Projection of Tensors to Retrieve Reflected Edges from an Image

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Abstract. Capturing a photograph through semi reflecting surfaces such as glass window, the captured image contains combination of transmitted objects and reflected objects. Objects behind the glass are called transmitted objects and reflection of objects at other side of glass falls on the glass surface are called reflected objects. Separation of reflected objects and transmitted objects from an image is wide scoped area in computer vision research. By considering reflected object edges are less significant comparing to transmitted object edges. This paper reveals an approach to separate reflected objects of an image using projection tensors and image smoothing algorithms.

Keywords: Projection Tensor, Reflected objects, Transmitted objects

1. Introduction

A photograph of a scene has reflecting or semi reflecting surfaces produces reflections of surrounding objects which are not directly visible in a photo. In general, reflected objects are not clear visible. Humans can easily decompose information in reflection layer but it is a challenging task in computer vision. This paper addresses a method of reflection layer segmentation from an image. On the basis of literature review, the image I is a combination of background objects B and reflected objects R. Mathematically image can be modelled as,

$$I = B + R \tag{1}$$

2. Related Work

Number of attempts have been made to extract reflection from an image. Reflection separation techniques are broadly categorised into two types: Reflection removal using more than one image as inputs and reflection removal using only one image as input. In the first category, reflection part is decomposed from an image using set of input image sequence. Reflection removal using multiple inputs is further categorised into four subcategories: Usage of image sequences or video [2,4,5,8,9,11,12], usage of flash in camera [13], usage of polarisers [6,14,15,16,17], usage of focus in camera [21]. Even though these methods work well but have practical constraints to use everyone. Li and Brown [2] used differences between constant background object and varied reflected objects from different angle of views to bifurcate reflection and background, this method takes substantial amount of computation time. Han et al. [4] decomposed reflection layer by completion of low-ranked matrix in gradient domain. Szeliski et al. [8] used constrained least squares to separate reflections. Guo et al. [9] method is relied on correlation between transmission layers with multiple images. Simon et al.[11] exploits spatio-temporal coherence of reflection to separate reflections. In the second category, Levin et al. [20] proposed a method to separate reflections based on local feature of image. Levin and Weiss [1] provide user interactions to decompose the reflection. Fan et al. [10] separate reflection using deep learning. Shih et al. [24] used ghosting effect of reflection to separate reflections from background.

3. Proposed Method

On inspection images containing background object edges as well as reflected object edges from glass surface, in many cases reflected edges are less significant and background edges are more significant. Based on this criterion image I in Eq. (1) can be modelled as

$$I = B' + R' \tag{2}$$

where, B' is more significant background edges and R' is less significant reflected edges.

Here proposed a method to segment glass reflected edges from an input image, Fig.1 shows its flow diagram.

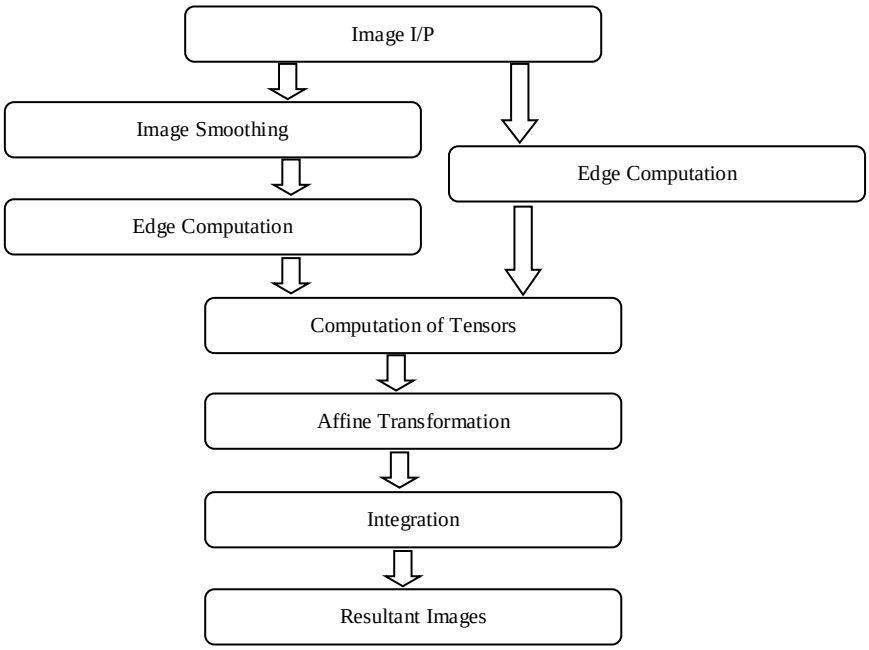


Fig. 1: Flow of the proposed approach

After reading an image as input *I*, convert it from RGB color space to YUV color space using Eq. (3).

$$\begin{aligned} Y &= 0.299R + 0.587G + 0.114B \\ U &= -0.147R - 0289G - 0.436B \\ V &= 0.615R - 0.515G - 0.100B \end{aligned} \tag{3}$$

To obtain *I'*, smooth an input image *I* or suppress less significant edges applied Gaussian filters Eq. (4) and convert the resultant image from RGB color space to YUV color space. Apply padding to both the images *I* and *I'* for integration operation purpose. Compute tensor matrix (Γ) using Eq. (5) for gradients ∇I , $\nabla I'$ of images *I* and *I'* respectively.

$$I' = \frac{1}{2\pi\sigma^2} e^{-\frac{x^2+y^2}{2\sigma^2}} \tag{4}$$

Where, σ is denoted as standard deviation.

$$\Gamma = (\nabla I \nabla I^T) * k_\sigma \tag{5}$$

Where, *k* is denoted as Gaussian kernel with σ variance.
Calculate the diffusion tensors *D* by using Eq. 6 proposed by Weickert [23]

$$D = \begin{bmatrix} D_{11} & D_{12} \\ D_{12} & D_{22} \end{bmatrix} = \begin{bmatrix} u_1 & u_2 \end{bmatrix} \begin{bmatrix} \mu_1 & 0 \\ 0 & \mu_2 \end{bmatrix} \begin{bmatrix} u_1^T \\ u_2^T \end{bmatrix} \tag{6}$$

Where, u_1, u_2 are eigen-vectors and μ_1 and μ_2 are eigen-values of tensor matrix Γ.
According to Aubert et al. [25], the tensor matrix Γ can be represented as:

$$\Gamma = \begin{bmatrix} X_1 & X_2 \end{bmatrix} \begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix} \begin{bmatrix} X_1^T \\ X_2^T \end{bmatrix} \tag{7}$$

Where, X_1 and X_2 are the eigen-vectors, λ_1 and λ_2 are corresponding eigen-values.
Compute projection tensor *D'* using Eq. 6 of tensor matrix Γ.

$$D' = \begin{bmatrix} X_1 & X_2 \end{bmatrix} \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} X_1^T \\ X_2^T \end{bmatrix} \tag{8}$$

Apply affine transformation to image gradient ∇I using *D'* of Eq.8 to remove local edges and integration operation to reconstruct the resultant images. Remove padding and convert resultant images from YUV to RGB color space. The resultant is decomposition of most significant edged

image (background) and less significant edged image (reflection). Fig. 2 shows complete algorithm of the proposed approach.

Step 1: Reading Input Image viz., *I*.
Step 2: Convert an image from RGB to YUV color space.
Step 3: Apply Gaussian filter to input image and obtain smoothed image viz., I_G.
Step 4: Convert smoothed image I_G from RGB to YUV color space.
Step 5: Apply padding to *I* and I_G.
Step 6: Calculate gradients of I_G.
Step 7: Calculate tensors T1= {t1,t2,..} for I_G.
Step 8: Find eigen values and eigen vectors for I_G.
Step 9: Calculate tensors T2= {t1,t2,...} for *I*.
Step 10: Find eigen values and eigen vectors for *I*.
Step 11: Calculate projection tensors *D*.
Step 12: Apply affine transformation using projection tensors *D* for each channel.
Step 13: Integration operation.
Step 14: Remove padding on resultant images.
Step 15: Convert resultant images from YUV to RGB color space.
Step 16: Post processing of resultant images.

Fig. 2: Algorithm of the proposed approach

4. Experimental Results

In this section, the experiments were conducted on system configured with Intel i7® PC (3.4GHz CPU, 8 GB RAM). Compared obtained results with Li and Brown [3], Levin and Weiss [1] methods which uses single image as input and Li and Brown [2] method which uses multiple images as input. The results shown in Fig. 3 and Fig. 4 are regenerated by using source codes from the authors' websites. In Levin and Weiss [1] approach provided user interactions to select edges belongs to background or reflection in an input image and it takes substantial amount of computational time to process the results and for users it is difficult to judge the edges belongs to background or foreground in complex input images.

For quantitative evaluations, structural similarity index (SSIM) Wang et al. [22] has been computed using Eq.9. SSIM is used as metric to evaluate similarity between two images by considering similarity in luminance, contrast and structure.

$$SSIM(x,y) = \frac{(2\mu_x\mu_y + c_1)(2\sigma_{xy} + c_2)}{(\mu_x^2 + \mu_y^2 + c_1)(\sigma_x^2 + \sigma_y^2 + c_2)} \tag{9}$$

Where μ_x and μ_y are means, σ_x and σ_y are standard deviations, $c_1 = (0.01\ MAX)^2$ and $c_2 = (0.03\ MAX)^2$.

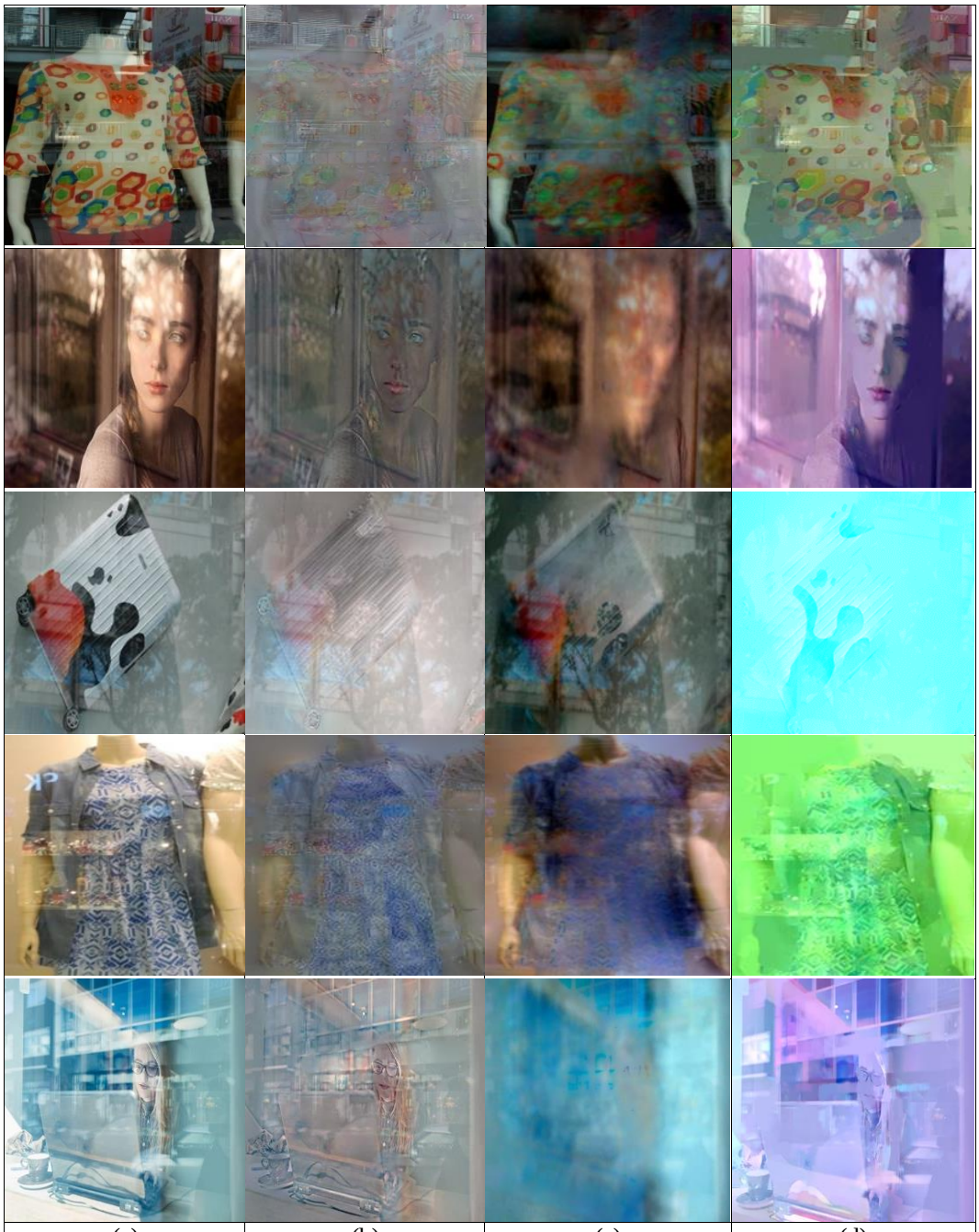
To assess quality of reconstructed image, peak signal to noise ratio (PSNR) has been computed using Eq. 10.

$$PSNR = 20\log\left(\frac{MAX}{\sqrt{MSE}}\right) \tag{10}$$

Where, *MAX* is denoted as dynamic range of the image.

Fig. 4 shows two example results of Li and Brown [2] which takes multiple images as inputs and the proposed method. We conducted experiment on all twelve case images of Li and Brown [2] provided in the authors website, with the proposed method and Li and Brown [2,3] and Table 1 shows comparison among them. SSIM, PSNR and Computational time are parameters. Due to non-availability of ground truth reflection images we considered the reflection result of Li and Brown [2] method as reference for computing PSNR and SSIM values. By analysing table 1, in terms of PSNR, SSIM and CPU time is evident for performance of the proposed approach.

Experimentation conducted with ground truth reflected images of SIR dataset Wan R et al. [21] and computed SSIM values are shows that proposed method has limitations to process synthetic images given in the dataset and this is treated as future scope of our research.



(a)	(b)	(c)	(d)

Fig. 3: Visual comparison of the proposed method with [3] and [1]. (a) Input image, (b) the proposed method, (c) Li and Brown [3] (d) Levin & Weiss [1]

(a) (b) (c)

Fig. 4: Visual comparison between the proposed method with [2]. (a) Input image, (b) the proposed method (c) Li & Brown [2].

Sl No.	SSIM of proposed method	SSIM of [3]	PSNR of proposed method	PSNR [3]	CPU time of proposed method	CPU time of [2]
Case 1	0.3821	0.5177	27.05db	24.74db	20.48 sec	119.62 sec
Case 2	0.4395	0.2498	26.27db	24.09db	15.10 sec	91.19 sec
Case 3	0.3933	0.4048	25.79db	24.09db	16.70 sec	52.87 sec
Case 4	0.5161	0.4228	34.48db	24.13db	17.11 sec	108.98 sec
Case 5	0.4491	0.3333	40.00db	24.09db	18.04 sec	119.08 sec
Case 6	0.5074	0.3207	30.09db	24.09db	8.03 sec	28.97 sec
Case 7	0.4740	0.3458	49.81db	24.09db	16.44 sec	104.70 sec
Case 8	0.3869	0.5010	43.04db	24.09db	13.88 sec	61.97 sec
Case 9	0.6679	0.5278	24.82db	24.37db	15.80 sec	97.97 sec
Case 10	0.5709	0.5111	25.94db	24.09db	16.45 sec	79.94 sec
Case 11	0.4174	0.3371	29.89db	24.09db	17.44 sec	112.61 sec
Case 12	0.6347	0.5902	27.93db	24.10db	15.56 sec	75.25 sec

Table 1: Comparison table of the proposed method with Li & Brown [2 and 3] with respect to SSIM, PSNR and CPU time.

5. Conclusion

This work presents a novel approach to extract reflection edges from an image contained both background and reflection has been developed. Proposed new image model that image is a combination of most significant background edges and less significant reflected edges. Exploited tensor matrices for input image and resultant smoothed image after Gaussian filter, computed projection tensor then applied affine transformation to extract less significant reflected edged image. Compared the proposed approach with standard existed reflection separation techniques and it shows fair performance of our method. Future scope of this work is to segment reflection edges from synthetic images.

Acknowledgement

Kuvempu university has been extended the financial support to carry out this work.

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