$$\delta(C, a) = E$$

$$\delta(D, b) = D$$

$$\delta(C, b) = D$$

$$\delta(E, a) = E$$

$$\delta(C, a) = E$$

$$\delta(E, b) = D$$

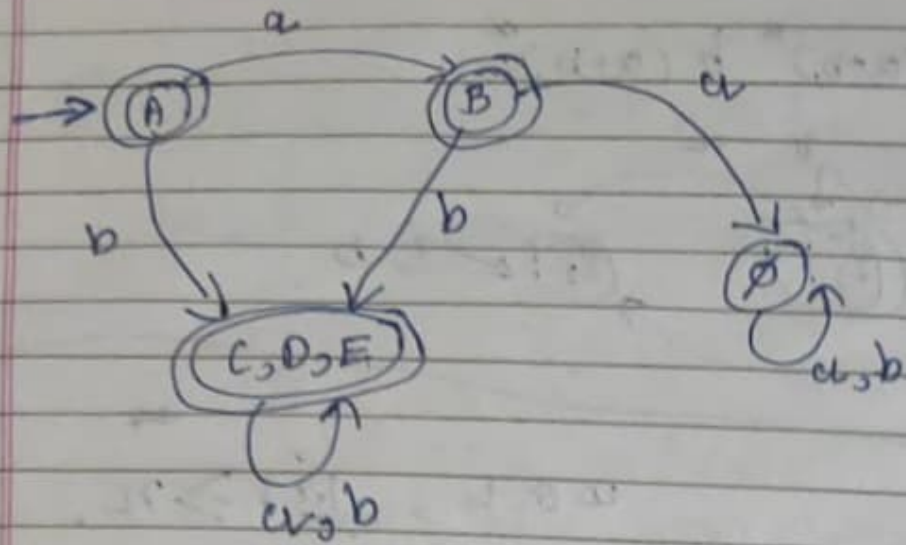
$$\delta(E, b) = D$$

$$\delta(E, a) = E$$

$$\delta(D, a) = E$$

$$\delta(E, b) = D$$

$$\delta(D, b) = D$$



②

1, 2, 3, 4, 5, 6, 7, 8

2	1							
3		1						
4	1	2	1					
5	2	1	2	1				
6	1		1	2	1			
7	2	1	2	1		1		
8	1	2	1		1	2	1	
	1	2	3	4	5	6	7	

$\delta(1, a) = 2$   
 $\delta(2, a) = 5$   
 $\delta(3, b) = 7$   
 $\delta(7, b) = 4$

2, 4, 6, 8

$\delta(1, a) = 2$   
 $\delta(2, a) = 5$   
 $\delta(3, b) = 7$   
 $\delta(7, b) = 4$

$\delta(1, a) = 2$   
 $\delta(2, a) = 5$   
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 $\delta(2, a) = 5$   
 $\delta(3, b) = 7$   
 $\delta(7, b) = 4$

$\delta(1, a) = 2$   
 $\delta(2, a) = 5$   
 $\delta(3, b) = 7$   
 $\delta(7, b) = 4$

$\delta(1, a) = 2$   
 $\delta(3, a) = 6$   
 $\delta(1, b) = 7$   
 $\delta(3, b) = 5$

$\delta(1, a) = 2$   
 $\delta(7, a) = 8$   
 $\delta(1, b) = 7$   
 $\delta(7, b) = 4$

$\delta(2, a) = 5$   
 $\delta(8, a) = 3$   
 $\delta(2, b) = 3$   
 $\delta(8, b) = 7$

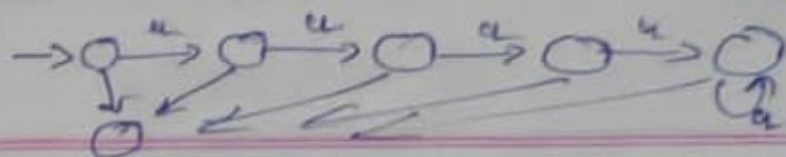
$\delta(1, a) = 2$   
 $\delta(5, a) = 8$   
 $\delta(1, b) = 7$   
 $\delta(5, b) = 8$

$\delta(2, a) = 5$   
 $\delta(5, a) = 8$

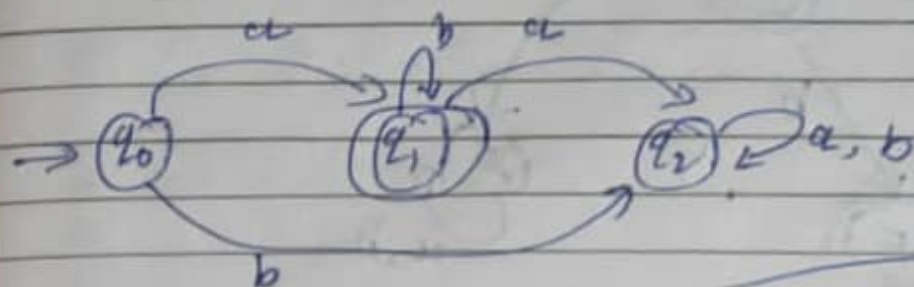
$\delta(2, a) = 5$   
 $\delta(6, a) = 7$   
 $\delta(2, b) = 3$   
 $\delta(6, b) = 7$

$\delta(3, a) = 6$   
 $\delta(5, a) = 8$   
 $\delta(3, b) = 5$   
 $\delta(5, b) = 8$





$$(a+b)^* a (a+b)^* b (a+b)^*$$



①

$$x = uvw$$

$$x \in L, |x| \geq n$$

①  $|uv| \leq n$

②  $|v| > 0$

③ for any  $m \geq 0, uv^m w \in L$

$$x = 0^n 1^n \quad x \in L$$

$$|x| = 2n \geq n$$

$$uv = 0^n$$

$$|uv| = n \leq n$$

$$uv = 0^{n-1} 0^1 \quad |v| > 0$$

$$uv = 0^{n-2} 0^2 \quad |v| > 0$$

$$\Rightarrow u = 0^{n-1} \quad v = 0^1$$

Now,  $uvw \in L \quad uvw = 0^n 1^n$

Now,  $m=2$

$$uv^m w = 0^{n-1} (0^1)^2 1^n$$

$$= 0^{n-1} (0^1)^2 1^n$$

$$= 0^{n+1} 1^n \notin L$$

∴ prove not Regular.

Tut-5  
Ques-19

$$(2) L = \{ x^n \mid x \in \{0, 1\}^n \}$$

$$|x| = (01)^n$$

$$x = (01)^n$$

$$n > 0$$

uv =

$$x = (01)^n$$

$$\text{Now } x^n = (01)^n (01)^n$$

$$|x| = x^n = (01)^n (01)^n$$

$$\text{Now } |x| = 4n \geq n$$

$$\text{Now } |x| = (01)^n (01)^n$$

$$\text{Now } uv = (01)^n$$

$$uv = 2n$$

$$|x| = 0^n 1^n 0^n 1^n$$

$$uv = 0^n$$

$$w = 1^n 0^n 1^n$$

$$|uv| = n \leq n$$

$$\therefore u = 0^{n-1}$$

$$v = 0$$

$$w = 1^n 0^n 1^n$$

Now,  $uvw \in L$

$$uv^m w = (0^{n-1}) (0)^m (1^n 0^n 1^n)$$

$$m = 2$$

$$= 0^{n-1} 0^2 (1^n 0^n 1^n)$$

$$= 0^{n+1} 1^n 0^n 1^n$$

$$= 0 (01)^n (01)^n$$

$$= 0 (01)^n (01)^n$$

$$\notin L$$

∴ prove



$$(3) L = \{ ww^R \mid w \in (a,b)^* \text{ and } |w| = 2 \}$$

$\Rightarrow$  for some integer  $n$

$$w = (ab)^n$$

$$w = (ab)^n$$

$$n=2$$

$$w = ab, ba, bbaa, aabb$$

$$w^R = w$$

$$x = (ab)^n (ba)^n$$

$$|x| = 4n \geq n$$

$$x = a^n b^n b^n a^n$$

$$\text{Now } uv = a^n$$

$$|uv| = n \leq n$$

$$u = a^{n-1}$$

$$v = a$$

$$w = b^n a^n$$

Now,  $uvw \in L$

$$uvm^w = (a^{n-1}) (a)^m (b^n a^n) \quad m \geq 0$$

Now  $m=2$

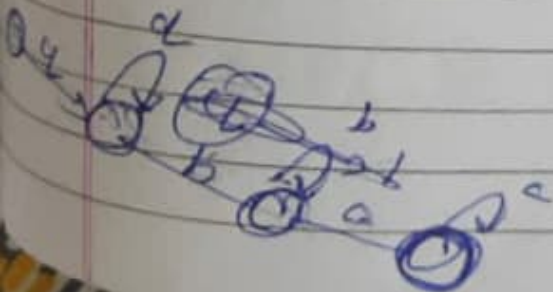
$$= a^{n-1} a^2 b^n a^n$$

$$= a a^n b^n a^n$$

$$= a (ab)^n (ba)^n$$

$$\notin L$$

$\therefore$  prove



# Tutorial - 6

Design CFG

(a)  $\{a^i b^j c^k / i = j + k\}$  (b)  $\{a^i b^j c^k / j = i + k\}$

$$\begin{aligned} \Rightarrow a^i b^j c^k \\ \Rightarrow a^{j+k} b^j c^k \\ \Rightarrow a^j b^j a^k c^k \\ \Rightarrow (ab)^j (ac)^k \\ \quad \quad \quad L_1 \quad \quad L_2 \end{aligned}$$

$$\begin{aligned} A &\rightarrow aAb / n \\ B &\rightarrow aBc / n \end{aligned}$$

$$\begin{aligned} \Rightarrow a^i b^{j+k} c^k \\ \Rightarrow a^i b^j b^k c^k \\ \Rightarrow (ab)^j (bc)^k \end{aligned}$$

$$\begin{aligned} A &\rightarrow aAb / n \\ B &\rightarrow bBc / n \\ S &\rightarrow AB \end{aligned}$$

$$S \rightarrow AB$$

(c)  $\{a^i b^j c^k / j = i \text{ or } j = k\}$

abcc ✓  
aabc

$$\begin{aligned} j=i \\ \Rightarrow a^i b^j c^k \\ \Rightarrow (ab)^i c^k \end{aligned}$$

$$\begin{aligned} j=k \\ \Rightarrow a^i b^k c^k \\ \Rightarrow a^i (bc)^k \end{aligned}$$

$$\begin{aligned} A &\rightarrow aAb / n \\ B &\rightarrow cB / n \end{aligned}$$

$$\begin{aligned} D &\rightarrow aD / n \\ E &\rightarrow bEc / n \end{aligned}$$

$$S_1 \rightarrow AB$$

$$S_2 \rightarrow DE$$

$$S \rightarrow S_1 / S_2$$

$$\begin{aligned} S &\rightarrow S_1 / S_2 \\ S_1 &\rightarrow AB \\ S_2 &\rightarrow DE \\ A &\rightarrow aAb / n \\ B &\rightarrow cB / n \\ D &\rightarrow aD / n \\ E &\rightarrow bEc / n \end{aligned}$$

$$\begin{aligned} S &\rightarrow S_2 \rightarrow DE \\ &\rightarrow aD bEc \\ &\quad \quad \quad aA \quad \quad \quad nC \end{aligned}$$

abcc  
aA

aAbcB  
aAbccB



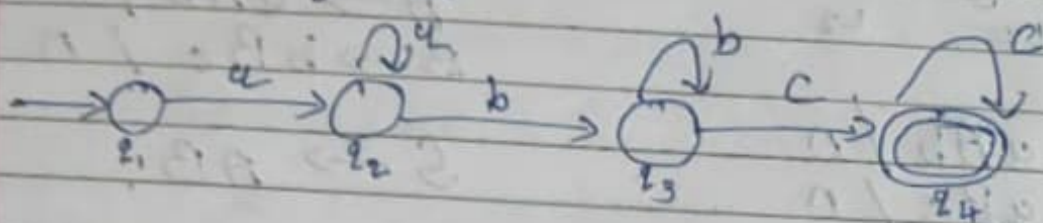
(4)  $L = \{ a^n b^m c^k \mid n, m, k \geq 1 \}$

$\Rightarrow X = (a^n b^m c^k)^i \quad i \geq 0$

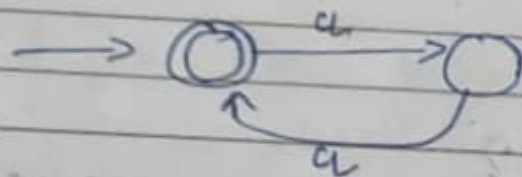
$|X| = (n+m+k)^i \geq i$

~~$X = a^n b^m c^k$~~

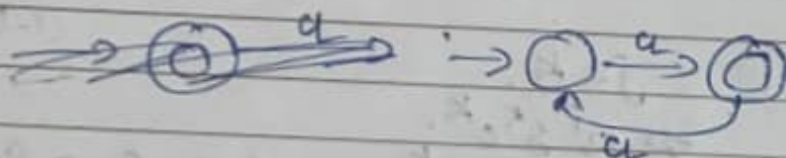
Is Regular?



(5)



(6)



(7)

$B^+$  4

(d)  $\{a^i b^j c^k / i=j \text{ or } i=k\}$

$i=j$   
 $\Rightarrow a^i b^j c^k$   
 $\Rightarrow (ab)^j c^k$

$A \rightarrow aAb / n$

$B \rightarrow cB / n$

$S_1 \rightarrow AB$

$i=k$   
 $\Rightarrow a^k b^j c^k$   
 $\Rightarrow \underbrace{a^k b^j c^k}_{\text{Diagram showing three separate blocks: } a^k, b^j, c^k}$

$D \rightarrow aD / n$

$E \rightarrow bE / n$

$F \rightarrow cF / n$

$S_2 \rightarrow DEF$

$S \rightarrow S_1 / S_2$

- CN 4  
 DAA 4  
 ML 4

(e)  $\{a^i b^j c^k / i < j \text{ or } i > k\}$

$\Rightarrow j = i + m \quad m > 0$

$\Rightarrow a^i b^i b^m c^k$   
 $\Rightarrow (ab)^i b^m c^k$

$A \rightarrow aAb / n$

$B \rightarrow bB / n$

$D \rightarrow cD / n$

$S_1 \rightarrow ABD$

$i = k + n \quad n > 0$

$\Rightarrow a^k a^n b^j c^k$   
 $\Rightarrow \text{Diagram showing three separate blocks: } a^k, a^n, b^j, c^k$

$E \rightarrow aE / n$

$F \rightarrow aF / n$

$G \rightarrow bG / n$

$H \rightarrow cH / n$

$S_2 \rightarrow EFGH$

$S \rightarrow S_1 / S_2$