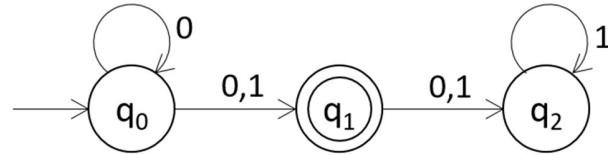


1. Convert the following NFA into its equivalent DFA.



Subset Construction Method:

- Step 1: q_0 is the start/initial state of the required DFA.
- Step 2: NFA has 3 states. Therefore, DFA has $8 (= 2^3)$ states, namely $[q_0]$, $[q_1]$, $[q_2]$, $[q_0q_1]$, $[q_1q_2]$, $[q_0q_2]$, $[q_0q_1q_2]$, ϕ .
- Step 3: Evaluate δ_D using δ_N and determine the Transition function of the DFA as follows:

$$\delta_D(q_0, 0) = \delta_N(q_0, 0) = [q_0q_1]$$

$$\delta_D(q_0, 1) = \delta_N(q_0, 1) = [q_1]$$

$$\delta_D(q_1, 0) = \delta_N(q_1, 0) = [q_2]$$

$$\delta_D(q_1, 1) = \delta_N(q_1, 1) = [q_2]$$

$$\delta_D(q_2, 0) = \delta_N(q_2, 0) = \phi$$

$$\delta_D(q_2, 1) = \delta_N(q_2, 1) = [q_2]$$

$$\delta_D([q_0q_1], 0) = \delta_N(q_0, 0) \cup \delta_N(q_1, 0) =$$

$$\{q_0, q_1\} \cup \{q_2\} = [q_0q_1q_2]$$

$$\delta_D([q_0q_1], 1) = \delta_N(q_0, 1) \cup \delta_N(q_1, 1) =$$

$$\{q_1\} \cup \{q_2\} = [q_1q_2]$$

$$\delta_D([q_0q_2], 0) = \delta_N(q_0, 0) \cup \delta_N(q_2, 0) =$$

$$\{q_0, q_1\} \cup \phi = [q_0q_1]$$

$$\delta_D([q_0q_2], 1) = \delta_N(q_0, 1) \cup \delta_N(q_2, 1) =$$

$$\{q_1\} \cup \{q_2\} = [q_1q_2]$$

$$\delta_D([q_1q_2], 0) = \delta_N(q_1, 0) \cup \delta_N(q_2, 0) = \{q_2\} = [q_2]$$

$$\delta_D([q_1q_2], 1) = \delta_N(q_1, 1) \cup \delta_N(q_2, 1) = \{q_2\} = [q_2]$$

$$\delta_D([q_0q_1q_2], 0) = \delta_N(q_0, 0) \cup \delta_N(q_1, 0) \cup \delta_N(q_2, 0) = \{q_0, q_1\} \cup \{q_2\} \cup \phi = [q_0q_1q_2]$$

$$\delta_D([q_0q_1q_2], 1) = \delta_N(q_0, 1) \cup \delta_N(q_1, 1) \cup \delta_N(q_2, 1) = \{q_1\} \cup \{q_2\} \cup \{q_2\} = [q_1q_2]$$

$$\delta_D(\phi, 0) = \delta_N(\phi, 0) = \phi$$

$$\delta_D(\phi, 1) = \delta_N(\phi, 1) = \phi$$

δ	0	1
$\rightarrow[q_0]$	$[q_0q_1]$	$[q_1]$
$*[q_1]$	$[q_2]$	$[q_2]$
$[q_2]$	ϕ	$[q_2]$
$*[q_0q_1]$	$[q_0q_1q_2]$	$[q_1q_2]$
$[q_0q_2]$	$[q_0q_1]$	$[q_1q_2]$
$*[q_1q_2]$	$[q_2]$	$[q_2]$
$*[q_0q_1q_2]$	$[q_0q_1q_2]$	$[q_1q_2]$
ϕ	ϕ	ϕ

- Step 4: Now, change the names of the states $\{[q_0], [q_1], [q_2], [q_0q_1], [q_0q_2], [q_1q_2], [q_0q_1q_2], \phi\}$ as $\{A, B, C, D, E, F, G, H\}$.

Step 5: Draw the Transition Function for the newly named states.

δ	0	1
$\rightarrow A$	D	B
*B	C	C
C	H	C
*D	G	F
E	D	F
*F	C	C
*G	G	F
H	H	H

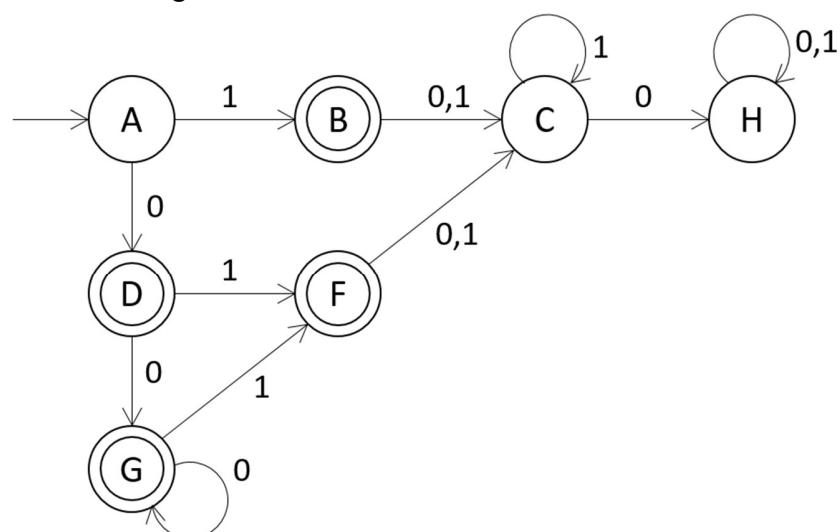
Step 6: Determine the states accessible from the start/initial state.

Here, the accessible states are: {A, D, B, G, F, C, H}.

Step 7: Draw the Transition Function for the accessible states only.

δ	0	1
$\rightarrow A$	D	B
*D	G	F
*B	C	C
*G	G	F
*F	C	C
C	H	C
H	H	H

Step 8: Draw the DFA using the Transition Function.



Step 9: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

$$Q = \{A, B, D, C, G, F, H\}$$

$$\Sigma = \{0, 1\}$$

A is the initial/start state

$$F = \{B, D, F, G\}$$

Lazy Evaluation Method:

Step 1: q_0 is start/initial state of the required DFA.

$$\delta_D([q_0q_1], 0) = \delta_N(q_0, 0) \cup \delta_N(q_1, 0) = \{q_0, q_1\} \cup \{q_2\} = [q_0q_1q_2]$$

$$\delta_D([q_0q_1], 1) = \delta_N(q_0, 1) \cup \delta_N(q_1, 1) = \{q_1\} \cup \{q_2\} = [q_1q_2]$$

$$\delta_D(q_1, 0) = \delta_N(q_1, 0) = [q_2]$$

$$\delta_D(q_1, 1) = \delta_N(q_1, 1) = [q_2]$$

$$\delta_D([q_0q_1q_2], 0) = \delta_N(q_0, 0) \cup \delta_N(q_1, 0) \cup \delta_N(q_2, 0) = \{q_0, q_1\} \cup \{q_2\} \cup \phi = [q_0q_1q_2]$$

$$\delta_D([q_0q_1q_2], 1) = \delta_N(q_0, 1) \cup \delta_N(q_1, 1) \cup \delta_N(q_2, 1) = \{q_1\} \cup \{q_2\} = [q_0q_1q_2]$$

$$\delta_D([q_1q_2], 0) = \delta_N(q_1, 0) \cup \delta_N(q_2, 0) = \{q_2\} = [q_2]$$

$$\delta_D([q_1q_2], 1) = \delta_N(q_1, 1) \cup \delta_N(q_2, 1) = \{q_2\} = [q_2]$$

$$\delta_D(q_2, 0) = \delta_N(q_2, 0) = \phi$$

$$\delta_D(q_2, 1) = \delta_N(q_2, 1) = [q_2]$$

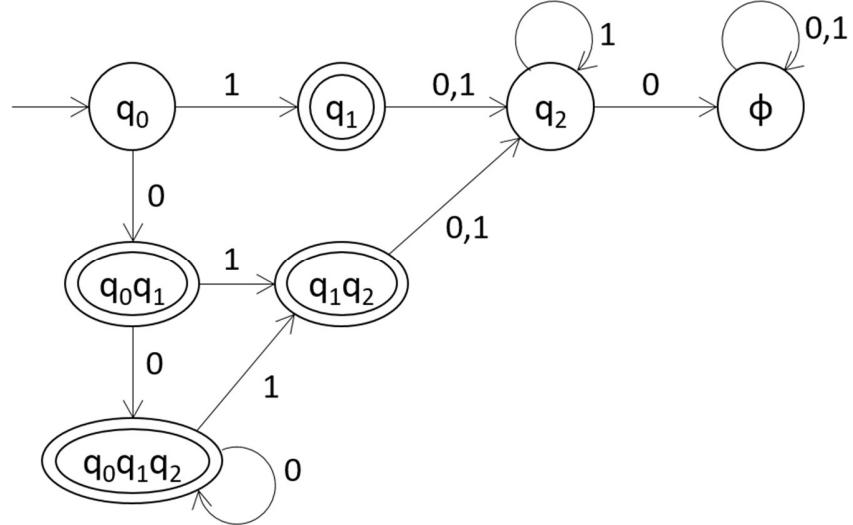
$$\delta_D(\phi, 0) = \delta_N(\phi, 0) = \phi$$

$$\delta_D(\phi, 1) = \delta_N(\phi, 1) = \phi$$

Step 3: Draw the Transition Function for the above determined states.

δ	0	1
$\rightarrow[q_0]$	$[q_0q_1]$	$[q_1]$
$*[q_0q_1]$	$[q_0q_1q_2]$	$[q_1q_2]$
$*[q_1]$	$[q_2]$	$[q_2]$
$*[q_0q_1q_2]$	$[q_0q_1q_2]$	$[q_1q_2]$
$*[q_1q_2]$	$[q_2]$	$[q_2]$
$[q_2]$	ϕ	$[q_2]$
ϕ	ϕ	ϕ

Step 4: Draw the DFA using the Transition Function.



Step 5: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

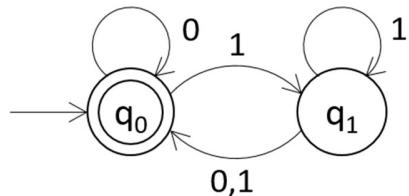
$$Q = \{[q_0], [q_1], [q_2], [q_0q_1], [q_1q_2], [q_0q_1q_2], \phi\}$$

$$\Sigma = \{0, 1\}$$

q_0 is the initial/start state

$$F = \{[q_1], [q_0q_1], [q_1q_2], [q_0q_1q_2]\}$$

2. Convert the following NFA into its equivalent DFA.



Subset Construction Method:

Step 1: q_0 is the start/initial state of the required DFA.

Step 2: NFA has 2 states. Therefore, DFA has $4 (= 2^2)$ states, namely $[q_0], [q_1], [q_0q_1], \phi$.

Step 3: Evaluate δ_D using δ_N and determine the Transition function of the DFA as follows:

$$\delta_D(q_0, 0) = \delta_N(q_0, 0) = [q_0]$$

$$\delta_D(q_0, 1) = \delta_N(q_0, 1) = [q_1]$$

$$\begin{aligned}
\delta_D(q_1, 0) &= \delta_N(q_1, 0) = [q_1] \\
\delta_D(q_1, 1) &= \delta_N(q_1, 1) = [q_1] \\
\delta_D([q_0q_1], 0) &= \delta_N(q_0, 0) \cup \delta_N(q_1, 0) = \\
&\{q_0\} \cup \{q_1\} = [q_0q_1] \\
\delta_D([q_0q_1], 1) &= \delta_N(q_0, 1) \cup \delta_N(q_1, 1) = \\
&\{q_1\} \cup \{q_0, q_1\} = [q_0q_1] \\
\delta_D(\phi, 0) &= \delta_N(\phi, 0) = \phi \\
\delta_D(\phi, 1) &= \delta_N(\phi, 1) = \phi
\end{aligned}$$

δ	0	1
$\rightarrow^*[q_0]$	$[q_0]$	$[q_1]$
$[q_1]$	$[q_1]$	$[q_0q_1]$
$*[q_0q_1]$	$[q_0q_1]$	$[q_0q_1]$
ϕ	ϕ	ϕ

Step 4: Now, change the names of the states $\{[q_0], [q_1], [q_0q_1], \phi\}$ as $\{A, B, C, D\}$.

Step 5: Draw the Transition Function for the newly named states.

δ	0	1
\rightarrow^*A	A	B
B	B	C
$*C$	C	C
D	D	D

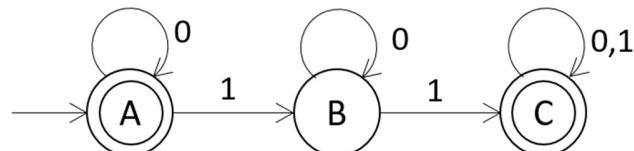
Step 6: Determine the states accessible from the start/initial state.

Here, the accessible states are: $\{A, B, C\}$.

Step 7: Draw the Transition Function for the accessible states only.

δ	0	1
\rightarrow^*A	A	B
B	B	C
$*C$	C	C

Step 8: Draw the DFA using the Transition Function.



Step 9: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

$$Q = \{A, B, C\}$$

$$\Sigma = \{0, 1\}$$

A is the initial/start state

$$F = \{A, C\}$$

Lazy Evaluation Method:

Step 1: q_0 is start/initial state of the required DFA.

$$\delta_D(q_0, 0) = \delta_N(q_0, 0) = [q_0]$$

$$\delta_D(q_0, 1) = \delta_N(q_0, 1) = [q_1]$$

Step 2: Using the states obtained from each transition, proceed with the calculation as follows:

$$\delta_D(q_1, 0) = \delta_N(q_1, 0) = [q_1]$$

$$\delta_D(q_1, 1) = \delta_N(q_1, 1) = [q_0q_1]$$

$$\delta_D([q_0q_1], 0) = \delta_N(q_0, 0) \cup \delta_N(q_1, 0) = \{q_0\} \cup \{q_1\} = [q_0q_1]$$

$$\delta_D([q_0q_1], 1) = \delta_N(q_0, 1) \cup \delta_N(q_1, 1) = \{q_1\} \cup \{q_0q_1\} = [q_0q_1]$$

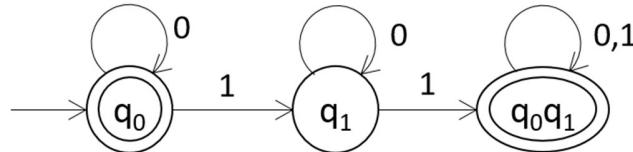
$$\delta_D(\phi, 0) = \delta_N(\phi, 0) = \phi$$

$$\delta_D(\phi, 1) = \delta_N(\phi, 1) = \phi$$

Step 3: Draw the Transition Function for the above determined states.

δ	0	1
$\rightarrow * [q_0]$	$[q_0]$	$[q_1]$
$[q_1]$	$[q_1]$	$[q_0q_1]$
$* [q_0q_1]$	$[q_0q_1]$	$[q_0q_1]$

Step 4: Draw the DFA using the Transition Function.



Step 5: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

$$Q = \{[q_0], [q_1], [q_0q_1]\}$$

$$\Sigma = \{0, 1\}$$

q_0 is the initial/start state

$$F = \{[q_0], [q_0q_1]\}$$

3. Convert the following NFA into its equivalent DFA.

δ	0	1
$\rightarrow q_0$	$\{q_0, q_1\}$	$\{q_2\}$
q_1	$\{q_0\}$	$\{q_1\}$
$* q_2$	ϕ	$\{q_0, q_1\}$

Subset Construction Method:

Step 1: q_0 is the start/initial state of the required DFA.

Step 2: NFA has 3 states. Therefore, DFA has $8 (= 2^3)$ states, namely $[q_0], [q_1], [q_2], [q_0q_1], [q_1q_2], [q_0q_2], [q_0q_1q_2], \phi$.

Step 3: Evaluate δ_D using δ_N and determine the Transition function of the DFA as follows:

$$\delta_D(q_0, 0) = \delta_N(q_0, 0) = [q_0q_1]$$

$$\delta_D(q_0, 1) = \delta_N(q_0, 1) = [q_2]$$

$$\delta_D(q_1, 0) = \delta_N(q_1, 0) = [q_0]$$

$$\delta_D(q_1, 1) = \delta_N(q_1, 1) = [q_1]$$

$$\delta_D(q_2, 0) = \delta_N(q_2, 0) = \phi$$

$$\delta_D(q_2, 1) = \delta_N(q_2, 1) = [q_0q_1]$$

$$\delta_D([q_0q_1], 0) = \delta_N(q_0, 0) \cup \delta_N(q_1, 0) =$$

$$\{q_1\} \cup \{q_0\} = [q_0q_1]$$

$$\delta_D([q_0q_1], 1) = \delta_N(q_0, 1) \cup \delta_N(q_1, 1) =$$

$$\{q_2\} \cup \{q_1\} = [q_1q_2]$$

$$\delta_D([q_0q_2], 0) = \delta_N(q_0, 0) \cup \delta_N(q_2, 0) =$$

$$\{q_0q_1\} \cup \phi = [q_0q_1]$$

$$\delta_D([q_0q_2], 1) = \delta_N(q_0, 1) \cup \delta_N(q_2, 1) = \{q_2\} \cup \{q_0q_1\} = [q_0q_1q_2]$$

$$\delta_D([q_1q_2], 0) = \delta_N(q_1, 0) \cup \delta_N(q_2, 0) = \{q_0\} \cup \phi = [q_0]$$

$$\delta_D([q_1q_2], 1) = \delta_N(q_1, 1) \cup \delta_N(q_2, 1) = \{q_1\} \cup \{q_0q_1\} = [q_0q_1]$$

$$\delta_D([q_0q_1q_2], 0) = \delta_N(q_0, 0) \cup \delta_N(q_1, 0) \cup \delta_N(q_2, 0) = \{q_0, q_1\} \cup \{q_0\} \cup \phi = [q_0q_1]$$

$$\delta_D([q_0q_1q_2], 1) = \delta_N(q_0, 1) \cup \delta_N(q_1, 1) \cup \delta_N(q_2, 1) = \{q_2\} \cup \{q_1\} \cup \{q_1q_0\} = [q_0q_1q_2]$$

$$\delta_D(\phi, 0) = \delta_N(\phi, 0) = \phi$$

$$\delta_D(\phi, 1) = \delta_N(\phi, 1) = \phi$$

Step 4: Now, change the names of the states $\{[q_0], [q_1], [q_2], [q_0q_1], [q_0q_2], [q_1q_2], [q_0q_1q_2], \phi\}$ as $\{A, B, C, D, E, F, G, H\}$.

Step 5: Draw the Transition Function for the newly named states.

δ	0	1
$\rightarrow A$	D	C
B	A	B
*C	H	D
D	D	F
*E	D	G
*F	A	D
*G	D	G
H	H	H

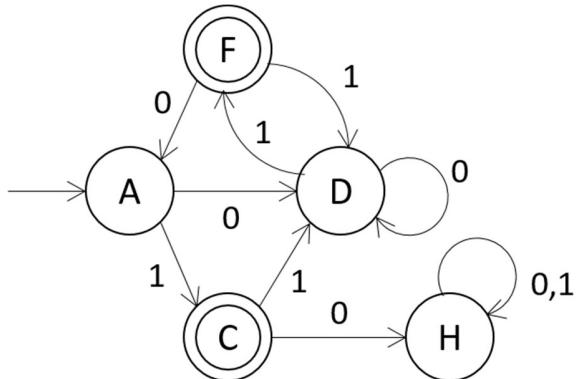
Step 6: Determine the states accessible from the start/initial state.

Here, the accessible states are: {A, D, C, H, F}.

Step 7: Draw the Transition Function for the accessible states only.

δ	0	1
$\rightarrow A$	D	C
D	D	F
*C	H	D
*F	A	D
H	H	H

Step 8: Draw the DFA using the Transition Function.



Step 9: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

$$Q = \{A, C, D, F, H\}$$

$$\Sigma = \{0, 1\}$$

A is the initial/start state

$$F = \{C, F\}$$

Lazy Evaluation Method:

Step 1: q_0 is start/initial state of the required DFA.

$$\delta_D(q_0, 0) = \delta_N(q_0, 0) = [q_0q_1]$$

$$\delta_D(q_0, 1) = \delta_N(q_0, 1) = [q_2]$$

Step 2: Using the states obtained from each transition, proceed with the calculation as follows:

$$\delta_D([q_0q_1], 0) = \delta_N(q_0, 0) \cup \delta_N(q_1, 0) = \{q_1\} \cup \{q_0\} = [q_0q_1]$$

$$\delta_D([q_0q_1], 1) = \delta_N(q_0, 1) \cup \delta_N(q_1, 1) = \{q_2\} \cup \{q_1\} = [q_1q_2]$$

$$\delta_D(q_2, 0) = \delta_N(q_2, 0) = \emptyset$$

$$\delta_D(q_2, 1) = \delta_N(q_2, 1) = [q_0q_1]$$

$$\delta_D([q_1q_2], 0) = \delta_N(q_1, 0) \cup \delta_N(q_2, 0) = \{q_0\} \cup \emptyset = [q_0]$$

$$\delta_D([q_1q_2], 1) = \delta_N(q_1, 1) \cup \delta_N(q_2, 1) = \{q_1\} \cup \{q_0q_1\} = [q_0q_1]$$

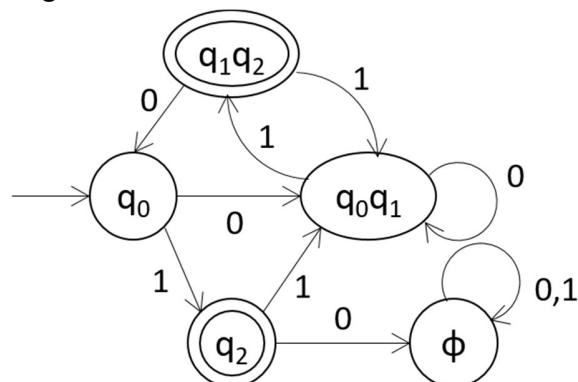
$$\delta_D(\phi, 0) = \delta_N(\phi, 0) = \phi$$

$$\delta_D(\phi, 1) = \delta_N(\phi, 1) = \phi$$

Step 3: Draw the Transition Function for the above determined states.

δ	0	1
$\rightarrow[q_0]$	$[q_0q_1]$	$[q_2]$
$[q_0q_1]$	$[q_0q_1]$	$[q_1q_2]$
$*[q_2]$	ϕ	$[q_0q_1]$
$*[q_1q_2]$	$[q_0]$	$[q_0q_1]$
ϕ	ϕ	ϕ

Step 4: Draw the DFA using the Transition Function.



Step 5: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

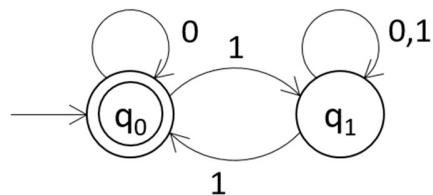
$$Q = \{[q_0], [q_2], [q_0q_1], [q_1q_2], \phi\}$$

$$\Sigma = \{0, 1\}$$

q_0 is the initial/start state

$$F = \{[q_2], [q_1q_2]\}$$

4. Convert the following NFA into its equivalent DFA.



Subset Construction Method:

Step 1: q_0 is the start/initial state of the required DFA.

Step 2: NFA has 2 states. Therefore, DFA has $4 (= 2^2)$ states, namely $[q_0]$, $[q_1]$, $[q_0q_1]$, ϕ .

Step 3: Evaluate δ_D using δ_N and determine the Transition function of the DFA as follows:

$$\delta_D(q_0, 0) = \delta_N(q_0, 0) = [q_0]$$

$$\delta_D(q_0, 1) = \delta_N(q_0, 1) = [q_1]$$

$$\delta_D(q_1, 0) = \delta_N(q_1, 0) = [q_1]$$

$$\delta_D(q_1, 1) = \delta_N(q_1, 1) = [q_0q_1]$$

$$\delta_D([q_0q_1], 0) = \delta_N(q_0, 0) \cup \delta_N(q_1, 0) =$$

$$\{q_0, q_1\} \cup \{q_2\} = [q_0q_1]$$

$$\delta_D([q_0q_1], 1) = \delta_N(q_0, 1) \cup \delta_N(q_1, 1) =$$

$$\{q_1\} \cup \{q_2\} = [q_0q_1]$$

$$\delta_D(\phi, 0) = \delta_N(\phi, 0) = \phi$$

$$\delta_D(\phi, 1) = \delta_N(\phi, 1) = \phi$$

δ	0	1
$\rightarrow^*[q_0]$	$[q_0]$	$[q_1]$
$[q_1]$	$[q_1]$	$[q_0q_1]$
$*[q_0q_1]$	$[q_0q_1]$	$[q_0q_1]$
ϕ	ϕ	ϕ

Step 4: Now, change the names of the states $\{[q_0], [q_1], [q_0q_1], \phi\}$ as $\{A, B, C, D\}$.

Step 5: Draw the Transition Function for the newly named states.

δ	0	1
\rightarrow^*A	A	B
B	B	C
$*C$	C	C
D	D	D

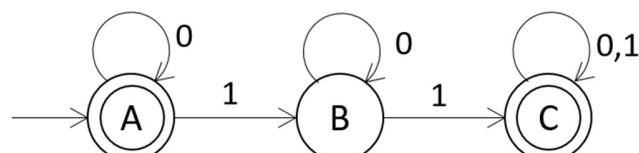
Step 6: Determine the states accessible from the start/initial state.

Here, the accessible states are: $\{A, B, C\}$.

Step 7: Draw the Transition Function for the accessible states only.

δ	0	1
\rightarrow^*A	A	B
B	B	C
$*C$	C	C

Step 8: Draw the DFA using the Transition Function.



Step 9: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

$$Q = \{A, B, C\}$$

$$\Sigma = \{0, 1\}$$

A is the initial/start state

$$F = \{A, C\}$$

Lazy Evaluation Method:

Step 1: q_0 is start/initial state of the required DFA.

$$\delta_D(q_0, 0) = \delta_N(q_0, 0) = [q_0]$$

$$\delta_D(q_0, 1) = \delta_N(q_0, 1) = [q_1]$$

Step 2: Using the states obtained from each transition, proceed with the calculation as follows:

$$\delta_D(q_1, 0) = \delta_N(q_1, 0) = [q_1]$$

$$\delta_D(q_1, 1) = \delta_N(q_1, 1) = [q_0q_1]$$

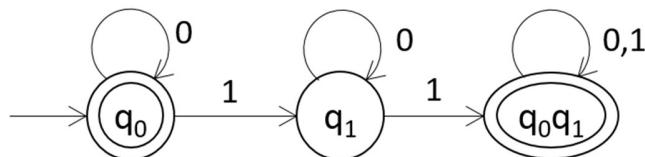
$$\delta_D([q_0q_1], 0) = \delta_N(q_0, 0) \cup \delta_N(q_1, 0) = \{q_0, q_1\} \cup \{q_2\} = [q_0q_1]$$

$$\delta_D([q_0q_1], 1) = \delta_N(q_0, 1) \cup \delta_N(q_1, 1) = \{q_1\} \cup \{q_2\} = [q_0q_1]$$

Step 3: Draw the Transition Function for the above determined states.

δ	0	1
$\rightarrow^*[q_0]$	$[q_0]$	$[q_1]$
$[q_1]$	$[q_1]$	$[q_0q_1]$
$*[q_0q_1]$	$[q_0q_1]$	$[q_0q_1]$

Step 4: Draw the DFA using the Transition Function.



Step 5: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

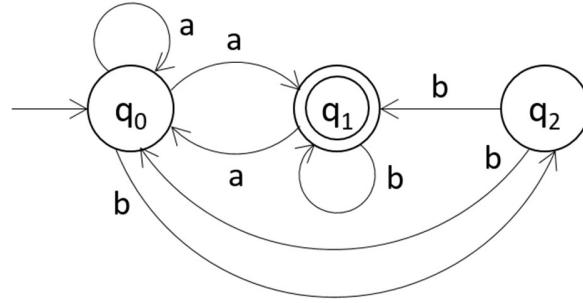
$$Q = \{[q_0], [q_1], [q_0q_1]\}$$

$$\Sigma = \{0, 1\}$$

q_0 is the initial/start state

$$F = \{[q_0], [q_0q_1]\}$$

5. Convert the following NFA into its equivalent DFA.



Subset Construction Method:

Step 1: q_0 is the start/initial state of the required DFA.

Step 2: NFA has 3 states. Therefore, DFA has $8 (= 2^3)$ states, namely $[q_0]$, $[q_1]$, $[q_2]$, $[q_0q_1]$, $[q_1q_2]$, $[q_0q_2]$, $[q_0q_1q_2]$, ϕ .

Step 3: Evaluate δ_D using δ_N and determine the Transition function of the DFA as follows:

$$\delta_D(q_0, a) = \delta_N(q_0, a) = [q_0q_1]$$

$$\delta_D(q_0, b) = \delta_N(q_0, b) = [q_2]$$

$$\delta_D(q_1, a) = \delta_N(q_1, a) = [q_0]$$

$$\delta_D(q_1, b) = \delta_N(q_1, b) = [q_1]$$

$$\delta_D(q_2, a) = \delta_N(q_2, a) = \phi$$

$$\delta_D(q_2, b) = \delta_N(q_2, b) = [q_0q_1]$$

$$\delta_D([q_0q_1], a) = \delta_N(q_0, a) \cup \delta_N(q_1, a) = \{q_0, q_1\} \cup \{q_0\} = [q_0q_1]$$

$$\delta_D([q_0q_1], b) = \delta_N(q_0, b) \cup \delta_N(q_1, b) = \{q_2\} \cup \{q_1\} = [q_1q_2]$$

$$\delta_D([q_0q_2], a) = \delta_N(q_0, a) \cup \delta_N(q_2, a) = \{q_0, q_1\} \cup \phi = [q_0q_1]$$

$$\delta_D([q_0q_2], b) = \delta_N(q_0, b) \cup \delta_N(q_2, b) = \{q_2\} \cup \{q_0q_1\} = [q_0q_1q_2]$$

$$\delta_D([q_1q_2], a) = \delta_N(q_1, a) \cup \delta_N(q_2, a) = \{q_0\} \cup \phi = [q_0]$$

$$\delta_D([q_1q_2], b) = \delta_N(q_1, b) \cup \delta_N(q_2, b) = \{q_1\} \cup \{q_0q_1\} = [q_0q_1]$$

$$\delta_D([q_0q_1q_2], a) = \delta_N(q_0, a) \cup \delta_N(q_1, a) \cup \delta_N(q_2, a) = \{q_0, q_1\} \cup \{q_0\} \cup \phi = [q_0q_1]$$

$$\delta_D([q_0q_1q_2], 1) = \delta_N(q_0, 1) \cup \delta_N(q_1, 1) \cup \delta_N(q_2, 1) = \{q_2\} \cup \{q_1\} \cup \{q_0q_1\} = [q_0q_1q_2]$$

$$\delta_D(\phi, a) = \delta_N(\phi, a) = \phi$$

$$\delta_D(\phi, b) = \delta_N(\phi, b) = \phi$$

Step 4: Now, change the names of the states $\{[q_0], [q_1], [q_2], [q_0q_1], [q_0q_2], [q_1q_2], [q_0q_1q_2], \phi\}$ as $\{A, B, C, D, E, F, G, H\}$.

δ	a	b
$\rightarrow[q_0]$	$[q_0q_1]$	$[q_2]$
$[q_1]$	$[q_0]$	$[q_1]$
$*[q_2]$	ϕ	$[q_0q_1]$
$[q_0q_1]$	$[q_0q_1]$	$[q_1q_2]$
$*[q_0q_2]$	$[q_0q_1]$	$[q_0q_1q_2]$
$*[q_1q_2]$	$[q_0]$	$[q_0q_1]$
$*[q_0q_1q_2]$	$[q_0q_1]$	$[q_0q_1q_2]$
ϕ	ϕ	ϕ

Step 5: Draw the Transition Function for the newly named states.

δ	a	b
$\rightarrow A$	D	C
B	A	B
*C	H	D
D	D	F
*E	D	G
*F	A	D
*G	D	G
H	H	H

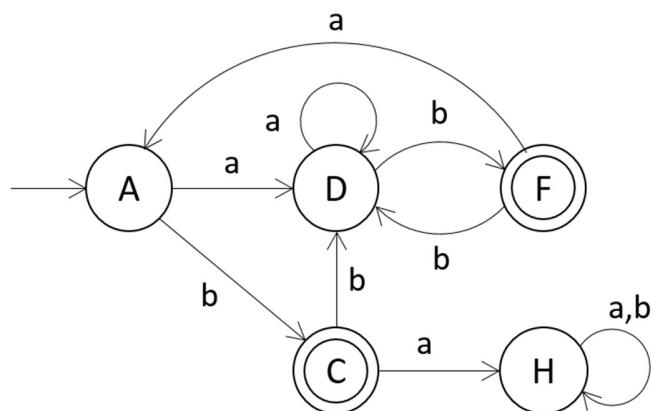
Step 6: Determine the states accessible from the start/initial state.

Here, the accessible states are: {A, C, D, F, H}.

Step 7: Draw the Transition Function for the accessible states only.

δ	a	b
$\rightarrow A$	D	C
D	D	F
*C	H	D
*F	A	D
H	H	H

Step 8: Draw the DFA using the Transition Function.



Step 9: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

$$Q = \{A, C, D, F, H\}$$

$$\Sigma = \{a, b\}$$

A is the initial/start state

$$F = \{C, F\}$$

Lazy Evaluation Method:

Step 1: q_0 is start/initial state of the required DFA.

$$\delta_D(q_0, a) = \delta_N(q_0, a) = [q_0q_1]$$

$$\delta_D(q_0, b) = \delta_N(q_0, b) = [q_2]$$

Step 2: Using the states obtained from each transition, proceed with the calculation as follows:

$$\delta_D(q_1, a) = \delta_N(q_1, a) = [q_0]$$

$$\delta_D(q_1, b) = \delta_N(q_1, b) = [q_1]$$

$$\delta_D(q_2, a) = \delta_N(q_2, a) = \phi$$

$$\delta_D(q_2, b) = \delta_N(q_2, b) = [q_0q_1]$$

$$\delta_D([q_0q_1], a) = \delta_N(q_0, a) \cup \delta_N(q_1, a) = \{q_0, q_1\} \cup \{q_0\} = [q_0q_1]$$

$$\delta_D([q_0q_1], b) = \delta_N(q_0, b) \cup \delta_N(q_1, b) = \{q_2\} \cup \{q_1\} = [q_1q_2]$$

$$\delta_D([q_1q_2], a) = \delta_N(q_1, a) \cup \delta_N(q_2, a) = \{q_0\} \cup \phi = [q_0]$$

$$\delta_D([q_1q_2], b) = \delta_N(q_1, b) \cup \delta_N(q_2, b) = \{q_1\} \cup \{q_0q_1\} = [q_0q_1]$$

$$\delta_D([q_0q_2], a) = \delta_N(q_0, a) \cup \delta_N(q_2, a) = \{q_0, q_1\} \cup \phi = [q_0q_1]$$

$$\delta_D([q_0q_2], b) = \delta_N(q_0, b) \cup \delta_N(q_2, b) = \{q_2\} \cup \{q_0q_1\} = [q_0q_1q_2]$$

$$\delta_D([q_0q_1q_2], a) = \delta_N(q_0, a) \cup \delta_N(q_1, a) \cup \delta_N(q_2, a) = \{q_0, q_1\} \cup \{q_0\} \cup \phi = [q_0q_1]$$

$$\delta_D([q_0q_1q_2], 1) = \delta_N(q_0, 1) \cup \delta_N(q_1, 1) \cup \delta_N(q_2, 1) = \{q_2\} \cup \{q_1\} \cup \{q_0q_1\} = [q_0q_1q_2]$$

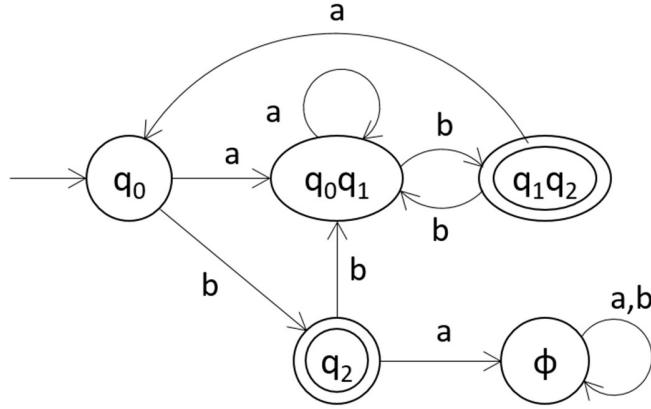
$$\delta_D(\phi, a) = \delta_N(\phi, a) = \phi$$

$$\delta_D(\phi, b) = \delta_N(\phi, b) = \phi$$

Step 3: Draw the Transition Function for the above determined states.

δ	a	b
$\rightarrow[q_0]$	$[q_0q_1]$	$[q_2]$
$[q_0q_1]$	$[q_0q_1]$	$[q_1q_2]$
$*[q_2]$	ϕ	$[q_0q_1]$
$*[q_1q_2]$	$[q_0]$	$[q_0q_1]$
ϕ	ϕ	ϕ

Step 4: Draw the DFA using the Transition Function.



Step 5: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

$$Q = \{[q_0], [q_2], [q_0q_1], [q_1q_2], \phi\}$$

$$\Sigma = \{a, b\}$$

q_0 is the initial/start state

$$F = \{[q_2], [q_1q_2]\}$$

6. Convert the following NFA into its equivalent DFA.

δ	a	b
$\rightarrow q_0$	$\{q_0, q_1\}$	$\{q_0\}$
q_1	$\{q_2\}$	$\{q_1\}$
q_2	$\{q_3\}$	$\{q_3\}$
$* q_3$	ϕ	$\{q_2\}$

Subset Construction Method:

Step 1: q_0 is the start/initial state of the required DFA.

Step 2: NFA has 4 states. Therefore, DFA has $16 (= 2^4)$ states, namely $[q_0], [q_1], [q_2], [q_3], [q_0q_1], [q_0q_2], [q_0q_3], [q_1q_2], [q_1q_3], [q_2q_3], [q_0q_1q_2], [q_0q_1q_3], [q_0q_2q_3], [q_1q_2q_3], [q_0q_1q_2q_3], \phi$.

Step 3: Evaluate δ_D using δ_N and determine the Transition function of the DFA as follows:

$$\delta_D (q_0, a) = \delta_N (q_0, a) = [q_0q_1]$$

$$\delta_D (q_0, b) = \delta_N (q_0, b) = [q_0]$$

$$\delta_D (q_1, a) = \delta_N (q_1, a) = [q_2]$$

$$\delta_D(q_1, b) = \delta_N(q_1, b) = [q_1]$$

$$\delta_D(q_2, a) = \delta_N(q_2, a) = [q_3]$$

$$\delta_D(q_2, b) = \delta_N(q_2, b) = [q_3]$$

$$\delta_D(q_3, a) = \delta_N(q_3, a) = \phi$$

$$\delta_D(q_3, b) = \delta_N(q_3, b) = [q_2]$$

$$\delta_D([q_0q_1], a) = \delta_N(q_0, a) \cup \delta_N(q_1, a)$$

$$= \{q_0, q_1\} \cup \{q_2\} = [q_0q_1q_2]$$

$$\delta_D([q_0q_1], b) = \delta_N(q_0, b) \cup \delta_N(q_1, b)$$

$$= \{q_0\} \cup \{q_1\} = [q_0q_1]$$

$$\delta_D([q_0q_2], a) = \delta_N(q_0, a) \cup \delta_N(q_2, a)$$

$$= \{q_0, q_1\} \cup \{q_3\} = [q_0q_1q_3]$$

$$\delta_D([q_0q_2], b) = \delta_N(q_0, b) \cup \delta_N(q_2, b)$$

$$= \{q_0\} \cup \{q_3\} = [q_0q_3]$$

$$\delta_D([q_0q_3], a) = \delta_N(q_0, a) \cup \delta_N(q_3, a)$$

$$= \{q_0, q_1\} \cup \phi = [q_0q_1]$$

$$\delta_D([q_0q_3], b) = \delta_N(q_0, b) \cup \delta_N(q_3, b)$$

$$= \{q_1\} \cup \{q_2\} = [q_1q_2]$$

$$\delta_D([q_1q_2], a) = \delta_N(q_1, a) \cup \delta_N(q_2, a)$$

$$= \{q_2\} \cup \{q_3\} = [q_2q_3]$$

$$\delta_D([q_1q_2], b) = \delta_N(q_1, b) \cup \delta_N(q_2, b)$$

$$= \{q_1\} \cup \{q_3\} = [q_1q_3]$$

$$\delta_D([q_1q_3], a) = \delta_N(q_1, a) \cup \delta_N(q_3, a)$$

$$= \{q_2\} \cup \phi = [q_2]$$

$$\delta_D([q_1q_3], b) = \delta_N(q_1, b) \cup \delta_N(q_3, b) = \{q_1\} \cup \{q_2\} = [q_1q_2]$$

$$\delta_D([q_2q_3], a) = \delta_N(q_2, a) \cup \delta_N(q_3, a) = \{q_3\} \cup \phi = [q_3]$$

$$\delta_D([q_2q_3], b) = \delta_N(q_2, b) \cup \delta_N(q_3, b) = \{q_3\} \cup \{q_2\} = [q_2q_3]$$

$$\delta_D([q_0q_1q_2], a) = \delta_N(q_0, a) \cup \delta_N(q_1, a) \cup \delta_N(q_2, a) = \{q_0, q_1\} \cup \{q_2\} \cup \{q_3\} = [q_0q_1q_2q_3]$$

$$\delta_D([q_0q_1q_3], a) = \delta_N(q_0, a) \cup \delta_N(q_1, a) \cup \delta_N(q_3, a) = \{q_0, q_1\} \cup \{q_3\} \cup \phi = [q_0q_1q_3]$$

$$\delta_D([q_0q_1q_3], b) = \delta_N(q_0, b) \cup \delta_N(q_1, b) \cup \delta_N(q_3, b) = \{q_0\} \cup \{q_1\} \cup \{q_3\} = [q_0q_1q_3]$$

$$\delta_D([q_0q_2q_3], a) = \delta_N(q_0, a) \cup \delta_N(q_2, a) \cup \delta_N(q_3, a) = \{q_0, q_2\} \cup \{q_3\} \cup \phi = [q_0q_2q_3]$$

$$\delta_D([q_1q_2q_3], a) = \delta_N(q_1, a) \cup \delta_N(q_2, a) \cup \delta_N(q_3, a) = \{q_2\} \cup \{q_3\} \cup \phi = [q_2q_3]$$

$$\delta_D([q_1q_2q_3], b) = \delta_N(q_1, b) \cup \delta_N(q_2, b) \cup \delta_N(q_3, b) = \{q_1\} \cup \{q_3\} \cup \{q_2\} = [q_1q_2q_3]$$

$$\delta_D([q_0q_1q_2q_3], a) = \delta_N(q_0, a) \cup \delta_N(q_1, a) \cup \delta_N(q_2, a) \cup \delta_N(q_3, a) = \{q_0, q_1\} \cup \{q_2\} \cup \{q_3\} \cup \phi = [q_0q_1q_2q_3]$$

δ	0	1
$\rightarrow[q_0]$	$[q_0q_1]$	$[q_0]$
$[q_1]$	$[q_2]$	$[q_1]$
$[q_2]$	$[q_3]$	$[q_3]$
$*[q_3]$	ϕ	$[q_2]$
$[q_0q_1]$	$[q_0q_1q_2]$	$[q_0q_1]$
$[q_0q_2]$	$[q_0q_1q_3]$	$[q_0q_3]$
$*[q_0q_3]$	$[q_0q_1]$	$[q_0q_2]$
$[q_1q_2]$	$[q_2q_3]$	$[q_1q_3]$
$*[q_1q_3]$	$[q_2]$	$[q_1q_2]$
$*[q_2q_3]$	$[q_3]$	$[q_2q_3]$
$[q_0q_1q_2]$	$[q_0q_1q_2q_3]$	$[q_0q_1q_3]$
$*[q_0q_1q_3]$	$[q_0q_1q_2]$	$[q_0q_1q_2]$
$*[q_0q_2q_3]$	$[q_0q_1q_3]$	$[q_0q_2q_3]$
$*[q_1q_2q_3]$	$[q_2q_3]$	$[q_1q_2q_3]$
$*[q_0q_1q_2q_3]$	$[q_0q_1q_2q_3]$	$[q_0q_1q_2q_3]$
ϕ	ϕ	ϕ

$$\delta_D([q_0q_1q_2q_3], b) = \delta_N(q_0, b) \cup \delta_N(q_1, b) \cup \delta_N(q_2, b) \cup \delta_N(q_3, b) = \{q_0\} \cup \{q_1\} \cup \{q_3\}$$

$$\cup \{q_2\} = [q_0q_1q_2q_3]$$

$$\delta_D(\phi, a) = \delta_N(\phi, a) = \phi$$

$$\delta_D(\phi, b) = \delta_N(\phi, b) = \phi$$

Step 4: Now, change the names of the states $[q_0]$, $[q_1]$, $[q_2]$, $[q_3]$, $[q_0q_1]$, $[q_0q_2]$, $[q_0q_3]$, $[q_1q_2]$, $[q_1q_3]$, $[q_2q_3]$, $[q_0q_1q_2]$, $[q_0q_1q_3]$, $[q_0q_2q_3]$, $[q_1q_2q_3]$, $[q_0q_1q_2q_3]$, ϕ . as {A, B, C, D, E, F, G, H, I, J, K, L, M, N, O, P}.

Step 5: Draw the Transition Function for the newly named states.

δ	0	1
$\rightarrow A$	E	A
B	C	B
C	D	D
*D	P	C
E	K	E
F	L	G
*G	E	F
H	J	I
*I	C	H
*J	D	J
K	O	L
*L	K	K
*M	L	M
*N	J	N
*O	O	O
P	P	P

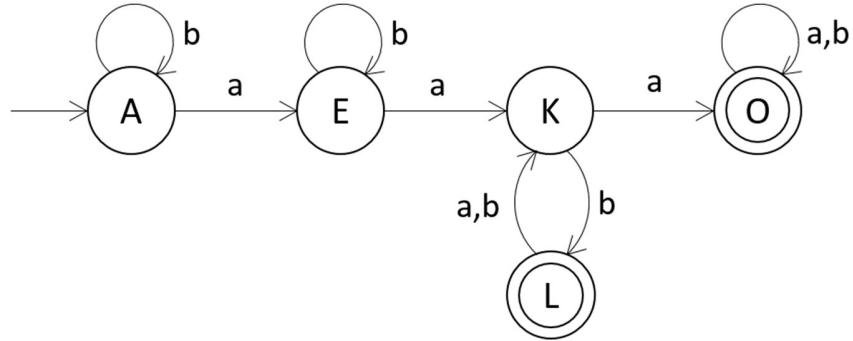
Step 6: Determine the states accessible from the start/initial state.

Here, the accessible states are: {A, E, K, L, O}.

Step 7: Draw the Transition Function for the accessible states only.

δ	0	1
$\rightarrow A$	E	A
E	K	E
K	O	L
*0	O	O
*L	K	K

Step 8: Draw the DFA using the Transition Function.



Step 9: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

$$Q = \{A, E, K, L, O\}$$

$$\Sigma = \{a, b\}$$

A is the initial/start state

$$F = \{L, O\}$$

Lazy Evaluation Method:

Step 1: q_0 is start/initial state of the required DFA.

$$\delta_D(q_0, a) = \delta_N(q_0, a) = [q_0q_1]$$

$$\delta_D(q_0, b) = \delta_N(q_0, b) = [q_0]$$

Step 2: Using the states obtained from each transition, proceed with the calculation as follows:

$$\delta_D([q_0q_1], a) = \delta_N(q_0, a) \cup \delta_N(q_1, a) = \{q_0, q_1\} \cup \{q_2\} = [q_0q_1q_2]$$

$$\delta_D([q_0q_1], b) = \delta_N(q_0, b) \cup \delta_N(q_1, b) = \{q_0\} \cup \{q_1\} = [q_0q_1]$$

$$\delta_D([q_0q_1q_2], a) = \delta_N(q_0, a) \cup \delta_N(q_1, a) \cup \delta_N(q_2, a) = \{q_0, q_1\} \cup \{q_2\} \cup \{q_3\} = [q_0q_1q_2q_3]$$

$$\delta_D([q_0q_1q_2], b) = \delta_N(q_0, b) \cup \delta_N(q_1, b) \cup \delta_N(q_2, b) = \{q_0\} \cup \{q_1\} \cup \{q_3\} = [q_0q_1q_3]$$

$$\delta_D([q_0q_1q_2q_3], a) = \delta_N(q_0, a) \cup \delta_N(q_1, a) \cup \delta_N(q_2, a) \cup \delta_N(q_3, a) = \{q_0, q_1\} \cup \{q_2\} \cup \{q_3\} \cup \emptyset = [q_0q_1q_2q_3]$$

$$\delta_D([q_0q_1q_2q_3], b) = \delta_N(q_0, b) \cup \delta_N(q_1, b) \cup \delta_N(q_2, b) \cup \delta_N(q_3, a) = \{q_0\} \cup \{q_1\} \cup \{q_3\} \cup \{q_2\} = [q_0q_1q_2q_3]$$

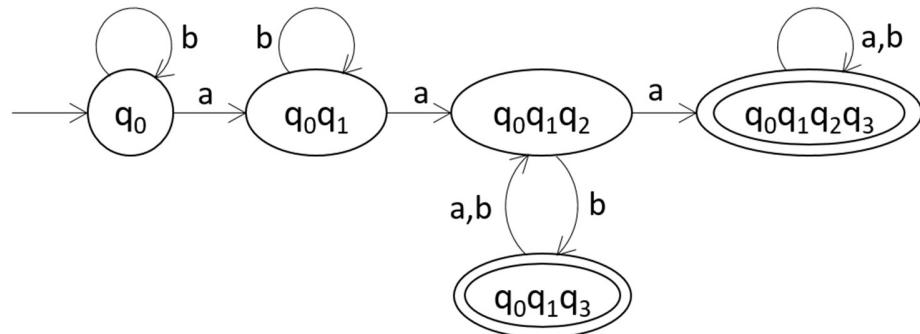
$$\delta_D([q_0q_1q_3], a) = \delta_N(q_0, a) \cup \delta_N(q_1, a) \cup \delta_N(q_3, a) = \{q_0, q_1\} \cup \{q_2\} \cup \emptyset = [q_0q_1q_2]$$

$$\delta_D([q_0q_1q_3], b) = \delta_N(q_0, b) \cup \delta_N(q_1, b) \cup \delta_N(q_3, b) = \{q_0\} \cup \{q_1\} \cup \{q_2\} = [q_0q_1q_2]$$

Step 3: Draw the Transition Function for the above determined states.

δ	0	1
$\rightarrow[q_0]$	$[q_0q_1]$	$[q_0]$
$[q_0q_1]$	$[q_0q_1q_2]$	$[q_0q_1]$
$[q_0q_1q_2]$	$[q_0q_1q_2q_3]$	$[q_0q_1q_3]$
$*[q_0q_1q_2q_3]$	$[q_0q_1q_2q_3]$	$[q_0q_1q_2q_3]$
$*[q_0q_1q_3]$	$[q_0q_1q_2]$	$[q_0q_1q_2]$

Step 4: Draw the DFA using the Transition Function.



Step 5: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

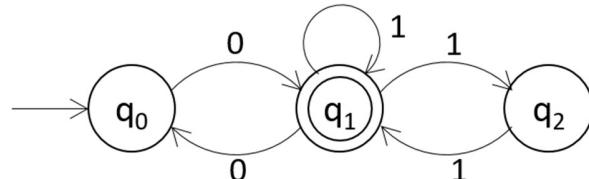
$$Q = \{[q_0], [q_0q_1], [q_0q_1q_2], [q_0q_1q_3], [q_0q_1q_2q_3]\}$$

$$\Sigma = \{a, b\}$$

q_0 is the initial/start state

$$F = \{[q_0q_1q_3], [q_0q_1q_2q_3]\}$$

7. Convert the following NFA into its equivalent DFA.



Subset Construction Method:

Step 1: q_0 is the start/initial state of the required DFA.

Step 2: NFA has 3 states. Therefore, DFA has $8 (= 2^3)$ states, namely $[q_0]$, $[q_1]$, $[q_2]$, $[q_0q_1]$, $[q_1q_2]$, $[q_0q_2]$, $[q_0q_1q_2]$, ϕ .

Step 3: Evaluate δ_D using δ_N and determine the Transition function of the DFA as follows:

$$\begin{aligned}
 \delta_D(q_0, 0) &= \delta_N(q_0, 0) = [q_1] \\
 \delta_D(q_0, 1) &= \delta_N(q_0, 1) = \phi \\
 \delta_D(q_1, 0) &= \delta_N(q_1, 0) = [q_0] \\
 \delta_D(q_1, 1) &= \delta_N(q_1, 1) = [q_1q_2] \\
 \delta_D(q_2, 0) &= \delta_N(q_2, 0) = \phi \\
 \delta_D(q_2, 1) &= \delta_N(q_2, 1) = [q_1] \\
 \delta_D([q_0q_1], 0) &= \delta_N(q_0, 0) \cup \delta_N(q_1, 0) = \\
 &\quad \{q_1\} \cup \{q_0\} = [q_0q_1] \\
 \delta_D([q_0q_1], 1) &= \delta_N(q_0, 1) \cup \delta_N(q_1, 1) = \\
 &\quad \phi \cup \{q_1q_2\} = [q_1q_2] \\
 \delta_D([q_0q_2], 0) &= \delta_N(q_0, 0) \cup \delta_N(q_2, 0) = \\
 &\quad \{q_1\} \cup \phi = [q_1] \\
 \delta_D([q_0q_2], 1) &= \delta_N(q_0, 1) \cup \delta_N(q_2, 1) = \phi \cup \{q_1\} = [q_1] \\
 \delta_D([q_1q_2], 0) &= \delta_N(q_1, 0) \cup \delta_N(q_2, 0) = \{q_0\} \cup \phi = [q_0] \\
 \delta_D([q_1q_2], 1) &= \delta_N(q_1, 1) \cup \delta_N(q_2, 1) = \{q_1q_2\} \cup \{q_1\} = [q_1q_2] \\
 \delta_D([q_0q_1q_2], 0) &= \delta_N(q_0, 0) \cup \delta_N(q_1, 0) \cup \delta_N(q_2, 0) = \{q_1\} \cup \{q_0\} \cup \phi = [q_0q_1] \\
 \delta_D([q_0q_1q_2], 1) &= \delta_N(q_0, 1) \cup \delta_N(q_1, 1) \cup \delta_N(q_2, 1) = \phi \cup \{q_1q_2\} \cup \{q_1\} = [q_1q_2] \\
 \delta_D(\phi, 0) &= \delta_N(\phi, 0) = \phi \\
 \delta_D(\phi, 1) &= \delta_N(\phi, 1) = \phi
 \end{aligned}$$

δ	0	1
$\rightarrow[q_0]$	$[q_1]$	ϕ
$*[q_1]$	$[q_0]$	$[q_1q_2]$
$[q_2]$	ϕ	$[q_1]$
$*[q_0q_1]$	$[q_0q_1]$	$[q_1q_2]$
$[q_0q_2]$	$[q_1]$	$[q_1]$
$*[q_1q_2]$	$[q_0]$	$[q_1q_2]$
$*[q_0q_1q_2]$	$[q_0q_1]$	$[q_1q_2]$
ϕ	ϕ	ϕ

Step 4: Now, change the names of the states $\{[q_0], [q_1], [q_2], [q_0q_1], [q_0q_2], [q_1q_2], [q_0q_1q_2], \phi\}$ as {A, B, C, D, E, F, G, H}.

Step 5: Draw the Transition Function for the newly named states.

δ	0	1
$\rightarrow A$	B	H
$*B$	A	F
C	H	B
$*D$	D	F
E	B	B
$*F$	A	F
$*G$	D	F
H	H	H

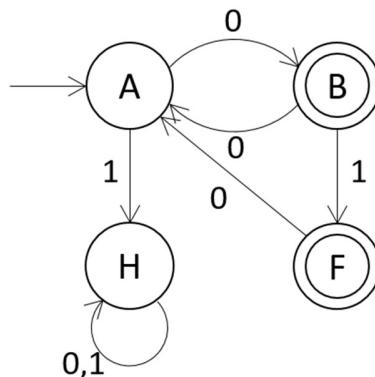
Step 6: Determine the states accessible from the start/initial state.

Here, the accessible states are: {A, B, F, H}.

Step 7: Draw the Transition Function for the accessible states only.

δ	0	1
$\rightarrow A$	B	H
*B	A	F
H	H	H
*F	A	F

Step 8: Draw the DFA using the Transition Function.



Step 9: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

$$Q = \{A, B, F, H\}$$

$$\Sigma = \{0, 1\}$$

A is the initial/start state

$$F = \{B, F\}$$

Lazy Evaluation Method:

Step 1: q_0 is start/initial state of the required DFA.

$$\delta_D(q_0, 0) = \delta_N(q_0, 0) = [q_1]$$

$$\delta_D(q_0, 1) = \delta_N(q_0, 1) = \phi$$

Step 2: Using the states obtained from each transition, proceed with the calculation as follows:

$$\delta_D(\phi, 0) = \delta_N(\phi, 0) = \phi$$

$$\delta_D(\phi, 1) = \delta_N(\phi, 1) = \phi$$

$$\delta_D(q_1, 0) = \delta_N(q_1, 0) = [q_0]$$

$$\delta_D(q_1, 1) = \delta_N(q_1, 1) = [q_1q_2]$$

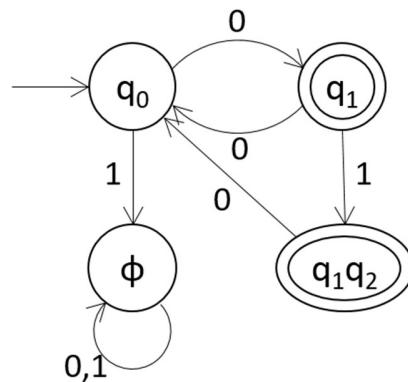
$$\delta_D([q_1q_2], 0) = \delta_N(q_1, 0) \cup \delta_N(q_2, 0) = \{q_0\} \cup \phi = [q_0]$$

$$\delta_D([q_1q_2], 1) = \delta_N(q_1, 1) \cup \delta_N(q_2, 1) = \{q_1q_2\} \cup \{q_1\} = [q_1q_2]$$

Step 3: Draw the Transition Function for the above determined states.

δ	0	1
$\rightarrow[q_0]$	$[q_1]$	ϕ
$*[q_1]$	$[q_0]$	$[q_1q_2]$
ϕ	ϕ	ϕ
$*[q_1q_2]$	$[q_0]$	$[q_1q_2]$

Step 4: Draw the DFA using the Transition Function.



Step 5: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

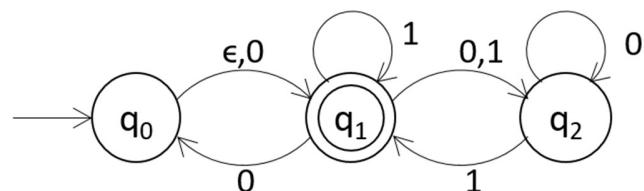
$$Q = \{[q_0], [q_1], [q_1q_2], \phi\}$$

$$\Sigma = \{0, 1\}$$

q_0 is the initial/start state

$$F = \{[q_1], [q_1q_2]\}$$

8. Convert the following Epsilon-NFA into its equivalent DFA.



Lazy Evaluation Method:

Step 1: Find Eclose of every state in the given E-NFA.

$$\text{Eclose } (q_0) = \{q_0, q_1\}$$

$$\text{Eclose } (q_1) = \{q_1\}$$

$$\text{Eclose } (q_2) = \{q_2\}$$

Step 2: $[q_0q_1]$ is start/initial state of the required DFA.

$$\delta_D ([q_0q_1], 0) = \text{Eclose} (\delta_N ([q_0q_1], 0)) = \text{Eclose} (\delta_N (q_0, 0) \cup \delta_N (q_1, 0)) = \text{Eclose} (\{q_1\} \cup \{q_0q_2\}) = [q_0q_1q_2]$$

$$\delta_D ([q_0q_1], 1) = \text{Eclose} (\delta_D ([q_0q_1], 1)) = \text{Eclose} (\delta_N (q_0, 1) \cup \delta_N (q_1, 1)) = \text{Eclose} (\{q_1\} \cup \{q_2\}) = [q_1q_2]$$

Step 3: Using the states obtained from each transition, proceed with the calculation as follows:

$$\delta_D ([q_0q_1q_2], 0) = \text{Eclose} (\delta_N (q_0, 0) \cup \delta_N (q_1, 0) \cup \delta_N (q_2, 0)) = \text{Eclose} (\{q_1\} \cup \{q_2\} \cup \{q_0\}) = [q_0q_1q_2]$$

$$\delta_D ([q_0q_1q_2], 1) = \text{Eclose} (\delta_N (q_0, 1) \cup \delta_N (q_1, 1) \cup \delta_N (q_2, 1)) = \text{Eclose} (\{q_1q_2\} \cup \{q_1\}) = [q_1q_2]$$

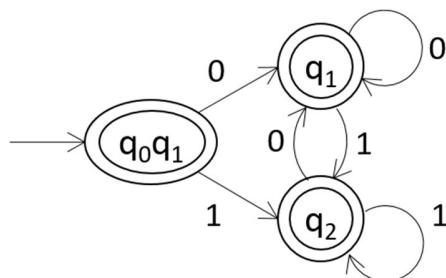
$$\delta_D ([q_1q_2], 0) = \text{Eclose} (\delta_N (q_1, 0) \cup \delta_N (q_2, 0)) = \text{Eclose} (\{q_0q_2\} \cup \{q_2\}) = [q_0q_1q_2]$$

$$\delta_D ([q_1q_2], 1) = \text{Eclose} (\delta_N (q_1, 1) \cup \delta_N (q_2, 1)) = \text{Eclose} (\{q_1q_2\} \cup \{q_1\}) = [q_1q_2]$$

Step 4: Draw the Transition Function for the above determined states.

δ	0	1
$\rightarrow^* [q_0q_1]$	$[q_0q_1q_2]$	$[q_1q_2]$
$*[q_1q_2]$	$[q_0q_1q_2]$	$[q_1q_2]$
$*[q_0q_1q_2]$	$[q_0q_1q_2]$	$[q_1q_2]$

Step 5: Draw the DFA using the Transition Function.



Step 6: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

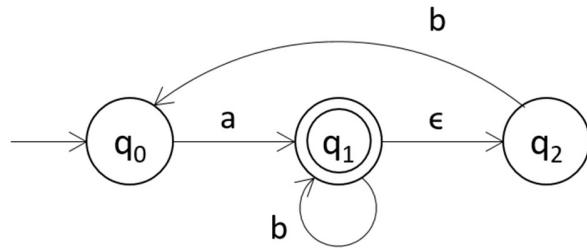
$$Q = \{[q_0q_1], [q_1q_2], [q_0q_1q_2]\}$$

$$\Sigma = \{0, 1\}$$

$[q_0q_1]$ is the initial/start state

$$F = \{[q_0q_1], [q_1q_2], [q_0q_1q_2]\}$$

9. Convert the following E-NFA into its equivalent DFA.



Lazy Evaluation Method:

Step 1: Find Eclose of every state in the given E-NFA.

$$\text{Eclose } (q_0) = \{q_0\}$$

$$\text{Eclose } (q_1) = \{q_1, q_2\}$$

$$\text{Eclose } (q_2) = \{q_2\}$$

Step 2: q_0 is start/initial state of the required DFA.

$$\delta_D (q_0, a) = \text{Eclose} (\delta_N (q_0, a)) = \text{Eclose} (q_1) = [q_1 q_2]$$

$$\delta_D (q_0, b) = \text{Eclose} (\delta_N (q_0, b)) = \text{Eclose} (\phi) = \emptyset$$

Step 3: Using the states obtained from each transition, proceed with the calculation as follows:

$$\delta_D ([q_1 q_2], a) = \text{Eclose} (\delta_N (q_1, a) \cup \delta_N (q_2, a)) = \text{Eclose} (\phi) = \emptyset$$

$$\delta_D ([q_1 q_2], b) = \text{Eclose} (\delta_N (q_1, b) \cup \delta_N (q_2, b)) = \text{Eclose} (\{q_1\} \cup \{q_0\}) = [q_0 q_1 q_2]$$

$$\delta_D (\emptyset, a) = \text{Eclose} (\delta_N (\emptyset, a)) = \emptyset$$

$$\delta_D (\emptyset, b) = \text{Eclose} (\delta_N (\emptyset, b)) = \emptyset$$

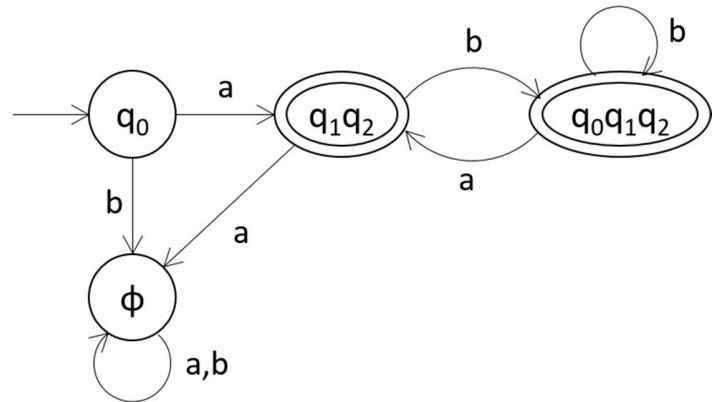
$$\delta_D ([q_0 q_1 q_2], a) = \text{Eclose} (\delta_N (q_0, a) \cup \delta_N (q_1, a) \cup \delta_N (q_2, a)) = \text{Eclose} (\{q_1\} \cup \emptyset) = [q_1 q_2]$$

$$\delta_D ([q_0 q_1 q_2], b) = \text{Eclose} (\delta_N (q_0, b) \cup \delta_N (q_1, b) \cup \delta_N (q_2, b)) = \text{Eclose} (\emptyset \cup \{q_1\} \cup \{q_0\}) = [q_0 q_1 q_2]$$

Step 4: Draw the Transition Function for the above determined states.

δ	0	1
$\rightarrow [q_0]$	$[q_1 q_2]$	\emptyset
$*[q_1 q_2]$	\emptyset	$[q_0 q_1 q_2]$
\emptyset	\emptyset	\emptyset
$*[q_0 q_1 q_2]$	$[q_1 q_2]$	$[q_0 q_1 q_2]$

Step 5: Draw the DFA using the Transition Function.



Step 6: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

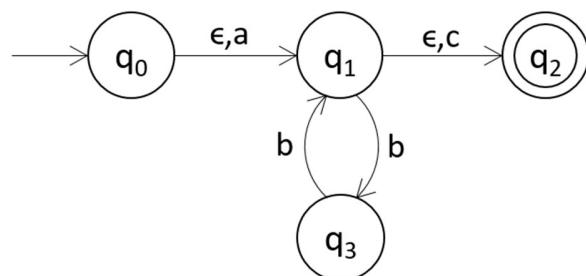
$$Q = \{[q_0], [q_1q_2], [q_0q_1q_2], \phi\}$$

$$\Sigma = \{a, b\}$$

q_0 is the initial/start state

$$F = \{[q_1q_2], [q_0q_1q_2]\}$$

10. Convert the following E-NFA into its equivalent DFA.



Lazy Evaluation Method:

Step 1: Find Eclose of every state in the given E-NFA.

$$\text{Eclose}(q_0) = \{q_0, q_1, q_2\}$$

$$\text{Eclose}(q_1) = \{q_1, q_2\}$$

$$\text{Eclose}(q_2) = \{q_2\}$$

$$\text{Eclose}(q_3) = \{q_3\}$$

Step 2: $[q_0q_1q_2]$ is start/initial state of the required DFA.

$$\delta_D([q_0q_1q_2], a) = \text{Eclose}(\delta_N(q_0, a) \cup \delta_N(q_1, a) \cup \delta_N(q_2, a)) = \text{Eclose}(\{q_1\} \cup \phi) = [q_1q_2]$$

$$\begin{aligned}\delta_D([q_0q_1q_2], b) &= \text{Eclose}(\delta_N(q_0, b) \cup \delta_N(q_1, b) \cup \delta_N(q_2, b)) = \text{Eclose}(\phi \cup \{q_3\} \cup \phi) \\ &= [q_3]\end{aligned}$$

$$\delta_D([q_0q_1q_2], c) = \text{Eclose}(\delta_N(q_0, c) \cup \delta_N(q_1, c) \cup \delta_N(q_2, c)) = \text{Eclose}(\phi \cup \{q_2\}) = [q_2]$$

Step 3: Using the states obtained from each transition, proceed with the calculation as follows:

$$\delta_D([q_0q_1], a) = \text{Eclose}(\delta_N(q_0, a) \cup \delta_N(q_1, a)) = \text{Eclose}(\{q_1\} \cup \phi) = [q_0q_1q_2]$$

$$\delta_D([q_0q_1], b) = \text{Eclose}(\delta_N(q_0, b) \cup \delta_N(q_1, b)) = \text{Eclose}(\phi \cup \{q_3\}) = [q_3]$$

$$\delta_D([q_0q_1], c) = \text{Eclose}(\delta_N(q_0, c) \cup \delta_N(q_1, c)) = \text{Eclose}(\phi \cup \{q_2\}) = [q_2]$$

$$\delta_D(q_3, a) = \text{Eclose}(\delta_N(q_3, a)) = \text{Eclose}(\phi) = \phi$$

$$\delta_D(q_3, b) = \text{Eclose}(\delta_N(q_3, b)) = \text{Eclose}(q_1) = [q_1q_2]$$

$$\delta_D(q_3, c) = \text{Eclose}(\delta_N(q_3, c)) = \text{Eclose}(\phi) = \phi$$

$$\delta_D(q_2, a) = \text{Eclose}(\delta_N(q_2, a)) = \text{Eclose}(\phi) = \phi$$

$$\delta_D(q_2, b) = \text{Eclose}(\delta_N(q_2, b)) = \text{Eclose}(\phi) = \phi$$

$$\delta_D(q_2, c) = \text{Eclose}(\delta_N(q_2, c)) = \text{Eclose}(\phi) = \phi$$

$$\delta_D([q_1q_2], a) = \text{Eclose}(\delta_N(q_1, a) \cup \delta_N(q_2, a)) = \text{Eclose}(\phi) = \phi$$

$$\delta_D([q_1q_2], b) = \text{Eclose}(\delta_N(q_1, b) \cup \delta_N(q_2, b)) = \text{Eclose}(\phi \cup \{q_3\}) = [q_3]$$

$$\delta_D([q_1q_2], c) = \text{Eclose}(\delta_N(q_1, c) \cup \delta_N(q_2, c)) = \text{Eclose}(\phi \cup \{q_2\}) = [q_2]$$

$$\delta_D(\phi, a) = \delta_N(\phi, a) = \phi$$

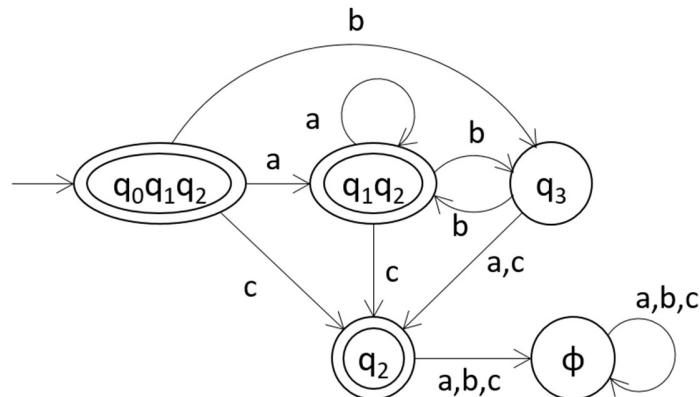
$$\delta_D(\phi, b) = \delta_N(\phi, b) = \phi$$

$$\delta_D(\phi, c) = \delta_N(\phi, c) = \phi$$

Step 4: Draw the Transition Function for the above determined states.

δ	a	b	c
$\rightarrow^* [q_0q_1q_2]$	$[q_1q_2]$	$[q_3]$	$[q_2]$
$*[q_1q_2]$	$[q_1q_2]$	$[q_3]$	$[q_2]$
$[q_3]$	ϕ	$[q_1q_2]$	ϕ
$*[q_2]$	ϕ	ϕ	ϕ
ϕ	ϕ	ϕ	ϕ

Step 5: Draw the DFA using the Transition Function.



Step 6: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

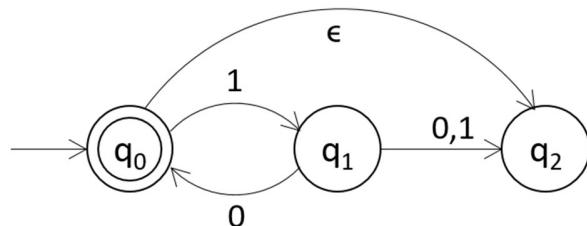
$$Q = \{[q_3], [q_2], [q_1q_2], [q_0q_1q_2], \phi\}$$

$$\Sigma = \{a, b, c\}$$

$[q_0q_1q_2]$ is the initial/start state

$$F = \{[q_2], [q_1q_2], [q_0q_1q_2]\}$$

11. Convert the following E-NFA into its equivalent DFA.



Lazy Evaluation Method:

Step 1: Find Eclose of every state in the given E-NFA.

$$\text{Eclose}(q_0) = \{q_0, q_2\}$$

$$\text{Eclose}(q_1) = \{q_1\}$$

$$\text{Eclose}(q_2) = \{q_2\}$$

Step 2: $[q_0q_2]$ is start/initial state of the required DFA.

$$\delta_D([q_0q_2], 0) = \text{Eclose}(\delta_N(q_0, 0) \cup \delta_N(q_2, 0)) = \text{Eclose}(\phi) = \phi$$

$$\delta_D([q_0q_2], 1) = \text{Eclose}(\delta_N(q_0, 1) \cup \delta_N(q_2, 1)) = \text{Eclose}(\{q_1\} \cup \phi) = [q_1]$$

Step 3: Using the states obtained from each transition, proceed with the calculation as follows:

$$\delta_D(\phi, 0) = \text{Eclose}(\delta_N(\phi, 0)) = \text{Eclose}(\phi) = \phi$$

$$\delta_D(\phi, 1) = \text{Eclose}(\delta_N(\phi, 1)) = \text{Eclose}(\phi) = \phi$$

$$\delta_D(q_1, 0) = \text{Eclose}(\delta_N(q_1, 0)) = \text{Eclose}(q_2) = [q_2]$$

$$\delta_D(q_1, 1) = \text{Eclose}(\delta_N(q_1, 1)) = \text{Eclose}(q_2) = [q_2]$$

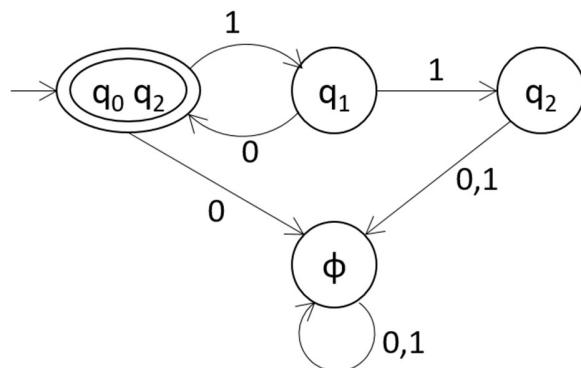
$$\delta_D(q_2, 0) = \text{Eclose}(\delta_N(q_2, 0)) = \text{Eclose}(\phi) = \phi$$

$$\delta_D(q_2, 1) = \text{Eclose}(\delta_N(q_2, 1)) = \text{Eclose}(\phi) = \phi$$

Step 4: Draw the Transition Function for the above determined states.

δ	0	1
$\rightarrow^* [q_0 q_2]$	ϕ	$[q_1]$
ϕ	ϕ	ϕ
$*[q_1]$	$[q_0 q_2]$	$[q_2]$
$[q_2]$	ϕ	ϕ

Step 5: Draw the DFA using the Transition Function.



Step 6: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

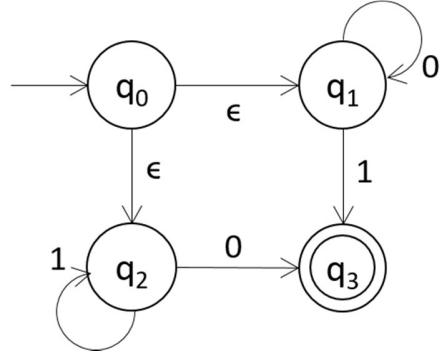
$$Q = \{[q_1], [q_2], [q_0 q_2], \phi\}$$

$$\Sigma = \{0, 1\}$$

$[q_0 q_2]$ is the initial/start state

$$F = \{[q_0 q_2]\}$$

12. Convert the following E-NFA into its equivalent DFA.



Lazy Evaluation Method:

Step 1: Find Eclose of every state in the given E-NFA.

$$\text{Eclose}(q_0) = \{q_0, q_1, q_2\}$$

$$\text{Eclose}(q_1) = \{q_1\}$$

$$\text{Eclose}(q_2) = \{q_2\}$$

$$\text{Eclose}(q_3) = \{q_3\}$$

Step 2: $[q_0q_1q_2]$ is start/initial state of the required DFA.

$$\delta_D([q_0q_1q_2], 0) = \text{Eclose}(\delta_N(q_0, 0) \cup \delta_N(q_1, 0) \cup \delta_N(q_2, 0)) = \text{Eclose}(\emptyset \cup \{q_1\} \cup \{q_3\}) = [q_1q_3]$$

$$\delta_D([q_0q_1q_2], 1) = \text{Eclose}(\delta_N(q_0, 1) \cup \delta_N(q_1, 1) \cup \delta_N(q_2, 1)) = \text{Eclose}(\emptyset \cup \{q_3\} \cup \{q_2\}) = [q_2q_3]$$

Step 3: Using the states obtained from each transition, proceed with the calculation as follows:

$$\delta_D([q_1q_3], 0) = \text{Eclose}(\delta_N(q_1, 0) \cup \delta_N(q_3, 0)) = \text{Eclose}(\{q_1\} \cup \emptyset) = [q_1]$$

$$\delta_D([q_1q_3], 1) = \text{Eclose}(\delta_N(q_1, 1) \cup \delta_N(q_3, 1)) = \text{Eclose}(\{q_3\} \cup \emptyset) = [q_3]$$

$$\delta_D([q_2q_3], 0) = \text{Eclose}(\delta_N(q_2, 0) \cup \delta_N(q_3, 0)) = \text{Eclose}(\{q_3\} \cup \emptyset) = [q_3]$$

$$\delta_D([q_2q_3], 1) = \text{Eclose}(\delta_N(q_2, 1) \cup \delta_N(q_3, 1)) = \text{Eclose}(\{q_2\} \cup \emptyset) = [q_2]$$

$$\delta_D(q_1, 0) = \text{Eclose}(\delta_N(q_1, 0)) = \text{Eclose}(q_1) = [q_1]$$

$$\delta_D(q_1, 1) = \text{Eclose}(\delta_N(q_1, 1)) = \text{Eclose}(q_3) = [q_3]$$

$$\delta_D(q_3, 0) = \text{Eclose}(\delta_N(q_3, 0)) = \text{Eclose}(\emptyset) = \emptyset$$

$$\delta_D(q_3, 1) = \text{Eclose}(\delta_N(q_3, 1)) = \text{Eclose}(\emptyset) = \emptyset$$

$$\delta_D(q_2, 0) = \text{Eclose}(\delta_N(q_2, 0)) = \text{Eclose}(q_3) = q_3$$

$$\delta_D(q_2, 1) = \text{Eclose}(\delta_N(q_2, 1)) = \text{Eclose}(q_2) = q_2$$

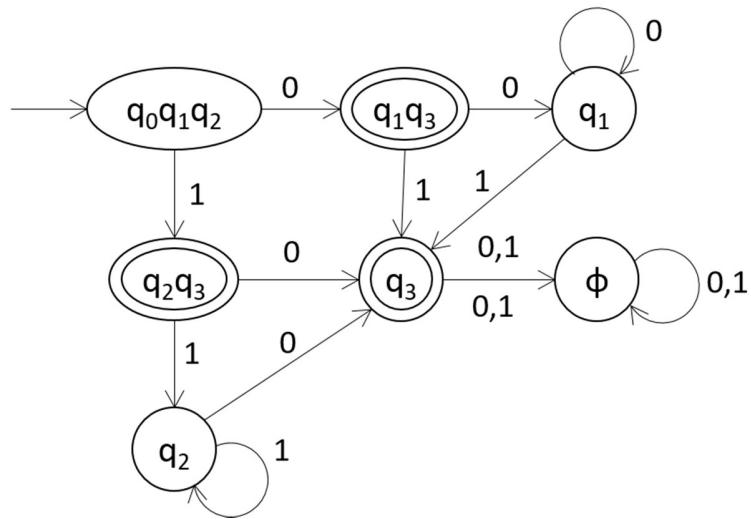
$$\delta_D(\emptyset, 0) = \text{Eclose}(\delta_N(\emptyset, 0)) = \text{Eclose}(\emptyset) = \emptyset$$

$$\delta_D(\emptyset, 1) = \text{Eclose}(\delta_N(\emptyset, 1)) = \text{Eclose}(\emptyset) = \emptyset$$

Step 4: Draw the Transition Function for the above determined states.

δ	0	1
$\rightarrow[q_0q_1q_2]$	$[q_1q_3]$	$[q_2q_3]$
$*[q_1q_3]$	$[q_1]$	$[q_3]$
$*[q_2q_3]$	$[q_3]$	$[q_2]$
$[q_1]$	$[q_1]$	$[q_3]$
$[q_2]$	$[q_3]$	$[q_2]$
$*[q_3]$	ϕ	ϕ
ϕ	ϕ	ϕ

Step 5: Draw the DFA using the Transition Function.



Step 6: Define the five tuples of the DFA: $A = \{Q, \Sigma, \delta_D, q_0, F\}$

$$Q = \{[q_3], [q_1], [q_2], [q_1q_2], [q_1q_3], [q_0q_1q_2], \phi\}$$

$$\Sigma = \{0, 1\}$$

$[q_0q_1q_2]$ is the initial/start state

$$F = \{[q_3], [q_1q_3], [q_2q_3]\}$$