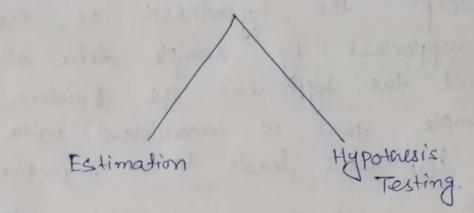
Statistical Inference

The process of drawing inferences or conclusions about population on the basis of Sample information is called Statistical Inference.



Estimation:

Estimation is a Procedure by which we obtain an estimate of population Parameter using the Sample information.

e.g x is an estimator of l.

Testing of hypothesis:

Testing of hypothesis is a procedure which enables us to decide on the basis of information obtained by sampling whether to accept or reject any specified stadement or hypothesis regarding parameter. e.g. a medical researcher may decide on the basis of experimental evidence whether smoking increase the risk of cancer or not.

H, Or HA.

Statistical Hypothesis:A Statement or assumption which may or may not be true is called hypothesis. => we accept the hypothesis as true if it is supported by sample data otherwise we reject the hypothesis. Or Evidence from the sample that is inconsistent with the Stated hypothesis leads to a rejection of hypothesis. Null and alternate hypothesis:-Null hypothesis is any hypothesis we wish to test for Possible Rejection under the assumption that it is the. Null hypothesis is denoted by => The term implies ussally that it is
"no effect" e.g. the drug is ineffective
in caring the porticular disease. or the coin is unbiased.

The null hypothesis should precèse.

=> The null hypothesis should assign a numarical value. e.g. Ho: U = 62.

Alternate hypothesis is any other hypothesis which we accept when null hypothesis is rejected.

=> It is denoted by H, or HA.

=> Null hypothesis is tested against afternate hypothesis is Ho: U= 62 then alternate hypothesis HI: U + 62 Or HI: U > 62, HI: U < 62 Simple and composite hypothesis:
A simple hypothesis is one in which all the parameters of the distribut are specified. e.g if heights of collège Students are normally distributed with $\sigma = 4$, the hypothesis that its mean u = 62. As the mean and variance together specify a normal distribution completely. A hypothesis is composite if all the parameters are not Specified. For instance if we hypothesize that 1762 or oze 4 the hypothesis becomes a composite hypothesis. The concept of simple and composite hypothesis applies to both mull & Test Statistic:-A sample statistic which provides basis for testing mull hypothesis.

> Every test statistic has a probability distribution which gives the probability of obtaining a specified value of the test statistic when null hypothesis is The sampling distribution of most commonly used test statistic are

Z, t, F and chisquare.

Acceptance and Rejection region:

All possible values which a test-statistic may assume can be divided into two mutually exclusive groups.

=> one group consisting of values which appear to be consistant with null hypothesis, this group is called acceptance region.

=) other group having values which are unlikely to occur if Ho is true, this group is known as rejection region. The rejection region is also called critical region.

=> The values that separates the critical region from acceptance region are called the critical values.

Type I and Type II Errors:

when we perform a hypothesis test, we derive the evidence from the Sample in the form of a test-Statistic-There is a possibility that the Sample evidence may lead us to make a wrong decision.

=) Rejection of null hypothesis Ho, when it is actually true is called Type I error.

=) Acception or non-rejection of mull hypothesis
Type II error.

Decision		1
True Situation	Do mot reject Accept Ho	Reject Ho
Ho is true	Correct	Wrong Decision (Type I Errox)
Ho is false		Correct Decision (NO Ensur)

Example:

In a courst trial the hypothesis is that the accused is innocent. After having heard the evidence presented during the trial, the sudge arrives at a decision. Suppose that the accused is, in fact innocent (i.e Ho is true) but the findings of the judge has rejected the true mull hypothesis and in doing so he has made type I Essor.

=) If on the other hand, the accused is in-fact quilty (i.e to is false) and the findings of judge is innocent, the judge has accepted a false null hypothesis and by accepting a false hypothesis, he has committed a type II error.

- The probability of committing type I Error is also called level of significance and denoted by α .
- =) Type II Essor is denoted by B.

X=P(Type I Error) = p(Reject Ho/Ho is)

B = P(Type II Essor) = P (Do not to / Ho is)
false)

General procedure for Testing hypothesis:

- 1) State the null and alternate hypothesis
- 2) Choose level of Significance.
- 3) choose an appropriate test-statistic and establish the C.R based on x-
- 4) Reject Ho if computed value of test-Statistic is sin the C.R, otherwise do not reject.
 - 5) Draw conclusions.

Testing hypothesis about mean (Single Sample)

- 1) Testing on a single mean when variance known. (Z-test)
- 2) Testing on a Single mean when variance is unknown- (t-test)
 and n < 30

one-tailed and two-tailed tests:
A test for which the entire rejection region is located in only one of the two-tails, either in the right side or in the left tail of the sampling distribution of test statistic is

called one talled test eg If Z is the test station

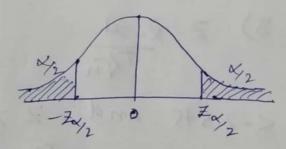
Rejection Region

Reject Ho if $Z < -Z_{\infty}$ Reject Ho if $Z > Z_{\infty}$ A one tailed test is used when the alternative hypothesis is formulated as

HI: $U > U_0$ or H_1 : $U < U_0$

=> If the rejection region is divided equally between the two tails of the distribution of test-statistic, the test is referred to as a two tailed test. i.e

HI: U = 100



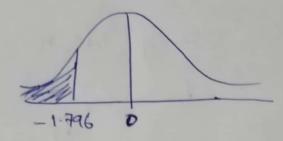
Reject Ho if Z <- Zx/2 Or Z > Zx/2

The location of the C.R can be determined only after Hi has been Stated."

Example 10.3 (case I when varionce (walpole, pg 338) Ho: U = 70 or U < 70 (vasiance Known) Hr: 4>70 2) K= 0.05 Z = X-11 C.R: Reject Ho if Z >1-645 7 = 71.8 - 70 Z = 2-02 5) As the calculated value of I lies, in rejection region so reject to and conclude that mean life span today is greater than 70 years. Example 10.4 1) Ho: U= 8 H1: 11+8 $2) \quad \alpha = 0.01$ (4) critical region: Reject to if Z <-2.575 5) Decision: Reject to and -2.595 conclude that the average breaking strength is not equal to 8.

Testing of mean when variance unknown. · t = x - 40 Two tailed Ho: U= llo HI: U = NO C.R Reject Ho if t <- (x2,n-1) or $t > t(x_2, n-1)$ one tailed test 1) Ho: U= No Hr: U>No Reject to if t > tx, (n-1) 2) Ho: U= No Hi: U < UO Reject to if t < -ta, (m-1) (walpole, pg 340) Example 10.5 1) Ho: M=46 H1: M< 46 2) X= 0.05 3) $t = \frac{x - u_0}{\sqrt[3]{n}}$ with n - 1 = 11 degrees of freedom. 4) C.R: Reject Ho if t <-1.796 with 11d.f. t = 42 - 46

t = -1.16



Decision: The average number of killowatt hours used annually by Home vacume cleaners in not significantly less than

Degrees of freedom

Number of items

that are free from restrictions.















On the first day, you can wear any of the 7 hats. On the second day, you can choose from the 6 remaining hats, on day 3 you can choose from 5 hats, and so on.

When day 6 rolls around, you still have a choice between 2 hats that you haven't worn yet that week. But after you choose your hat for day 6, you have no choice for the hat that you wear on Day You must wear the one remaining hat. You had 7-1 = 6 days of "hat" freedom in which the hat you wore could vary!