

## ⇒ Regression Analysis - I

- ↳ It is statistical method used to examine the relationship b/w one dependent var. and one or more ind. variable.
- ↳ Its goal is to understand how dep. variable changes when one or more dep. variable altered

### flow LF:-

- Define the research quest.
- Collect & prepare data
- Visualize the data
- Check assumptions
- fit linear regression model
- Interpret the model (Regression Analysis)
- Validate the model
- Report results
- Statistical inference
  - ↳ by using Sample we try to conclude about population

|      |    |            |
|------|----|------------|
| Cgpa | 99 | target 111 |
| -    | -  | -          |
| -    | -  | -          |
| -    | -  | -          |

$$f(\text{Lps}) \rightarrow \text{Lps} = f(\text{Cgpa}, \text{L2}) + \varepsilon$$

calculate it

irreducible error

parametric

non-parametric

we assume it is  
following linear or  
curve regression

we don't assume  
anything together  
start from scratch

$$\hookrightarrow \text{Lps} = \beta_0 + \beta_1 \text{Cgpa} + \beta_2 \text{L2}$$

while calculating we  
get values  $b_0, b_1, b_2 \neq \beta_0, \beta_1, \beta_2$

Q

$$f'(\text{Cgpa}, \text{L2})$$

So error  $\hat{=} f() - f'(())$

↳ fixed

reducible error

$f()$  → True relation of  $x$  &  $y$  for population

$f'()$  → estimated  $\cdot \sim \sim \sim \cdot$  given sample

i) Prediction → Suppose we have Cgpa & L2 &  
Now we want to predict other  
people's Lps

$\text{LPA} = \beta_0 + \beta_1 (\text{CGPA} + \text{F1})$   
 → any person come we put its CGPA & F1  
 and get LPA

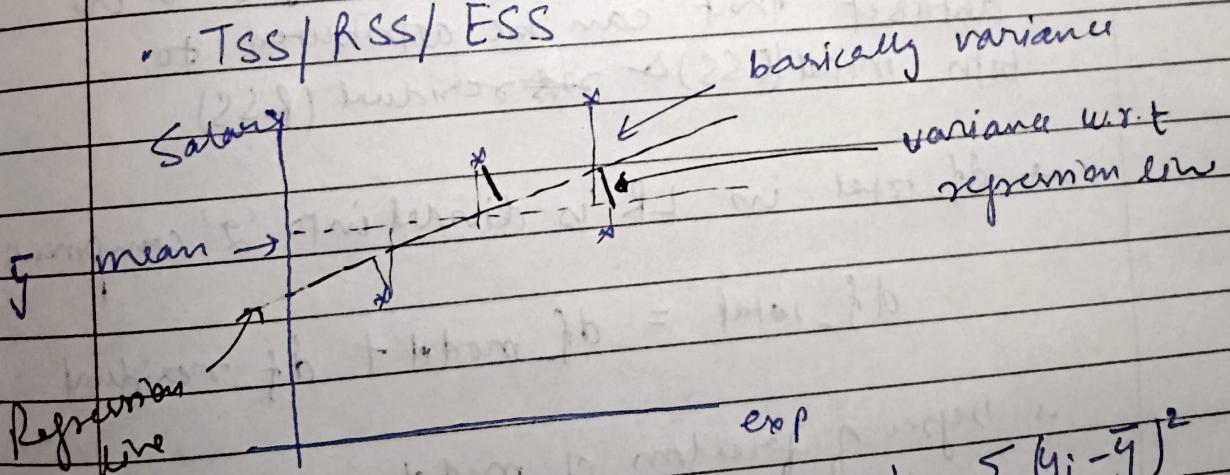
→ Inference → In this we do relationship study, like select b/w LPA & CGPA :  
 how it changes etc

→ Linear regression is good in inference  
 if inference good then prediction weak  
 & vice versa

• F-statistics & Prob(F-statistics) ⇒ They tell whether there is any select b/w X (input columns) & Y (output column)

for this we have to do hypothesis test called F-test for overall significance

• TSS / RSS / ESS



TSS (Total sum of squares) =  $\sum (y_i - \bar{y})^2$   
 It tells overall variance in the data

RSS (Residual Sum of Squares)

$$= \sum (y_i - \hat{y}_i)^2$$

- It tells variance present in data w.r.t regression line (means even after knowing the exp. we can't tell why variant occur)

ESS (Explained Sum of Squares)

$$= TSS - RSS$$

$$TSS = ESS + RSS$$

Degree of freedom -

$$\hookrightarrow \# \text{rows} - 1 = n - 1$$

$$df_{\text{total}} = n - 1$$

It represent overall variability (TSS) in dataset that can be attributed to both model (ESS) & ~~residual~~ residual (RSS).

$\rightarrow$  df\_total in LR is divided into '2' component -

$$df_{\text{total}} = df_{\text{model}} + df_{\text{residual}}$$

$\rightarrow$  Degree of freedom of model -

$\hookrightarrow$  equal to no. of independent variables ( $k$ )

$$x_1 \quad x_2 \quad | \quad y \quad \quad \quad \quad x_2$$

$\rightarrow$  Degree of freedom of residual -

$\hookrightarrow n - \text{no. of estimated parameters}$   
including intercept

$$= n - (k + 1)$$

$\Rightarrow$  F-test for overall significance is a statistical test used to find whether there is relation by columns.

exp | Salary ↗ whether salary is affected by experience or not