

## מבוא להצפנה – תרגיל 4

.1

.א.

In this chapter we calculate the private key  $d$  using the extended Euclidean algorithm.

```
i = 0, r = 33,      s = 0, t = 1
i = 1, r = 17, q = 1, s = 1, t = 0
i = 2, r = 16, q = 1, s = -1, t = 1
i = 3, r = 1, q = 16, s = 2, t = -1
```

-----  
we got that  $1 = 17 \cdot (2) + 33 \cdot (-1)$

-----  
So:

The value of  $s$  is 2

The value of  $t$  is -1

-----  
Now we calculate:

$C_a^s \cdot C_b^t = m^{(se_a)} \cdot m^{(te_b)} = m^{(se_a + te_b)} = m \pmod{16157}$

Calculate  $11671^{-1}$ :

First we need to calculate the inverse of 11671:  $11671^{-1} = 11671^{-1} \pmod{16157}$

Now we calculate it using the extended Euclidean algorithm:

```
i = 0, r = 16157,      s = 0, t = 1
i = 1, r = 11671, q = 1, s = 1, t = 0
i = 2, r = 4486, q = 2, s = -1, t = 1
i = 3, r = 2699, q = 1, s = 3, t = -2
i = 4, r = 1787, q = 1, s = -4, t = 3
i = 5, r = 912, q = 1, s = 7, t = -5
i = 6, r = 875, q = 1, s = -11, t = 8
i = 7, r = 37, q = 23, s = 18, t = -13
i = 8, r = 24, q = 1, s = -425, t = 307
i = 9, r = 13, q = 1, s = 443, t = -320
i = 10, r = 11, q = 1, s = -868, t = 627
i = 11, r = 2, q = 5, s = 1311, t = -947
i = 12, r = 1, q = 2, s = -7423, t = 5362
```

-----  
we got that  $1 = 11671 \cdot (-7423) + 16157 \cdot (5362)$

-----  
So:

The value of  $s$  is -7423

The value of  $t$  is 5362

-----

```
The inverse of 11671 is -7423 (mod 16157)
11671-1 = -7423 = 8734 (mod 16157)
Now we calculate 11671-1 = 87341 (mod 16157):
using the square and multiply algorithm:
1 in binary is [1]
-----
i = 0
e_i = 1
z2 = 1 (mod 16157)
z*8734 = 8734*8734 = 8734 (mod 16157)
-----
And we got that 11671-1 = 8734 (mod 16157)

=====
Now we calculate:
72242 = (mod 16157)

2 in binary is [1, 0]
-----
i = 0
e_i = 1
z2 = 1 (mod 16157)
z*7224 = 7224*7224 = 7224 (mod 16157)
-----
i = 1
e_i = 0
z2 = 12 = 15223 (mod 16157)
-----
And we got that 72242 = 15223 (mod 16157)

=====
The message is: 15223X8734 = 1729 (mod 16157)
=====
```

ב.

In this chapter we calculate the private key  $d$  using the extended Euclidean algorithm.

```
i = 0, r = 33,      s = 0, t = 1
i = 1, r = 17, q = 1, s = 1, t = 0
i = 2, r = 16, q = 1, s = -1, t = 1
i = 3, r = 1, q = 16, s = 2, t = -1
```

we got that  $1 = 17 \cdot (2) + 33 \cdot (-1)$

So:

The value of  $s$  is 2

The value of  $t$  is -1

Now we calculate:

$$C_a^s \cdot C_b^t = m^{(se_a)} \cdot m^{(te_b)} = m^{(se_a + te_b)} = m \pmod{16157}$$

Calculate  $11449^{-1}$ :

First we need to calculate the inverse of 11449:  $11449^{-1} = 11449^{-1} \pmod{16157}$

Now we calculate it using the extended Euclidean algorithm:

```
i = 0, r = 16157,      s = 0, t = 1
i = 1, r = 11449, q = 1, s = 1, t = 0
i = 2, r = 4708, q = 2, s = -1, t = 1
i = 3, r = 2033, q = 2, s = 3, t = -2
i = 4, r = 642, q = 3, s = -7, t = 5
i = 5, r = 107, q = 6, s = 24, t = -17
```

we got that  $107 = 11449 \cdot (24) + 16157 \cdot (-17)$

So:

The value of  $s$  is 24

The value of  $t$  is -17

The inverse of 11449 is 24  $\pmod{16157}$

$$11449^{-1} = 24 = 24 \pmod{16157}$$

Now we calculate  $11449^{-1} = 24^1 \pmod{16157}$ :

using the square and multiply algorithm:

1 in binary is [1]

$i = 0$

$e_i = 1$

$$z^2 = 1 \pmod{16157}$$

$$z^{24} = 24^{24} = 24 \pmod{16157}$$

```
-----  
And we got that  $11449^{-1} = 24 \pmod{16157}$ 
```

```
=====
```

Now we calculate:

$13910^2 \pmod{16157}$

2 in binary is [1, 0]

```
-----
```

i = 0

e\_i = 1

$z^2 = 1 \pmod{16157}$

$z * 13910 = 13910 * 13910 = 13910 \pmod{16157}$

```
-----
```

i = 1

e\_i = 0

$z^2 = 1^2 = 8025 \pmod{16157}$

```
-----
```

And we got that  $13910^2 = 8025 \pmod{16157}$

```
=====
```

The message is:  $8025 * 24 = 14873 \pmod{16157}$

```
=====
```

.2

.א

To check if 18 is a creator of the group  $Z_{349}$  we will calculate the following:

=====

1.  $324^0 = 5832 \bmod 349 = 324$
2.  $248^1 = 4464 \bmod 349 = 248$
3.  $276^2 = 4968 \bmod 349 = 276$
4.  $82^3 = 1476 \bmod 349 = 82$
5.  $80^4 = 1440 \bmod 349 = 80$
6.  $44^5 = 792 \bmod 349 = 44$
7.  $94^6 = 1692 \bmod 349 = 94$
8.  $296^7 = 5328 \bmod 349 = 296$
9.  $93^8 = 1674 \bmod 349 = 93$
10.  $278^9 = 5004 \bmod 349 = 278$
11.  $118^{10} = 2124 \bmod 349 = 118$
12.  $30^{11} = 540 \bmod 349 = 30$
13.  $191^{12} = 3438 \bmod 349 = 191$
14.  $297^{13} = 5346 \bmod 349 = 297$
15.  $111^{14} = 1998 \bmod 349 = 111$
16.  $253^{15} = 4554 \bmod 349 = 253$
17.  $17^{16} = 306 \bmod 349 = 17$
18.  $306^{17} = 5508 \bmod 349 = 306$
19.  $273^{18} = 4914 \bmod 349 = 273$
20.  $28^{19} = 504 \bmod 349 = 28$
21.  $155^{20} = 2790 \bmod 349 = 155$
22.  $347^{21} = 6246 \bmod 349 = 347$
23.  $313^{22} = 5634 \bmod 349 = 313$
24.  $50^{23} = 900 \bmod 349 = 50$
25.  $202^{24} = 3636 \bmod 349 = 202$
26.  $146^{25} = 2628 \bmod 349 = 146$
27.  $185^{26} = 3330 \bmod 349 = 185$
28.  $189^{27} = 3402 \bmod 349 = 189$
29.  $261^{28} = 4698 \bmod 349 = 261$
30.  $161^{29} = 2898 \bmod 349 = 161$
31.  $106^{30} = 1908 \bmod 349 = 106$
32.  $163^{31} = 2934 \bmod 349 = 163$
33.  $142^{32} = 2556 \bmod 349 = 142$
34.  $113^{33} = 2034 \bmod 349 = 113$
35.  $289^{34} = 5202 \bmod 349 = 289$
36.  $316^{35} = 5688 \bmod 349 = 316$
37.  $104^{36} = 1872 \bmod 349 = 104$
38.  $127^{37} = 2286 \bmod 349 = 127$
39.  $192^{38} = 3456 \bmod 349 = 192$

```
40.  $315^{39} = 5670 \bmod 349 = 315$ 
41.  $86^{40} = 1548 \bmod 349 = 86$ 
42.  $152^{41} = 2736 \bmod 349 = 152$ 
43.  $293^{42} = 5274 \bmod 349 = 293$ 
44.  $39^{43} = 702 \bmod 349 = 39$ 
45.  $4^{44} = 72 \bmod 349 = 4$ 
46.  $72^{45} = 1296 \bmod 349 = 72$ 
47.  $249^{46} = 4482 \bmod 349 = 249$ 
48.  $294^{47} = 5292 \bmod 349 = 294$ 
49.  $57^{48} = 1026 \bmod 349 = 57$ 
50.  $328^{49} = 5904 \bmod 349 = 328$ 
51.  $320^{50} = 5760 \bmod 349 = 320$ 
52.  $176^{51} = 3168 \bmod 349 = 176$ 
53.  $27^{52} = 486 \bmod 349 = 27$ 
54.  $137^{53} = 2466 \bmod 349 = 137$ 
55.  $23^{54} = 414 \bmod 349 = 23$ 
56.  $65^{55} = 1170 \bmod 349 = 65$ 
57.  $123^{56} = 2214 \bmod 349 = 123$ 
58.  $120^{57} = 2160 \bmod 349 = 120$ 
59.  $66^{58} = 1188 \bmod 349 = 66$ 
60.  $141^{59} = 2538 \bmod 349 = 141$ 
61.  $95^{60} = 1710 \bmod 349 = 95$ 
62.  $314^{61} = 5652 \bmod 349 = 314$ 
63.  $68^{62} = 1224 \bmod 349 = 68$ 
64.  $177^{63} = 3186 \bmod 349 = 177$ 
65.  $45^{64} = 810 \bmod 349 = 45$ 
66.  $112^{65} = 2016 \bmod 349 = 112$ 
67.  $271^{66} = 4878 \bmod 349 = 271$ 
68.  $341^{67} = 6138 \bmod 349 = 341$ 
69.  $205^{68} = 3690 \bmod 349 = 205$ 
70.  $200^{69} = 3600 \bmod 349 = 200$ 
71.  $110^{70} = 1980 \bmod 349 = 110$ 
72.  $235^{71} = 4230 \bmod 349 = 235$ 
73.  $42^{72} = 756 \bmod 349 = 42$ 
74.  $58^{73} = 1044 \bmod 349 = 58$ 
75.  $346^{74} = 6228 \bmod 349 = 346$ 
76.  $295^{75} = 5310 \bmod 349 = 295$ 
77.  $75^{76} = 1350 \bmod 349 = 75$ 
78.  $303^{77} = 5454 \bmod 349 = 303$ 
79.  $219^{78} = 3942 \bmod 349 = 219$ 
80.  $103^{79} = 1854 \bmod 349 = 103$ 
81.  $109^{80} = 1962 \bmod 349 = 109$ 
82.  $217^{81} = 3906 \bmod 349 = 217$ 
83.  $67^{82} = 1206 \bmod 349 = 67$ 
84.  $159^{83} = 2862 \bmod 349 = 159$ 
85.  $70^{84} = 1260 \bmod 349 = 70$ 
86.  $213^{85} = 3834 \bmod 349 = 213$ 
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```
87. 344^86 = 6192 mod 349 = 344
88. 259^87 = 4662 mod 349 = 259
89. 125^88 = 2250 mod 349 = 125
90. 156^89 = 2808 mod 349 = 156
91. 16^90 = 288 mod 349 = 16
92. 288^91 = 5184 mod 349 = 288
93. 298^92 = 5364 mod 349 = 298
94. 129^93 = 2322 mod 349 = 129
95. 228^94 = 4104 mod 349 = 228
96. 265^95 = 4770 mod 349 = 265
97. 233^96 = 4194 mod 349 = 233
98. 6^97 = 108 mod 349 = 6
99. 108^98 = 1944 mod 349 = 108
100. 199^99 = 3582 mod 349 = 199
101. 92^100 = 1656 mod 349 = 92
102. 260^101 = 4680 mod 349 = 260
103. 143^102 = 2574 mod 349 = 143
104. 131^103 = 2358 mod 349 = 131
105. 264^104 = 4752 mod 349 = 264
106. 215^105 = 3870 mod 349 = 215
107. 31^106 = 558 mod 349 = 31
108. 209^107 = 3762 mod 349 = 209
109. 272^108 = 4896 mod 349 = 272
110. 10^109 = 180 mod 349 = 10
111. 180^110 = 3240 mod 349 = 180
112. 99^111 = 1782 mod 349 = 99
113. 37^112 = 666 mod 349 = 37
114. 317^113 = 5706 mod 349 = 317
115. 122^114 = 2196 mod 349 = 122
116. 102^115 = 1836 mod 349 = 102
117. 91^116 = 1638 mod 349 = 91
118. 242^117 = 4356 mod 349 = 242
119. 168^118 = 3024 mod 349 = 168
120. 232^119 = 4176 mod 349 = 232
121. 337^120 = 6066 mod 349 = 337
122. 133^121 = 2394 mod 349 = 133
123. 300^122 = 5400 mod 349 = 300
124. 165^123 = 2970 mod 349 = 165
125. 178^124 = 3204 mod 349 = 178
126. 63^125 = 1134 mod 349 = 63
127. 87^126 = 1566 mod 349 = 87
128. 170^127 = 3060 mod 349 = 170
129. 268^128 = 4824 mod 349 = 268
130. 287^129 = 5166 mod 349 = 287
131. 280^130 = 5040 mod 349 = 280
132. 154^131 = 2772 mod 349 = 154
133. 329^132 = 5922 mod 349 = 329
```

```
134.  $338^{133} = 6084 \bmod 349 = 338$ 
135.  $151^{134} = 2718 \bmod 349 = 151$ 
136.  $275^{135} = 4950 \bmod 349 = 275$ 
137.  $64^{136} = 1152 \bmod 349 = 64$ 
138.  $105^{137} = 1890 \bmod 349 = 105$ 
139.  $145^{138} = 2610 \bmod 349 = 145$ 
140.  $167^{139} = 3006 \bmod 349 = 167$ 
141.  $214^{140} = 3852 \bmod 349 = 214$ 
142.  $13^{141} = 234 \bmod 349 = 13$ 
143.  $234^{142} = 4212 \bmod 349 = 234$ 
144.  $24^{143} = 432 \bmod 349 = 24$ 
145.  $83^{144} = 1494 \bmod 349 = 83$ 
146.  $98^{145} = 1764 \bmod 349 = 98$ 
147.  $19^{146} = 342 \bmod 349 = 19$ 
148.  $342^{147} = 6156 \bmod 349 = 342$ 
149.  $223^{148} = 4014 \bmod 349 = 223$ 
150.  $175^{149} = 3150 \bmod 349 = 175$ 
151.  $9^{150} = 162 \bmod 349 = 9$ 
152.  $162^{151} = 2916 \bmod 349 = 162$ 
153.  $124^{152} = 2232 \bmod 349 = 124$ 
154.  $138^{153} = 2484 \bmod 349 = 138$ 
155.  $41^{154} = 738 \bmod 349 = 41$ 
156.  $40^{155} = 720 \bmod 349 = 40$ 
157.  $22^{156} = 396 \bmod 349 = 22$ 
158.  $47^{157} = 846 \bmod 349 = 47$ 
159.  $148^{158} = 2664 \bmod 349 = 148$ 
160.  $221^{159} = 3978 \bmod 349 = 221$ 
161.  $139^{160} = 2502 \bmod 349 = 139$ 
162.  $59^{161} = 1062 \bmod 349 = 59$ 
163.  $15^{162} = 270 \bmod 349 = 15$ 
164.  $270^{163} = 4860 \bmod 349 = 270$ 
165.  $323^{164} = 5814 \bmod 349 = 323$ 
166.  $230^{165} = 4140 \bmod 349 = 230$ 
167.  $301^{166} = 5418 \bmod 349 = 301$ 
168.  $183^{167} = 3294 \bmod 349 = 183$ 
169.  $153^{168} = 2754 \bmod 349 = 153$ 
170.  $311^{169} = 5598 \bmod 349 = 311$ 
171.  $14^{170} = 252 \bmod 349 = 14$ 
172.  $252^{171} = 4536 \bmod 349 = 252$ 
173.  $348^{172} = 6264 \bmod 349 = 348$ 
174.  $331^{173} = 5958 \bmod 349 = 331$ 
175.  $25^{174} = 450 \bmod 349 = 25$ 
176.  $101^{175} = 1818 \bmod 349 = 101$ 
177.  $73^{176} = 1314 \bmod 349 = 73$ 
178.  $267^{177} = 4806 \bmod 349 = 267$ 
179.  $269^{178} = 4842 \bmod 349 = 269$ 
180.  $305^{179} = 5490 \bmod 349 = 305$ 
```



```
181. 255^180 = 4590 mod 349 = 255
182. 53^181 = 954 mod 349 = 53
183. 256^182 = 4608 mod 349 = 256
184. 71^183 = 1278 mod 349 = 71
185. 231^184 = 4158 mod 349 = 231
186. 319^185 = 5742 mod 349 = 319
187. 158^186 = 2844 mod 349 = 158
188. 52^187 = 936 mod 349 = 52
189. 238^188 = 4284 mod 349 = 238
190. 96^189 = 1728 mod 349 = 96
191. 332^190 = 5976 mod 349 = 332
192. 43^191 = 774 mod 349 = 43
193. 76^192 = 1368 mod 349 = 76
194. 321^193 = 5778 mod 349 = 321
195. 194^194 = 3492 mod 349 = 194
196. 2^195 = 36 mod 349 = 2
197. 36^196 = 648 mod 349 = 36
198. 299^197 = 5382 mod 349 = 299
199. 147^198 = 2646 mod 349 = 147
200. 203^199 = 3654 mod 349 = 203
201. 164^200 = 2952 mod 349 = 164
202. 160^201 = 2880 mod 349 = 160
203. 88^202 = 1584 mod 349 = 88
204. 188^203 = 3384 mod 349 = 188
205. 243^204 = 4374 mod 349 = 243
206. 186^205 = 3348 mod 349 = 186
207. 207^206 = 3726 mod 349 = 207
208. 236^207 = 4248 mod 349 = 236
209. 60^208 = 1080 mod 349 = 60
210. 33^209 = 594 mod 349 = 33
211. 245^210 = 4410 mod 349 = 245
212. 222^211 = 3996 mod 349 = 222
213. 157^212 = 2826 mod 349 = 157
214. 34^213 = 612 mod 349 = 34
215. 263^214 = 4734 mod 349 = 263
216. 197^215 = 3546 mod 349 = 197
217. 56^216 = 1008 mod 349 = 56
218. 310^217 = 5580 mod 349 = 310
219. 345^218 = 6210 mod 349 = 345
220. 277^219 = 4986 mod 349 = 277
221. 100^220 = 1800 mod 349 = 100
222. 55^221 = 990 mod 349 = 55
223. 292^222 = 5256 mod 349 = 292
224. 21^223 = 378 mod 349 = 21
225. 29^224 = 522 mod 349 = 29
226. 173^225 = 3114 mod 349 = 173
227. 322^226 = 5796 mod 349 = 322
```

```
228. 212^227 = 3816 mod 349 = 212
229. 326^228 = 5868 mod 349 = 326
230. 284^229 = 5112 mod 349 = 284
231. 226^230 = 4068 mod 349 = 226
232. 229^231 = 4122 mod 349 = 229
233. 283^232 = 5094 mod 349 = 283
234. 208^233 = 3744 mod 349 = 208
235. 254^234 = 4572 mod 349 = 254
236. 35^235 = 630 mod 349 = 35
237. 281^236 = 5058 mod 349 = 281
238. 172^237 = 3096 mod 349 = 172
239. 304^238 = 5472 mod 349 = 304
240. 237^239 = 4266 mod 349 = 237
241. 78^240 = 1404 mod 349 = 78
242. 8^241 = 144 mod 349 = 8
243. 144^242 = 2592 mod 349 = 144
244. 149^243 = 2682 mod 349 = 149
245. 239^244 = 4302 mod 349 = 239
246. 114^245 = 2052 mod 349 = 114
247. 307^246 = 5526 mod 349 = 307
248. 291^247 = 5238 mod 349 = 291
249. 3^248 = 54 mod 349 = 3
250. 54^249 = 972 mod 349 = 54
251. 274^250 = 4932 mod 349 = 274
252. 46^251 = 828 mod 349 = 46
253. 130^252 = 2340 mod 349 = 130
254. 246^253 = 4428 mod 349 = 246
255. 240^254 = 4320 mod 349 = 240
256. 132^255 = 2376 mod 349 = 132
257. 282^256 = 5076 mod 349 = 282
258. 190^257 = 3420 mod 349 = 190
259. 279^258 = 5022 mod 349 = 279
260. 136^259 = 2448 mod 349 = 136
261. 5^260 = 90 mod 349 = 5
262. 90^261 = 1620 mod 349 = 90
263. 224^262 = 4032 mod 349 = 224
264. 193^263 = 3474 mod 349 = 193
265. 333^264 = 5994 mod 349 = 333
266. 61^265 = 1098 mod 349 = 61
267. 51^266 = 918 mod 349 = 51
268. 220^267 = 3960 mod 349 = 220
269. 121^268 = 2178 mod 349 = 121
270. 84^269 = 1512 mod 349 = 84
271. 116^270 = 2088 mod 349 = 116
272. 343^271 = 6174 mod 349 = 343
273. 241^272 = 4338 mod 349 = 241
274. 150^273 = 2700 mod 349 = 150
```

```
275. 257^274 = 4626 mod 349 = 257
276. 89^275 = 1602 mod 349 = 89
277. 206^276 = 3708 mod 349 = 206
278. 218^277 = 3924 mod 349 = 218
279. 85^278 = 1530 mod 349 = 85
280. 134^279 = 2412 mod 349 = 134
281. 318^280 = 5724 mod 349 = 318
282. 140^281 = 2520 mod 349 = 140
283. 77^282 = 1386 mod 349 = 77
284. 339^283 = 6102 mod 349 = 339
285. 169^284 = 3042 mod 349 = 169
286. 250^285 = 4500 mod 349 = 250
287. 312^286 = 5616 mod 349 = 312
288. 32^287 = 576 mod 349 = 32
289. 227^288 = 4086 mod 349 = 227
290. 247^289 = 4446 mod 349 = 247
291. 258^290 = 4644 mod 349 = 258
292. 107^291 = 1926 mod 349 = 107
293. 181^292 = 3258 mod 349 = 181
294. 117^293 = 2106 mod 349 = 117
295. 12^294 = 216 mod 349 = 12
296. 216^295 = 3888 mod 349 = 216
297. 49^296 = 882 mod 349 = 49
298. 184^297 = 3312 mod 349 = 184
299. 171^298 = 3078 mod 349 = 171
300. 286^299 = 5148 mod 349 = 286
301. 262^300 = 4716 mod 349 = 262
302. 179^301 = 3222 mod 349 = 179
303. 81^302 = 1458 mod 349 = 81
304. 62^303 = 1116 mod 349 = 62
305. 69^304 = 1242 mod 349 = 69
306. 195^305 = 3510 mod 349 = 195
307. 20^306 = 360 mod 349 = 20
308. 11^307 = 198 mod 349 = 11
309. 198^308 = 3564 mod 349 = 198
310. 74^309 = 1332 mod 349 = 74
311. 285^310 = 5130 mod 349 = 285
312. 244^311 = 4392 mod 349 = 244
313. 204^312 = 3672 mod 349 = 204
314. 182^313 = 3276 mod 349 = 182
315. 135^314 = 2430 mod 349 = 135
316. 336^315 = 6048 mod 349 = 336
317. 115^316 = 2070 mod 349 = 115
318. 325^317 = 5850 mod 349 = 325
319. 266^318 = 4788 mod 349 = 266
320. 251^319 = 4518 mod 349 = 251
321. 330^320 = 5940 mod 349 = 330
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```
322.  $7^{321} = 126 \bmod 349 = 7$ 
323.  $126^{322} = 2268 \bmod 349 = 126$ 
324.  $174^{323} = 3132 \bmod 349 = 174$ 
325.  $340^{324} = 6120 \bmod 349 = 340$ 
326.  $187^{325} = 3366 \bmod 349 = 187$ 
327.  $225^{326} = 4050 \bmod 349 = 225$ 
328.  $211^{327} = 3798 \bmod 349 = 211$ 
329.  $308^{328} = 5544 \bmod 349 = 308$ 
330.  $309^{329} = 5562 \bmod 349 = 309$ 
331.  $327^{330} = 5886 \bmod 349 = 327$ 
332.  $302^{331} = 5436 \bmod 349 = 302$ 
333.  $201^{332} = 3618 \bmod 349 = 201$ 
334.  $128^{333} = 2304 \bmod 349 = 128$ 
335.  $210^{334} = 3780 \bmod 349 = 210$ 
336.  $290^{335} = 5220 \bmod 349 = 290$ 
337.  $334^{336} = 6012 \bmod 349 = 334$ 
338.  $79^{337} = 1422 \bmod 349 = 79$ 
339.  $26^{338} = 468 \bmod 349 = 26$ 
340.  $119^{339} = 2142 \bmod 349 = 119$ 
341.  $48^{340} = 864 \bmod 349 = 48$ 
342.  $166^{341} = 2988 \bmod 349 = 166$ 
343.  $196^{342} = 3528 \bmod 349 = 196$ 
344.  $38^{343} = 684 \bmod 349 = 38$ 
345.  $335^{344} = 6030 \bmod 349 = 335$ 
346.  $97^{345} = 1746 \bmod 349 = 97$ 
347.  $1^{346} = 18 \bmod 349 = 1$ 
348.  $18^{347} = 324 \bmod 349 = 18$ 
```

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The group is:

```
[18, 324, 248, 276, 82, 80, 44, 94, 296, 93, 278, 118, 30, 191,
297, 111, 253, 17, 306, 273, 28, 155, 347, 313, 50, 202, 146,
185, 189, 261, 161, 106, 163, 142, 113, 289, 316, 104, 127, 192,
315, 86, 152, 293, 39, 4, 72, 249, 294, 57, 328, 320, 176, 27,
137, 23, 65, 123, 120, 66, 141, 95, 314, 68, 177, 45, 112, 271,
341, 205, 200, 110, 235, 42, 58, 346, 295, 75, 303, 219, 103,
109, 217, 67, 159, 70, 213, 344, 259, 125, 156, 16, 288, 298,
129, 228, 265, 233, 6, 108, 199, 92, 260, 143, 131, 264, 215, 31,
209, 272, 10, 180, 99, 37, 317, 122, 102, 91, 242, 168, 232, 337,
133, 300, 165, 178, 63, 87, 170, 268, 287, 280, 154, 329, 338,
151, 275, 64, 105, 145, 167, 214, 13, 234, 24, 83, 98, 19, 342,
223, 175, 9, 162, 124, 138, 41, 40, 22, 47, 148, 221, 139, 59,
15, 270, 323, 230, 301, 183, 153, 311, 14, 252, 348, 331, 25,
101, 73, 267, 269, 305, 255, 53, 256, 71, 231, 319, 158, 52, 238,
96, 332, 43, 76, 321, 194, 2, 36, 299, 147, 203, 164, 160, 88,
188, 243, 186, 207, 236, 60, 33, 245, 222, 157, 34, 263, 197, 56,
310, 345, 277, 100, 55, 292, 21, 29, 173, 322, 212, 326, 284,
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187, 225, 211, 308, 309, 327, 302, 201, 128, 210, 290, 334, 79,
26, 119, 48, 166, 196, 38, 335, 97, 1, 18]
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The duplicates are: [18]

- The length of the group is: 349
- The length of the group without duplicates is: 348

YES 18 is a creator of the group Z\_349

שם: שחר אשר  
ת.ז. 209305408

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