

# CSE-361: Compiler Design

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# Parsing : Part-II

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# PREDICTIVE PARSING

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- The goal is to construct a top-down parser that never backtracks
- Always leftmost derivations
- We must transform a grammar in two ways:
  - eliminate left recursion
  - perform left factoring
- These rules eliminate most common causes for backtracking although they do not guarantee a completely backtrack-free parsing

# LEFT RECURSION: INFINITE LOOPING PROBLEM

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- ❑ A grammar is left-recursive if it has a non-terminal A, such that there is a derivation :

$$A \xRightarrow{+} A\alpha, \text{ for some string } \alpha.$$

- ❑ Top-Down parsing can't reconcile this type of grammar, **since it could consistently make choice which wouldn't allow termination.**

$$A \Rightarrow A\alpha \Rightarrow A\alpha\alpha \Rightarrow A\alpha\alpha\alpha \dots \text{ etc. } A \rightarrow A\alpha \mid \beta$$

- ❑ So we have to convert our left-recursive grammar into an equivalent grammar which is not left-recursive.
- ❑ The left-recursion may appear in a single step of the derivation (*immediate left-recursion*), or may appear in more than one step of the derivation.

# IMMEDIATE LEFT RECURSION

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➤  $A \rightarrow A \alpha \mid \beta$       where  $\beta$  does not start with  $A$

$\Downarrow$       eliminate immediate left recursion

$A \rightarrow \beta A'$       where  $A'$  is a new nonterminal

$A' \rightarrow \alpha A' \mid \varepsilon$       an equivalent grammar

More General (but still immediate):

$A \rightarrow A\alpha_1 \mid A\alpha_2 \mid A\alpha_3 \mid \dots \mid \beta_1 \mid \beta_2 \mid \beta_3 \mid \dots$

Transform into:

$A \rightarrow \beta_1 A' \mid \beta_2 A' \mid \beta_3 A' \mid \dots$

$A' \rightarrow \alpha_1 A' \mid \alpha_2 A' \mid \alpha_3 A' \mid \dots \mid \varepsilon$

# IMMEDIATE LEFT RECURSION ELIMINATION: EXAMPLE

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**Our Example :**

$$\begin{array}{lcl} E \rightarrow E + T \mid T & \longrightarrow & \left\{ \begin{array}{l} E \rightarrow TE' \\ E' \rightarrow + TE' \mid \epsilon \end{array} \right. \\ T \rightarrow T * F \mid F & \longrightarrow & \left\{ \begin{array}{l} T \rightarrow FT' \\ T' \rightarrow * FT' \mid \epsilon \end{array} \right. \\ F \rightarrow ( E ) \mid \text{id} & \longrightarrow & F \rightarrow ( E ) \mid \text{id} \end{array}$$

# LEFT RECURSION IN MORE THAN ONE STEP

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- A grammar cannot be immediately left-recursive, but it still can be left-recursive.
- By just eliminating the immediate left-recursion, we may not get a grammar which is not left-recursive.

*Example:*

$S \rightarrow A\underline{f} \mid \underline{b}$

$A \rightarrow A\underline{c} \mid S\underline{d} \mid \underline{e}$

Is  $A$  left recursive? Yes.

Is  $S$  left recursive? Yes, but not immediate left recursion.  $S \Rightarrow A\underline{f} \Rightarrow S\underline{d}f$

# LEFT RECURSION IN MORE THAN ONE STEP: ELIMINATION

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## Approach:

Look at the rules for  $S$  only (ignoring other rules)... No left recursion.

Look at the rules for  $A$ ...

Do any of  $A$ 's rules start with  $S$ ? Yes.

$$A \rightarrow Sd$$

Get rid of the  $S$ . Substitute in the righthand sides of  $S$ .

$$A \rightarrow Af\bar{d} \mid \bar{b}d$$

The modified grammar:

$$S \rightarrow Af \mid \bar{b}$$

$$A \rightarrow A\bar{c} \mid Af\bar{d} \mid \bar{b}d \mid \bar{e}$$

Now eliminate immediate left recursion involving  $A$ .

$$S \rightarrow Af \mid \bar{b}$$

$$A \rightarrow \bar{b}dA' \mid \bar{e}A'$$

$$A' \rightarrow \bar{c}A' \mid f\bar{d}A' \mid \epsilon$$

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# LEFT RECURSION IN MORE THAN ONE STEP: ELIMINATION

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*The Original Grammar:*

$S \rightarrow A\underline{f} \mid \underline{b}$

$A \rightarrow A\underline{c} \mid S\underline{d} \mid B\underline{e}$

$B \rightarrow A\underline{g} \mid S\underline{h} \mid \underline{k}$

*So Far:*

$S \rightarrow A\underline{f} \mid \underline{b}$

$A \rightarrow \underline{b}dA' \mid B\underline{e}A'$

$A' \rightarrow \underline{c}A' \mid \underline{f}dA' \mid \epsilon$

# LEFT RECURSION IN MORE THAN ONE STEP: ELIMINATION

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## The Original Grammar:

$S \rightarrow A\underline{f} \mid \underline{b}$

$A \rightarrow A\underline{c} \mid S\underline{d} \mid B\underline{e}$

$B \rightarrow A\underline{g} \mid S\underline{h} \mid \underline{k}$

## So Far:

$S \rightarrow A\underline{f} \mid \underline{b}$

$A \rightarrow \underline{b}dA' \mid B\underline{e}A'$

$A' \rightarrow \underline{c}A' \mid \underline{f}dA' \mid \epsilon$

$B \rightarrow A\underline{g} \mid S\underline{h} \mid \underline{k}$

Look at the B rules next;  
Does any righthand side  
start with "S"?

# LEFT RECURSION IN MORE THAN ONE STEP: ELIMINATION

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*The Original Grammar:*

$S \rightarrow A\underline{f} \mid \underline{b}$

$A \rightarrow A\underline{c} \mid S\underline{d} \mid B\underline{e}$

$B \rightarrow A\underline{g} \mid S\underline{h} \mid \underline{k}$

*So Far:*

$S \rightarrow A\underline{f} \mid \underline{b}$

$A \rightarrow \underline{b}dA' \mid B\underline{e}A'$

$A' \rightarrow \underline{c}A' \mid \underline{f}dA' \mid \epsilon$

$B \rightarrow A\underline{g} \mid A\underline{f}h \mid \underline{b}h \mid \underline{k}$

Substitute, using the rules for “S”

$A\underline{f}\dots \mid \underline{b}\dots$

# LEFT RECURSION IN MORE THAN ONE STEP: ELIMINATION

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*The Original Grammar:*

$S \rightarrow A\underline{f} \mid \underline{b}$

$A \rightarrow A\underline{c} \mid S\underline{d} \mid B\underline{e}$

$B \rightarrow A\underline{g} \mid S\underline{h} \mid \underline{k}$

*So Far:*

$S \rightarrow A\underline{f} \mid \underline{b}$

$A \rightarrow \underline{b}dA' \mid B\underline{e}A'$

$A' \rightarrow \underline{c}A' \mid \underline{f}dA' \mid \epsilon$

$B \rightarrow A\underline{g} \mid A\underline{f}h \mid \underline{b}h \mid \underline{k}$

Does any righthand side  
start with “A”?

# LEFT RECURSION IN MORE THAN ONE STEP: ELIMINATION

*The Original Grammar:*

$S \rightarrow A\underline{f} \mid \underline{b}$

$A \rightarrow A\underline{c} \mid S\underline{d} \mid B\underline{e}$

$B \rightarrow A\underline{g} \mid S\underline{h} \mid \underline{k}$

*So Far:*

$S \rightarrow A\underline{f} \mid \underline{b}$

$A \rightarrow \underline{b}dA' \mid B\underline{e}A'$

$A' \rightarrow \underline{c}A' \mid \underline{f}dA' \mid \epsilon$

$B \rightarrow \underline{b}dA'g \mid B\underline{e}A'g \mid A\underline{f}h \mid \underline{b}h \mid \underline{k}$



Substitute, using the rules for “A”

$\underline{b}dA' \dots \mid B\underline{e}A' \dots$

# LEFT RECURSION IN MORE THAN ONE STEP: ELIMINATION

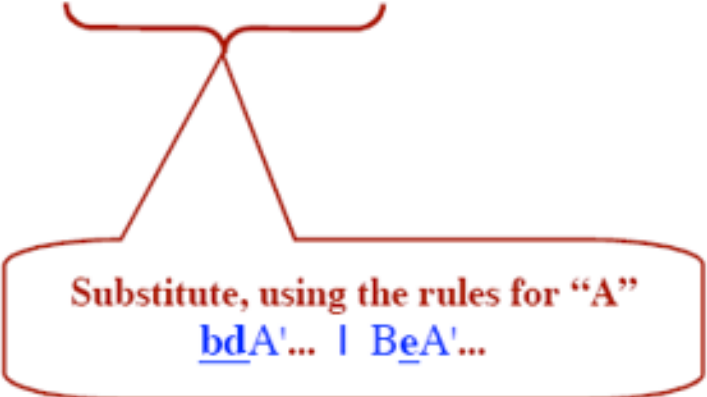
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*The Original Grammar:*

$S \rightarrow A\underline{f} \mid \underline{b}$   
 $A \rightarrow A\underline{c} \mid S\underline{d} \mid B\underline{e}$   
 $B \rightarrow A\underline{g} \mid S\underline{h} \mid \underline{k}$

*So Far:*

$S \rightarrow A\underline{f} \mid \underline{b}$   
 $A \rightarrow \underline{b}dA' \mid B\underline{e}A'$   
 $A' \rightarrow \underline{c}A' \mid \underline{f}dA' \mid \epsilon$   
 $B \rightarrow \underline{b}dA'g \mid B\underline{e}A'g \mid \underline{b}dA'fh \mid B\underline{e}A'fh \mid \underline{b}h \mid \underline{k}$



Substitute, using the rules for “A”  
 $\underline{b}dA' \dots \mid B\underline{e}A' \dots$

# LEFT RECURSION IN MORE THAN ONE STEP: ELIMINATION

## The Original Grammar:

$S \rightarrow A\underline{f} \mid \underline{b}$   
 $A \rightarrow A\underline{c} \mid S\underline{d} \mid B\underline{e}$   
 $B \rightarrow A\underline{g} \mid S\underline{h} \mid \underline{k}$

## So Far:

$S \rightarrow A\underline{f} \mid \underline{b}$   
 $A \rightarrow \underline{b}dA' \mid B\underline{e}A'$   
 $A' \rightarrow \underline{c}A' \mid \underline{f}dA' \mid \epsilon$   
 $B \rightarrow \underline{b}dA'g \mid B\underline{e}A'g \mid \underline{b}dA'fh \mid B\underline{e}A'fh \mid \underline{b}h \mid \underline{k}$

Finally, eliminate any immediate  
Left recursion involving "B"

## Next Form

$S \rightarrow A\underline{f} \mid \underline{b}$   
 $A \rightarrow \underline{b}dA' \mid B\underline{e}A'$   
 $A' \rightarrow \underline{c}A' \mid \underline{f}dA' \mid \epsilon$   
 $B \rightarrow \underline{b}dA'gB' \mid \underline{b}dA'fhB' \mid \underline{b}hB' \mid \underline{k}B'$   
 $B' \rightarrow \underline{e}A'gB' \mid \underline{e}A'fhB' \mid \epsilon$

# LEFT RECURSION IN MORE THAN ONE STEP: ELIMINATION

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*The Original Grammar:*

$S \rightarrow A\underline{f} \mid \underline{b}$

$A \rightarrow A\underline{c} \mid S\underline{d} \mid B\underline{e} \mid C$

$B \rightarrow A\underline{g} \mid S\underline{h} \mid \underline{k}$

$C \rightarrow B\underline{k}mA \mid AS \mid \underline{j}$

If there is another nonterminal,  
then do it next.

*So Far:*

$S \rightarrow A\underline{f} \mid \underline{b}$

$A \rightarrow \underline{b}dA' \mid B\underline{e}A' \mid CA'$

$A' \rightarrow \underline{c}A' \mid \underline{f}dA' \mid \epsilon$

$B \rightarrow \underline{b}dA'\underline{g}B' \mid \underline{b}dA'\underline{f}hB' \mid \underline{b}hB' \mid \underline{k}B' \mid CA'\underline{g}B' \mid CA'\underline{f}hB'$

$B' \rightarrow \underline{e}A'\underline{g}B' \mid \underline{e}A'\underline{f}hB' \mid \epsilon$



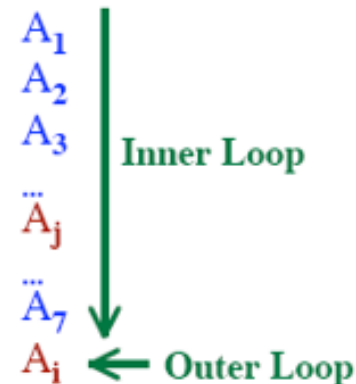
# ALGORITHM FOR ELIMINATING LEFT RECURSION

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Assume the nonterminals are ordered  $A_1, A_2, A_3, \dots$

(In the example: S, A, B)

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for each nonterminal  $A_i$  (for  $i = 1$  to  $N$ ) do  
  for each nonterminal  $A_j$  (for  $j = 1$  to  $i-1$ ) do  
    Let  $A_j \rightarrow \beta_1 \mid \beta_2 \mid \beta_3 \mid \dots \mid \beta_N$  be all the rules for  $A_j$   
    if there is a rule of the form  
       $A_i \rightarrow A_j \alpha$   
    then replace it by  
       $A_i \rightarrow \beta_1 \alpha \mid \beta_2 \alpha \mid \beta_3 \alpha \mid \dots \mid \beta_N \alpha$   
    endIf  
  endFor  
  Eliminate immediate left recursion  
    among the  $A_i$  rules  
endFor
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# Left Factoring: Common Prefix Problem

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**Problem :** Uncertain which of 2 rules to choose:

$stmt \rightarrow \text{if } expr \text{ then } stmt \text{ else } stmt$   
 $\quad | \text{if } expr \text{ then } stmt$

**When do you know which one is valid ?**

**What's the general form of  $stmt$  ?**

$A \rightarrow \alpha\beta_1 \mid \alpha\beta_2$                        $\alpha : \text{if } expr \text{ then } stmt$   
 $\beta_1 : \text{else } stmt \quad \beta_2 : \in$

**Transform to:**

$A \rightarrow \alpha A'$

$A' \rightarrow \beta_1 \mid \beta_2$

**EXAMPLE:**

$stmt \rightarrow \text{if } expr \text{ then } stmt \text{ rest}$

$rest \rightarrow \text{else } stmt \mid \in$

# Left Factoring : Example

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$A \rightarrow \underline{ab}B \mid \underline{a}B \mid \underline{cd}g \mid \underline{cde}B \mid \underline{cdf}B$

$\Downarrow$

$A \rightarrow \underline{a}A' \mid \underline{cd}g \mid \underline{cde}B \mid \underline{cdf}B$

$A' \rightarrow \underline{b}B \mid B$

$\Downarrow$

$A \rightarrow \underline{a}A' \mid \underline{cd}A''$

$A' \rightarrow \underline{b}B \mid B$

$A'' \rightarrow g \mid \underline{e}B \mid \underline{f}B$

# Left Factoring : Example

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$$A \rightarrow ad \mid a \mid ab \mid abc \mid b$$
$$\Downarrow$$
$$A \rightarrow aA' \mid b$$
$$A' \rightarrow d \mid \varepsilon \mid b \mid bc$$
$$\Downarrow$$
$$A \rightarrow aA' \mid b$$
$$A' \rightarrow d \mid \varepsilon \mid bA''$$
$$A'' \rightarrow \varepsilon \mid c$$

# Reading Materials

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- Chapter -4 of your Text book:
  - Compilers: Principles, Techniques, and Tools

THE END

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