

SYDE 675 Pattern Recognition

Assignment 1

Due Feb 1 2017

(Labs are to be done individually. Do not write a formal report.)

Purpose

This lab investigates orthonormal transformations and statistical and distance-based classification.

Class Data

We will consider four cases. The first three are Gaussian, with the following given means and covariances:

1. $\mu_A = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$ $\Sigma_A = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ $\mu_B = \begin{bmatrix} 3 \\ 0 \end{bmatrix}$ $\Sigma_B = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$
2. $\mu_A = \begin{bmatrix} -1 \\ 0 \end{bmatrix}$ $\Sigma_A = \begin{bmatrix} 4 & 3 \\ 3 & 4 \end{bmatrix}$ $\mu_B = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$ $\Sigma_B = \begin{bmatrix} 4 & 3 \\ 3 & 4 \end{bmatrix}$
3. $\mu_A = \begin{bmatrix} 0 \\ 0 \end{bmatrix}$ $\Sigma_A = \begin{bmatrix} 3 & 1 \\ 1 & 2 \end{bmatrix}$ $\mu_B = \begin{bmatrix} 3 \\ 0 \end{bmatrix}$ $\Sigma_B = \begin{bmatrix} 7 & -3 \\ -3 & 4 \end{bmatrix}$
4. See LEARN for Matlab file `case4.mat`

In each case, each cluster has $N_A = N_B = 200$ data points. For MAP we assume the clusters to be equally likely.

Generating Clusters

Use the Matlab function **randn** to assist in the generation of the 2D clusters for cases 1-3. The **randn** function will produce normally (ie, Gaussian) distributed data with mean 0 and variance 1.0. To create the correlated data as required, you will need to **apply a transformation to the uncorrelated, equal-variance data.**

Distance Classifiers

We will be considering six classifiers:

1. Minimum Euclidean Distance (MED), with the sample mean as the prototype.
2. Minimum Generalized-Euclidean Distance (GED, also called MICD in the 372 notes), using *sample* means and covariances.
3. Nonparametric classifier NN using a Euclidean distance.
4. Nonparametric classifier 3-NN using a Euclidean distance.
5. Nonparametric classifier 5-NN using a Euclidean distance.
6. Although not distance-based, we will also show the MAP classifier as a reference, for the first three cases, using exact means and covariances.

For *each* of the four cases plot the class samples, the MED and GED classification boundaries, and for cases 1-3 the unit standard deviation contours and MAP classification boundary, all superimposed on the same plot. (ie, four plots; one per case)

Also produce three plots, one for NN, one for 3-NN, and one for the 5-NN classifier, for case 3. On each plot superimpose the optimal (MAP) classification boundary.

Note that you should *not* try to find the boundaries analytically. Approach the problem numerically: grid the domain, classify each point, and then generate a contour plot (`help contour` in MATLAB).

Comment briefly on both sets of plots.