Statistical Methods

Lecture 2 – Describing Data-Sets

Luke Dickens

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Frequency tables and graphs

Grouped data and histograms

List Comprehensions



List comprehensions are a simple, compact way to construct, and convert between, lists. Let's see some on this week's notebook.

Frequency tables and graphs

Grouped data and histograms

Frequency counts



One of the most common form of statistical procedures is to count the frequency of occurrences.

- data can be numeric, but doesn't have to be
- can display as a collection of observations
- OR as a table of frequency counts
- OR as a plot
- OR ...



All forms can represent the same data. We sometimes want to transform data into representations that better show the patterns.

Some terms



- variable a characteristic that changes or varies over time and/or for different individuals/objects, e.g. body temperature
- experimental unit the individual or object on which a variable is measured.
- measurement (or data value) results when a variable is measured on an experimental unit
- population the set of all measurements of interest
- **sample** a subset of measurements selected from the population

Definitions as found in [MBB12]

Different representations



Representations from [Ros17, Chp. 2] of the sick day data.

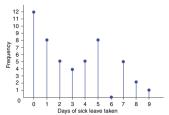
Table 2.1 A Frequency Table of Sick Leave Data

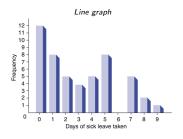
Value	Frequency	Value	Frequency		
0	12	5	8		
1	8	6	0		
2	5	7	5		
3	4	8	2		
4	5	9	1		

Frequency table

12
11
10
9
8
8
8
8
8
8
8
12
14
3
2
1
0
1
2
3
4
5
6
7
8
9
Days of sick leave taken

Frequency polygon





Bar graph



Key features of a plot might include:

- Zero counts
- Symmetry
- Outliers
- Any other patterns

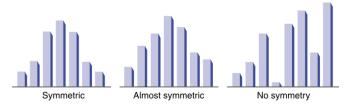


Image from [Ros17] showing types of symmetry.

Frequency tables and graphs

Grouped data and histograms

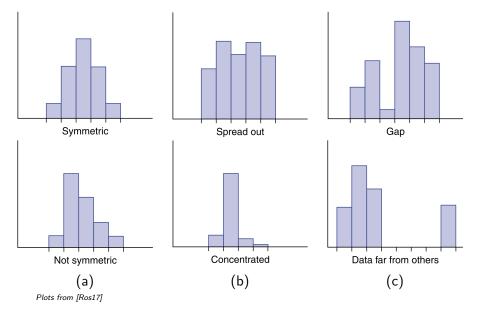
Histograms



- Data grouped by class intervals or bins
- Fewer bins: clearer patterns but hides information
- More bins: retains information but patterns may be lost
- Bins typically same size
- End points must belong to just one group, e.g. use left-end inclusion convention
- Relative frequencies also possible

Characteristics detected by histograms





Frequency tables and graphs

Grouped data and histograms

Stem and Leaf Plots



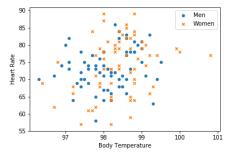
- Simplified view by grouping
- More information than histograms
- Order leaf entries for clarity
- Dual plots for comparison

Girls		Boys
5	14	
7, 5, 5, 5, 4	15	3, 8, 9
8, 4, 2, 1, 0	16	2, 5, 7, 7, 7, 8, 8, 9
9, 8, 7, 6, 6, 4, 2, 1, 1, 0, 0	17	0, 2, 3, 6, 6, 7, 7
5 7, 5, 5, 5, 4 8, 4, 2, 1, 0 9, 8, 7, 6, 6, 4, 2, 1, 1, 0, 0	18	0, 1, 4, 5

Stem and leaf plot of children's heights by gender sourced from here.

Sets of paired-data





Plot of body temperature vs heart-rate by gender.

Data from [Sho96]

- When values are paired, two measurements for single observational unit
- Look for relationships between measurements
- Can identify outliers more readily

References I



- [MBB12] William Mendenhall, Robert Beaver, and Barbara Beaver, *Introduction to Probability and Statistics*, 14th ed., Duxbury Press, 2012.
- [Ros17] Sheldon M. Ross, Introductory Statistics, 4 ed., Academic Press, 2017.
- [Sho96] Allen Shoemaker, What's Normal? Temperature, Gender and Heart Rate, J. Stat. Educ. 4 (1996), no. 2.