

⊛ Never blindly trust anything.

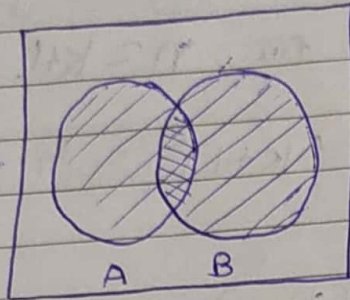
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# Tutorial 1

①



$$= (A-B) \cup (B-A) \cup (A \cap B)$$

$$= A \cup B$$

$$n(A \cup B) \leq n(A) + n(B)$$

$$\therefore n(A \cup B) = n(A) + n(B) - n(A \cap B)$$

②

$$P \vee \neg(P \rightarrow Q)$$

Ans. P.

$$\begin{aligned} P \vee \neg(P \rightarrow Q) & \therefore P \vee \neg(P \rightarrow Q) \\ P \vee (\neg P \rightarrow \neg Q) & \therefore P \vee \neg(\neg P \vee Q) \\ P \vee (\neg P \vee \neg Q) & \therefore P \vee (P \wedge \neg Q) \\ & \therefore P \vee P \wedge \neg Q \\ & \therefore P \wedge \neg Q \end{aligned}$$

$$\begin{aligned} & \therefore (P \vee P) \wedge (P \vee \neg Q) \\ & \therefore (P \vee P) \wedge (X) \\ & \therefore P. \end{aligned}$$

$$X \equiv (P \vee \neg Q)$$



③ Relationship bet<sup>n</sup>  $2^{A \cup B}$  and  $2^A \cup 2^B$ .

$\Rightarrow$  Let  $A$  &  $B$  are ordinary sets

Let  $x \in 2^A \cup 2^B$

$\therefore x \in 2^A$  or  $x \in 2^B$

$\therefore x \subseteq A$  or  $x \subseteq B$

$\therefore x \subseteq A \cup B$

$\therefore x \in 2^{A \cup B}$

as  $x$  is arbitrary element of  $2^A \cup 2^B$

$\therefore 2^A \cup 2^B \subseteq 2^{A \cup B}$  for any arbitrary  $A$  &  $B$

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$$\forall L, L^* = (L^*)^*$$

I've started with

## 4th question

$$\text{def. } L^* = \bigcup_{i \in \mathbb{N}} L^i, L^0 = \{\epsilon\}, L^1 = \{L\}, L^{i+1} = \{uv \mid u \in L^i, v \in L\}$$

$$\text{then } (L^*)^* = \bigcup_{i \in \mathbb{N}} (L^*)^i, (L^*)^0 = \{\epsilon\}, (L^*)^1 = \{L^*\}, (L^*)^{i+1} = \{uv \mid u \in (L^*)^i, v \in L^*\}$$

$$L \cdot L^0 \in (L^*)^* = L^* \cdot \epsilon = L^* \therefore L \subseteq (L^*)^*$$

$L \cdot L^0 = L^*, L \cdot L^1 = L^* \text{ (def)}, L \cdot L^{i+1} = L^* \cdot L^i = L^* \cdot L^* \text{ but the } * \text{ operator is closed under concatenation, thus, } L \cdot L^i \in L^* \therefore (L^*)^* \subseteq L^*$

$$\therefore L^* = (L^*)^*$$

I simply don't have an intuition on whether this attempt at a proof is correct and I would appreciate any insight about it since the subsequent problems are to show  $L^+ = (L^+)^+$  and then to argue whether  $(L^*)^+ = (L^+)^*$



bezglasniac and 3 more users found this answer helpful



THANKS 1



3.0 (2 votes)



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5 Relationship bet<sup>n</sup>  $L_1 \cdot (L_2 \cap L_3)$  and  $L_1 L_2 \cap L_1 L_3$

$\Rightarrow$  String  $w \in L_1 \cdot (L_2 \cap L_3)$

Let  $w = xy$ ,  $x \in L_1$   $y \in L_2 \cap L_3$   
 $\therefore y \in L_2$  &  $y \in L_3$

$$\rightarrow L_1 \cdot (L_2 \cap L_3) \subseteq L_1 L_2 \cap L_1 L_3$$

$$\rightarrow L_1 L_2 \cap L_1 L_3 \subseteq L_1 \cdot (L_2 \cap L_3)$$

$\Rightarrow$  Both equal.  $L_1 (L_2 \cap L_3) = L_1 L_2 \cap L_1 L_3$



$$\textcircled{6} \quad n \geq 0. \quad \sum_{i=1}^n i^2 = n(n+1)(2n+1)/6$$

Basic.  $i=0$ . (LHS) = 0, RHS = 0.  
LHS = RHS.

Assume that this is true for  $n=k$ .

$$\sum_{i=1}^k i^2 = k(k+1)(2k+1)/6.$$

prove that it is true for  $n = k+1$ .

$$\sum_{i=1}^{k+1} i^2 = \sum_{i=1}^k i^2 + (k+1)^2$$

$$= k(k+1)(2k+1) + (k+1)^2$$

$$= \frac{(k+1)(k+2)(2(k+1)+1)}{6}$$

proved

[7]

$\Rightarrow$

$x^n$  is reverse.

$\rightarrow$

$$x = a$$

Basic

~~Basic~~

$$LHS = 1$$

$$(RHS = 1 \cdot S =$$

$$LHS = RHS$$

of addition or multiplication

Assume for

$$|x^n| = k$$

$$x = a^k$$

~~Basic~~

~~Basic~~

$$|(a^k)^n| = |a^k|$$

k is length.



$$n = k+1.$$

$$a^{k+1} = (a^k \cdot a)$$

$$= |a^k| + |a|$$

$$= (a^k)^n + (a^n)$$

$$\therefore |a^{k+1}| = (a^{k+1})^n$$

## [8] Recursive definition..

a. The set  $N$  of all Natural numbers

→ Rec. def. for set of all Natural numbers will be the set of containing all natural numbers

→ 1. min value ~~1~~ / Basic condition / Min string  
 $1 \in S$ .

→ 2. For any  $x$ ,  $x \in N$ . then  $x+1 \in N$ .

$$X = \{1, 2, 3, \dots\}$$

→ 3. No other element will belong to the set unless it satisfy condition 1 & 2.

Write in proper format like que.

- b.
1.  $x = 7$
  2.  $x+7, x-7 \in S$
  3. No other element will belong to set unless satisfy cond. 1 & 2

c. ~~1.~~  $00 \in U$

2.  $1x \in U$

$x1 \in U$

$0x \in U$

$x0 \in U$

3. No other ele...