Chapter 4: Digital Image Processing Image Enhancement in the Frequency Domain

Basic steps for filtering in the frequency domain Frequency domain filtering operation Filter Inverse Fourier Fourier function transform H(u, v)transform H(u,v)F(u,v)F(u, v)Pre-Postprocessing processing f(x, y)g(x, y)Input Enhanced image image **FIGURE 4.5** Basic steps for filtering in the frequency domain. 2



Basics of filtering in the frequency domain

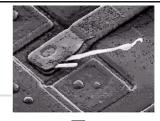
- 1. multiply the input image by $(-1)^{x+y}$ to center the transform to u = M/2 and v = N/2 (if M and N are even numbers, then the shifted coordinates will be integers)
- 2. computer F(u,v), the DFT of the image from (1)
- 3. multiply F(u,v) by a filter function H(u,v)
- 4. compute the inverse DFT of the result in (3)
- 5. obtain the real part of the result in (4)
- 6. multiply the result in (5) by $(-1)^{x+y}$ to cancel the multiplication of the input image.

3



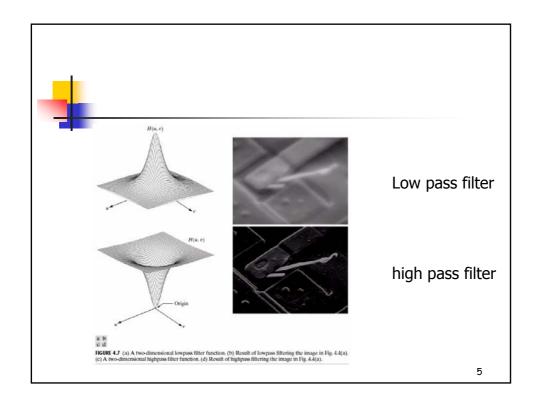
Notch filter

- this filter is to force the F(0,0) which is the average value of an image (dc component of the spectrum)
- the output has prominent edges
- in reality the average of the displayed image can't be zero as it needs to have negative gray levels. the output image needs to scale the gray level





$$H(u,v) = \begin{cases} 0 & \text{if } (u,v) = (M/2, N/2) \\ 1 & \text{otherwise} \end{cases}$$

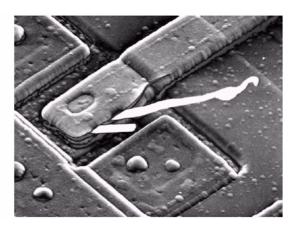


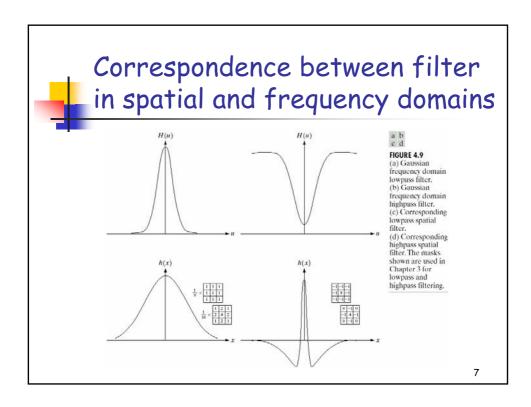


Add the $\frac{1}{2}$ of filter height to F(0,0) of the high pass filter

FIGURE 4.8

Result of highpass filtering the image in Fig. 4.4(a) with the filter in Fig. 4.7(c), modified by adding a constant of one-half the filter height to the filter function. Compare with Fig. 4.4(a).





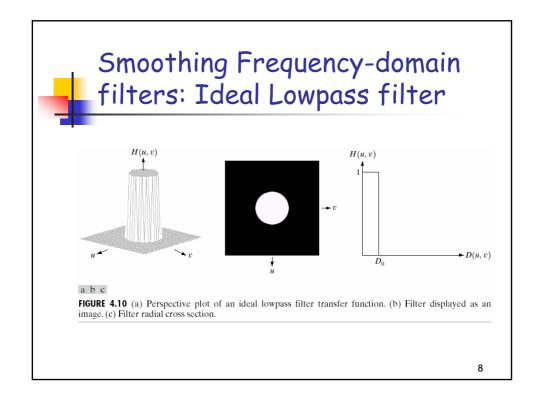
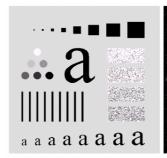
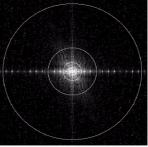




image power circles





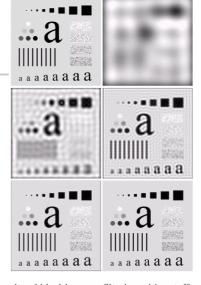
a b

FIGURE 4.11 (a) An image of size 500×500 pixels and (b) its Fourier spectrum. The superimposed circles have radii values of 5, 15, 30, 80, and 230, which enclose 92.0, 94.6, 96.4, 98.0, and 99.5% of the image power, respectively.

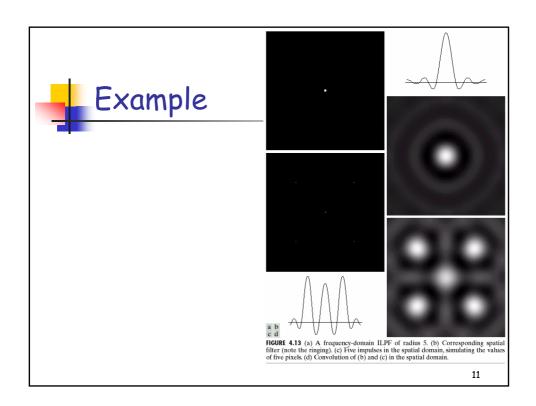
9

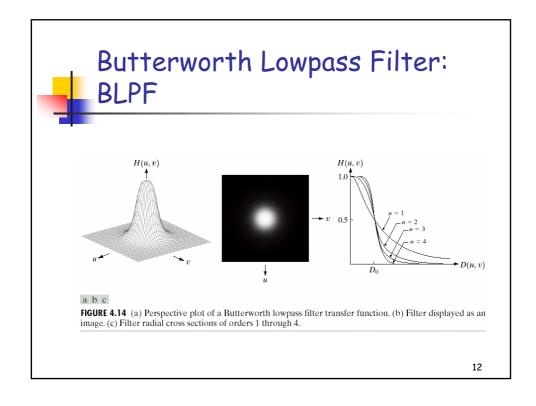


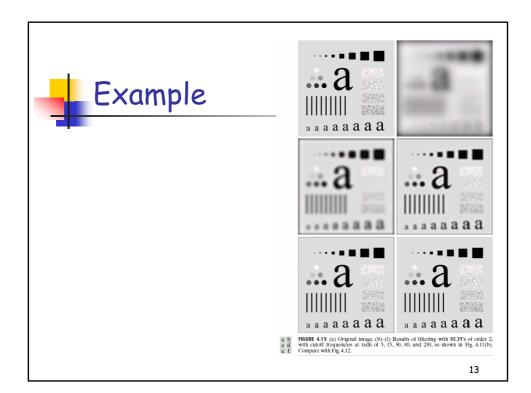
Result of ILPF

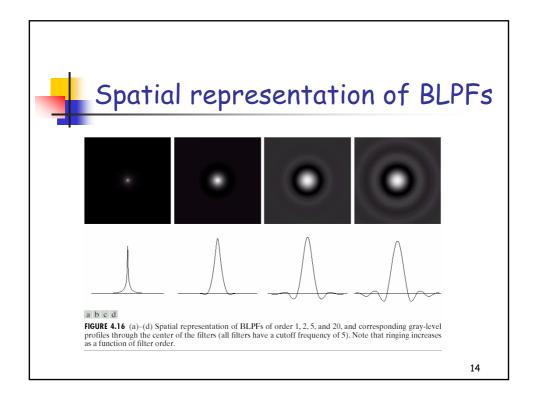


a b c d e f **FIGURE 4.12** (a) Original image. (b)–(f) Results of ideal lowpass filtering with cutoff frequencies set at radii values of 5, 15, 30, 80, and 230, as shown in Fig. 4.11(b). The power removed by these filters was 8, 5.4, 3.6, 2, and 0.5% of the total, respectively.











Gaussian Lowpass Filter: GLPF

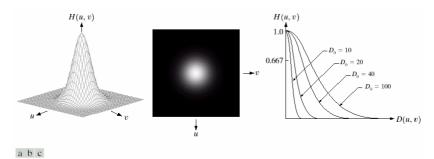
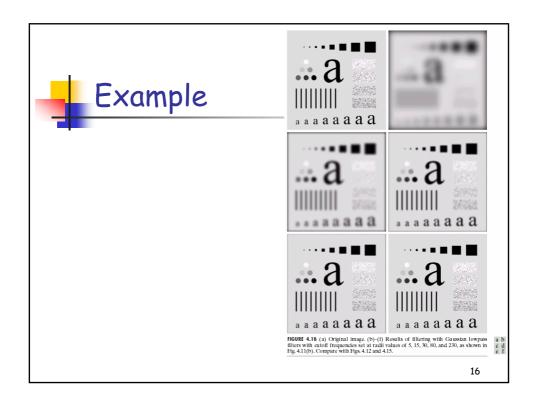


FIGURE 4.17 (a) Perspective plot of a GLPF transfer function. (b) Filter displayed as an image. (c) Filter radial cross sections for various values of D_0 .





Example

a b

FIGURE 4.19

(a) Sample text of poor resolution (note broken characters in magnified view).
(b) Result of filtering with a GLPF (broken character segments were joined).

Historically, certain computer programs were written using only two digits rather than four to define the applicable year. Accordingly, the company's software may recognize a date using "00" as 1900 rather than the year 2000.

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Example



abc

FIGURE 4.20 (a) Original image (1028×732 pixels), (b) Result of filtering with a GLPF with $D_0 = 100$. (c) Result of filtering with a GLPF with $D_0 = 80$. Note reduction in skin fine lines in the magnified sections of (b) and (c).



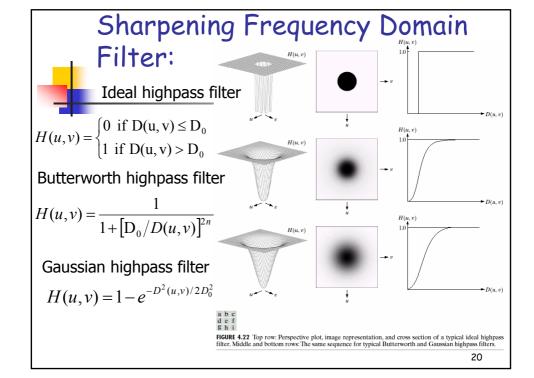




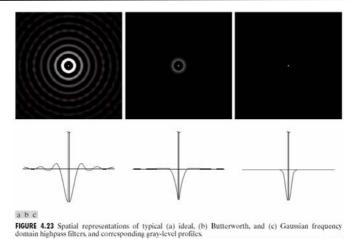


a b c

FIGURE 4.21 (a) Image showing prominent scan lines. (b) Result of using a GLPF with $D_0 = 30$. (c) Result of using a GLPF with $D_0 = 10$. (Original image courtesy of NOAA.)



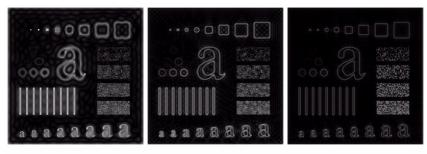
Spatial representation of Ideal, Butterworth and Gaussian highpass filters



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Example: result of IHPF

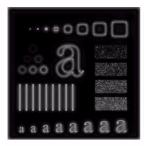


a b c

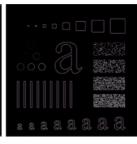
FIGURE 4.24 Results of ideal highpass filtering the image in Fig. 4.11(a) with $D_0 = 15$, 30, and 80, respectively. Problems with ringing are quite evident in (a) and (b).



Example: result of BHPF







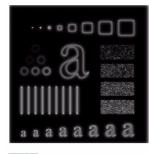
a b c

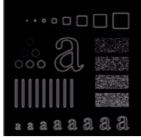
FIGURE 4.25 Results of highpass filtering the image in Fig. 4.11(a) using a BHPF of order 2 with $D_0 = 15$, 30, and 80, respectively. These results are much smoother than those obtained with an ILPF.

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Example: result of GHPF

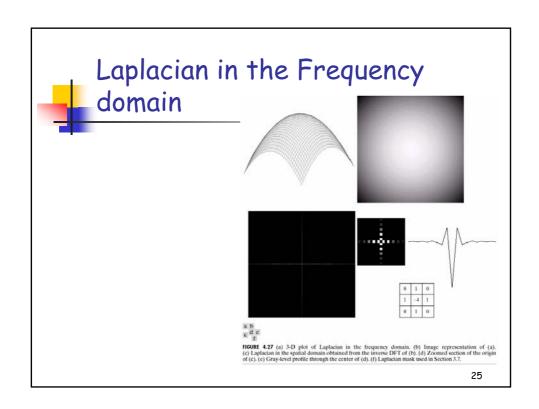


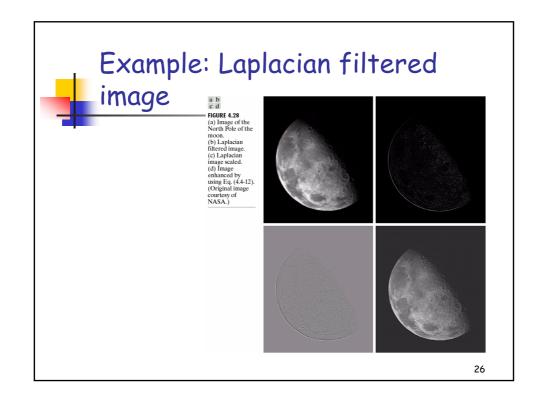




a b c

FIGURE 4.26 Results of highpass filtering the image of Fig. 4.11(a) using a GHPF of order 2 with $D_0 = 15$, 30, and 80, respectively. Compare with Figs. 4.24 and 4.25.

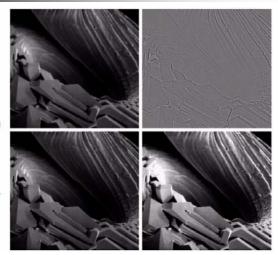






Example: high-boost filter

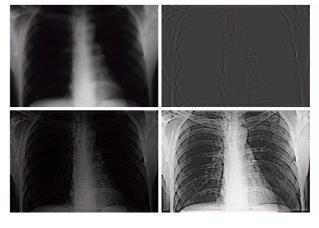
a b c d
c d
Same as Fig. 3.43, but using
frequency domain
filtering. (a) Input
image.
(b) Laplacian of
(a). (c) Image
obtained using
Eq. (4.4-17) with
A = 2. (d) Same
as (c), but with
A = 2.7. (Original
image courtesy of
Mr. Michael
Shaffer,
Department of
Geological
Sciences,
University of
Oregon, Eugene.)



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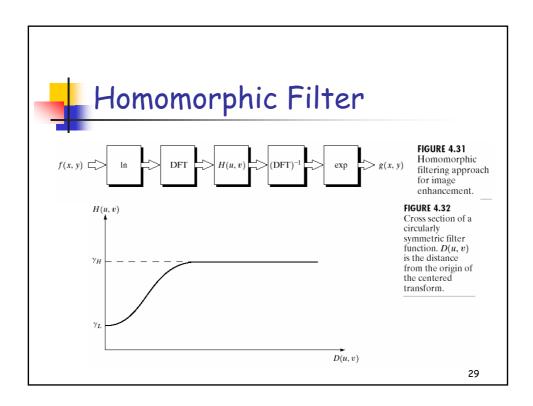
Examples



a b c d

FIGURE 4.30

(a) A chest X-ray image. (b) Result of Butterworth highpass filtering. (c) Result of highfrequency emphasis filtering. (d) Result of performing histogram equalization on (c). (Original image courtesy Dr. Thomas R. Gest, Division of Anatomical Sciences, University of Michigan Medical School.)





Result of Homomorphic filter

a b

FIGURE 4.33

(a) Original image. (b) Image processed by homomorphic filtering (note details inside shelter).

(Stockham.)



