

Q Describe image Sampling and Quantization

Ans:- An image may be continuous with respect to  $x$  and  $y$  coordinates & also in amplitude.

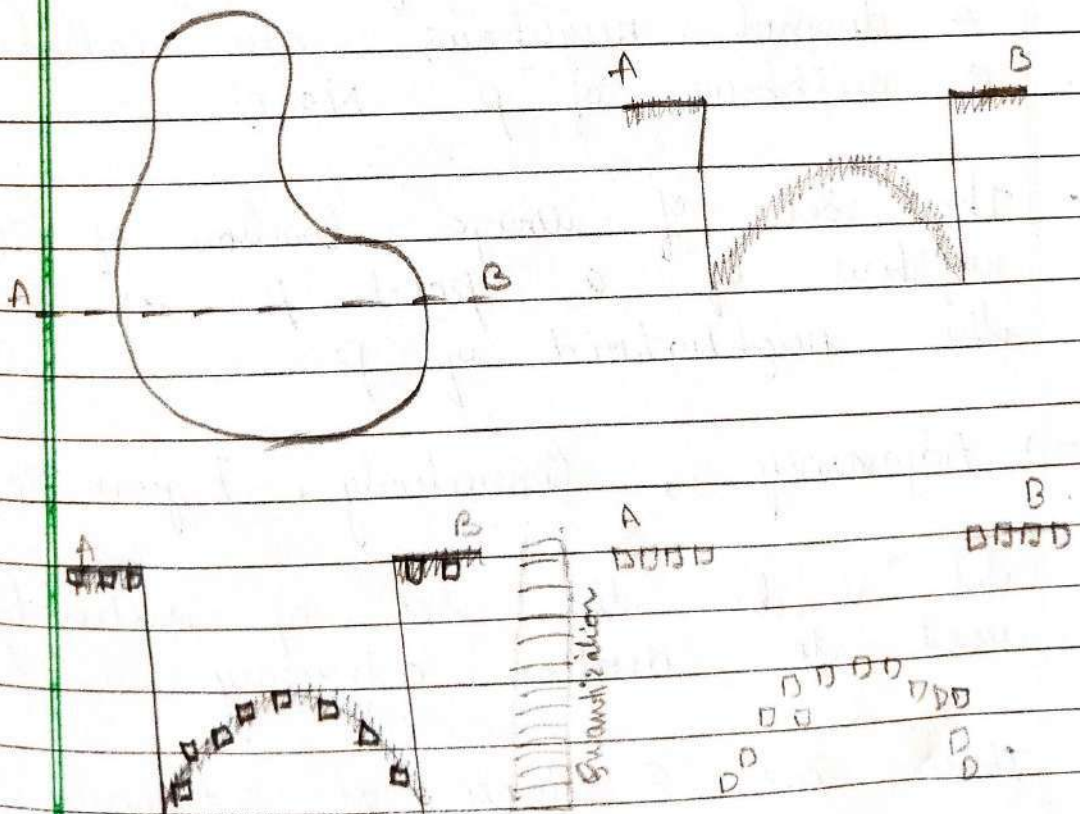
- Digitizing the coordinates value is called Sampling
- Digitizing the amplitude value is called as quantization
- The one dimensional function in fig 2.16 b is a plot of amplitude value of the continuous image along the line segment AB in fig 2.16 (a). The random variations are due to image noise. To sample this function we take equal spaced samples along line AB as in fig 2.16 (c)
- The samples are shown in small dark squares superimposed on the function and their spatial locations are indicated by corresponding tick mark in the bottom of figure
- The set of dark square constitute a sampled function.



• The values of the samples still span a continuous range of intensity values. To form digital function. The intensity value also be converted into discrete.

• The accuracy achieved in quantization is highly dependent on the noise content of the sampled signal.

• The method of sampling is determined by the sensor arrangement used to generate image.



Sampling  
(a) Continuous image (b) A scanned line shows intensity variation along AB in continuous  
(c) Sampling & Quantization (d) digital scan



Q Illustrate basic relationship between pixels.

Ans → Neighbour of a pixel :- A pixel  $p$  at coordinates  $(x, y)$  has two horizontal & two vertical neighbours with coordinates

$$(x+1, y), (x-1, y), (x, y+1), (x, y-1)$$

- (i) Set of pixel called as <sup>neighbour of</sup> 4-~~r~~ pixel  $N_4(p)$   
 (ii) four diagonal neighbour  $N_D(p)$

$$(x+1, y+1), (x+1, y-1), (x-1, y+1), (x-1, y-1)$$

- (iii) The combination of 4 neighbours and 4 diagonal neighbours are called as 8 neighbours of  $p$   $N_8(p)$ .

- The set of image location of the neighbours of a point  $p$  is called the neighborhood of  $p$ .

→ Adjacency, Connectivity, Region & Boundary

Let  $V$  be the set of intensity values used to define adjacency.

There are 3 types of adjacency.



(i) 4 adjacency: two pixels  $p$  &  $q$  with values from  $V$  are 4 adjacent if  $q$  is in the set  $N_4(p)$ .

(ii) 8 adjacency: two pixels  $p$  &  $q$  with values from  $V$  are 8 adjacency if  $q$  is in the set  $N_8(p)$ .

(iii)  $m$  adjacency: It is also called as mixed adjacency. Two pixels  $p$  &  $q$  with values from  $V$  are  $m$  adjacency if

- (a)  $q$  is in  $N_4(p)$  or
- (b)  $q$  is in  $N_D(p)$  and the set  $N_4(p) \cap N_4(q)$  has no pixels whose value from  $V$ .

- Let  $S$  represent a subset of pixels in an image.

- Two pixels  $p$  &  $q$  are said to be Connected in  $S$  if there exists a path between them consisting entirely of pixels in  $S$ .

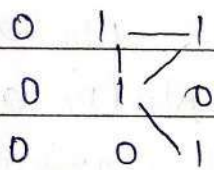
- The set of pixels that are Connected to it in  $S$  is called a Connected Component in  $S$ . & if it has only one Component then that Component is Connected to  $S$ .



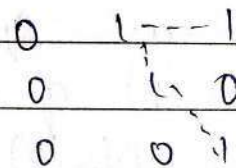
called as Connected Set

- Let  $R$  represent a subset of pixels in an image we call  $R$  as a region of that image if  $R$  is Connected Set.
- Two Region  $R_i$  &  $R_j$  are said to be adjacent if their union forms a Connected set.  $k_s$  Regions that are not adjacent are said to be disjoint

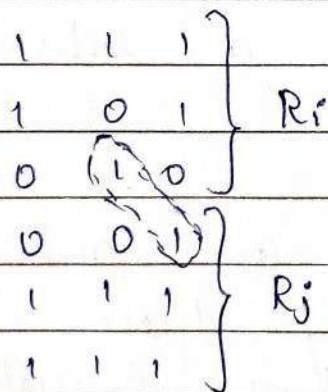
Eg:-



8 adjacency



m adjacency.



Two Regions

- for pixels  $p, q$  &  $s$  with coordinate  $(x, y)$ ,  $(u, v)$  &  $(w, z)$  respectively,  $D$  is a Distance function or metric if



- (a)  $D(P, q) \geq 0$  ( $D(P, q) = 0$  if  $P = q$ ),  
 (b)  $D(P, q) = D(q, P)$ ,  
 (c)  $D(P, s) \leq D(P, q) + D(q, s)$ .

→ The Euclidean distance

$$D_e(P, q) = [(x-u)^2 + (y-v)^2]^{1/2}$$

→ The  $D_4$  distance (city block distance)

$$D_4(P, q) = |x-u| + |y-v|$$

→ The  $D_8$  distance (chessboard distance)

$$D_8(P, q) = \max(|x-u|, |y-v|)$$

Q. Describe basic of intensity transformation & spatial filtering.

Ans. The spatial domain processes -

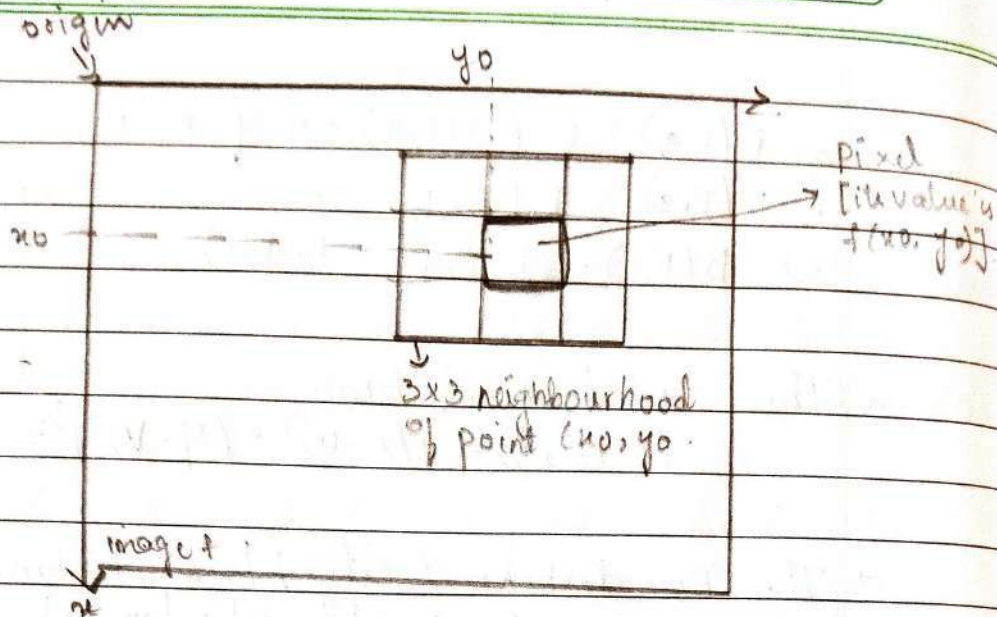
$$g(x, y) = T[f(x, y)]$$

$f(x, y)$  = input image

$g(x, y)$  = output image

$T$  = operator on  $f$  defined over a neighbourhood of point  $(x, y)$ .





The figure shows the basic implementation of the equation on single image.

- The point  $(x_0, y_0)$  shown is an arbitrary location in the image and the small region shows neighbourhood of  $(x_0, y_0)$
- The smallest possible neighbourhood is of size  $1 \times 1$ .  $g$  depends only on the value of  $f$  at a single point  $(x, y)$  &  $T$  becomes an intensity called as grey level or - mapping.

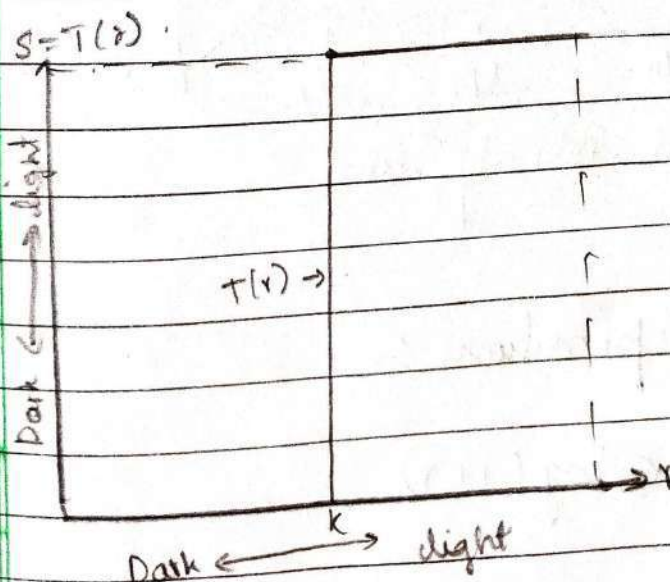
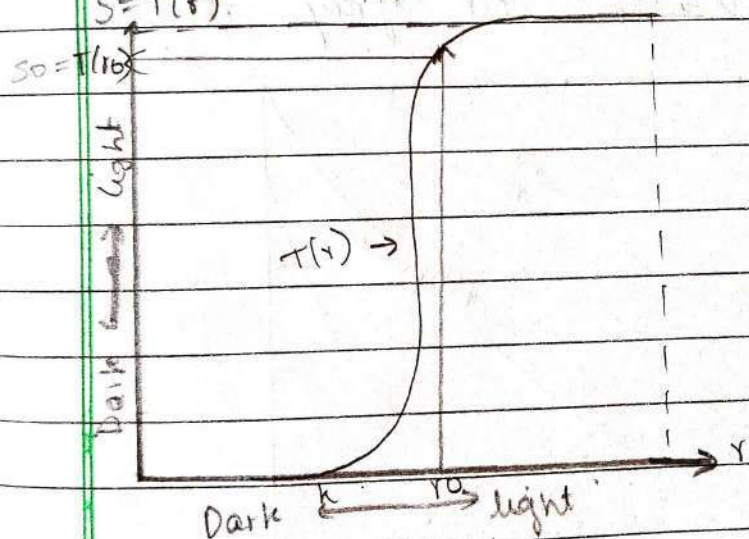
$$S = T(x).$$

- Applying the transformation to every pixel in  $f$  to generate the corresponding pixels in  $g$  would be to produce an image of higher



Contrast than the original. By darkening the intensity level below  $k$  and brightening the level above  $k$ . This is known as Contrast Stretching.

- The opposite is true for values of  $r$  higher than  $k$ . An intensity value  $r_0$  is mapped to obtain value  $s_0$  where  $T(r)$  produces two level (binary) image called as thresholding function  $S = T(r)$ .



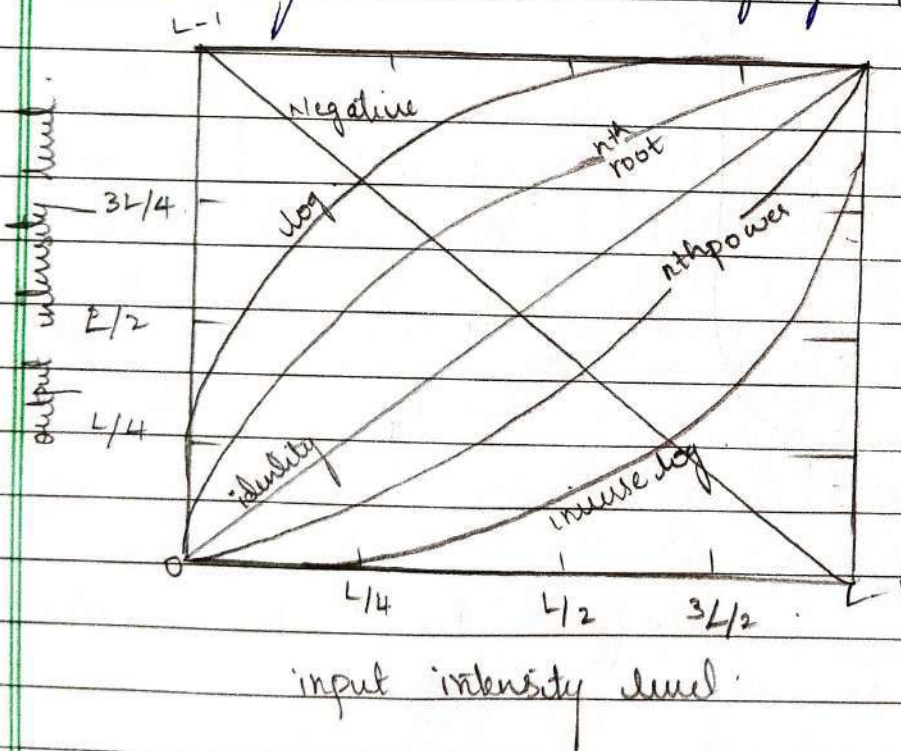


Q Describe basic intensity transformation functions

Ans: (i) Image Negative :- The negative of an image with intensity levels in the range  $[0, L-1]$  is obtained by using negative transformation function,

$$S = L-1-r$$

This type of processing is used in enhancing white or gray regions.



(ii) log transformation :-

$$S = C \log(1+r)$$



$c$  is constant &  $r \geq 0$

- The shape of the log curve shows that this transformation maps a narrow range of low intensity in the input into wider range of output levels
- The opposite of this is true and is known as inverse log transformation

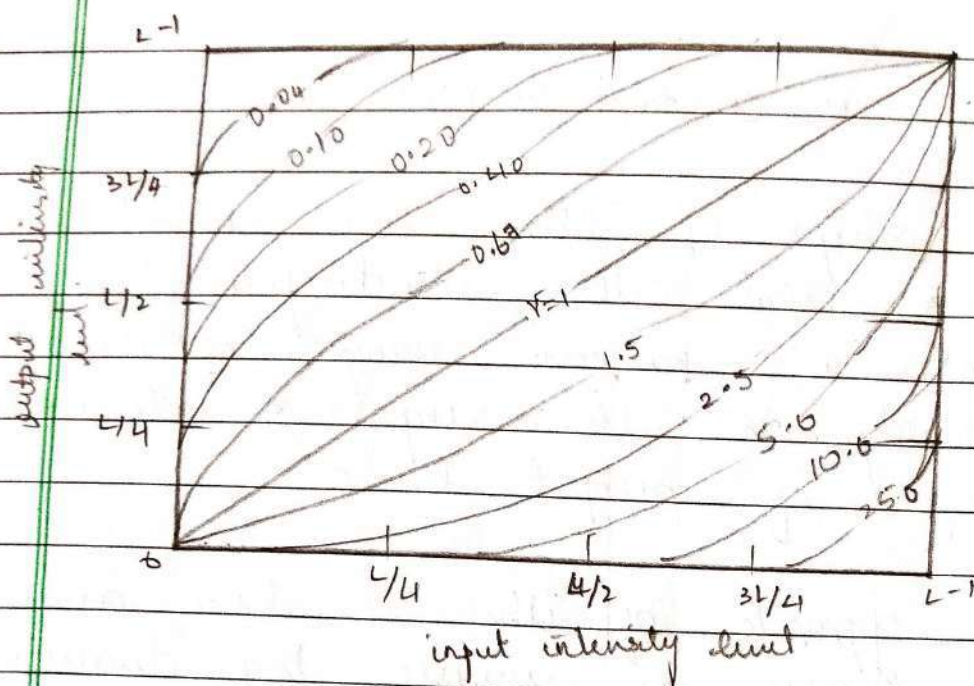
(iii) power log (Gamma) Transformations

$$S = Cr^r$$

where  $c$  &  $r$  are positive constants.

- As with log transformations power log curve with fraction of  $r$  map a narrow range of dark input values into a wider range of output values.
- if  $r > 1$  then brighter to darker is generated & if  $r < 1$  then lighter to darker is generated





Q Describe piece wise linear transformation function.

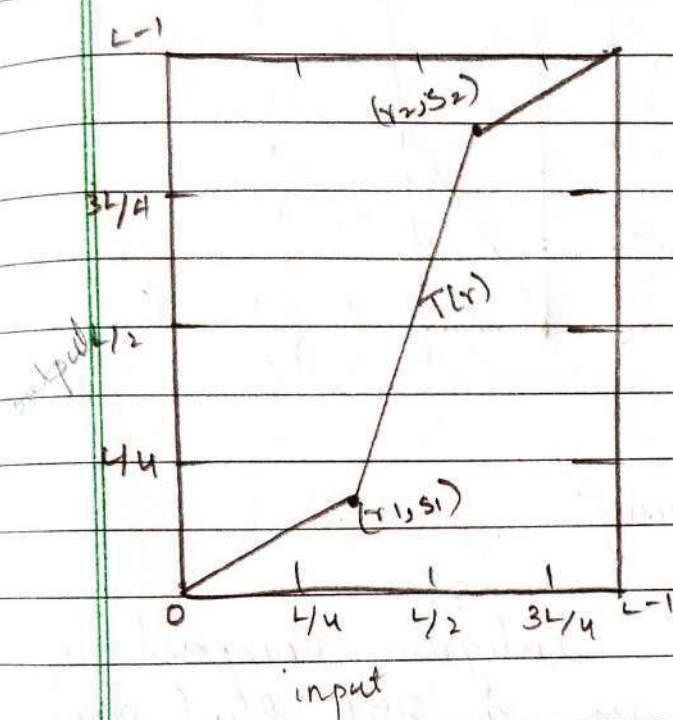
Ans i) Contrast Stretching: low contrast images can result from poor illumination. lack of dynamic range in the imaging sensor during image acquisition.

• Contrast Stretching expands the range of intensity level in image so that it spans the full intensity range of the medium.

• The location of points  $(r_1, s_1)$  &  $(r_2, s_2)$  control the shape of transformation. if  $r_1 = s_1$  &  $r_2 = s_2$  the transformation is linear & produces no change in intensity.



- if  $r_1 = r_2$  &  $s_1 = 0, s_2 = L-1$  the transformation becomes thresholding function that creates binary image.

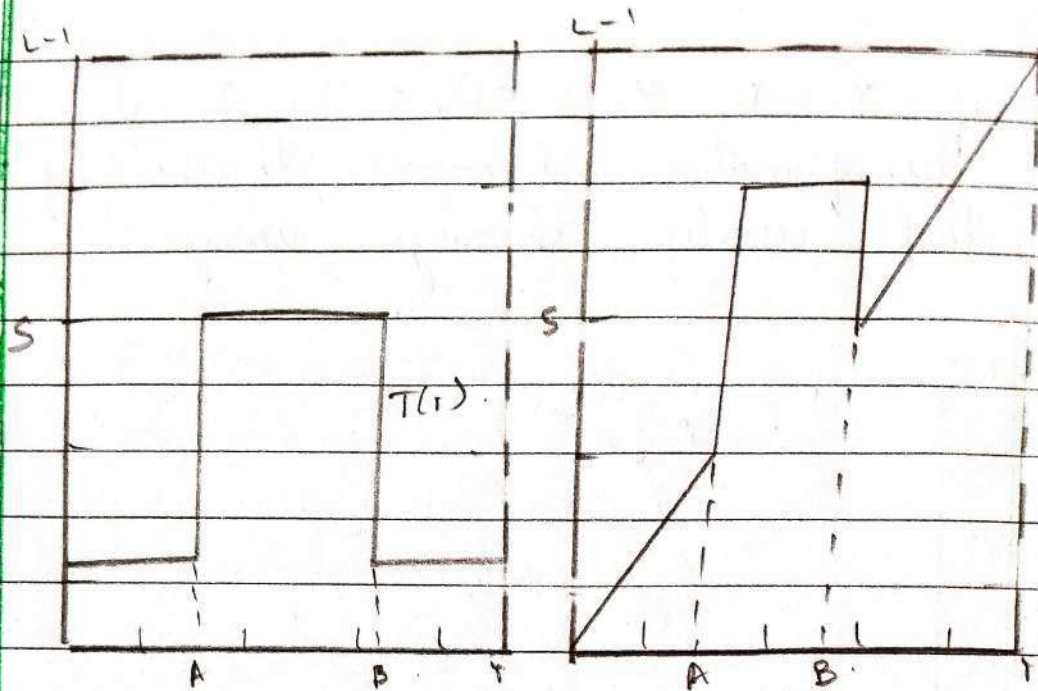


- (ii) Intensity level slicing: It is used to highlight a specific range of intensity in an image.

- One approach is to display in one value (white) all the values in the range & other (black) all other intensities - produces binary image

- The second approach is based on transformation brightens the desired range of intensity but leaves all other intensity level in image unchanged.





### (iii) bit-plane slicing:

pixel values are integers composed of bits eg: Values in a 256 level gray scale image are composed of 8 bits (one byte).

- An 8-bit image may be considered as being composed of eight one-bit planes. with 1 plane containing the lowest order bit of all pixel image & plane 8 all the highest order bits.



