

Q-1) A supply system has following loads
a lighting load of ~~1000~~ 900 kW,
Industrial load = 1200 kW at 0.907
P.F. = 0.907 (lag)

→ A load of 600 kW @ 0.8 leading
P.F.

→ 500 kW @ 0.6 lagging.

→ A synchronous motor 600 kW
having overall efficiency $\eta = 95\%$.
calculate P.F. of motor so that
distribution station is operating at
Unity P.F.

Q-2
Resistor

Heat by dielectric heating,
12 x 12 x 3 cm. $f = 20 \text{ MHz}$,

Power absorb = 450 W

Relative permittivity $\epsilon_r = 5$

P.F. = 0.05

Calculate Voltage & current,
→ If Voltage is limited to 1700 V AC
what will be d to get same
loss.

Q1

Lighting load works at unity p.f.
 \therefore its lagging kVAR = 0

Lagging kVAR are taken by (ii) & (iv)
 (iii) & (v) take leading kVAR

For station p.f. to be unity, tot lagging kVAR must be neutralised by tot. leading kVAR.
 We know $kVAR = kW \tan \phi$

$$\begin{aligned} \therefore \text{Tot lagging kVAR by taken by (ii) \& (iv)} \\ &= 400 \tan(\cos^{-1} 0.707) + 500 \tan(\cos^{-1} 0.6) \\ &= 1200 \tan(\cos^{-1} 0.707) + 500 \tan(\cos^{-1} 0.6) \\ &= 1200 + 666.6 \\ &= 1866.66 \end{aligned}$$

Leading kVAR taken by (iii)

$$\begin{aligned} &= 600 \tan(\cos^{-1} 0.8) \\ &= 450 \end{aligned}$$

$$\begin{aligned} \therefore \text{Leading kVAR to be taken by synch. motor:} \\ &= 1866.66 - 450 = \underline{\underline{1416.66 \text{ kVAR}}} \end{aligned}$$

$$\cancel{\tan \phi} = \cancel{\frac{kVAR}{kW}}$$

$$\text{Motor input} = \frac{\text{output}}{\text{efficiency}} = \frac{600}{0.95} = \underline{\underline{631.5 \text{ kW}}}$$

$$\begin{aligned} \text{If } \phi \text{ is phase angle of synch. motor, then} \\ \tan \phi = \frac{kVAR}{kW} = \frac{1416.66}{631.5} = \underline{\underline{2.245}} \end{aligned}$$

$$\phi = 73.32^\circ$$

$$p.f. \text{ of synch. motor} = \cos \phi = \boxed{0.406} \quad \text{leading}$$

Q2 $12 \times 12 \times 3$ dielectric $\therefore A = 144 \text{ cm}^2$, $d = 3 \text{ cm}$
 $f = 20 \text{ MHz}$
 $P = 450 \text{ W}$
 $\epsilon_r = 5$ $p.f. = 0.05$

Cal. voltage & current.

If voltage is limited to 1700 V , what will be freq. to get same loss?

$$P = 2\pi f C V^2 \times p.f. \quad \epsilon_0 = 8.89 \times 10^{-12}$$

$$C = \frac{A}{d} \times \epsilon_0 \epsilon_r = 21.33 \times 10^{-12}$$

$$\therefore V = \sqrt{\frac{P}{2\pi f C p.f.}}$$

$$= \sqrt{\frac{450}{2 \times 3.14 \times 20 \times 10^6 \times 21.33 \times 10^{-12} \times 0.05}}$$

$$= 1.832 \times 10^3 \text{ V}$$

$$\boxed{V = 1832 \text{ V}}$$

$$I = \frac{P}{V \times p.f.} = \frac{450}{1832 \times 0.05} = \boxed{4.91 \text{ A}}$$

$$H \propto V^2 f \quad \therefore \left(\frac{V_2}{V_1}\right)^2 = \left(\frac{f_1}{f_2}\right)$$

$$\therefore f_2 = f_1 \left(\frac{V_1}{V_2}\right)^2 = 20 \left(\frac{1832}{1700}\right)^2 = \boxed{23.22 \text{ MHz}}$$

Specific heat of water $C_{pw} = 4.19 \text{ kJ/kg K}$

$C_{pic} = 2.1 \text{ kJ/kg K}$

Latent heat of ice = 336 kJ/kg

Energy required to convert
1 ton of water
↓
1 ton of ice

Q-4

8-0 50 Hz 415 V induction motor develop 100 HP power at 0.95 p.f. with the efficiency of 93%. A capacitor bank is connected in delta across the supply to raise the p.f. to 0.95 lagging. Each capacitor unit is built up of 4 similar 1000 μF capacitor, connected in series. Determine the capacitance of each capacitor.

$\cos \phi_1 = \frac{P}{S_1}$ $\cos \phi_2 = \frac{P}{S_2}$

$0.95 = \frac{P}{S_1}$

$0.95 = \frac{P}{S_2}$

8-0 50 Hz 415 V

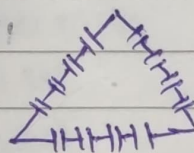
$V_L = 415 \text{ V}$

$\cos \phi_1 = 0.95 \text{ (lag)}$

$\cos \phi_2 = 0.95 \text{ (lag)}$

$P = 100 \text{ HP}$

$= 74.5 \text{ kW}$



$\eta = 93\%$

$\phi_1 = \cos^{-1}(0.95) = 18.4^\circ$

$\phi_2 = \cos^{-1}(0.95) = 18.19^\circ$

$S_1 = \frac{P}{\eta \cos \phi_1} = \frac{74.5}{0.93 \cos(18.4^\circ)} = 85.66 \text{ KVAR}$

$S_2 = \frac{P}{\eta \cos \phi_2} = \frac{74.5}{0.93 \cos(18.19^\circ)} = 24.47 \text{ KVAR}$

Capacitor injected capacitance = 65.66 - 24.49
= 41.19 KVAR

Per capacitor phase injected

capacitance = $\frac{41.19}{3} = 13.74$ KVAR

→ $I_{CP} = \frac{V_L}{X_C}$

$= \frac{V_L}{\frac{1}{2\pi f C}}$

$= V_L \times 2\pi f C$

$= 415 \times 2 \times 3.14 \times 50 \times$

$= \frac{130.34}{1000} \times 10^3 \text{ C A}$

→ KVAR = $\frac{V_L \times I_{CP}}{1000}$

$13.73 = \frac{415 \times 130.34 \times 10^3 \times C}{10^3}$

$C = \frac{105.39 \times 10^3}{415 \times 130.34} \text{ F}$

$C = 253 \mu\text{F}$

WH 2.4P =

each capacitor's capacitance = 253 x 4 μF
= 1012 μF

3- ϕ Induction motor 5 kW, P.F. 0.75 lags
 Bank of capacitors is connected in
 delta across the supply terminals.
 P.F. is raised to 0.9 lags determine
 kVAR rating of capacitor bank
 connected to each phase.

For star

$$V_L = \sqrt{3} V_{ph}$$

$$I_L = I_{ph}$$

For Delta

$$V_L = V_{ph}$$

$$I_L = \sqrt{3} I_{ph}$$

$$P = 5 \text{ kW}$$

$$P_{f1} = 0.75 (\text{lag})$$

$$P_{f2} = 0.9 (\text{lag})$$

Determine kVAR of capacitor bank connected to each phase.

$$\phi_1 = \cos^{-1}(0.75) = 41.41^\circ$$

$$\phi_2 = \cos^{-1}(0.9) = 25.84^\circ$$

VAR rating of capacitor bank = $P (\tan \phi_1 - \tan \phi_2)$

$$Q_{csh} = 5 (\tan 41.41^\circ - \tan 25.84^\circ)$$

$$Q_{csh} = 1.99 \text{ kVAR}$$

Rating in each phase = $\frac{Q_{csh}}{3}$

$$= 0.663 \text{ kVAR}$$

$$\phi_1 = P \tan \phi_1 = 74.5 \tan(46.01) = 65.70 \text{ kVAR}$$

$$\phi_2 = P \tan \phi_2 = 74.5 \tan(20.21) = 24.47 \text{ kVAR}$$

Q-6

1- ϕ AC

- i) lighting load 20 kW unit pf
- ii) Induction motor ~~100 kW~~ 150 kW ~~0.75~~ 0.75 (lag)
- iii) Synch. motor 50 kW 0.9 (lead)

Calc. kW & kVAR - Also represent phase diagram

$$kVA_1 = \frac{kW_1}{\cos \phi_1} = 20 \text{ kVA}$$

$$kVA_2 = \frac{kW_2}{\cos \phi_2} = \frac{150}{0.75} = 200 \text{ kVA}$$

$$kVA_3 = \frac{50}{0.9} = 55.55 \text{ kVA}$$

$$\phi_1 = P \tan \phi_1 = 0$$

$$\phi_2 = 150 \times \tan(\cos^{-1} 0.75) = 132.24 \text{ kVAR}$$

$$\phi_3 = 50 \times \tan^*(\cos^{-1} 0.9) = 24.22 \text{ kVAR}$$

$$P = \text{Tot kW} = 20 + 150 + 50 = 220 \text{ kW}$$

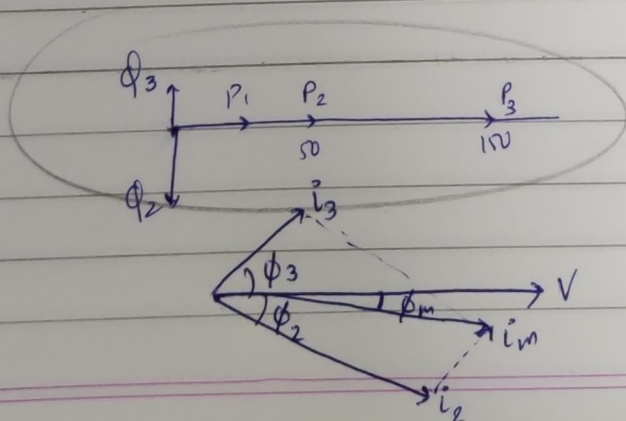
$$\phi = \text{Tot } \phi = 0 - 132.24 + 24.22 = -108.02 \text{ kVAR}$$

$$S = \text{Tot kVA} = \sqrt{(kW)^2 + (kVAR)^2} = \sqrt{(220)^2 + (-108.02)^2}$$

$$S = 245.08 \text{ kVA}$$

$$\text{Net p.f} = P/S = \frac{220}{245.08} = 0.897 \approx 0.9 \text{ (lag)}$$

But resultant
kVAR is lagging



As generator is
same, voltage will be
same

① Estimate efficiency = 91% high frequency furnace to melt 10 min \rightarrow 1.5 kg Al. Input to the furnace 5 kW. Initial Temp 15 $^{\circ}$ C

Specific Heat = 550 J/kg $^{\circ}$ C
 Latent Heat = 32 kJ/kg
 Melting Temp: 660 $^{\circ}$ C

$$\rightarrow IJ = 24 \times 10^{-7} \text{ kWh}$$

$$E = m [c (t_2 - t_1) + L]$$

$$= 1.5 \times 10^3 [550 (660 - 15) + 32000]$$

$$= 1.5 [550 (645) + 32000] \times 10^3$$

$$= 0.195 \text{ kWh}$$

$$\text{Eff} = \frac{\text{Energy required}}{\text{Wt/P}}$$

$$= \frac{0.195 \times 6}{5}$$

$$23.4 \%$$

② Induction Furnace. Operating at 10 V Secondary 500W, 0.5 PF, when hearth is full. If Secondary Voltage maintain constant, Estimate power absorb & PF, when the hearth is half full.

JW

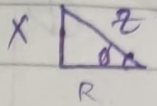
500 A per 2

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Heavith is full

$$I = \frac{P}{V \cos \phi} = \frac{500 \times 10^3}{10 \times 10^5} = 10^5$$

$$Z = \frac{V}{I} = \frac{10}{10^5} = 10^{-4}$$



$$R = Z \cos \phi = 10^{-4} \times 0.5 = 5 \times 10^{-5}$$

$$X = Z \sin \phi = 10^{-4} \times \frac{\sqrt{3}}{2} = 8.6 \times 10^{-5}$$

Heavith is here

$$R' = 2R = 10^{-4}$$

$$X' = X \quad Z' = \sqrt{R'^2 + X'^2}$$

$$\sqrt{10^{-4} + 0.86 \times 10^{-4}} = 1.2 \times 10^{-4}$$

$$PF = \frac{R'}{Z'} = \frac{10^{-4}}{1.2 \times 10^{-4}} \quad I' = \frac{V}{Z'}$$

$$P = I'^2 R'$$

26/09/22

Load of 500 kW at P.F. 0.7 lagging, if P.F. is raised to unity how many kW can ultimate supply from same KVA loading

$$\cos \phi = P/S$$

$$0.7 = \frac{500}{S}$$

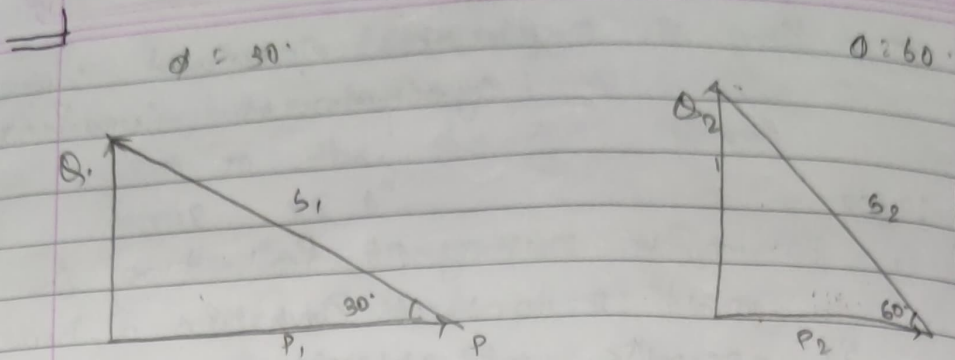
$$S = \frac{P}{0.7} = 714.29 \text{ KVA}$$

$$P_2 = S \times \cos \phi$$

$$= 714.29 \times 1$$

$$= 714.29 \text{ kW}$$

more kW provided = 214.29 kW.



$$\cos \theta = \frac{P}{S_1}$$

$$\cos \theta_2 = \frac{P_2}{S_2}$$

$$S_1 = \frac{5 \text{ kW}}{0.866}$$

$$S_2 = \frac{5 \text{ kW}}{0.5}$$

$$S_1 + S_2 = 5.81 \text{ KVA} \quad \text{---} \quad 10 \text{ KVA}$$

→ Advantages of good P.F.

→ Reactive power ↓

→ Reduce bill

→ I^2R losses ↓

→ Striking of grid

→ Overall cost ↓

→ temp rise ↓

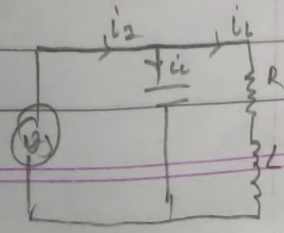
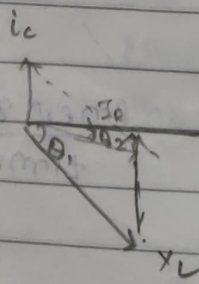
→ Life cycle equipment ↑

→ False trigger ↓

→ Disadvantages of bad P.F.

How to improve P.F.?

→ By adding Capacitor bank



Q How to measure required capacity
of synchronous capacitor.

19/09

Ex. Estimate rating of induction furnace
to melt 2 tons of Zinc in 2 hours if
it operates at efficiency of 80%.

Specific heat of Zn = 0.1 kcal/kg

Latent heat of fusion of Zn = 26.67 kcal/kg

Melting point of Zn = 555°C

Starting temp. = 35°C

Power rating = 9 kWh

$$\text{Heat Energy} = m [c(t_2 - t_1) + L]$$

$$= 2 \times 10^3 [0.1 (555 - 35) + 26.67] \times 10^3$$

↓
kcal
to
cal

$$= 2 \times 10^3 (52 + 26.67) \times 10^3$$

$$= 2 \times 78.67 \times 10^6 \text{ cal}$$

$$= 157.34 \times 10^6 \text{ cal}$$

$$= 157340 \text{ kcal} = \frac{157340}{860}$$

$$\text{Energy IP} = \frac{\text{Energy required}}{\text{Efficiency}}$$

= kWh

$$= \frac{157.34 \times 10^6 \text{ cal}}{0.80 \times 860}$$

$$= 228.69 \text{ kWh}$$

Rating of

furnace =

$$\frac{\text{Energy IP}}{\text{time}} = \frac{228.69}{2 \text{ h}}$$

$$= 228.69 \text{ kW}$$

c = specific heat
 L = Latent heat

Q

Calc. kVA & kW run from supply
3 ϕ elec. arc furnace

$$I = 4500 \text{ A}$$

$$V_{arc} = 50 \text{ V}$$

$$R = 0.002 \Omega$$

$$X_{02} = 0.004$$

$$\text{efficiency} = \eta = 60\%$$

Calc. time req. to melt 3 tons of steel
when $c_{\text{steel}} = 0.12$, $L_{\text{steel}} = 8.89 \text{ kcal/kg}$,
 $\theta_{\text{melt steel}} = 1370^\circ\text{C}$, $\theta_{\text{initial}} = 20^\circ\text{C}$

ci Volt drop due to resistance

$$V_r = I \times R_s = 4500 \times 0.002 = \underline{9 \text{ V}}$$

due to
reactance

$$V_x = I \times X_s = 4500 \times 0.004 = \underline{18 \text{ V}}$$

$$\begin{aligned} \text{Tot volt} = V_t &= \sqrt{V_r^2 + V_x^2} = \sqrt{9^2 + 18^2} \\ &= \sqrt{(V_{arc} + V_r)^2 + V_x^2} \\ &= \sqrt{(50 + 9)^2 + 18^2} = \underline{62 \text{ V}} \end{aligned}$$

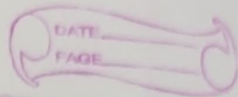
$$\text{Supply p.f} \rightarrow \text{pf} = \frac{(V + V_r)}{V_t} = \frac{59}{62} = \underline{0.95}$$

Tot pow drawn

$$\begin{aligned} P &= 3 \times V_t \times I \times \text{pf} \\ &= 3 \times 62 \times 4500 \times 0.95 \text{ W} \end{aligned}$$

$$\boxed{P = 795.15 \text{ kW}}$$

$$\frac{\text{kcal}}{860} = \text{kWh}$$



$$m = 3000 \text{ kg} = 3 \text{ tonnes}$$

$$c_{\text{steel}} = 0.12$$

$$L_{\text{steel}} = 8.89 \text{ kcal/kg}$$

$$\text{Energy} = m \cdot c_{\text{steel}} (t_2 - t_1) + mL$$

$$= 3000 \times 0.12 (1350) + 3000 \times 8.89$$

$$= 512.66 \times 10^3 \text{ kcal}$$

$$= \boxed{596 \text{ kWh}}$$

$$\begin{aligned} \text{Actual power utilised} &= P_a = 0.60 \times P \\ &= \underline{\underline{477 \text{ kW}}} \end{aligned}$$

Time req. for melting

$$T = \frac{\text{Energy}}{\text{Power}} = \frac{596}{477}$$

$$= \underline{\underline{1.25 \text{ h}}}$$

$$= \boxed{\underline{\underline{75 \text{ mins}}}}$$