

## Regularization - I

(Interview imp)

→ Bias Variance tradeoff -

$$\rightarrow \underset{x}{\text{cgo}} | \underset{y}{\{\mathbf{g}_1, \mathbf{g}_2\}}$$

we want a fn st:  $y = f(x)$

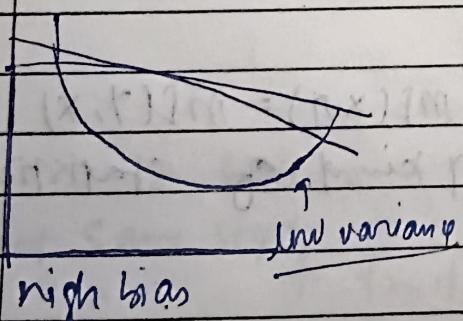
$$\& \quad y = f(x) + \underbrace{\text{error}}_{\text{irreducible}}$$

we want  $f(x)$  for popul<sup>n</sup> but we only have sample so we get  $f'(x)$   
 $\hat{y} = f'(x)$

$$y - \hat{y} = f(x) - f'(x) \cdot [\text{reducible error}]$$

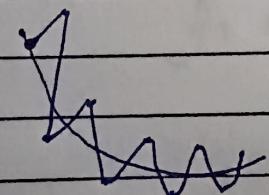
• Bias → inability of ML model to fit in training data

high bias → very less fit (low variance)  
 low bias



Variance - how much m2 "predict" changes when training data is changed

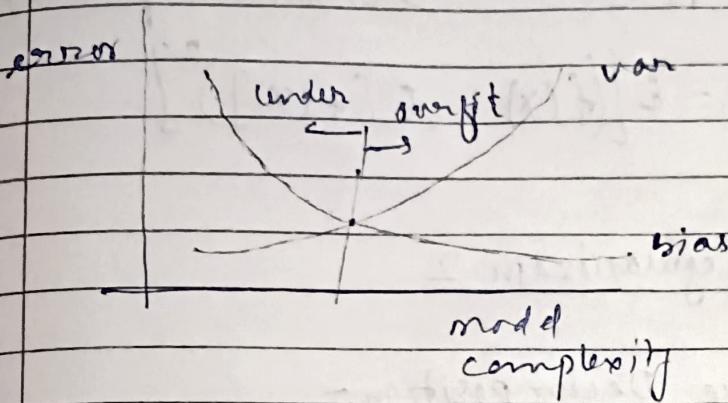
→ low bias but high variance



- High bias then underfitting
- Low bias then overfitting

We want low bias & low variance

But if we minimize bias then var. increases



- Expected values -

↳ avg outcome of a R.V over a large no. of trials or experiments

$$\text{Discrete RV} \Rightarrow E(x) = x_1 p(x_1) + x_2 p(x_2) + \dots + x_n p(x_n)$$

$\Rightarrow$  Expected value  $\xrightarrow{\text{means}}$  Population mean  
 $\text{Var}[x] \rightarrow$  Var of population

$$\text{Var}[x] = E[x^2] - (E[x])^2$$

$$E[(x - E[x])^2]$$

### Bias -

↳ a systematic error that a model introduces because it cannot capture true reltn in data  
 ↳ It is diff b/w "Expected predict" of our model & correct value which we are trying to predict.

→ true  $f'$   $f(x)$  we know  $f'(x)$   
So

$$\text{bias} = E[f'(x)] - f(x)$$

$$\text{if } E[f'(x)] = f(x)$$

$\Rightarrow \text{bias} = 0 \Rightarrow \text{Unbiased predictor}$

$$\cdot \text{var}(f'(x)) = E[(f'(x) - E[f'(x)])^2]$$