



# VARDHAMAN COLLEGE OF ENGINEERING (AUTONOMOUS)

II B. Tech II Semester Regular Examinations, July – 2024

(Regulations: VCE-R22)

## DESIGN AND ANALYSIS OF ALGORITHMS

(Common to Computer Science and Engineering,  
Computer Science and Engineering (AIML), Information Technology &  
Artificial Intelligence and Machine Learning)

Date: 16 July, 2024 FN

Time: 3 hours

Max Marks: 60

### Answer All Questions

#### PART – A

- |    |    |   |     |    |           |
|----|----|---|-----|----|-----------|
| 1. | a) | Distinguish the best-case, average-case, and worst-case efficiency of an algorithm. | CO1 | L2 | <b>1M</b> |
|    | b) | Write down the control abstraction for the divide and conquer strategy.             | CO1 | L2 | <b>1M</b> |
|    | c) | Mention the Properties of Greedy method.  | CO2 | L1 | <b>1M</b> |
|    | d) | Time Complexity of job sequencing with deadlines.                                   | CO2 | L1 | <b>1M</b> |
|    | e) | List the difference between an optimal solution and a feasible solution.            | CO3 | L1 | <b>1M</b> |
|    | f) | What is the knapsack problem?   | CO3 | L1 | <b>1M</b> |
|    | g) | Define State Space Tree.  | CO4 | L1 | <b>1M</b> |
|    | h) | Define E node and live node.  | CO4 | L1 | <b>1M</b> |
|    | i) | When can a path be terminated in a branch and bound algorithm?                      | CO5 | L2 | <b>1M</b> |
|    | j) | Define P and NP problems.   | CO5 | L1 | <b>1M</b> |

#### PART – B

- |             |    |   |     |    |           |
|-------------|----|---|-----|----|-----------|
| 2.          | a) | Illustrate briefly on Big oh Notation, Omega Notation and Theta Notations. Depict the same graphically and explain.   | CO1 | L3 | <b>5M</b> |
|             | b) | Write the algorithm for merge sort and Trace 76, 23, 45, 13, 98, 52, 84 and 18.   | CO1 | L2 | <b>5M</b> |
| <b>(OR)</b> |    |   |     |    |           |
|             | c) | Apply Strassen's algorithm for matrix multiplication to multiply the matrices with an example and justify how the Strassen's algorithm is better.   | CO1 | L3 | <b>5M</b> |
|             | d) | Apply quick sort technique and arrange the records with the following index values in the ascending order. 2, 3, 8, 5, 4, 7, 6, 9, 1. Explain with algorithm and analyze time complexity. | CO1 | L3 | <b>5M</b> |
| 3.          | a) | Write the Dijkstra's Algorithm.   | CO2 | L3 | <b>5M</b> |
|             | b) | Apply prims algorithm to find Minimum spanning Tree.  | CO2 | L3 | <b>5M</b> |

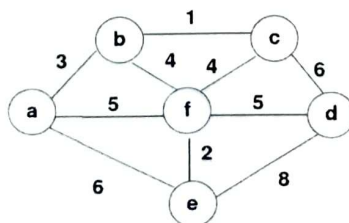


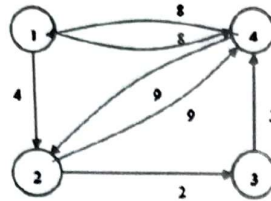
Fig.1

**(OR)**

- |    |  |     |    |           |
|----|--|-----|----|-----------|
| c) | Solve the following instance of Knapsack problem by Greedy Method. | CO2 | L3 | <b>5M</b> |
|    | W=15, n=6.   |     |    |           |
|    | (p1, p2, p3, p4, p5, p6) = (40, 35, 18, 4, 10, 2)                  |     |    |           |
|    | (w1, w2, w3, w4, w5, w6) = (5, 7, 2, 4, 5, 1)                      |     |    |           |
| d) | Write the Kruskal's algorithm for finding minimum Spanning tree.   | CO2 | L3 | <b>5M</b> |

4. a) Solve the All Pair shortest Path problem for the following graph.

CO3 L3 5M



**Fig.2**

- b) Plan the following instance of the 0/1 knapsack problem given the knapsack capacity in  $W=5$  using dynamic programming and explain it.

CO3 L4 5M

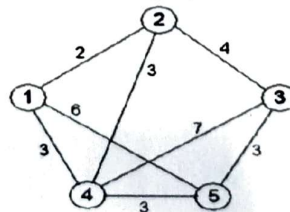
Item	Weight	Profit
1	1	5
2	2	4
3	4	8
4	5	6

(OR)

- c) Describe the Travelling salesman problem and discuss how to solve it using dynamic Programming. CO3 L3 5M
- d) Use function OBST to compute  $w(i, j)$ ,  $r(i, j)$ , and  $c(i, j)$ ,  $0 \leq i < j \leq 4$ , for the identifier set  $(a_1, a_2, a_3, a_4) = (\text{cout}, \text{float}, \text{if}, \text{while})$  with  $p(1) = 1/20$ ,  $p(2) = 1/5$ ,  $p(3) = 1/10$ ,  $p(4) = 1/20$ ,  $q(0) = 1/5$ ,  $q(1) = 1/10$ ,  $q(2) = 1/5$ ,  $q(3) = 1/20$ , and  $q(4) = 1/20$ . Using the  $r(i, j)$ 's, construct the optimal binary search tree. CO3 L3 5M
5. a) Construct the State space tree for 4 Queens Problem (Show at least one solution). CO4 L2 5M
- b) Find the solution for subset sum problem and represent the solution via state space tree Where  $n = 4$ ,  $w = \{3, 4, 5, 6\}$ ,  $d = 9$ . CO4 L3 5M

(OR)

- c) Write generic template backtracking algorithm. CO4 L3 5M
- d) Discuss Graph coloring problem. Draw the state space tree for 'm' coloring when  $n=3$  and  $m=3$ . CO4 L3 5M
6. a) Apply the Least Cost Branch and Bound (LCBB) algorithm to solve the travelling salesman problem for the graph below. CO5 L3 10M



**Fig.3**

(OR)

- c) Write the non-deterministic sorting algorithm and also analyze its complexity? CO5 L2 5M
- d) Define the following with an example: CO5 L2 5M
- Class P
  - Class NP
  - NP-Complete
  - NP-Hard