

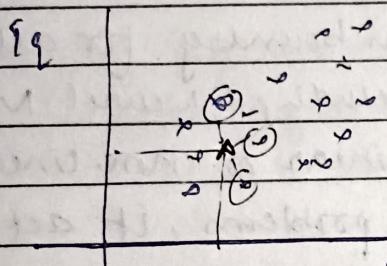
Advance KNN :-

→ KNN can be applied in both classification and regression.

KNN Regressor :-

Suppose $cgpa | iq | package$

↳ given & we have to find package



i) find dist. of query pt
to all the pts.

ii) Sort them

iii) Let $K = 3$

$cgpa$ ↳ take closest 3 pts.

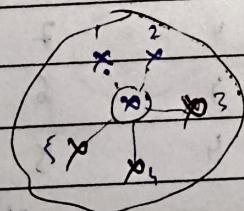
→ take more package
and find avg.

↳ In this if -

→ K value is large then underfitting

→ K is "small" overfitting

→ weighted KNN :-



in uniform KNN we say
it as black as # black
is more
But

In weighted KNN we calculate
weight :-

$$\text{weight} = \frac{1}{\text{dist}}$$

Dist wt

| | | |
|-----------|-----|------|
| 1 - blue | 0.2 | 5 |
| 2 - blue | 0.5 | 2 |
| 3 - Black | 1 | 1 |
| 4 - * | 2 | 0.5 |
| 5 - * | 3 | 0.33 |

$$wt \text{ of Blue} = 5+2=7$$

$$wt \text{ of Black} = 1.83 \quad \text{So it should be Blue}$$

• Types of distances -

1) Euclidean dist -

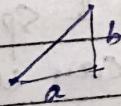
$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\text{general (n-dim)} = \sqrt{\sum_{i=1}^n (x_{2i} - x_{1i})^2}$$

↳ also called L2 norm

2) Manhattan distance (taxi cab dist)

manhattan dist = a+b



$$m = \sum_{i=1}^d |x_{2i} - x_{1i}|$$

• Problem with euclidean dist

- (i) axis should be of same scale
- (ii) Curse of dimensionality

- For hyperparameter of KNN we have a parameter metric.

default value of metric is mineuksi] where now $p=2$
(default)

- $p=2 \rightarrow$ euclidean dist (L2 norm)
 $p=1 \rightarrow$ manhattan " (L1 norm)

$$\text{mineuksi} = \left(\sum_{i=1}^d (|x_{2i} - x_{1i}|)^p \right)^{1/p}$$

$$p=2, 5 \rightarrow L2, 5 \text{ norm etc}$$

- Time complexity →

$O(nd)$ $n \rightarrow$ #rows in training data
 $d \rightarrow$ " features" "

- Space complexity -

$O(nd)$

→ So KNN takes very time & space so there are diff algo we can use to reduce it -

- i) brute :- we have used this till now
- ii) ball-tree
- iii) kd-tree

$$\hookrightarrow \text{time complexity} = O(d \log n)$$

→ Normally we store data in array but in kd-tree we store data in k-dimensional BST.