

### Activity-3

**Problem-1** use truth table

- a) Show that  $(p \wedge \neg q) \wedge (\neg p \vee q)$  is a contradiction
- b) Show that  $(p \rightarrow q) \leftrightarrow (\neg q \rightarrow \neg p)$  is tautology

**Problem-2** Use De Morgan's laws to find the negation of each of the following statements.

- I. Jan is rich and happy.
- II. Carlos will bicycle or run tomorrow.
- III. The fan is slow or it is very hot.

**Problem-3** Prove the following equivalences by using laws of logic:

$$(p \wedge (\neg (\neg p \vee q))) \vee (p \wedge q) \equiv p$$

**Problem-4** write inverse, converse and contrapositive of the following

If my car is in repair shop, then I can't get to class

**Problem-5** Use symbols to write logical form of argument and use truth table to test the argument for validity

If Maxwell is not on team A , then David is on team B

IF David is not on team B , then Maxwell is on team A

Therefore Maxwell is not on team A or David is not on team B

**Problem-6** show that the following argument is valid

$$p \vee (q \vee r)$$

$$\neg r$$

$$\therefore p \vee q$$

**Problem-7** state which rule of inference is used in the argument

- i) If it rains today, then we will not have a barbecue today. If we do not have a barbecue today, then we will have a barbecue tomorrow.  
Therefore, if it rains today, then we will have a barbecue tomorrow.
- ii) "It is below freezing and raining now. Therefore, it is below freezing now."