

Activation Functions:

1. Sigmoid function

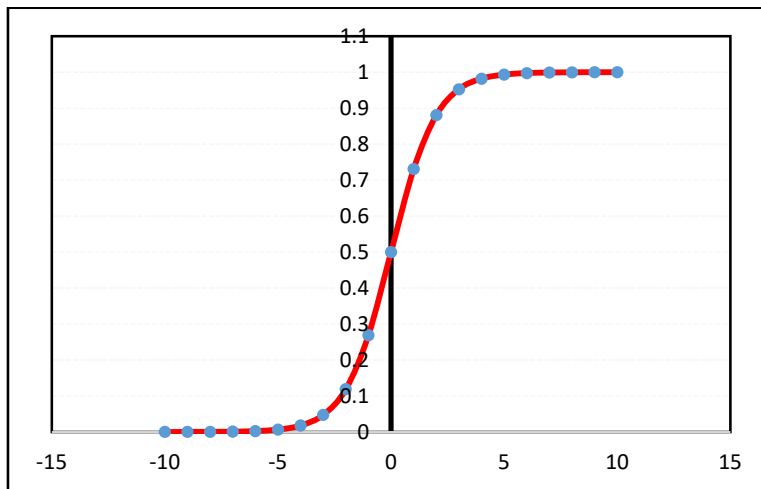
$$\sigma = \frac{1}{1 + e^{-x}}$$

$\sigma$  ranges from (0, 1).

When the input is negative, is close to 0.

When is positive, is close to 1.

At  $x = 0$ ,  $\sigma = 0.5$

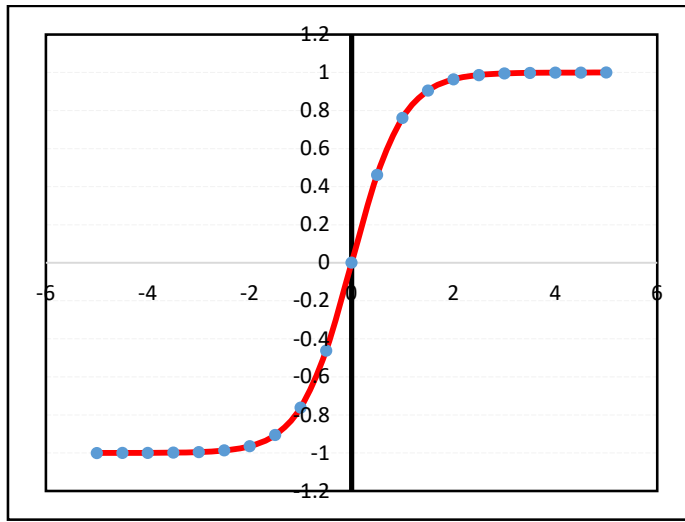


2.      tanh function

$$\tanh(x) = \frac{(e^x - e^{-x})}{(e^x + e^{-x})}$$

tanh(x) ranges from (-1, 1).

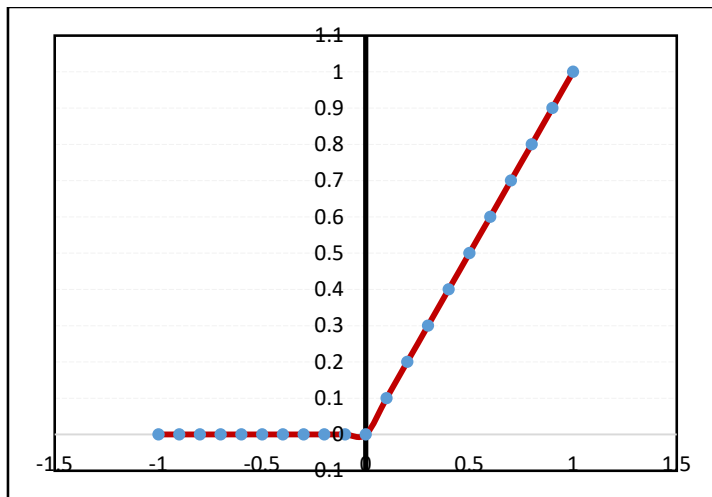
At x = 0, tanh(x) = 0



3. ReLU function

$$f(x) = \max(0, x)$$

$$f(x) = \begin{cases} 0 & \text{if } x \leq 0 \\ x & \text{if } x > 0 \end{cases}$$

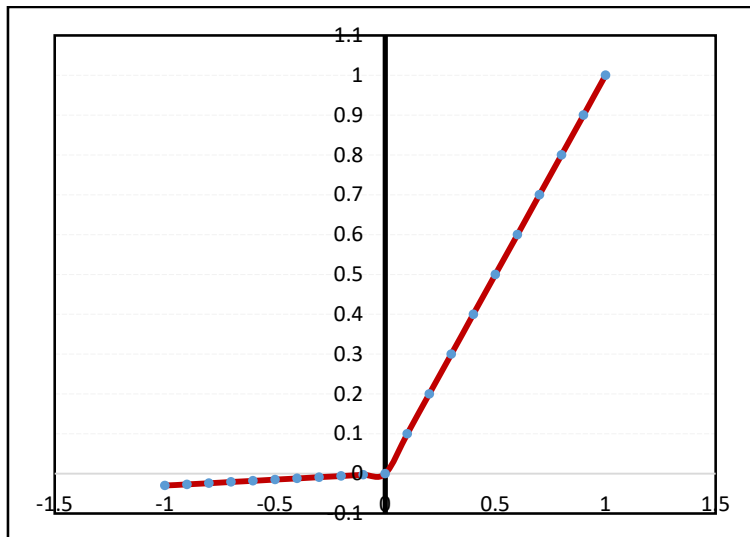


#### 4. Leaky ReLU

$$f(x) = \max(\alpha x, x)$$

$$f(x) = \begin{cases} \alpha x & \text{if } x \leq 0 \\ x & \text{if } x > 0 \end{cases}$$

A represent the very small constant, for an example, 0.03



## 5. SoftMax

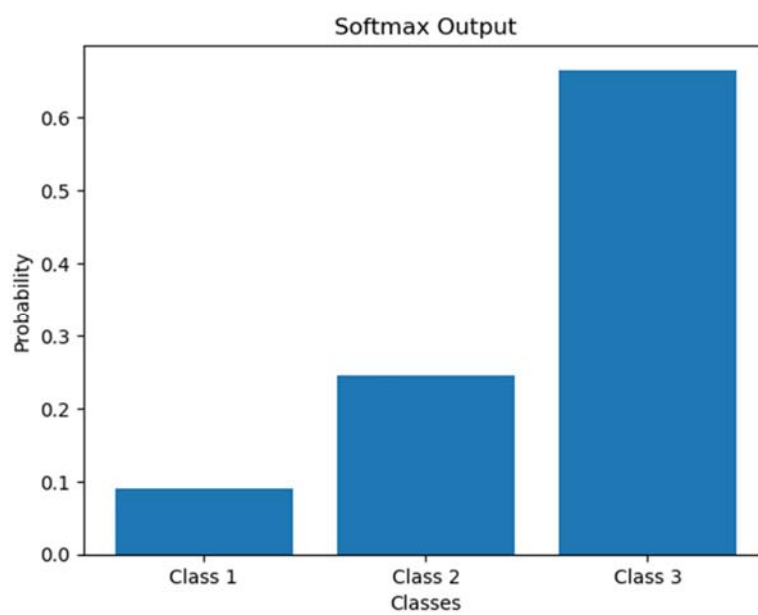
$$\sigma(x)_i = \frac{e^{x_i}}{\sum_{n=1}^n e^{x_n}}$$

$x = [1.0, 2.0, 3.0]$

$\exp(x) = [2.718, 7.389, 20.086]$

$\text{sum}(\exp(x)) = 30.193$

$\sigma(x) = [0.090, 0.245, 0.665]$



6. Exponential Linear Unit (ELU)

$$\alpha > 0$$

$$f(x) = \begin{cases} x & \text{if } x > 0 \\ \alpha (e^x - 1) & \text{if } x \leq 0 \end{cases}$$

