מבוא להצפנה – תרגיל 3

.1

א.

```
a = 2
b0 = 2^11799 = 1014 mod 47197
b1 = 1014^2 = 37059 \mod 47197
47197 is not a pseudoprime or a Strong pseudoprime to base 2
a = 3
b0 = 3^11799 = 1 \mod 47197
47197 is a Strong pseudoprime to base 3
a = 4
b0 = 4^11799 = 37059 mod 47197
b1 = 37059<sup>2</sup> = 31175 mod 47197
47197 is not a pseudoprime or a Strong pseudoprime to base 4
a = 5
b0 = 5^11799 = 40004 \mod 47197
b1 = 40004^2 = 11337 \mod 47197
47197 is not a pseudoprime or a Strong pseudoprime to base 5
a = 6
b0 = 6^11799 = 1014 mod 47197
b1 = 1014^2 = 37059 \mod 47197
47197 is not a pseudoprime or a Strong pseudoprime to base 6
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```
a = 7
b0 = 7^11799 = 34445 \mod 47197
b1 = 34445<sup>2</sup> = 19839 mod 47197
47197 is not a pseudoprime or a Strong pseudoprime to base 7
a = 8
b0 = 8^11799 = 9014 mod 47197
b1 = 9014^2 = 26159 \mod 47197
47197 is not a pseudoprime or a Strong pseudoprime to base 8
a = 9
b0 = 9^11799 = 1 \mod 47197
47197 is a Strong pseudoprime to base 9
a = 10
b0 = 10^11799 = 21833 mod 47197
b1 = 21833^2 = 37386 mod 47197
47197 is not a pseudoprime or a Strong pseudoprime to base 10
```

ב.

```
a = 2
n = 47197, k = 2, r = 11799
b0 = 2^11799 = 1014 mod 47197
b1 = 1014^2 = 37059 \mod 47197
47197 is composite
gcd(47197, 37059) = 1
a = 3
n = 47197, k = 2, r = 11799
b0 = 3^11799 = 1 \mod 47197
47197 is probably prime
a = 4
n = 47197, k = 2, r = 11799
b0 = 4^11799 = 37059 mod 47197
b1 = 37059<sup>2</sup> = 31175 mod 47197
47197 is composite
gcd(47197, 31175) = 109
and we found that the composite is 47197 = 109 * 433
```

.2

```
-----
x = 218
x^2 - 47197 = 327
sqrt(x^2 - 47197) = 18.083141320025124
x = 219
x^2 - 47197 = 764
sqrt(x^2 - 47197) = 27.640549922170507
x = 220
x^2 - 47197 = 1203
sqrt(x^2 - 47197) = 34.68429039204925
x = 221
x^2 - 47197 = 1644
sqrt(x^2 - 47197) = 40.54626986542659
x = 222
x^2 - 47197 = 2087
sqrt(x^2 - 47197) = 45.68369512200168
x = 223
x^2 - 47197 = 2532
sqrt(x^2 - 47197) = 50.3189825016365
x = 224
x^2 - 47197 = 2979
sqrt(x^2 - 47197) = 54.58021619598075
x = 225
x^2 - 47197 = 3428
sqrt(x^2 - 47197) = 58.54912467321779
x = 226
x^2 - 47197 = 3879
sqrt(x^2 - 47197) = 62.281618476080084
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```
x = 227
x^2 - 47197 = 4332
sqrt(x^2 - 47197) = 65.81793068761733
x = 228
x^2 - 47197 = 4787
sqrt(x^2 - 47197) = 69.18814927427962
x = 229
x^2 - 47197 = 5244
sqrt(x^2 - 47197) = 72.41546796092669
x = 230
x^2 - 47197 = 5703
sqrt(x^2 - 47197) = 75.5182097245426
x = 231
x^2 - 47197 = 6164
sqrt(x^2 - 47197) = 78.51114570556209
x = 232
x^2 - 47197 = 6627
sqrt(x^2 - 47197) = 81.40638795573723
x = 233
x^2 - 47197 = 7092
sqrt(x^2 - 47197) = 84.2140130857092
x = 234
x^2 - 47197 = 7559
sqrt(x^2 - 47197) = 86.94250974063263
x = 235
x^2 - 47197 = 8028
sqrt(x^2 - 47197) = 89.59910713840847
```

```
x = 236
x^2 - 47197 = 8499
sqrt(x^2 - 47197) = 92.19002115196633
x = 237
x^2 - 47197 = 8972
sqrt(x^2 - 47197) = 94.72064188971694
x = 238
x^2 - 47197 = 9447
sqrt(x^2 - 47197) = 97.19567891629751
x = 239
x^2 - 47197 = 9924
sqrt(x^2 - 47197) = 99.61927524329818
x = 240
x^2 - 47197 = 10403
sqrt(x^2 - 47197) = 101.99509792141973
x = 241
x^2 - 47197 = 10884
sqrt(x^2 - 47197) = 104.32641084595981
x = 242
x^2 - 47197 = 11367
sqrt(x^2 - 47197) = 106.61613386350116
 x = 243
x^2 - 47197 = 11852
sqrt(x^2 - 47197) = 108.86689120205463
x = 244
x^2 - 47197 = 12339
sqrt(x^2 - 47197) = 111.0810514894417
```

```
x = 245
x^2 - 47197 = 12828
sqrt(x^2 - 47197) = 113.26076107814215
x = 246
x^2 - 47197 = 13319
sqrt(x^2 - 47197) = 115.40797199500561
x = 247
x^2 - 47197 = 13812
sqrt(x^2 - 47197) = 117.52446553803169
x = 248
x^2 - 47197 = 14307
sqrt(x^2 - 47197) = 119.61187232043481
x = 249
x^2 - 47197 = 14804
sqrt(x^2 - 47197) = 121.67168939404104
x = 250
x^2 - 47197 = 15303
sqrt(x^2 - 47197) = 123.70529495538985
x = 251
x^2 - 47197 = 15804
sqrt(x^2 - 47197) = 125.71396103854178
 -----
x = 252
x^2 - 47197 = 16307
sqrt(x^2 - 47197) = 127.69886452118516
x = 253
x^2 - 47197 = 16812
sqrt(x^2 - 47197) = 129.66109670984585
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```
x = 254
x^2 - 47197 = 17319
sqrt(x^2 - 47197) = 131.6016717219048
x = 255
x^2 - 47197 = 17828
sqrt(x^2 - 47197) = 133.52153384379613
x = 256
x^2 - 47197 = 18339
sqrt(x^2 - 47197) = 135.42156401400774
x = 257
x^2 - 47197 = 18852
sqrt(x^2 - 47197) = 137.30258555467918
x = 258
x^2 - 47197 = 19367
sqrt(x^2 - 47197) = 139.16536925542934
_____
x = 259
x^2 - 47197 = 19884
sqrt(x^2 - 47197) = 141.01063789657857
x = 260
x^2 - 47197 = 20403
sqrt(x^2 - 47197) = 142.83907028540895
x = 261
x^2 - 47197 = 20924
sqrt(x^2 - 47197) = 144.65130486794789
x = 262
x^2 - 47197 = 21447
sqrt(x^2 - 47197) = 146.4479429695071
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```
x = 263
x^2 - 47197 = 21972
sqrt(x^2 - 47197) = 148.22955170950223
x = 264
x^2 - 47197 = 22499
sqrt(x^2 - 47197) = 149.9966666296288
x = 265
x^2 - 47197 = 23028
sqrt(x^2 - 47197) = 151.74979406905302
x = 266
x^2 - 47197 = 23559
sqrt(x^2 - 47197) = 153.48941331570722
x = 267
x^2 - 47197 = 24092
sqrt(x^2 - 47197) = 155.21597855890997
x = 268
x^2 - 47197 = 24627
sqrt(x^2 - 47197) = 156.9299206652447
x = 269
x^2 - 47197 = 25164
sqrt(x^2 - 47197) = 158.63164879682742
 -----
x = 270
x^2 - 47197 = 25703
sqrt(x^2 - 47197) = 160.3215518886965
x = 271
x^2 - 47197 = 26244
sqrt(x^2 - 47197) = 162.0
```

The factors are: x-y and x+y, where x and y are the values from the table above, and n is the number to be factored.

x = 271, y = 162.0, n = 47197

 $109.0 \times 433.0 = (271-162.0)(271+162.0) = 271^2 - 162.0^2 = 47197$

.3

. $433-1=432=2^4\times 3^3$ ו- $109-1=108=2^3\times 3^3$. p-1|B| אם $p|a^{B!}-1$ אם על העובדה כי p-1|B| אם p-1 אם פולארד מבוססת על העובדה כי q-1 אינו מחלק את q-1 אינו מחלק את q-1 וו פיסיפויים טובים ש- q-1 וו ביותר הוא q-1 אבל במקרה הזה, עבור q-1 וו q-1 וו ביותר q-1 וו בייתר q-1 וו ביותר q-1 וו ביותר q-1 וו ביותר q-1 וו ביותר

.4

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.5