

ASSIGNMENT on STA102



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Section: 04

STA102
Statistics and Probability
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JIM

Assignment - 3

Answer to the question no 1

The data in ascending order.

28, 42, 45, 48, 49, 50, 55, 58, 60

(i)

Range = Large value - ~~sm~~ small value

$$= 60 - 28$$

$$= 32$$

Here,

Large value = 60

Smaller value = 28

Comment: The difference between the most value and the most smallest value is 32.

largest

$$Q_1 = \left(\frac{n+1}{100} \times 25 \right)^{\text{th}} \text{ value}$$

$$= \left(\frac{10 \times 25}{100} \right)^{\text{th}} \text{ value}$$

$$= 2.5^{\text{th}} \text{ value}$$

Here,

$$n = 9$$

$$\text{So, } 2.5^{\text{th}} \text{ value} = 42 + (45 - 42) \times 0.5 = 43.5$$

$$Q_3 = \left(\frac{10 \times 75}{100} \right)^{\text{th}} \text{ value} = 7.5^{\text{th}} \text{ value.}$$

$$\text{So, } 7.5^{\text{th}} \text{ value} = 55 + (58 - 55) \times 0.5 = 56.5$$

$$\text{So, The } QQR = Q_3 - Q_1 = 56.5 - 43.5 = 13$$

Comment: The difference between the largest and smallest 25% is 13.

(ii)

We know,

$$\text{Sample variance, } s^2 = \frac{\sum (x - \bar{x})^2}{n-1}$$

$$\begin{aligned} \bar{x} &= \frac{28+42+45+48+49+50+55+58+60}{9} \\ &= 48.33 \end{aligned}$$

$$s^2 = \frac{(28-48.33)^2 + (42-48.33)^2 + (45-48.33)^2 + (48-48.33)^2 + (49-48.33)^2 + (50-48.33)^2 + (55-48.33)^2 + (58-48.33)^2 + (60-48.33)^2}{9-1}$$

$$= 92.75$$

Comment: On an average, the squared distance from the mean is 92.75.

$$\begin{aligned} s &= \sqrt{\frac{\sum (x - \bar{x})^2}{n-1}} = \sqrt{s^2} \\ &= \sqrt{\frac{792}{8}} = \sqrt{92.75} \\ &= 9.63 \end{aligned}$$

Comment: On an average, the squared distance from the mean is 9.63.

(\bar{x})

from \bar{x} we get the
Standard deviation
variance of Pomona Air Quality index value for

Pomona p.e.s,

$$s_p = 9.63$$

$$\text{and } \bar{x}_p = 48.33$$

$$\text{So, } CV_p = \frac{9.63}{48.33} \times 100 = 19.93\%$$

According to the question

$$s_A = 11.66$$

$$\bar{x}_A = 48.5$$

$$\text{So, } CV_A = \frac{11.66}{48.5} \times 100 = 24.04\%$$

Comment: On an average, Anaheim's air quality is
more scattered than the air quality of Pomona.

Answer to the question no 2

Data in ascending order:

32 32 32 37 37 40 40 40 40 40
42 46 46 46 46 46 46 52 52 52
52 52 52

a

$$\begin{aligned}\text{Mean} &= \frac{\sum x}{n} \\ &= \frac{1000}{23} \\ &= 43.48\end{aligned}$$

$$\begin{aligned}\text{here,} \\ \sum x &= 1000 \\ n &= 23\end{aligned}$$

$$\text{Median} = \left(\frac{n+1}{2} \right)^{\text{th}} \text{ value} = 12^{\text{th}} \text{ value} = 46$$

$$\begin{aligned}\text{SD} &= \sqrt{\frac{\sum (x - \bar{x})^2}{n-1}} \\ &= \sqrt{\frac{1015.74}{23-1}} \\ &= 6.795\end{aligned}$$

$$\begin{aligned}\text{here} \\ \sum (x - \bar{x})^2 &= 1015.74\end{aligned}$$

So,

$$\text{Coefficient of skewed} = \frac{3(43.48 - 46)}{6.795}$$

Comment:

$$= -1.14$$

The shape of the data is left skewed.

b

Here,

$$\text{Min} = 32$$

$$Q_1 = \left(\frac{29 \times 25}{100} \right) = 6^{\text{th}} \text{ value} = 40$$

$$Q_2 = \left(\frac{29 \times 50}{100} \right) = 12^{\text{th}} \text{ value} = 46$$

$$Q_3 = \left(\frac{29 \times 75}{100} \right) = 18^{\text{th}} \text{ value} = 52$$

$$\text{Max} = 52$$

$$IQR = Q_3 - Q_1 = 12$$

$$\text{Upper Limit} = Q_3 + (1.5 \times IQR) = 70$$

$$\text{Lower Limit} = Q_1 - (1.5 \times IQR) = 22$$

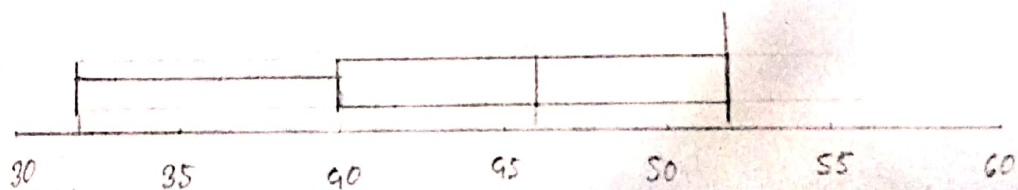


Figure: Box plot of customer visited ~~on~~ Smith's True value store in Bellville, Ohio, over last 28 days.

There is no outlier.

Answer to the question no 3

a

The median is 450.

b

The first quantile is 300.

The third quantile is 750.

c

The IQR = $Q_3 - Q_1 = 750 - 300 = 450$.

d

~~Beyond 0-1350 poin, a value is considered a outlier.~~

Upper Limit = $750 + (1.5 \times 450) = 1425$

Lower Limit = $300 - (1.5 \times 450) = -375$

Beyond -375 to 1425 points, a value is considered as outlier.

e

The outlier in the figure is on the 1500 poin.

f

∴ The distribution is positively skewed.