

**M.S. Ramaiah Institute of Technology  
(Autonomous Institute, Affiliated to VTU)**

**Department of Computer Science and Engineering**

**Course Name: Artificial Intelligence and Machine Learning**

**Course Code: CS52**

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# Unit I

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## **Introduction: (Chapter 1 of Text Book 1)**

What is AI?

Foundation of Artificial Intelligence

History of Artificial Intelligence

## **Intelligent Agents: (Chapter 2 of Text Book 1)**

Agents and Environments

Rationality

The Nature of Environments

The Structure of Agents

## **Problem-solving by search: (Chapter 3 of Text Book 1)**

Problem-Solving Agents

Example Problems

Searching for Solution

Uniformed Search Strategies

Informed Search Strategies

Heuristic Functions

# What is Artificial Intelligence?

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Artificial intelligence (AI) is the study of ideas that enable computers to be intelligent.

The goals of the field of artificial intelligence are to make computers more useful and to understand the principles that make intelligence possible.

- Systems that think like humans ; Systems that think rationally
- Systems that act like humans ; Systems that act rationally

# What is Artificial Intelligence? (contd..)

<b>Thinking Humanly</b>  “The exciting new effort to make computers think . . . <i>machines with minds</i> , in the full and literal sense.” (Haugeland, 1985)  “[The automation of] activities that we associate with human thinking, activities such as decision-making, problem solving, learning . . .” (Bellman, 1978)	<b>Thinking Rationally</b>  “The study of mental faculties through the use of computational models.” (Charniak and McDermott, 1985)  “The study of the computations that make it possible to perceive, reason, and act.” (Winston, 1992)
<b>Acting Humanly</b>  “The art of creating machines that perform functions that require intelligence when performed by people.” (Kurzweil, 1990)  “The study of how to make computers do things at which, at the moment, people are better.” (Rich and Knight, 1991)	<b>Acting Rationally</b>  “Computational Intelligence is the study of the design of intelligent agents.” (Poole <i>et al.</i> , 1998)  “AI . . . is concerned with intelligent behavior in artifacts.” (Nilsson, 1998)

Some definitions of artificial intelligence, organized into four categories.

Eight definitions of AI, laid out along two dimensions.

Top - thought processes and reasoning,

Bottom - address behavior.

Left measure success - Human performance

Right ideal performance measure, called rationality

# What is Artificial Intelligence? (contd..)

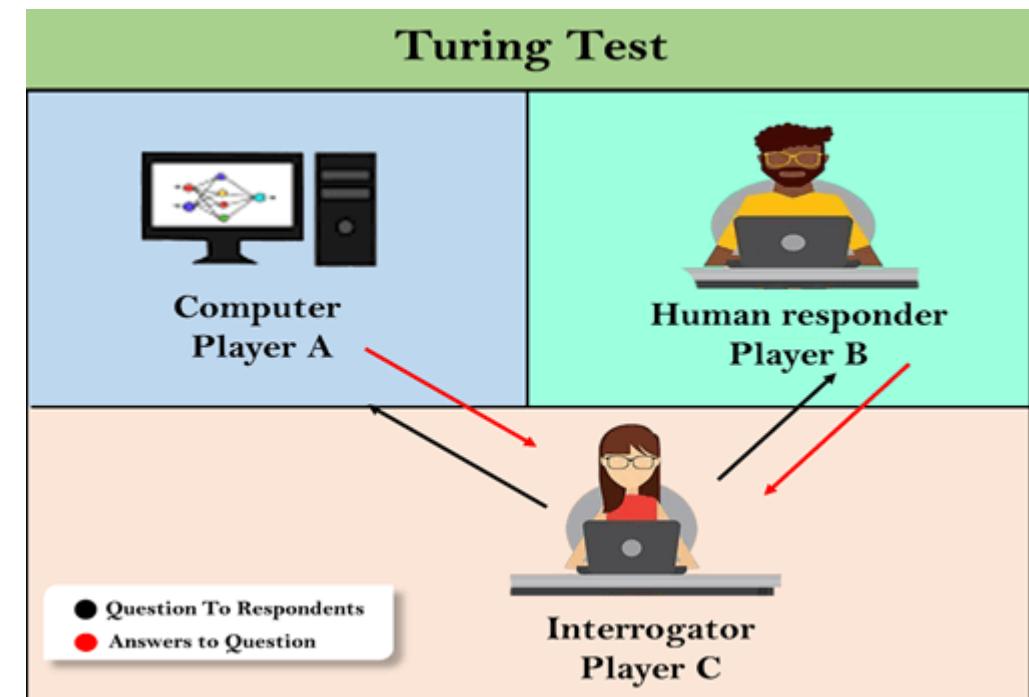
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- Acting humanly: The Turing Test approach
- Thinking humanly: The cognitive modeling approach
- Thinking rationally: The “laws of thought” approach
- Acting rationally: The rational agent approach



# What is Artificial Intelligence? (contd..)

- Acting humanly: The Turing Test approach
- The Turing Test, proposed by Alan Turing (1950), was designed to provide a satisfactory operational definition of intelligence.
- A computer passes the test if a human interrogator, after posing some written questions, cannot tell whether the written responses come from a person or from a computer.

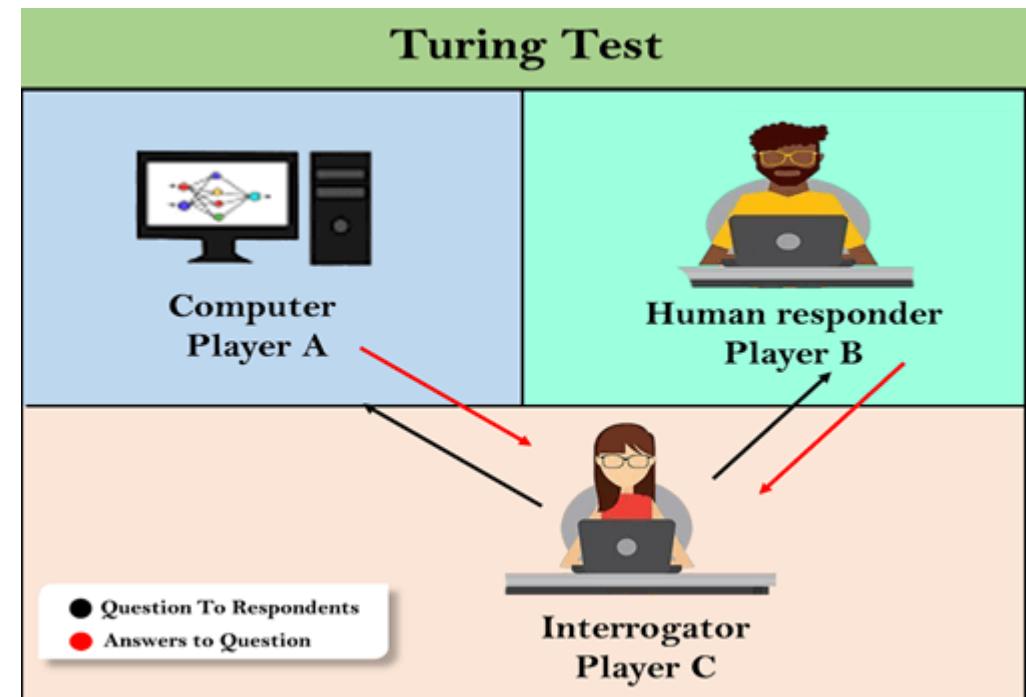


# What is Artificial Intelligence? (contd..)

## • Acting humanly: The Turing Test approach

The computer would need to possess the following capabilities:

- Natural language processing to enable it to communicate successfully in English;
- Knowledge representation to store what it knows or hears;
- automated reasoning to use the stored information to answer questions and to draw new conclusions;
- machine learning to adapt to new circumstances and to detect and extrapolate patterns

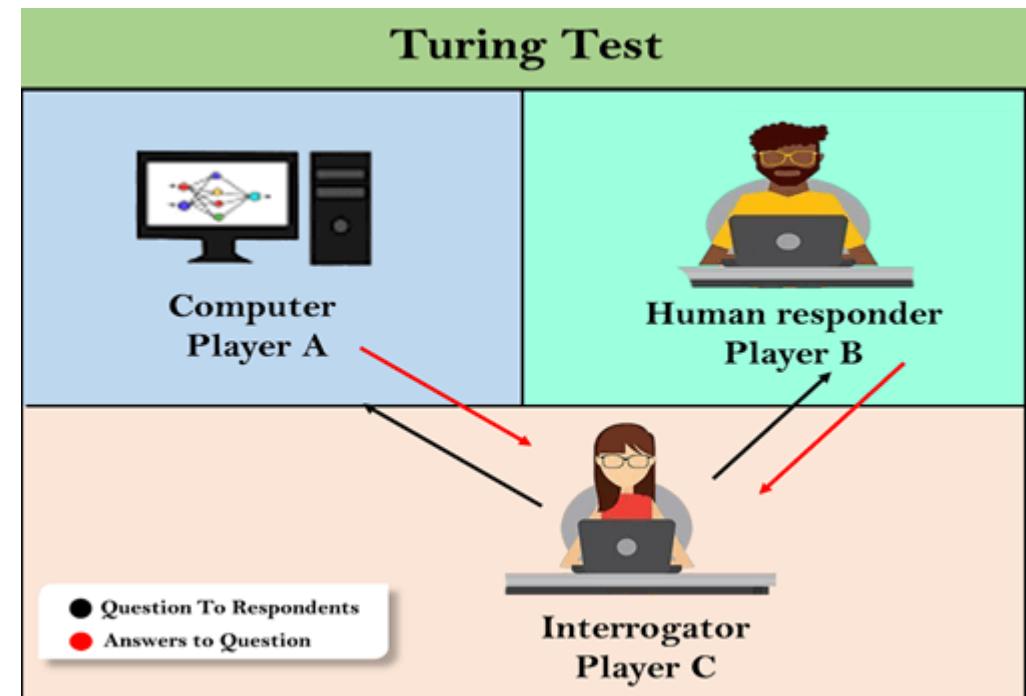


# What is Artificial Intelligence? (contd..)

- Acting humanly: The Turing Test approach

The computer would need to possess the following capabilities:

- Computer vision to perceive objects,
- Robotics to manipulate objects and move about.



# What is Artificial Intelligence? (contd..)

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- Thinking humanly: The cognitive modeling approach
- There are three ways to do this:
  - through introspection—trying to catch our own thoughts as they go by;
  - through psychological experiments—observing a person in action; and
  - through brain imaging—observing the brain in action.

If the program's input–output behavior matches corresponding human behavior, that is evidence that some of the program's mechanisms could also be operating in humans.

# What is Artificial Intelligence? (contd..)

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- Thinking humanly: The cognitive modeling approach

If we are going to say that a given program thinks like a human, we must have some way of determining how humans think.

We need to get inside the actual workings of human minds.

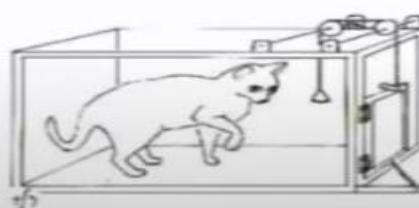
# What is Artificial Intelligence? (contd..)

- Thinking humanly: The cognitive modeling approach

## INTROSPECTION



## PSYCHOLOGICAL EXPERIMENT



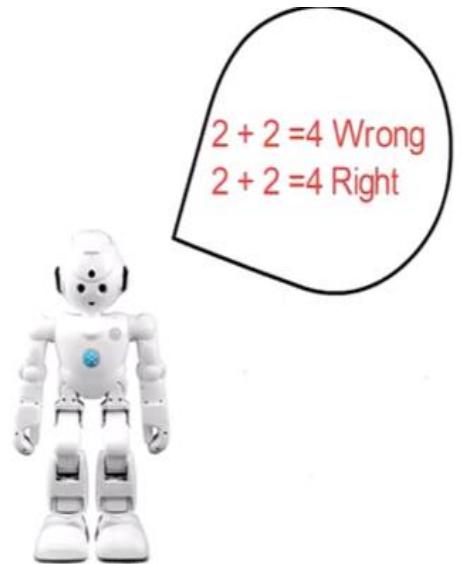
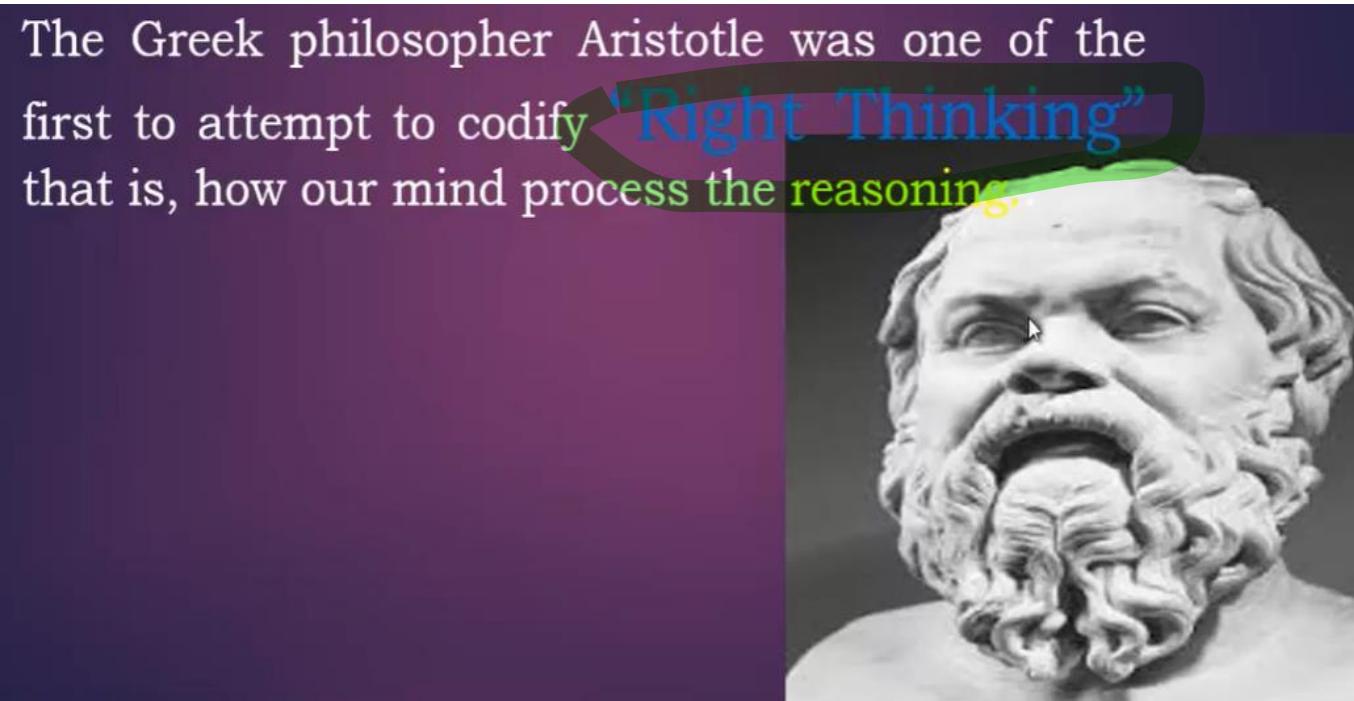
## BRAIN IMAGING



**HOW TO GET INSIDE OUR MIND**

# What is Artificial Intelligence? (contd..)

- Thinking rationally: The “laws of thought” approach

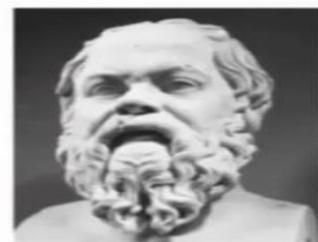
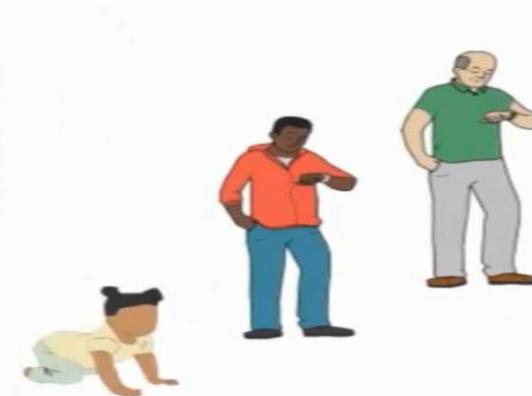


# What is Artificial Intelligence? (contd..)

- Thinking rationally: The “laws of thought” approach

Syllogisms

- Socrates has given the thinking process in terms of syllogisms which are very popular in philosophy
- Syllogisms provided patterns for argument structures that always yielded correct conclusions when given correct premises
- Example, “Socrates is a man; all men are mortal; therefore, Socrates is mortal.”



**SOCRATES IS A MAN**



**ALL MEN ARE MORTAL**

**THEREFORE SOCRATES IS MORTAL**

# What is Artificial Intelligence? (contd..)

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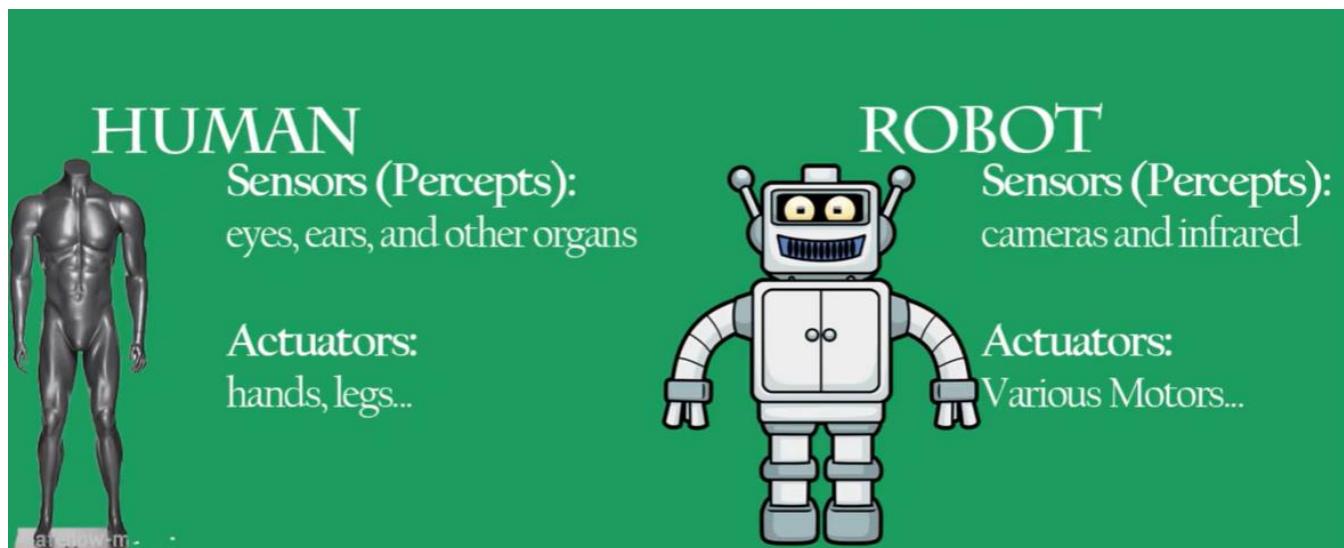
- Thinking rationally: The “laws of thought” approach
- These laws of thought were LOGIC supposed to govern the operation of the mind; their study initiated the field called logic
- There are two main obstacles to this approach.
  - First, it is not easy to take informal knowledge and state it in the formal terms required by logical notation, particularly when the knowledge is less than 100% certain.
  - Second, there is a big difference between solving a problem “in principle” and solving it in practice.

# What is Artificial Intelligence? (contd..)

- **Acting rationally: The rational agent approach**

An agent is just something that acts (Latin agree- to do).

An agent can be viewed as perceiving its environment through sensors and acting upon that environment through actuators



# What is Artificial Intelligence? (contd..)

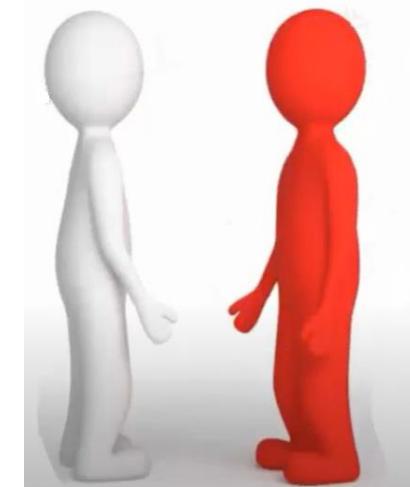
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- Acting rationally: The rational agent approach
- All computer programs do something, but computer agents are expected to do more: operate autonomously, perceive their environment, persist over a prolonged time period, adapt to change, and create and pursue goals.

# What is Artificial Intelligence? (contd..)

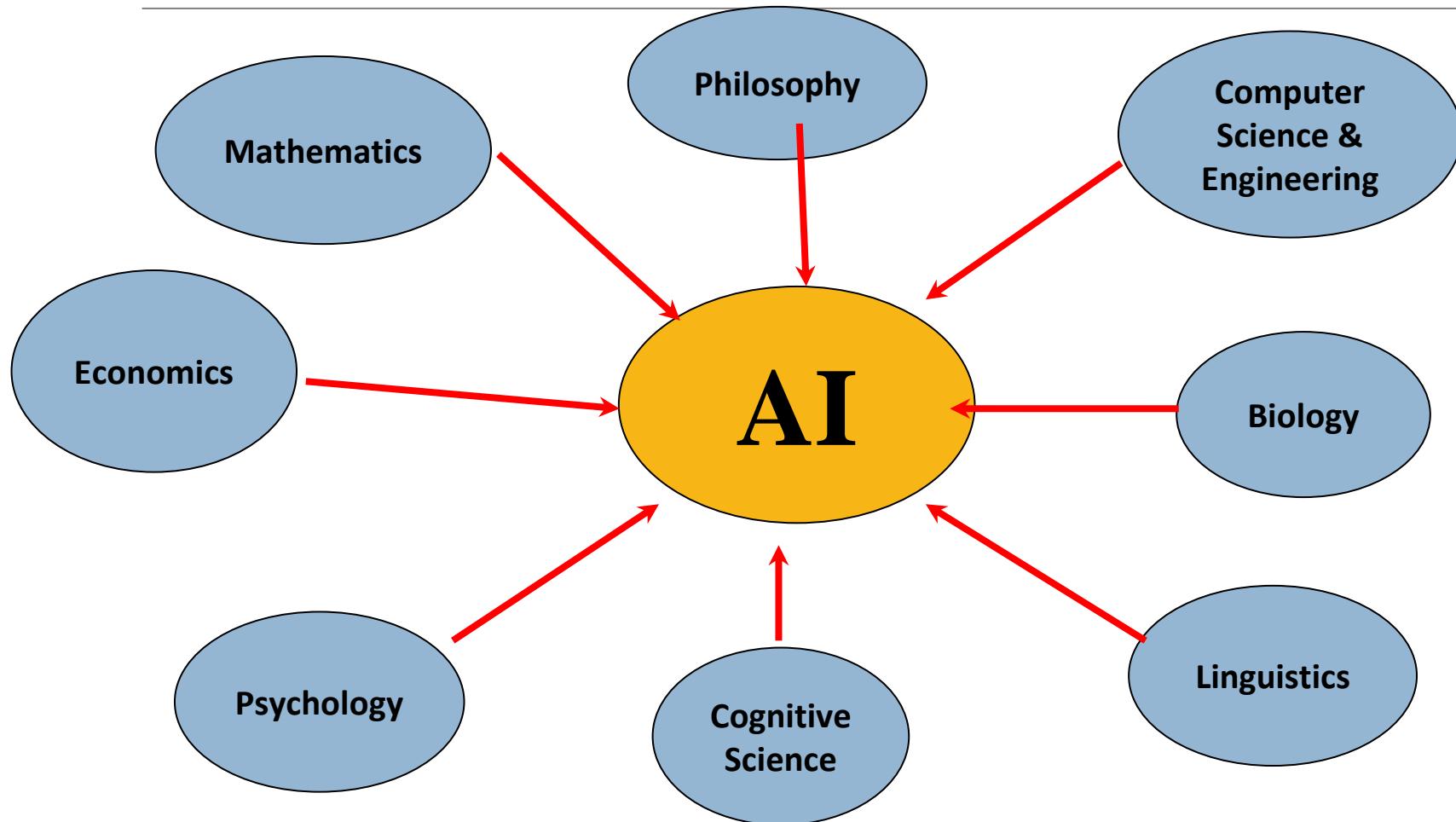
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- Acting rationally: The rational agent approach
- A rational agent is one that acts so as to achieve the best outcome or, when there is uncertainty, the best expected outcome.



# Foundations of AI

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# Foundations of AI

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- **Philosophy** Logic, methods of reasoning, mind as physical system foundations of learning, language, rationality
- **Mathematics** Formal representation and proof algorithms, computation, (un)decidability, (in)tractability, probability
- **Economics** utility, decision theory
- **Neuroscience** physical substrate for mental activity
- **Psychology** phenomena of perception and motor control, experimental techniques
- **Computer engineering** building fast computers
- **Control theory** design systems that maximize an objective function over time
- **Linguistics** knowledge representation, grammar

# Foundations of AI-Philosophy

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- Where does knowledge come from?
- How does knowledge lead to action?
- Aristotle (384–322 B.C.): was the first to formulate a precise set of laws governing the rational part of the mind.
- Thomas Hobbes (1588–1679) proposed that reasoning was like numerical computation, that “we add and subtract in our silent thoughts.”
- Rene Descartes(1596-1650): Developed dualistic theory of mind and matter. Descartes attempted to demonstrate the existence of god and the distinction between the human soul and body.
- The empiricism movement, starting with Francis Bacon’s (1561– 1626).
- The confirmation theory of Carnap and Carl Hempel (1905–1997) attempted to analyze the acquisition of knowledge from experience.
- Carnap’s book The Logical Structure of the World (1928) defined an explicit computational procedure for extracting knowledge from elementary experiences. It was probably the first theory of mind as a computational process.

# Foundations of AI- Mathematics

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- What are the formal rules to draw valid conclusions?
- What can be computed?
- George Boole (1815–1864), who worked out the details of propositional, or Boolean, logic (Boole, 1847).
- In 1879, Gottlob Frege (1848–1925) extended Boole's logic to include objects and relations, creating the first order logic that is used today.
- The first nontrivial algorithm is thought to be Euclid's algorithm for computing greatest common divisors.
- Besides logic and computation, the third great contribution of mathematics to AI is the PROBABILITY theory of probability. The Italian Gerolamo Cardano (1501–1576) first framed the idea of probability, describing it in terms of the possible outcomes of gambling events.
- Thomas Bayes (1702–1761) proposed a rule for updating probabilities in the light of new evidence. Bayes' rule underlies most modern approaches to uncertain reasoning in AI systems.

# Foundations of AI- Economics

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- How should we make decisions to maximize payoff?
- How should we do this when the payoff may be far in the future?
- The science of economics got its start in 1776, Smith was the first to treat it as a science, using the idea that economies can be thought of as consisting of individual agents maximizing their own economic well-being.
- Decision theory, which combines probability theory with utility theory, provides a formal and complete framework for decisions (economic or otherwise) made under uncertainty.
- Von Neumann and Morgenstern's development of game theory included the surprising result that, for some games, a rational agent should adopt policies that are (or least appear to be) randomized. Unlike decision theory, game theory does not offer an unambiguous prescription for selecting actions.

# Foundations of AI- Neuroscience

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- How do brains process information?
- Neuroscience is the study of the nervous system, particularly the brain.
- 335 B.C. Aristotle wrote, “Of all the animals, man has the largest brain in proportion to his size.”
- Nicolas Rashevsky (1936, 1938) was the first to apply mathematical models to the study of the nervous system.
- The measurement of intact brain activity began in 1929 with the invention by Hans Berger of the electroencephalograph (EEG).
- The recent development of functional magnetic resonance imaging (fMRI) (Ogawa et al., 1990; Cabeza and Nyberg, 2001) is giving neuroscientists unprecedentedly detailed images of brain activity, enabling measurements that correspond in interesting ways to ongoing cognitive processes.



# Foundations of AI - Psychology

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- How do humans and animals think and act?
  - Behaviorism movement, led by John Watson(1878-1958). Behaviorists insisted on studying only objective measures of the percepts(stimulus) given to an animal and its resulting actions(or response). Behaviorism discovered a lot about rats and pigeons but had less success at understanding human.
  - Cognitive psychology , views the brain as an information processing device.



# Foundations of AI- Computer Engineering

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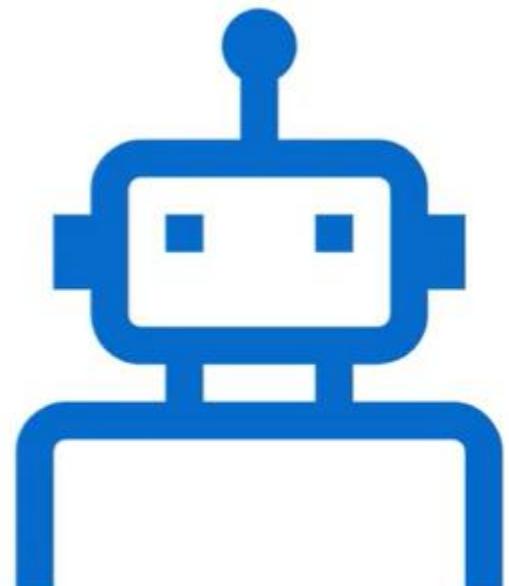
- How can we build an efficient computer?
- The first operational computer was the electromechanical Heath Robinson,<sup>8</sup> built in 1940 by Alan Turing's team for a single purpose: deciphering German messages.
- The first operational programmable computer was the Z-3, the invention of Konrad Zuse in Germany in 1941.
- The first electronic computer, the ABC, was assembled by John Atanasoff and his student Clifford Berry between 1940 and 1942 at Iowa State University.
- The first programmable machine was a loom, devised in 1805 by Joseph Marie Jacquard (1752–1834), that used punched cards to store instructions for the pattern to be woven.



# Foundations of AI- Control theory and Cybernetics

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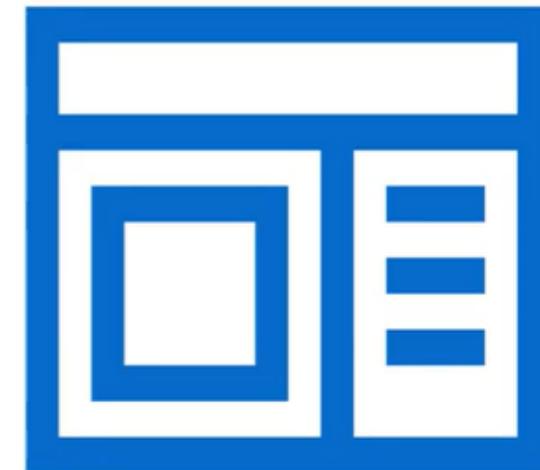
- How can artifacts operate under their own control?
  - Ktesibios of Alexandria (c. 250 B.C.) built the first self-controlling machine: a water clock with a regulator that maintained a constant flow rate. This invention changed the definition of what an artifact could do.
  - Modern control theory, especially the branch known as stochastic optimal control, has as its goal the design of systems that maximize an objective function over time. This roughly **OBJECTIVE FUNCTION** matches our view of AI: designing systems that behave optimally.



# Foundations of AI-Linguistics

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- How does language relate to thought?
  - In 1957, B. F. Skinner published *Verbal Behavior*. This was a comprehensive, detailed account of the behaviorist approach to language learning, written by the foremost expert in the field.
  - Noam Chomsky, who had just published a book on his own theory, *Syntactic Structures*. Chomsky pointed out that the behaviorist theory did not address the notion of creativity in language.
  - Modern linguistics and AI, then, were “born” at about the same time, and grew up together, intersecting in a hybrid field called computational linguistics or natural language processing.



# History of Artificial Intelligence

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- 1943 McCulloch & Pitts: Boolean circuit model of brain
- 1950 Turing's "Computing Machinery and Intelligence"
- **1956** Dartmouth meeting: "Artificial Intelligence" adopted
- 1952—69 Look, Ma, no hands!
- 1950s Early AI programs, including Samuel's checkers program, Newell & Simon's Logic Theorist, Gelernter's Geometry Engine
- 1965 Robinson's complete algorithm for logical reasoning
- 1966—73 AI discovers computational complexity  
Neural network research almost disappears
- 1969—79 Early development of knowledge-based systems
- 1980-- AI becomes an industry
- 1986-- Neural networks return to popularity
- 1987-- AI becomes a science
- 1995-- The emergence of intelligent agents

# History of Artificial Intelligence

## Stone age (1943-1956)

- Early work on neural networks and logic (Herbert Simon, 1943)
- Birth of AI: Dartmouth workshop - summer 1956
- John McCarthy's name for the field: artificial intelligence



**Herbert Simon in 1991**

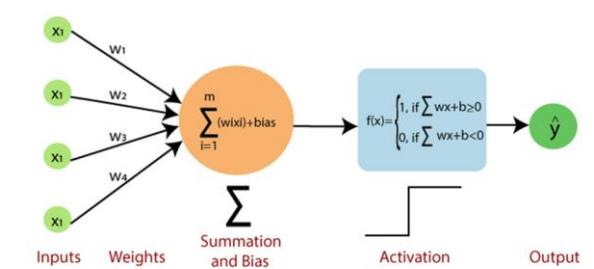


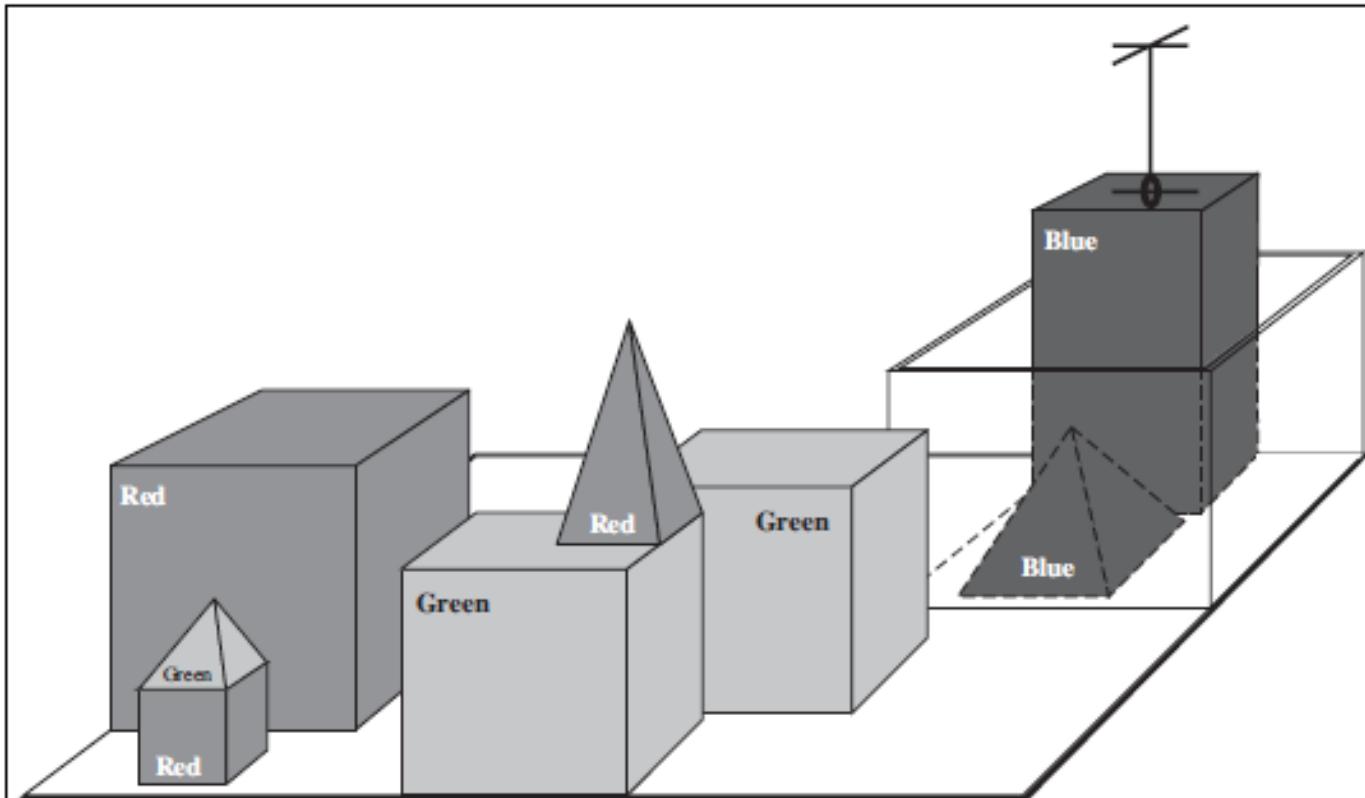
**John McCarthy in AAAI-2002**

# Early enthusiasm, great expectations (1952-1969)

## Dark ages (1969-1973) Why?

- AI did not scale up: combinatorial explanation.
- Failure of natural language translation approach based on simple grammars and word dictionary.
- Funding for natural language processing stopped.
- Failure of perceptron to learn such a simple function.
- Realization of the difficulty of the learning process.
- There is no Symbolic concept learning.





**Figure 1.4** A scene from the blocks world. SHRDLU (Winograd, 1972) has just completed the command “Find a block which is taller than the one you are holding and put it in the box.”

- The most famous microworld was the blocks world, which consists of a set of solid blocks placed on a tabletop (or more often, a simulation of a tabletop)
- A typical task in this world is to rearrange the blocks in a certain way, using a robot hand that can pick up one block at a time.

# Renaissance (1969-1979)

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Change of problem solving paradigm: From search-based problem solving to knowledge-based problem solving.

## Industrial age (1980-present)

- Building expert systems with formal knowledge acquisition techniques.
- There exists successful commercial expert systems.
- Many AI companies.
- Exploration of different learning strategies.
- Reasoning, Genetic algorithms, Neural networks, etc.)

# The Maturity and return of neural networks (1986-1995)

- Many successful applications of neural networks , machine learning, and data mining.
- Base claims on theorems and experiments rather than on intuition.
- Show relevance to real-world applications rather than toy examples.
- The reinvention of the back propagation learning algorithm for neural networks and other optimization process.



# Intelligent agents (1995-present)

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- The realization that the previously isolated subfields of AI (speech recognition, planning, robotics, computer vision, machine learning, knowledge representation, etc.) need to be reorganized when their results are to be tied together into a single agent design.
- A process of reintegration of different sub-areas of AI to build a “whole agent”:

**Multi-agent systems**--Agents for different types of applications, web search engine agents.

- 1997: The Deep Blue chess program beats the current world chess champion, Garry Kasparov, in a widely followed match.

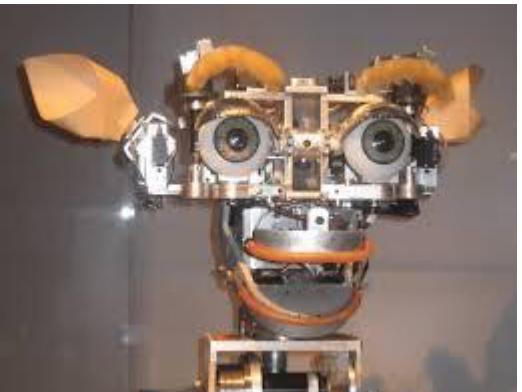


- First official Robo-Cup soccer match featuring table-top matches with 40 teams of interacting robots and over 5000 spectators.



- Late 90's: Web crawlers and other AI-based information extraction programs become essential in widespread use of the world-wide-web.
- Demonstration of an Intelligent Room and Emotional Agents at MIT's AI Lab.
- Initiation of work on the Oxygen Architecture, which connects mobile and stationary computers in an adaptive network.

- 2000: Interactive robot pets (a.k.a. "smart toys") become commercially available, realizing the vision of the 18th cen. novelty toy makers.
- Cynthia Breazeal at MIT publishes her dissertation on Sociable Machines, describing KISMET, a robot with a face that expresses emotions.



# Questions

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1. Define in your own words: (a) intelligence, (b) artificial intelligence, (c) agent, (d) rationality, (e) logical reasoning.
2. Is AI a science, or is it engineering? Or neither or both? Explain.
3. “Surely computers cannot be intelligent—they can do only what their programmers tell them.” Is the latter statement true, and does it imply the former?
4. “Surely animals, humans, and computers cannot be intelligent—they can do only what their constituent atoms are told to do by the laws of physics.” Is the latter statement true, and does it imply the former?

# Questions

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**Examine the AI literature to discover whether the following tasks can currently be solved by computers:**

- a. Playing a decent game of table tennis (Ping-Pong).
- b. Driving in the center of Cairo, Egypt.
- c. Driving in Victorville, California.
- d. Buying a week's worth of groceries at the market.
- e. Buying a week's worth of groceries on the Web.
- f. Playing a decent game of bridge at a competitive level.
- g. Discovering and proving new mathematical theorems.
- h. Writing an intentionally funny story.
- i. Giving competent legal advice in a specialized area of law.
- j. Translating spoken English into spoken Swedish in real time.
- k. Performing a complex surgical operation.

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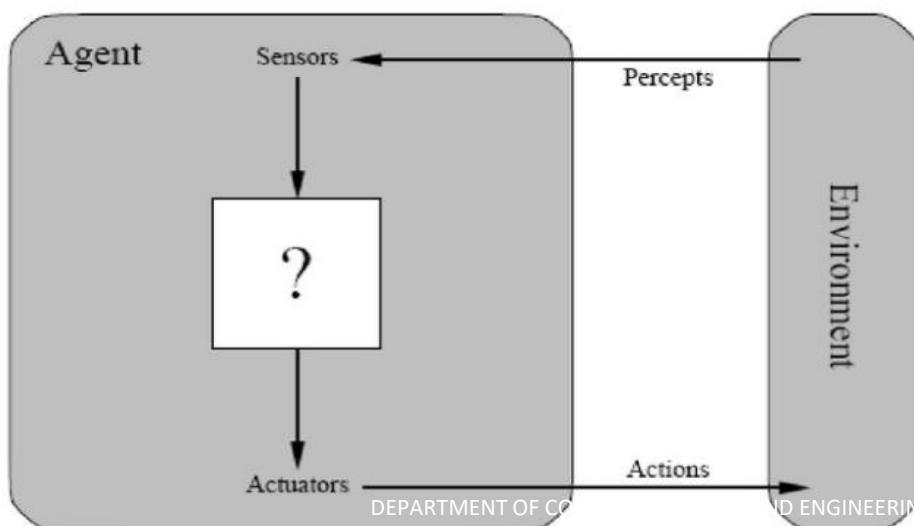
Informed Search Strategies

Heuristic Functions

# Agents

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- An **agent** is anything that can be viewed as **perceiving** its environment through **sensors** and **acting** upon that environment through **actuators**
  - Perceive the environment through **sensors** ( $\rightarrow$ Percepts)
  - Act upon the environment through **actuators** ( $\rightarrow$ Actions)



# Agents

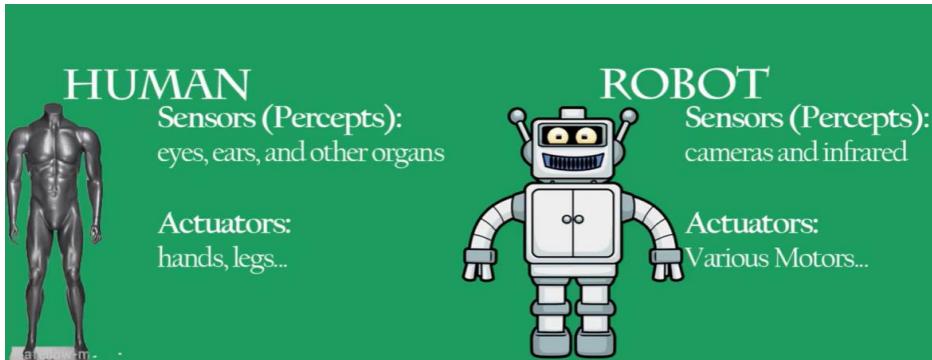
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- Examples:

- Human agent

- Robotic agent

- Software agent

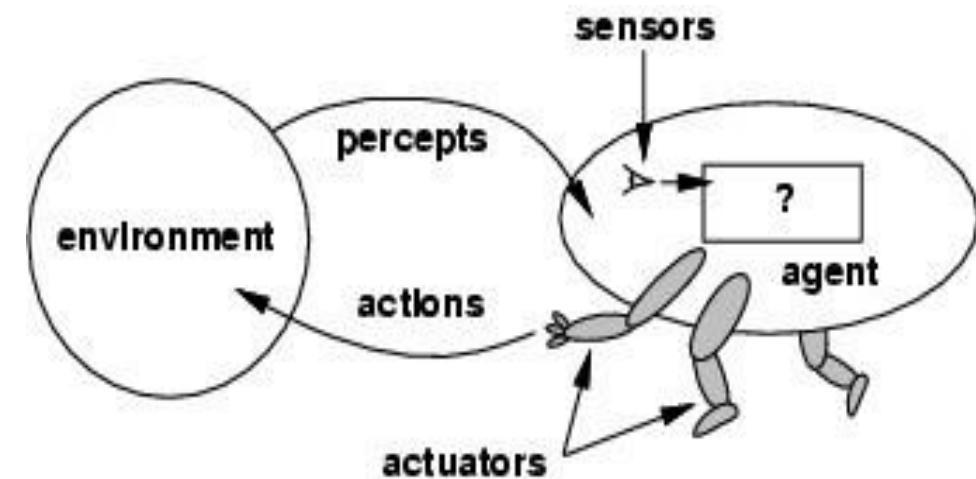


- Receives keystrokes as sensory inputs and acts on the environment by displaying on the screen
      - Receives file contents as sensory inputs and acts on the environment by writing files
      - Receives network packets as sensory inputs and acts on the environment by sending network packets.

# Agents

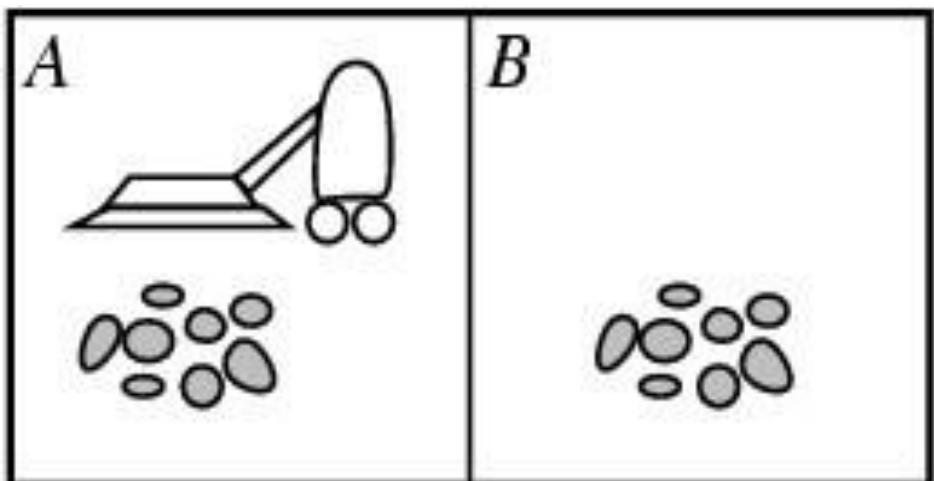
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- **Percept**: the agent's perceptual inputs at any given instant
- **Percept sequence**: the complete history of everything the agent has perceived
- **Agent function** maps any given percept sequence to an action
- **Agent program** runs on the physical architecture to produce
- **Agent = architecture + program**



# Agents -> Example : Vacuum-Cleaner World

- **Percepts:** location and contents, e.g., [A, dirty]
- **Actions:** Left, Right, Suck, NoOp



Percept sequence	Action
[A, Clean]	Right
[A, Dirty]	Suck
[B, Clean]	Left
[B, Dirty]	Suck
[A, Clean], [A, Clean]	Right
[A, Clean], [A, Dirty]	Suck
:	:
[A, Clean], [A, Clean], [A, Clean]	Right
[A, Clean], [A, Clean], [A, Dirty]	Suck
:	:

Partial tabulation of a simple agent function for the vacuum-cleaner world

# Rationality

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- An agent should "**do the right thing**", based on what it can perceive and the actions it can perform. The right action is the one that will cause the agent to be most successful
- **Performance measure:** An **objective criterion for success of an agent's behavior**
- Back to the vacuum-cleaner example
  - **Amount of dirt cleaned within certain time**
  - +1 credit for each clean square per unit time
- General rule: measure what one wants rather than how one thinks the agent should behave

# Rationality- Rational Agent

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What is rational at any given time depends on four things:

- The performance measure that defines the criterion of success.
- The agent's prior knowledge of the environment.
- The actions that the agent can perform.
- The agent's percept sequence to date.
- Definition:
  - For each possible percept sequence, a rational agent should select an action that is expected to maximize its performance measure, given the evidence provided by the percept sequence and whatever built-in knowledge the agent has.

# Rationality –Vacuum Cleaner Example

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- A simple agent that cleans a square if it is dirty and moves to the other square if not
- Is it rational?
- **Assumption:**
  - performance measure: 1 point for each clean square at each time step
  - The “geography” of the environment is known a priori
  - **actions = {left, right, suck, no-op}**
  - agent is able to perceive the location and dirt in that location

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## Rationality - Omniscience, Learning and Autonomy

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- Omniscience is the state of possessing unlimited knowledge about all things possible.
- Omniscience is knowing everything
- Expert chess player exemplifies a kind of omniscience by determining his/her opponent's moves, but each possible move opens up certain countermoves.
- An omniscient agent knows the actual outcome of its actions and can act accordingly; but omniscience is impossible in reality.

## Rationality - Omniscience, Learning and Autonomy

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- Distinction between rationality and **omniscience**
  - expected performance vs. actual performance
- Agents can perform actions in order to modify future percepts so as to obtain useful information (**information gathering, exploration**)
- An agent can also **learn** from what it perceives
- An agent is **autonomous** if its behavior is determined by its own experience (with ability to learn and adapt)

# The Nature of Environments

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To build rational agents - Think about task environments are the “problems” to which rational agents are the “solutions.”

- How to specify a task environment, illustrating the process with a number of examples.
- Task environments come in a variety of flavors.
- The flavor of the task environment directly affects the appropriate design for the agent program.

# The Nature of Environments

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- Specifying the task environment is always the first step in designing agent
- **PEAS**: **P**erformance, **E**nvironment, **A**ctuators, **S**ensors

**P**      **Performance** – how we measure the system's achievements

**E**      **Environment** – what the agent is interacting with

**A**      **Actuators** – what produces the outputs of the system

**S**      **Sensors** – what provides the inputs to the system

# Taxi Driver Example

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Agent Type	Performance Measure	Environment	Actuators	Sensors
Taxi driver	Safe, fast, legal, comfortable trip, maximize profits	Roads, other traffic, pedestrians, customers	Steering, accelerator, brake, signal, horn, display	Cameras, sonar, speedometer, GPS, odometer, accelerometer, engine sensors, keyboard
PEAS description of the task environment for an automated taxi.				

# Mushroom-Picking Robot

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<b>Performance Measure</b>	<b>Environment</b>	<b>Actuators</b>	<b>Sensors</b>
Percentage of good mushrooms in correct bins	Conveyor belt with mushrooms, bins	Jointed arm and hand	camera, joint angle sensors



# Medical Diagnosis System

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<b>Performance Measure</b>	<b>Environment</b>	<b>Actuators</b>	<b>Sensors</b>
healthy patient, minimize costs, lawsuits	patient, hospital, staff	display questions, tests, diagnosis, treatments, referrals	keyboard entry of symptoms , findings, patient's answers





Agent Type	Performance Measure	Environment	Actuators	Sensors
Medical diagnosis system	Healthy patient, reduced costs	Patient, hospital, staff	Display of questions, tests, diagnoses, treatments, referrals	Keyboard entry of symptoms, findings, patient's answers
Satellite image analysis system	Correct image categorization	Downlink from orbiting satellite	Display of scene categorization	Color pixel arrays
Part-picking robot	Percentage of parts in correct bins	Conveyor belt with parts; bins	Jointed arm and hand	Camera, joint angle sensors
Refinery controller	Purity, yield, safety	Refinery, operators	Valves, pumps, heaters, displays	Temperature, pressure, chemical sensors
Interactive English tutor	Student's score on test	Set of students, testing agency	Display of exercises, suggestions, corrections	Keyboard entry

Examples of agent types and their PEAS descriptions.

# Properties of Task Environments

---

- Fully observable vs partially observable
- Deterministic vs stochastic
- Episodic vs sequential
- Static vs dynamic
- Discrete vs continuous
- Single agent vs multiagent

|

# Fully observable vs partially observable

---

- If an agent's sensors give it access to the complete state of the environment at each point in time, then we say that the task environment is fully observable.
- A task environment is effectively fully observable if the sensors detect all aspects that are relevant to the choice of action; **relevance**(depends on the performance measure.)
- Fully observable environments are convenient because the agent need not maintain any internal state to keep track of the world.
- An environment might be partially observable because of noisy and inaccurate sensors or because parts of the state are simply missing from the sensor data
- For example, a vacuum agent with only a local dirt sensor cannot tell whether there is dirt in other squares, and an automated taxi cannot see what other drivers are thinking.  
**If the agent has no sensors at all then the environment is unobservable.**

# Deterministic vs stochastic

---

- If the **next state of the environment** is completely **determined by the current state and the action executed by the agent**, then we say the environment is **deterministic**; otherwise, it is **stochastic**.
- **nondeterministic** environment is one in which actions are characterized by their possible outcomes, but no probabilities are attached to them.

# Episodic vs sequential

---

- In an episodic task environment, the agent's experience is divided into atomic episodes.
- In each episode the agent receives a percept and then performs a single action.
- Crucially, the next episode does not depend on the actions taken in previous episodes.
- Many classification tasks are episodic.
- For example, an agent that has to spot defective parts on an assembly line bases each decision on the current part, regardless of previous decisions; moreover, the current decision doesn't affect whether the next part is defective.
  
- In sequential environments, on the other hand, the current decision could affect all future decisions.
- Chess and taxi driving are sequential: in both cases, short-term actions can have long-term consequences. Episodic environments are much simpler than sequential environments because the agent does not need to think ahead.

# Static vs dynamic

---

- If the environment can change while an agent is deliberating, then we say the environment is **dynamic** for that agent; otherwise, it is static.
- Static environments are easy to deal with because the agent need not keep looking at the world while it is deciding on an action, nor need it worry about the passage of time.
- Crossword puzzles are static.
- Dynamic environments, on the other hand, are continuously asking the agent what it wants to do; if it hasn't decided yet, that counts as deciding to do nothing.
- Taxi driving is clearly dynamic: the other cars and the taxi itself keep moving while the driving algorithm dithers about what to do next.
- If the environment itself does not change with the passage of time but the agent's performance score does, then we say the environment is **semidynamic**.
- Chess, when played with a clock, is **semidynamic**.

## Discrete vs continuous

---

- The discrete/continuous distinction applies to the *state* of the environment, to the way *time* is handled, and to the *percepts* and *actions* of the agent.
- For example, the chess environment has a finite number of distinct states (excluding the clock).
- Chess also has a **discrete set of percepts and actions**.
- Taxi driving is a **continuous-state and continuous-time problem**: the speed and location of the taxi and of the other vehicles sweep through a range of continuous values and do so smoothly over time. Taxi-driving actions are also continuous (steering angles, etc.).
- Input from digital cameras is discrete but is typically treated as representing continuously varying intensities and locations.

## Known vs. unknown

---

- In a known environment, the outcomes (or outcome probabilities if the environment is stochastic) for all actions are given. Obviously, if the environment is unknown
- the agent will have to learn how it works in order to make good decisions.

## Known

- In a known environment, the results for all actions are known to the agent.
- Example: Card game



## Unknown

- In unknown environment, agent needs to learn how it works in order to perform an action.
- Example: A new video game



## **Single agent vs multiagent**

---

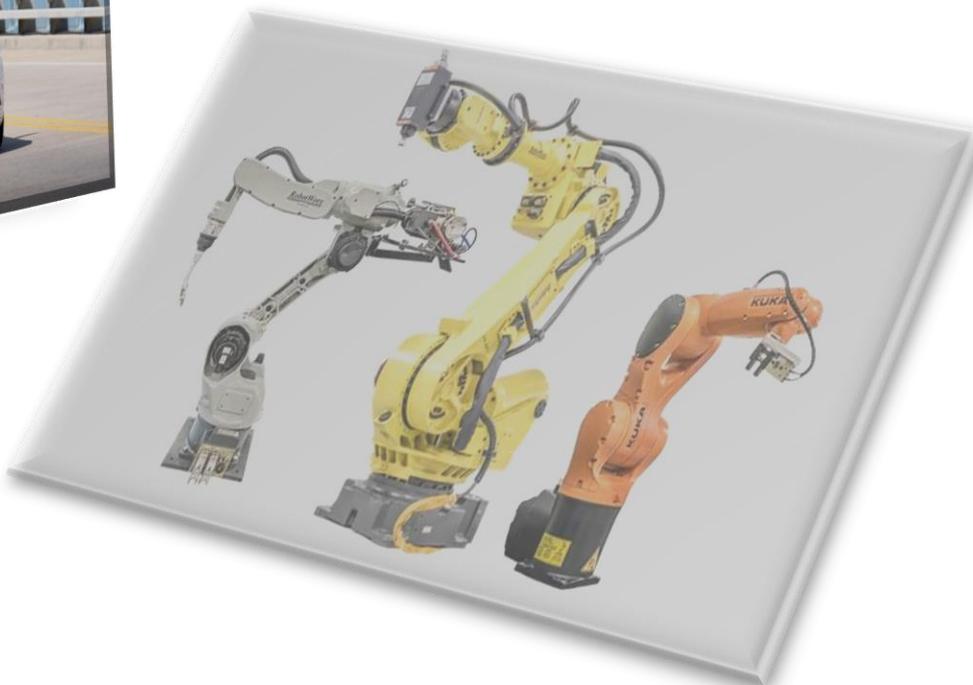
- For example, an agent solving a crossword puzzle by itself is clearly in a single-agent environment, whereas an agent playing chess is in a two agent environment.

# Examples

---

Task Environment	Observable	Agents	Deterministic	Episodic	Static	Discrete
Crossword puzzle	Fully	Single	Deterministic	Sequential	Static	Discrete
Chess with a clock	Fully	Multi	Deterministic	Sequential	Semi	Discrete
Poker	Partially	Multi	Stochastic	Sequential	Static	Discrete
Backgammon	Fully	Multi	Stochastic	Sequential	Static	Discrete
Taxi driving	Partially	Multi	Stochastic	Sequential	Dynamic	Continuous
Medical diagnosis	Partially	Single	Stochastic	Sequential	Dynamic	Continuous
Image analysis	Fully	Single	Deterministic	Episodic	Semi	Continuous
Part-picking robot	Partially	Single	Stochastic	Episodic	Dynamic	Continuous
Refinery controller	Partially	Single	Stochastic	Sequential	Dynamic	Continuous
Interactive English tutor	Partially	Multi	Stochastic	Sequential	Dynamic	Discrete
<b>Figure 2.6</b> Examples of task environments and their characteristics.						

- The environment type largely determines the agent design
- The real world is (of course) partially observable, stochastic, sequential, dynamic, continuous, multi-agent



# The Structure of Agents

---

- Let us understand the different kinds of agent programs and how to convert them into learning agents that can improvise their agent function and generate better actions.

---

The job of **AI** is to design an **agent program** that implements the **agent function**—the **mapping from percepts to actions**.

**Agent Program** will run on computing device with physical sensors and actuators—we call this the architecture:

**Agent = architecture + program .**



# Agent programs

---

The agent programs will have the same **skeleton**: they take the current percept as input from the sensors and return an action to the actuators

Difference between the

- Agent program takes the current percept as input
- Agent function takes the entire percept history.

Percept sequence	Action
[A, Clean]	Right
[A, Dirty]	Suck
[B, Clean]	Left
[B, Dirty]	Suck
[A, Clean], [A, Clean]	Right
[A, Clean], [A, Dirty]	Suck
:	:
[A, Clean], [A, Clean], [A, Clean]	Right
[A, Clean], [A, Clean], [A, Dirty]	Suck
:	:

Partial tabulation of a simple agent function for the vacuum-cleaner world

Figure 2.7 shows a trivial agent program that keeps track of the percept sequence and then uses it to index into a table of actions to decide what to do.

Table above represents explicitly the agent function that the agent program embodies.

```

function TABLE-DRIVEN-AGENT(percept) returns an action
  persistent: percepts, a sequence, initially empty
    table, a table of actions, indexed by percept sequences, initially fully specified
  append percept to the end of percepts
  action  $\leftarrow$  LOOKUP(percepts, table)
  return action

```

**Figure 2.7** The TABLE-DRIVEN-AGENT program is invoked for each new percept and returns an action each time. It retains the complete percept sequence in memory.

# Table-Driven Agent

---

- Designer needs to construct a table that contains the appropriate action for every possible percept sequence
  
- **Drawbacks?**
  - huge table
  - take a long time to construct such a table
  - no autonomy
  - Even with learning, need a long time to learn the table entries

# Basic Agent Types/Agent programs

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- Arranged in order of increasing generality:
  - Simple reflex agents
  - Model-based reflex agents
  - Goal-based agents
  - Utility-based agents
  - Learning agents

# Basic Agent Types

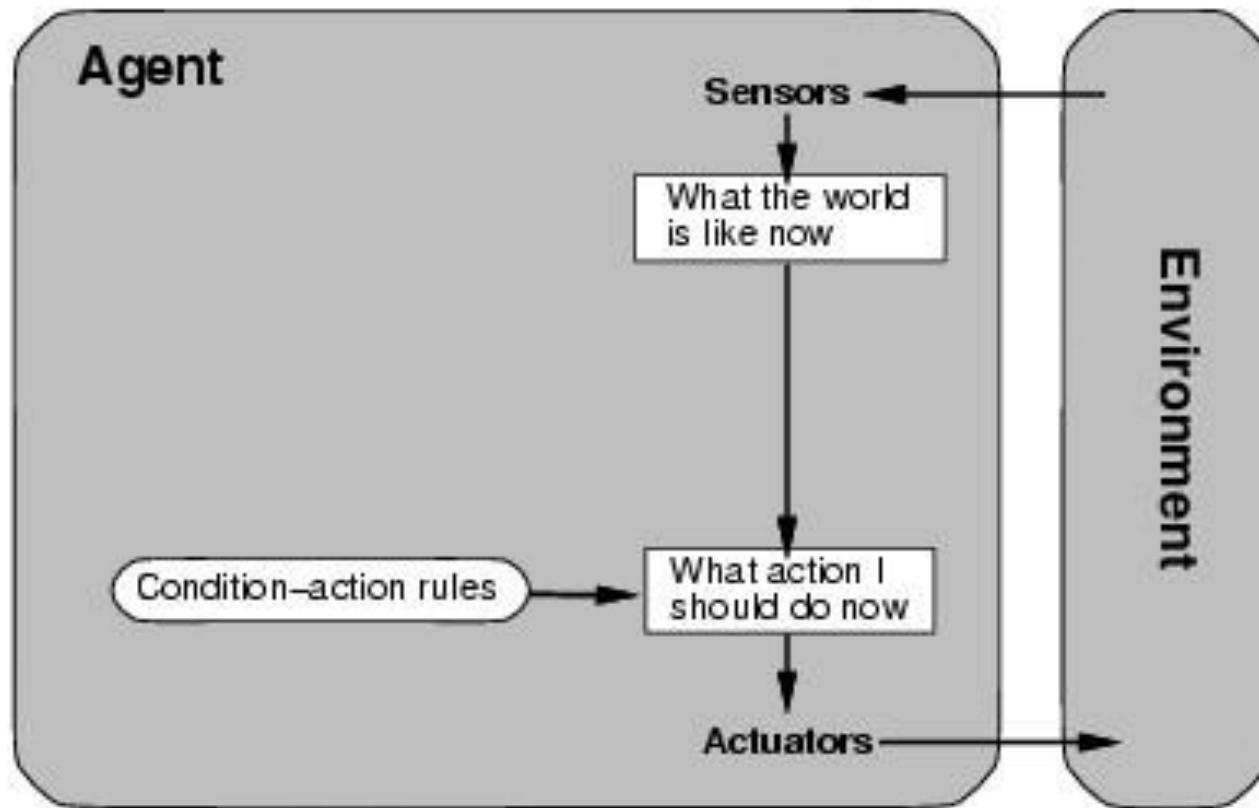
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## Simple Reflex Agent

- They choose actions only based on the **current situation** ignoring the history of perceptions.
- Perform actions only on simple situation.
- They will work only if the environment is **fully observable**
- The agent function is based on the **condition-action rule**: "if condition, then action".
- This can only be done based on the pre-determined rules that are present in the knowledge base
- **Example:** if car-in-front-brakes

# Simple Reflex Agent

---



# Five Basic Agent Types

---

## Simple reflex agents

Example: Medical diagnosis system

if the patient has reddish brown spots then start the treatment for measles.

INTERRUPT-INPUT – function generates an abstracted description of the current state from the percept.

RULE-MATCH – function returns the first rule in the set of rules that matches the given state description.

RULE-ACTION – the selected rule is executed as action of the given percept.

## Pseudo-Code

**function** SIMPLE-REFLEX-AGENT(*percept*) **returns** an action

**persistent:** *rules*, a set of condition–action rules

*state*  $\leftarrow$  INTERPRET-INPUT(*percept*)

*rule*  $\leftarrow$  RULE-MATCH(*state, rules*)

*action*  $\leftarrow$  *rule.ACTION*

**return** *action*

INTERRUPT-INPUT – function generates an abstracted description of the current state from the percept.

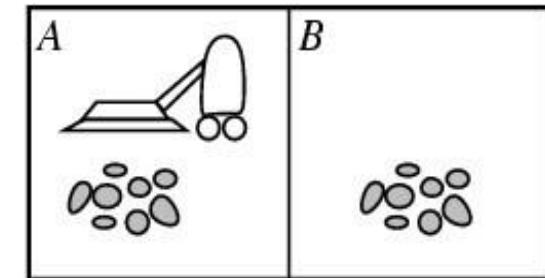
RULE-MATCH – function returns the first rule in the set of rules that matches the given state description.

RULE-ACTION – the selected rule is executed as action of the given percept.

## Pseudo-Code

**function** SIMPLE-REFLEX-AGENT(*percept*) **returns** an action  
**persistent:** *rules*, a set of condition–action rules

```
state  $\leftarrow$  INTERPRET-INPUT(percept)
rule  $\leftarrow$  RULE-MATCH(state, rules)
action  $\leftarrow$  rule.ACTION
return action
```



**function** REFLEX-VACUUM-AGENT([*location*,*status*]) **returns** an action

```
if status = Dirty then return Suck
else if location = A then return Right
else if location = B then return Left
```

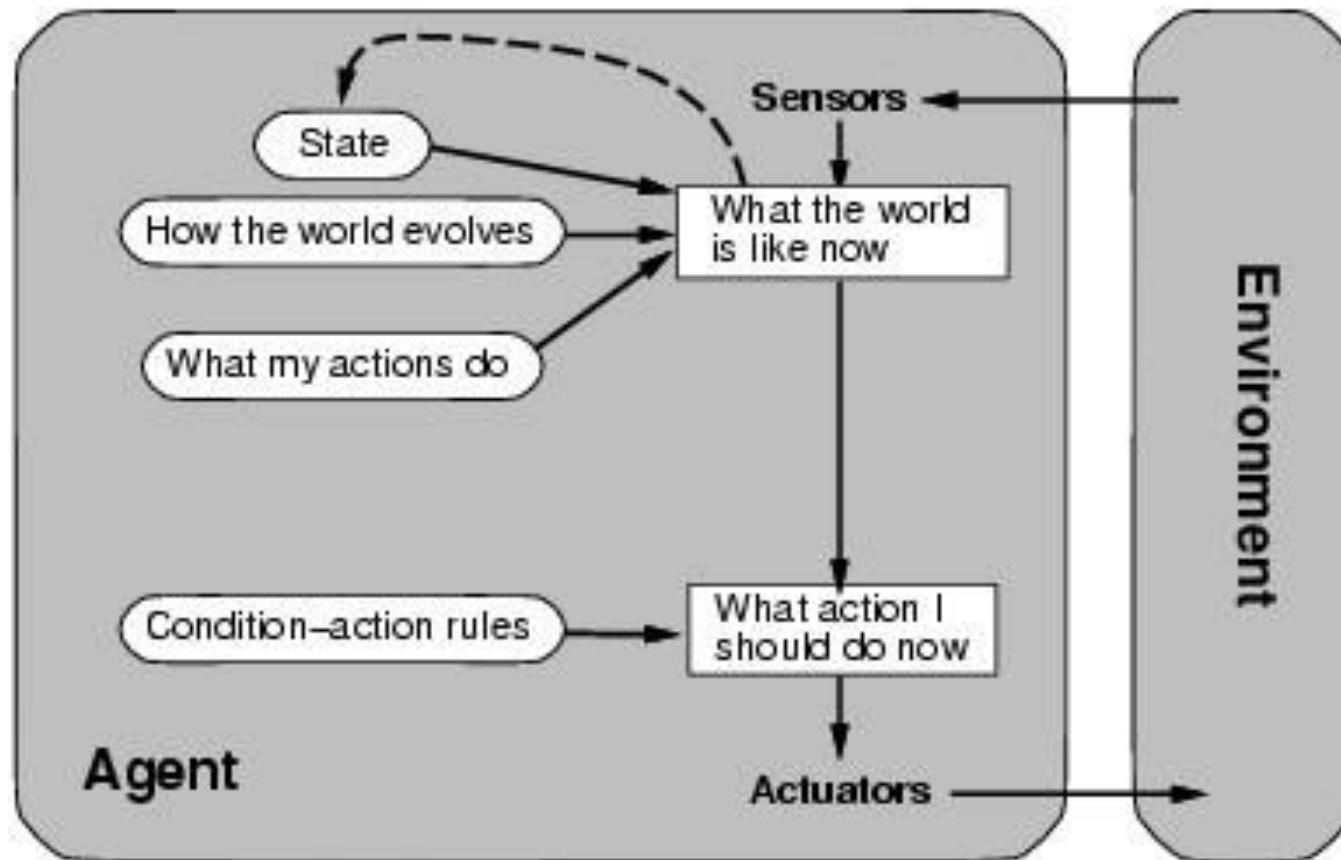
- 
- **Infinite loops** are often unavoidable for simple reflex agent operating in partially observable environments
    - No location sensor
  - **Randomization** will help
  - A randomized simple reflex agent might outperform a deterministic simple reflex agent
  - Better way: keep track of the part of the world it can't see now
    - Maintain internal states

# Model-Based Reflex Agent

---

- A model-based reflex agent is an intelligent agent that uses **percept history** and **internal memory** to make decisions about the "**model**" of the world around it.
- The Model-based agent can work in a **partially observable environment**, and track the situation.
- **Model** – knowledge about “how the things happen in the world”.
- **Internal State** – It is a representation of unobserved aspects of current state depending on percept history.
- **Updating the state requires the information about**
  - How the world evolves.
  - How the agent’s actions affect the world.

# Model-Based Reflex Agent



Agent should maintain some sort of **internal state** that depends on the percept history and thereby reflects at least some of the unobserved aspects of the current state.

# Model-Based Reflex Agent

---

Updating this internal state information requires two kinds of knowledge to be encoded in the agent program.

First, we need some information about how the world evolves independently of the agent—for example, that an overtaking car generally will be closer behind than it was a moment ago.

Second, we need some information about how the agent's own actions affect the world—for example, that when the agent turns the steering wheel clockwise, the car turns to the right, or that after driving for five minutes northbound on the freeway, one is usually about five miles north of where one was five minutes ago.

# Model-Based Reflex Agent

---

This knowledge about “how the world works”—whether implemented in simple Boolean circuits or in complete scientific theories—is called a **model** of the world.

An agent that uses such a model is called a **model-based agent**.

# Pseudo-Code

---

**function** MODEL-BASED-REFLEX-AGENT(*percept*) **returns** an action

**persistent:** *state*, the agent's current conception of the world state

*model*, a description of how the next state depends on current state and action

*rules*, a set of condition-action rules

*action*, the most recent action, initially none

*state*  $\leftarrow$  UPDATE-STATE(*state*, *action*, *percept*, *model*)

*rule*  $\leftarrow$  RULE-MATCH(*state*, *rules*)

*action*  $\leftarrow$  *rule.ACTION*

**return** *action*

---

# Goal-Based Agent

- They choose their actions in order to **achieve goals**.
- This allows the agent a way to choose among multiple possibilities, selecting the one which reaches a goal state.
- They usually require **search** and **planning**.
- Example : A GPS system finding a path to certain destination

# Basic Agent Types

---

## Goal-based reflex agents

- An agent knows the description of current state and also needs some sort of goal information that describes situations that are desirable.
- The action matches with the current state is selected depends on the goal state.
- The goal based agent is more flexible for more than one destination also.
- After identifying one destination, the new destination is specified, goal based agent is activated to come up with a new behavior.

# Basic Agent Types

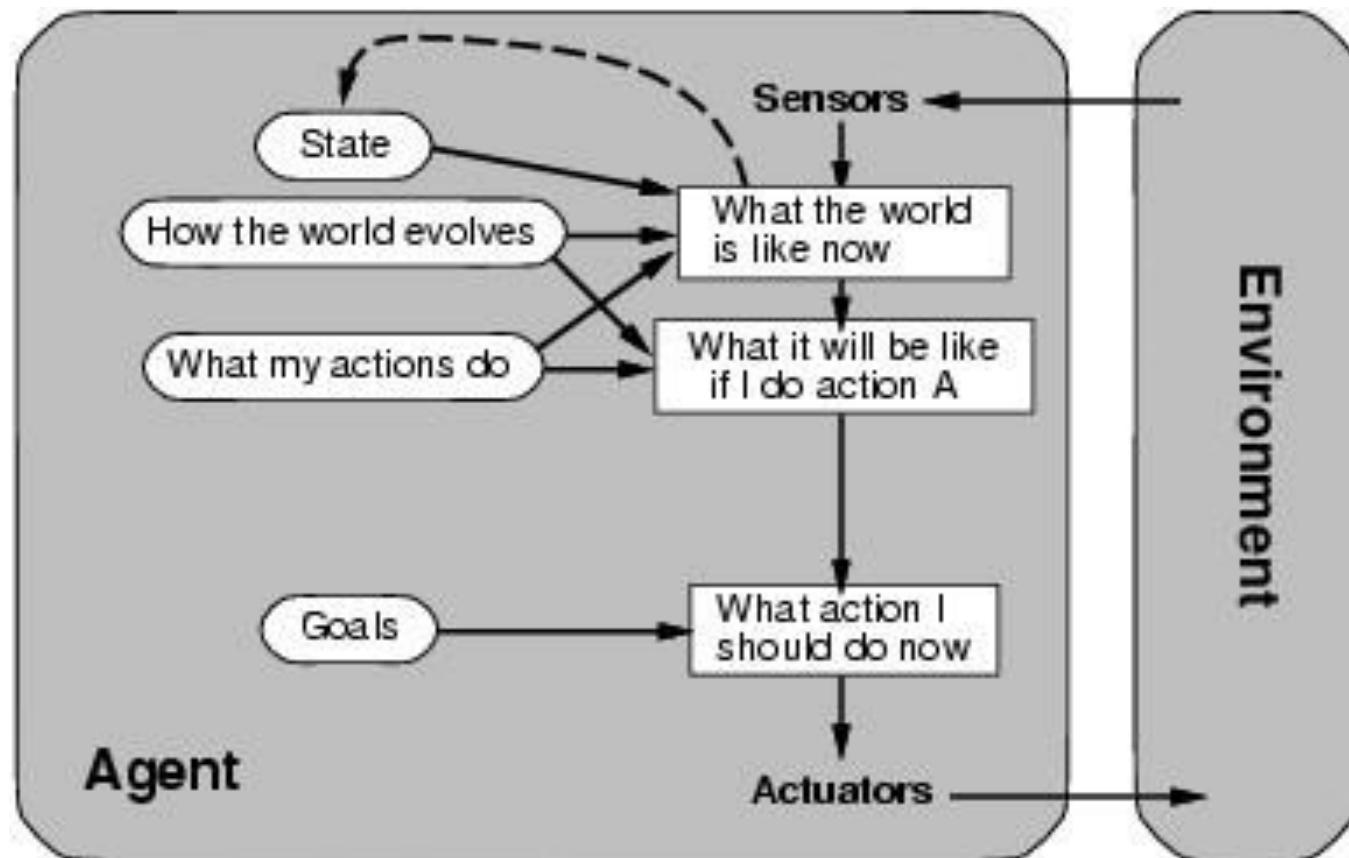
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## Goal-based reflex agents

- Search and Planning are the subfields of AI devoted to finding action sequences that achieve the agents goals.
- The goal-based agent appears less efficient,
- it is more flexible because the knowledge that supports its decisions is represented explicitly and can be modified.
- The goal-based agent's behavior can easily be changed to go to a different location.

# Goal-Based Agent

---



# Utility-Based Agent

- A utility-based agent is an agent that acts based not only on what the goal is, but the **best way** to reach that goal.
- They choose actions based on a preference (utility) for each state.
- **Example :** A GPS system finding a shortest/fastest/safer to certain destination.

# Basic Agent Types

---

## Utility-based reflex agents

- An agent generates a goal state with high – quality behavior (utility) that is, if more than one sequence exists to reach the goal state then the sequence with more reliable, safer, quicker and cheaper than others to be selected.
- A utility function maps a state (or sequence of states) onto a real number, which describes the associated degree of happiness.

# Basic Agent Types

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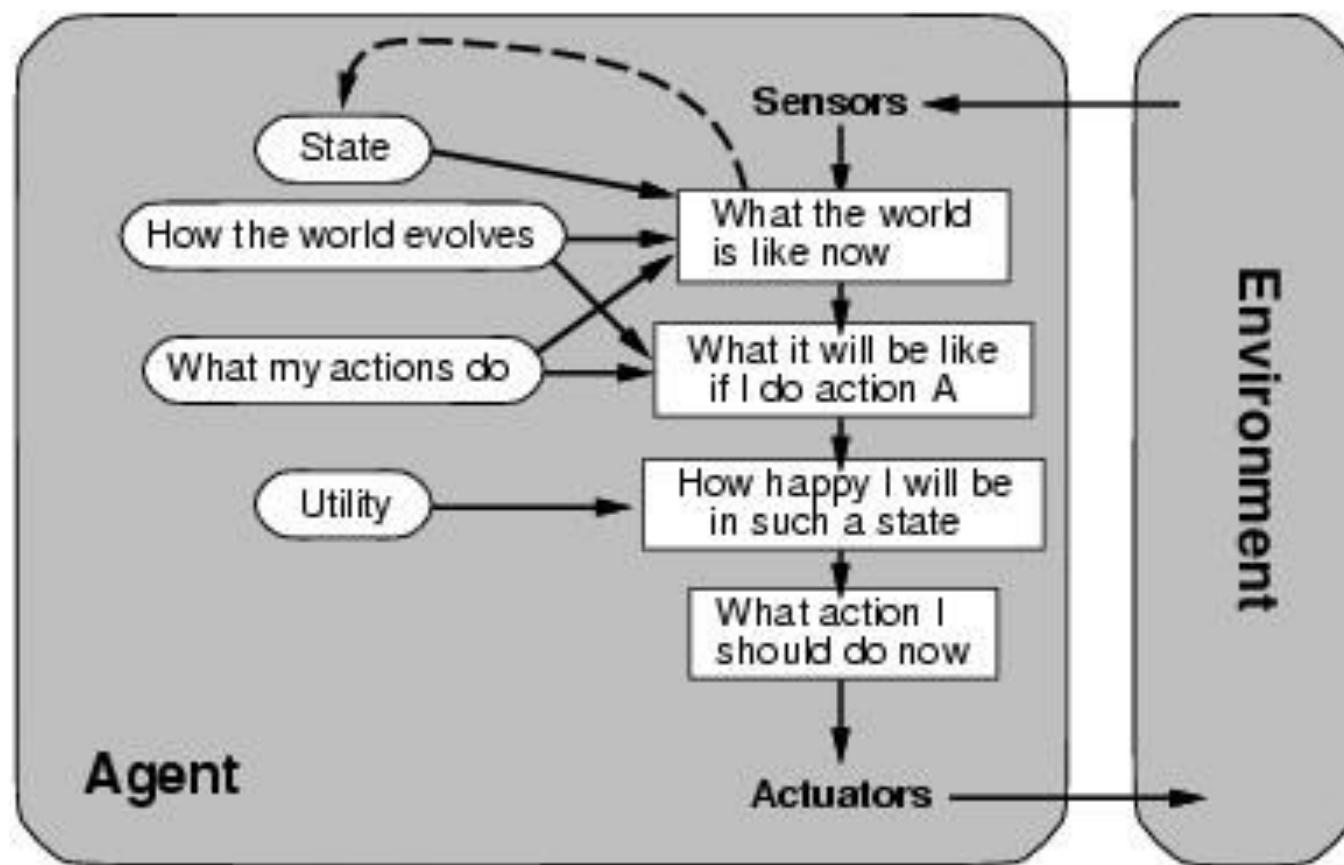
## Utility-based reflex agents

The utility function can be used for two different cases:

- First, when there are conflicting goals, only some of which can be achieved (for e.g., speed and safety), the utility function specifies the appropriate tradeoff.
- Second, when the agent aims for several goals, none of which can be achieved with certainty, then the success can be weighted up against the importance of the goals.

# Utility-Based Agent

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# Utility Function

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- Utility function maps a state or a sequence of states onto a real number  degree of happiness
  
- Conflicting goals
  - Speed and safety
- Multiple goals

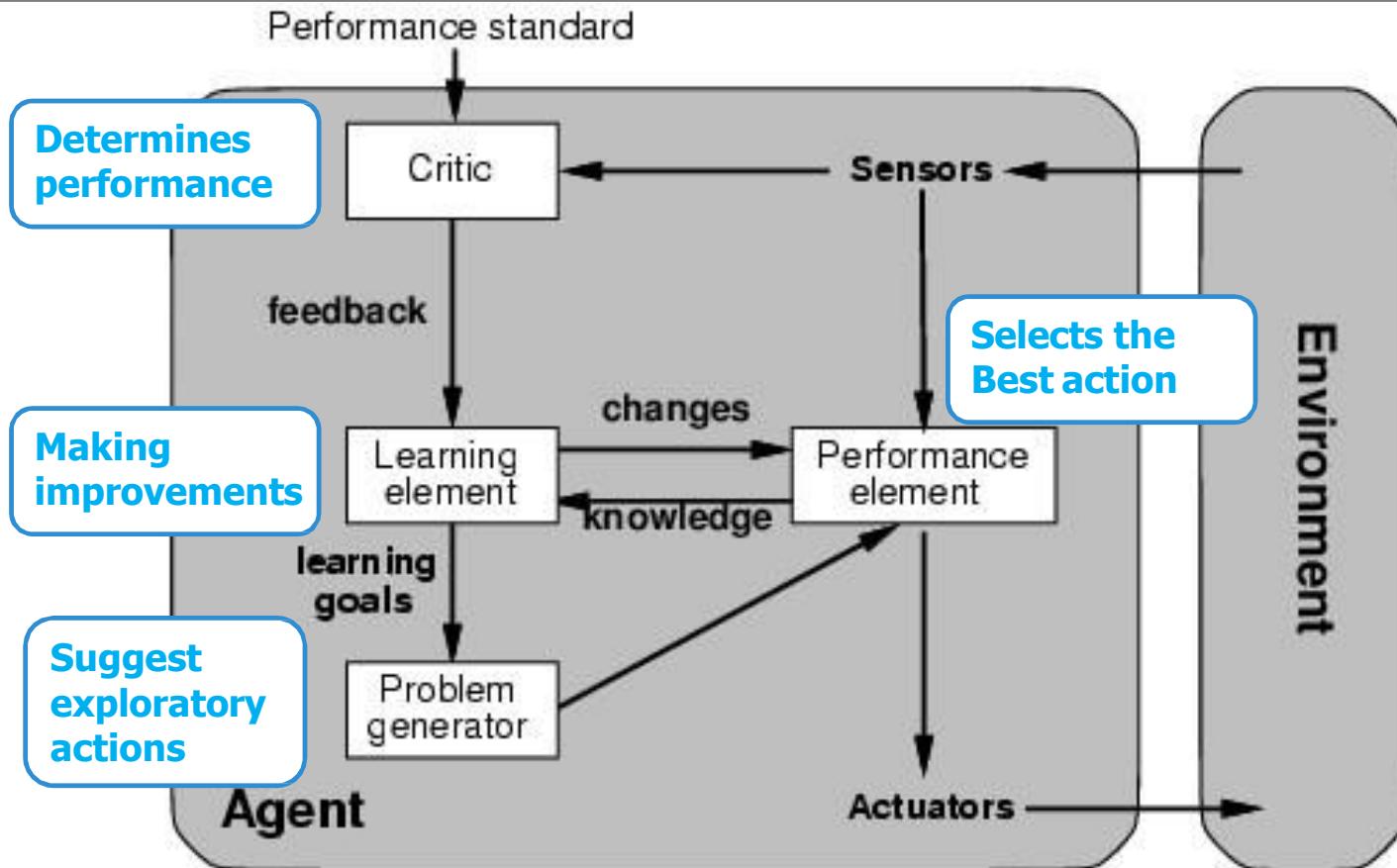
# Learning Agent

---

## Why would we want an agent to learn?

- First, the designers cannot anticipate all possible situations that the agent might find itself in.
  - For example, a robot designed to navigate mazes must learn the layout of each new maze it encounters.
- Second, the designers cannot anticipate all changes over time
- Third, sometimes human programmers have no idea how to program a solution themselves.

# Learning Agent



# Forms of Learning

---

A Learning agent learn from its past experiences or it has learning capabilities.

Four components of an agent are

**Performance element**: Selects external action :Takes in percepts and decides on actions

**Learning element** :It is responsible for making improvements by observing performance

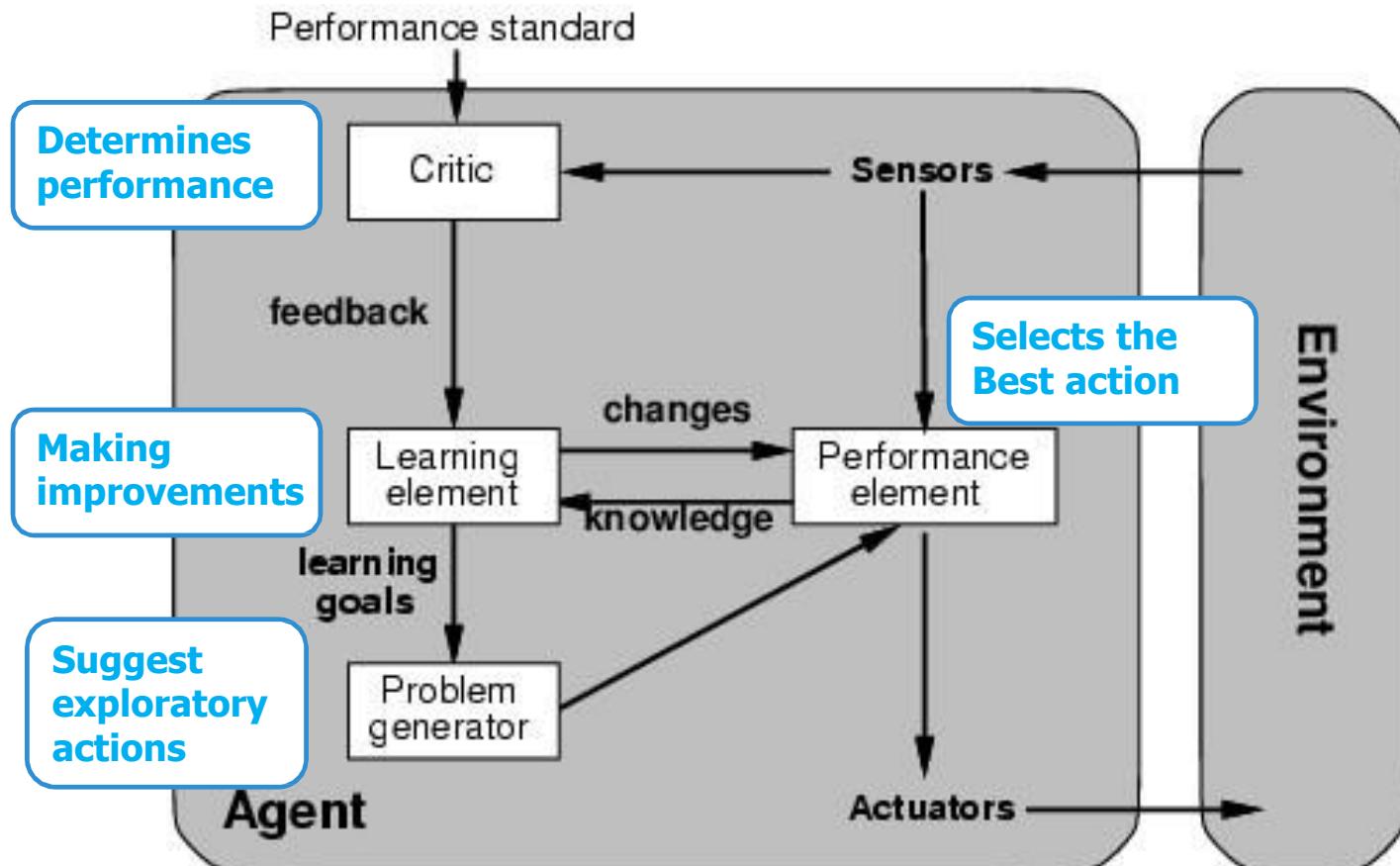
**Critic**: Learning element takes feedback from critic which describes how well the agent is doing with respect to a fixed performance standard.

**Problem Generator**: This component is responsible for suggesting actions that will lead to new and informative experiences.

# Forms of Learning

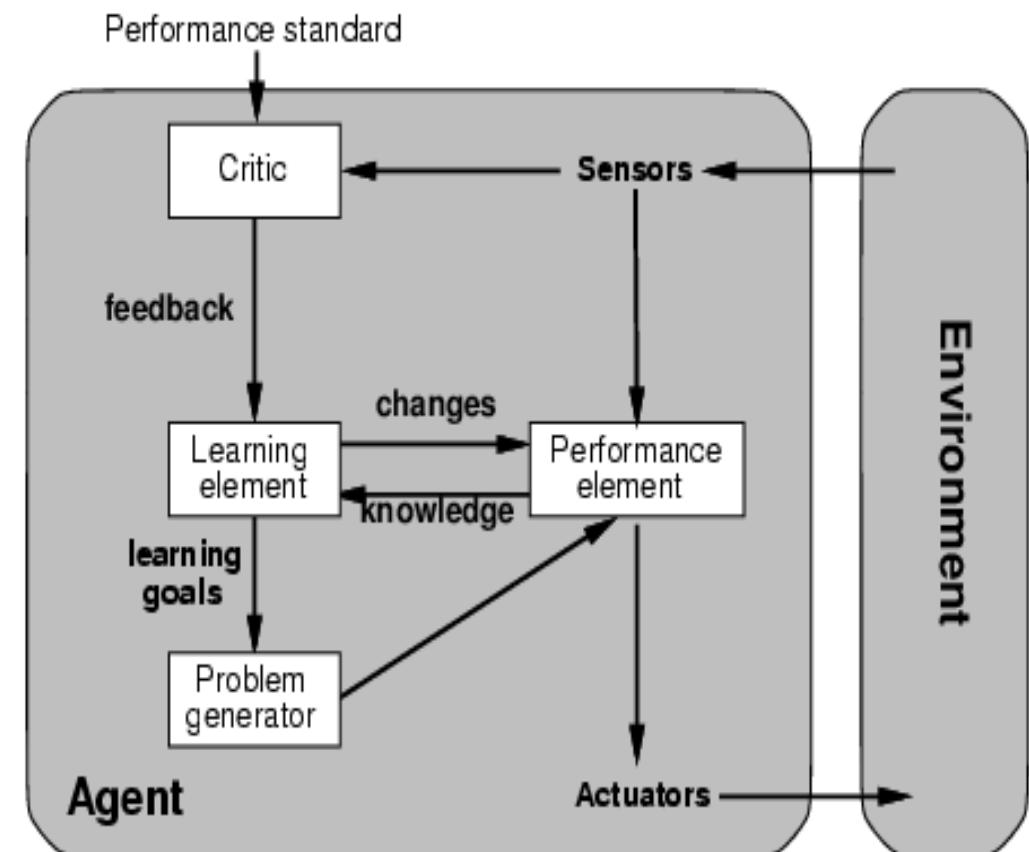
A learning agent in AI is the type of agent that can learn from its past experiences or it has learning capabilities.

It starts to act with basic knowledge and then is able to act and adapt automatically through learning.



# Components Learning Agent

- Learning element
- Performance element
- Critic
- Problem generator

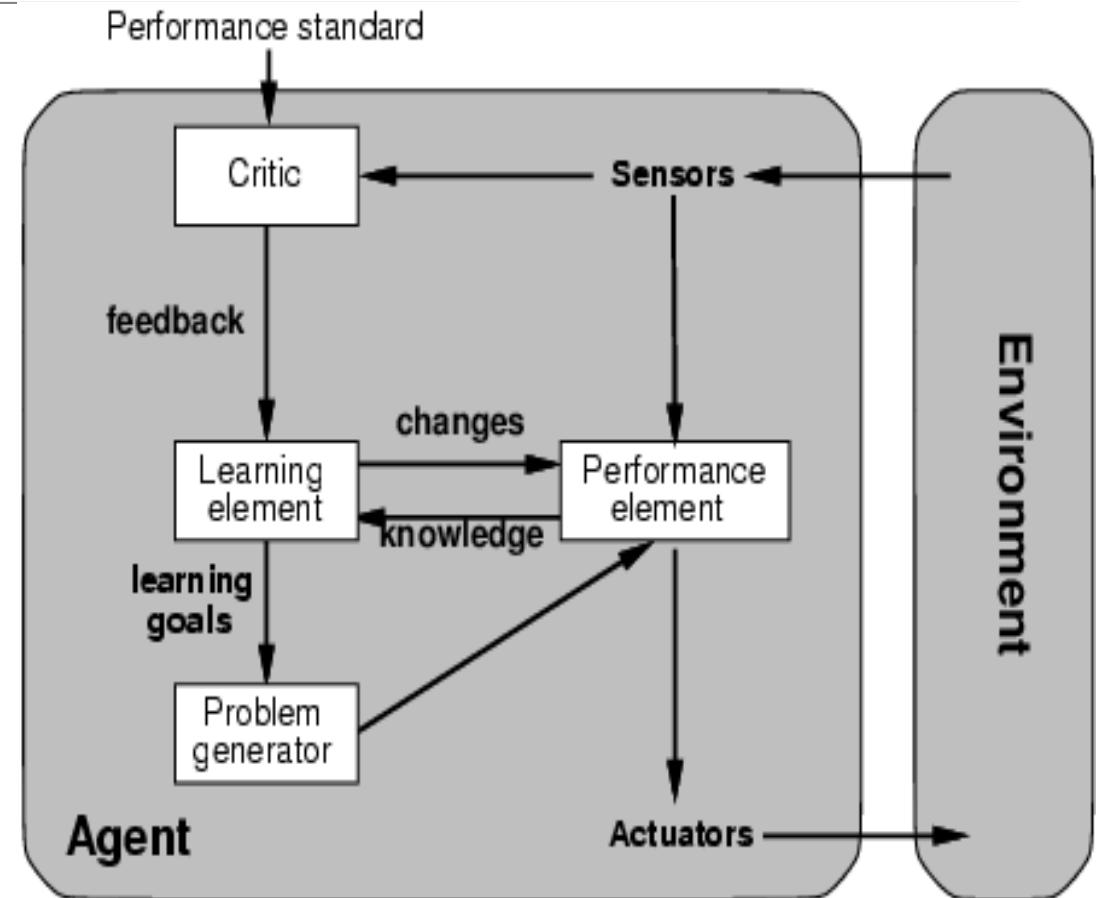


# Performance Element

Selects external actions

Collects percepts, decides  
on actions

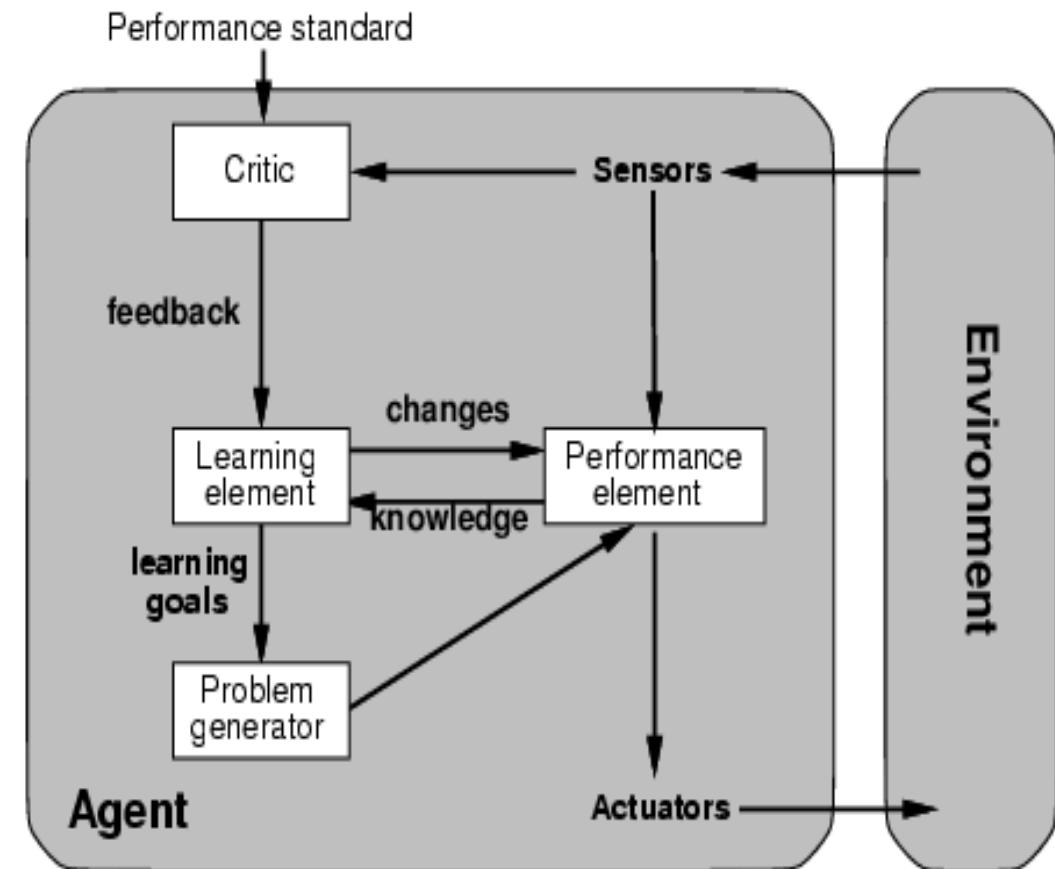
Incorporated most aspects  
of our previous agent  
design



# Learning Element

Responsible for making improvements.

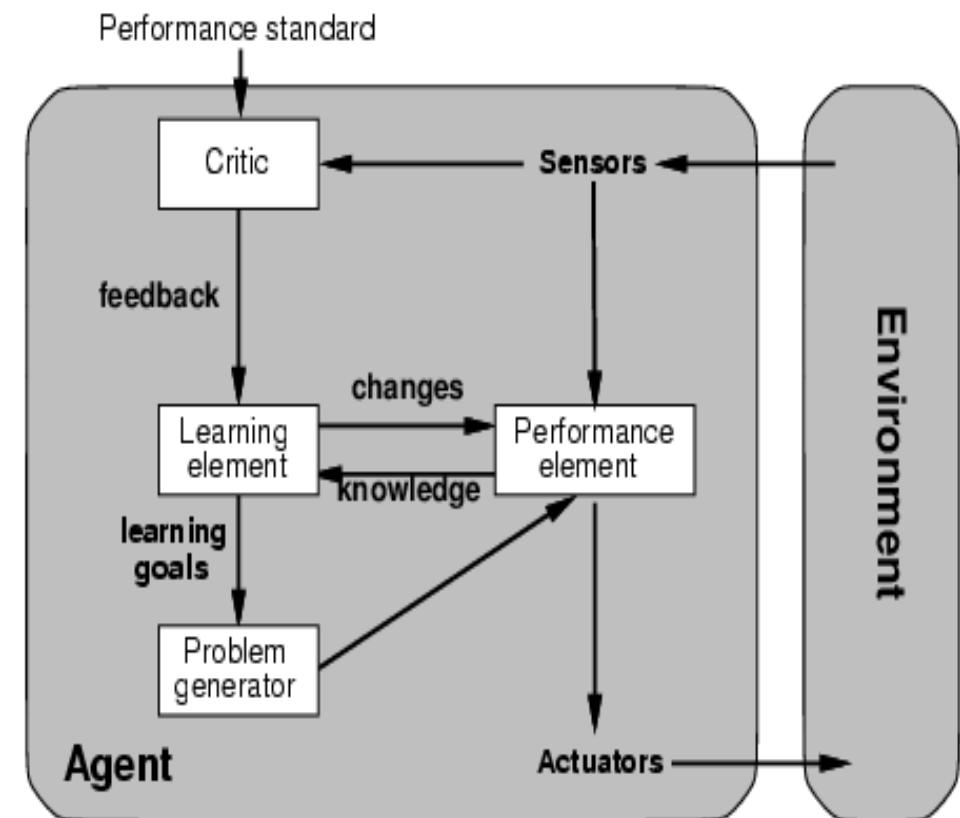
Uses knowledge about the agent and feedback on its actions to improve performance.



# Critic

Informs the learning element about the performance of the action must use a fixed standard of performance

- should be from the outside
- an internal standard could be modified to improve performance
  - sometimes used by humans to justify or disguise low performance



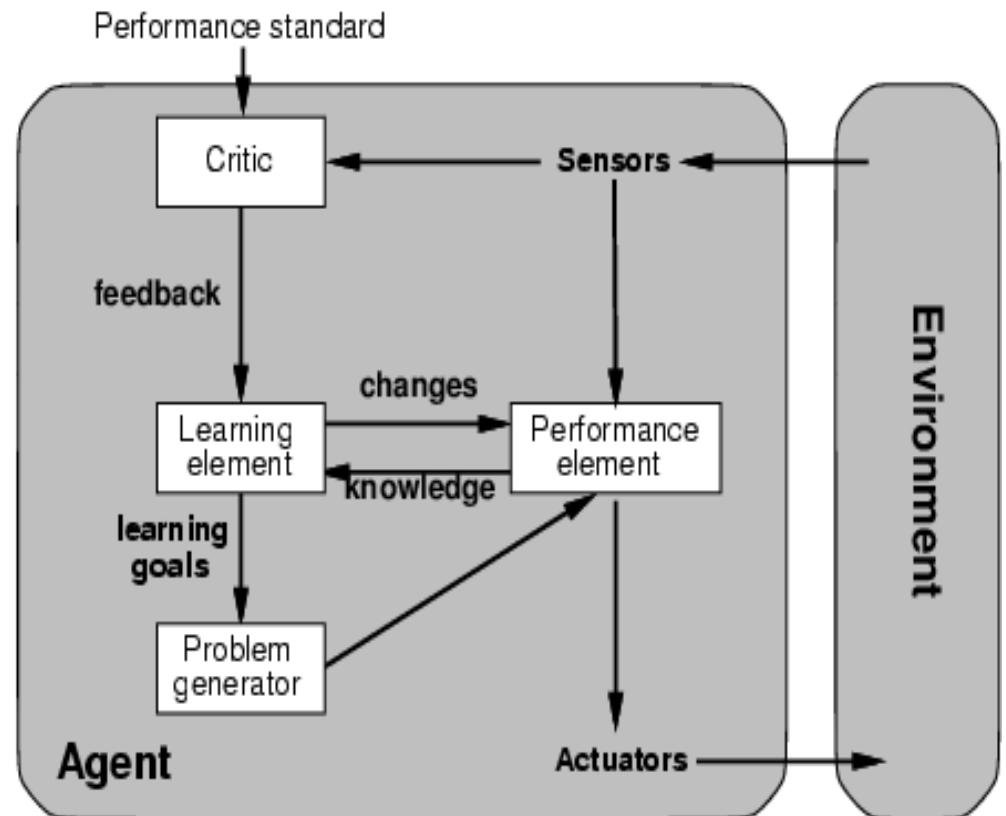
# Problem Generator

Suggests actions that might lead to new experiences

may lead to some sub-optimal decisions in the short run

- in the long run, hopefully better actions may be discovered

otherwise no exploration would occur

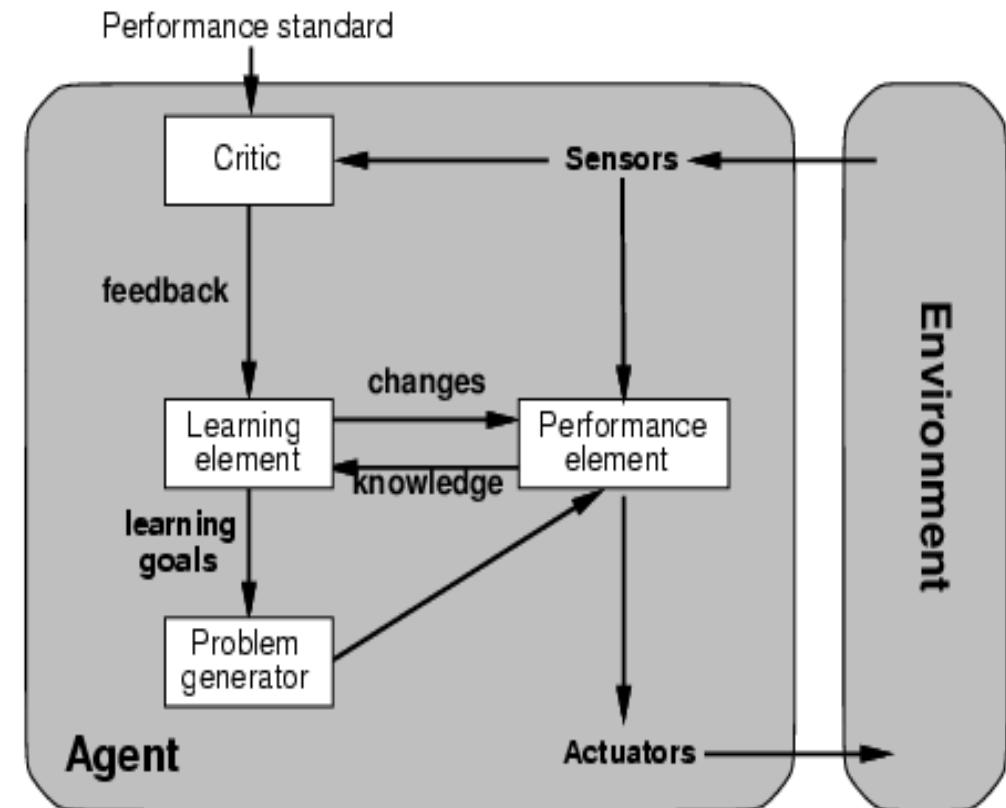


# Example : Automated Taxi

**Performance element** : Collection of knowledge and procedures the taxi has for selecting its driving actions. The taxi goes out on the road and drives.

**Critic**: Observes the world and passes information along to the learning element.

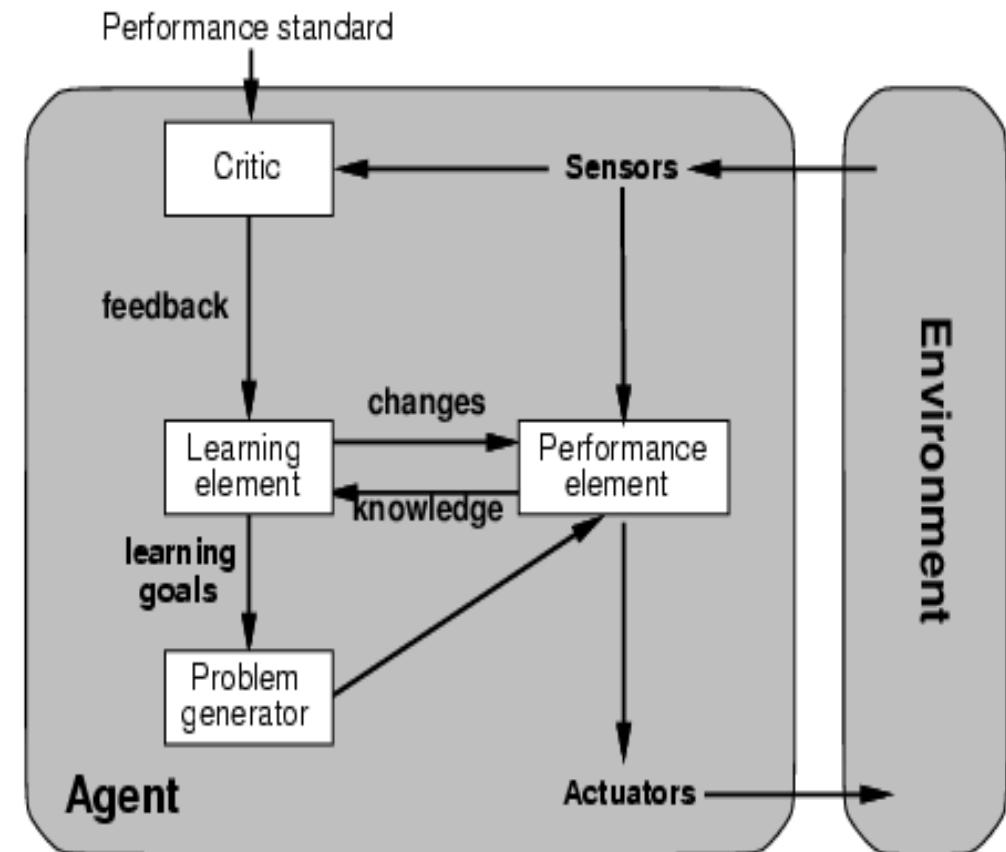
For example, after the taxi makes a quick left turn across three lanes of traffic, the critic observes the shocking language used by other drivers.



# Example : Automated Taxi

**Learning element :** Formulate a rule saying this was a bad action, and the performance element is modified by installation of the new rule.

**Problem generator:** Identify certain areas of behavior in need of improvement and suggest experiments, such as trying out the brakes on different road surfaces under different conditions.



# Unit I

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## **Introduction: (Chapter 1 of Text Book 1)**

What is AI?

Foundation of Artificial Intelligence

History of Artificial Intelligence

## **Intelligent Agents: (Chapter 2 of Text Book 1)**

Agents and Environments

Rationality

The Nature of Environments

The Structure of Agents

## **Problem-solving by search: (Chapter 3 of Text Book 1)**

Problem-Solving Agents

Example Problems

Searching for Solution

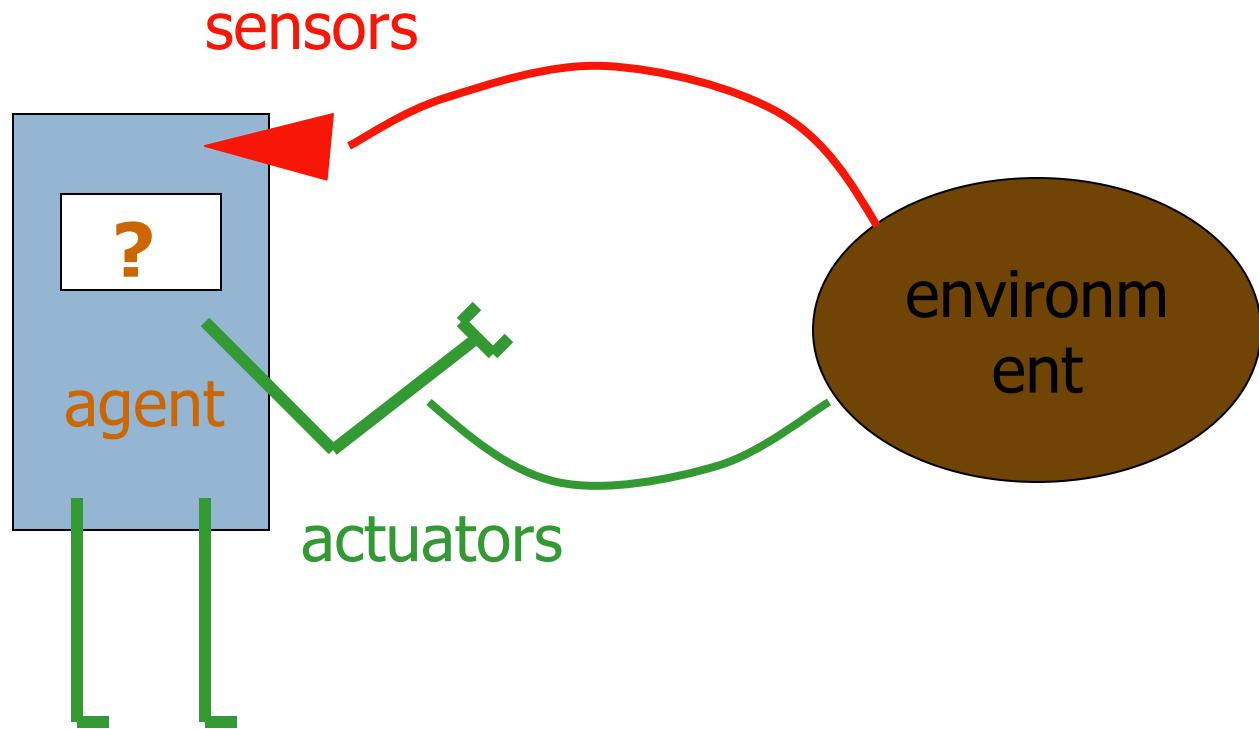
Uniformed Search Strategies

Informed Search Strategies

Heuristic Functions

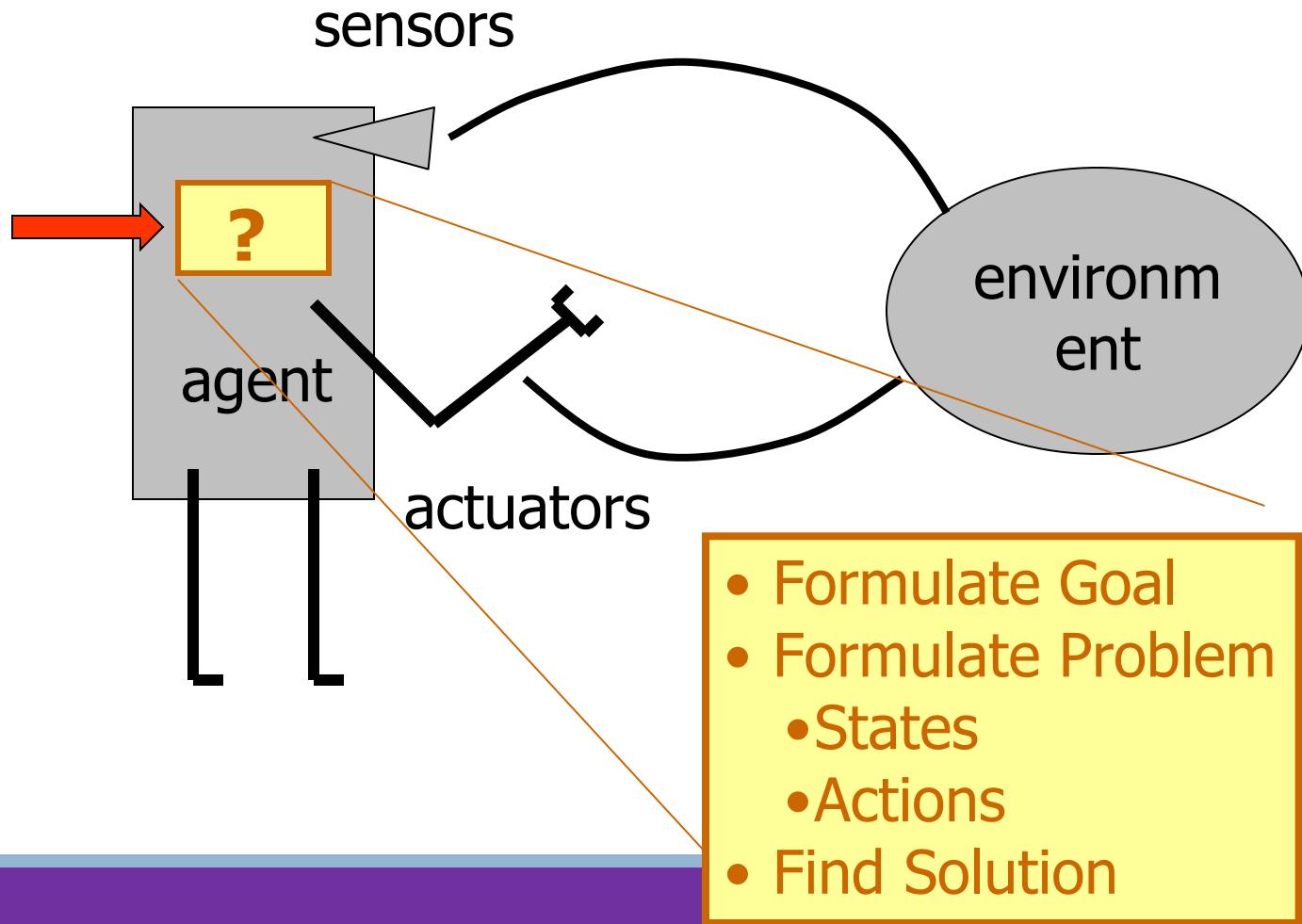
# Problem-Solving Agent

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# Problem-Solving Agent

---



# Problem Solving by Searching

---

Reflex agent is simple

- base their actions on
- a direct mapping from states to actions
- but cannot work well in environments
  - which this mapping would be too large to store
  - and would take too long to learn

Hence, goal-based agent is used

# Problem-Solving Agents



# Problem-solving agent

---

- A kind of goal-based agent
- It solves problem by
  - finding sequences of actions that lead to desirable states (goals)
- To solve a problem,
  - the first step is the ***goal formulation***, based on the current situation

# Goal formulation

---

The goal is formulated

- as a set of world states, in which the goal is satisfied

Reaching from initial state → goal state

- Actions are required

*Actions* are the operators

- causing transitions between world states
- **Actions** should be abstract enough at a certain degree, instead of very detailed
- E.g., turn left VS turn left 30 degree, etc.

# Problem formulation

The process of deciding

- what actions and states to consider, given a goal

Example: Travelling agent

drive Arad → Bucharest

- in-between states and actions defined
- States: Some places in Sibiu, Timisoara, Zerind.
- Actions: Turn left, Turn right, go straight, accelerate & brake, etc.





# Example: Route finding

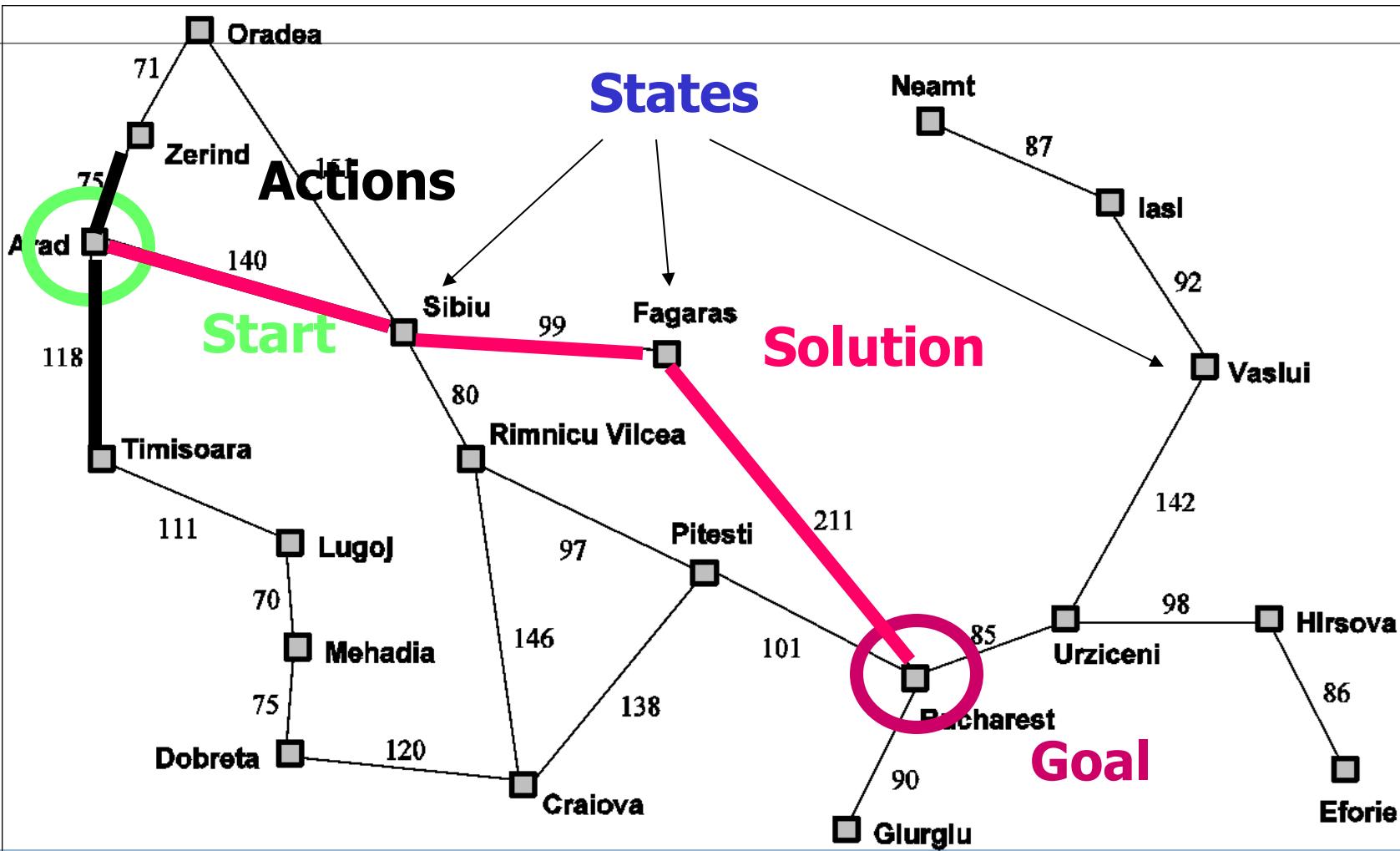


# Holiday Planning

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- On holiday in Romania; Currently in Arad. Flight leaves tomorrow from Bucharest.
- Formulate Goal:  
Be in Bucharest
- Formulate Problem:  
States: various cities  
Actions: drive between cities
- Find solution:  
Sequence of cities: Arad, Sibiu, Fagaras, Bucharest

# Problem Solving



# Search

---

Because there are many ways to achieve the same goal

- Those ways are together expressed as a tree
- Multiple options of unknown value at a point,
  - the agent can examine different possible sequences of actions, and choose the best
- This process of looking for the best sequence is called ***search***
- The best sequence is then a list of actions, called ***solution***

# Search algorithm

---

Defined as

- taking a problem as input
- and returns a solution in the form of an action sequence

Once a solution is found

- the agent follows the solution
- and carries out the list of actions – execution phase

Design of an agent

- “Formulate, search, execute”

# Design of an agent “Formulate, search, execute”

```
function SIMPLE-PROBLEM-SOLVING-AGENT(percept) returns an action
  persistent: seq, an action sequence, initially empty
              state, some description of the current world state
              goal, a goal, initially null
              problem, a problem formulation

  state  $\leftarrow$  UPDATE-STATE(state, percept)
  if seq is empty then
    goal  $\leftarrow$  FORMULATE-GOAL(state)
    problem  $\leftarrow$  FORMULATE-PROBLEM(state, goal)
    seq  $\leftarrow$  SEARCH(problem)
    if seq = failure then return a null action
  action  $\leftarrow$  FIRST(seq)
  seq  $\leftarrow$  REST(seq)
  return action
```

**Figure 3.1** A simple problem-solving agent. It first formulates a goal and a problem, searches for a sequence of actions that would solve the problem, and then executes the actions one at a time. When this is complete, it formulates another goal and starts over.

# Well-defined problems and solutions

---

A problem is defined by 5 components:

- Initial state
- Possible actions
- Transition model
- Goal Test
- Path cost

# Well-defined problems and solutions

---

A problem is defined by 5 components:

- The initial state that the agent starts in.

For example, the initial state for our agent in Romania might be described as In(Arad)

- A description of the possible actions available to the agent.

Given a particular state  $s$ , ACTIONS( $s$ ) returns the set of actions that can be executed in  $s$ .

In(Arad), the applicable actions are {Go(Sibiu), Go(Timisoara), Go(Zerind)}.

# Well-defined problems and solutions

- TRANSITION MODEL

A description of what each action does;

Specified by a function  $\text{RESULT}(s, a)$  that returns the state that results from  $\text{SUCCESSOR}$  doing action  $a$  in state  $s$ .

$\text{RESULT}(\text{In(Arad}), \text{Go(Zerind)}) = \text{In(Zerind)}$  .

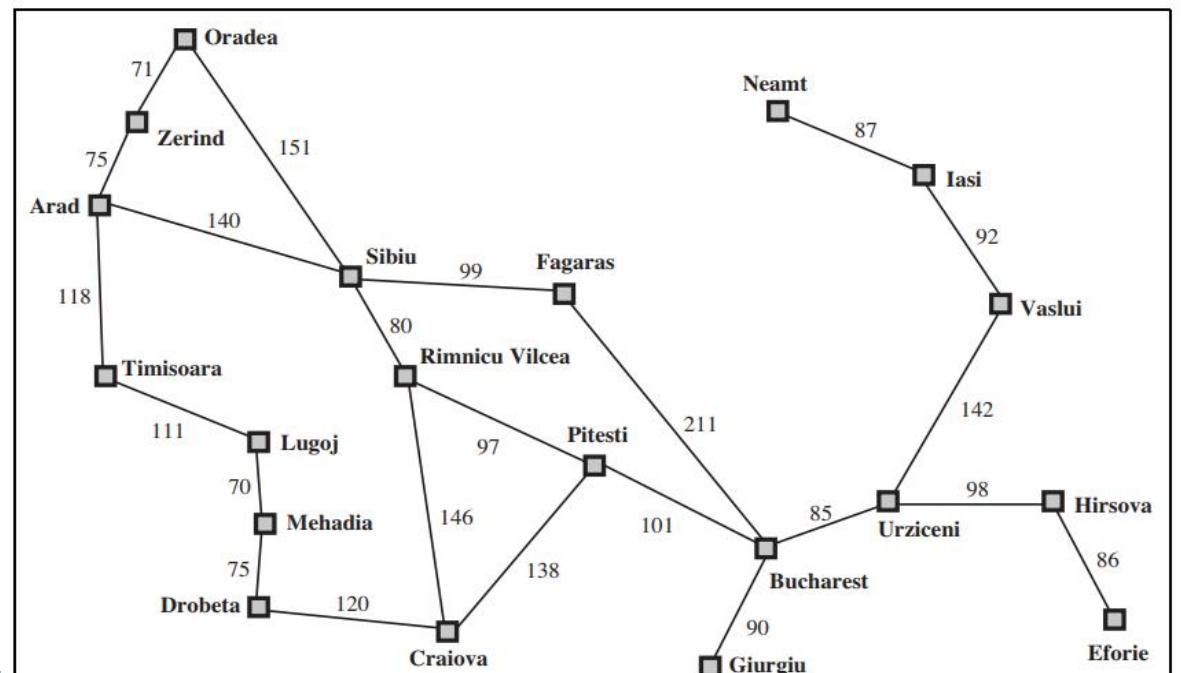


Figure 3.2 A simplified road map of part of Romania.

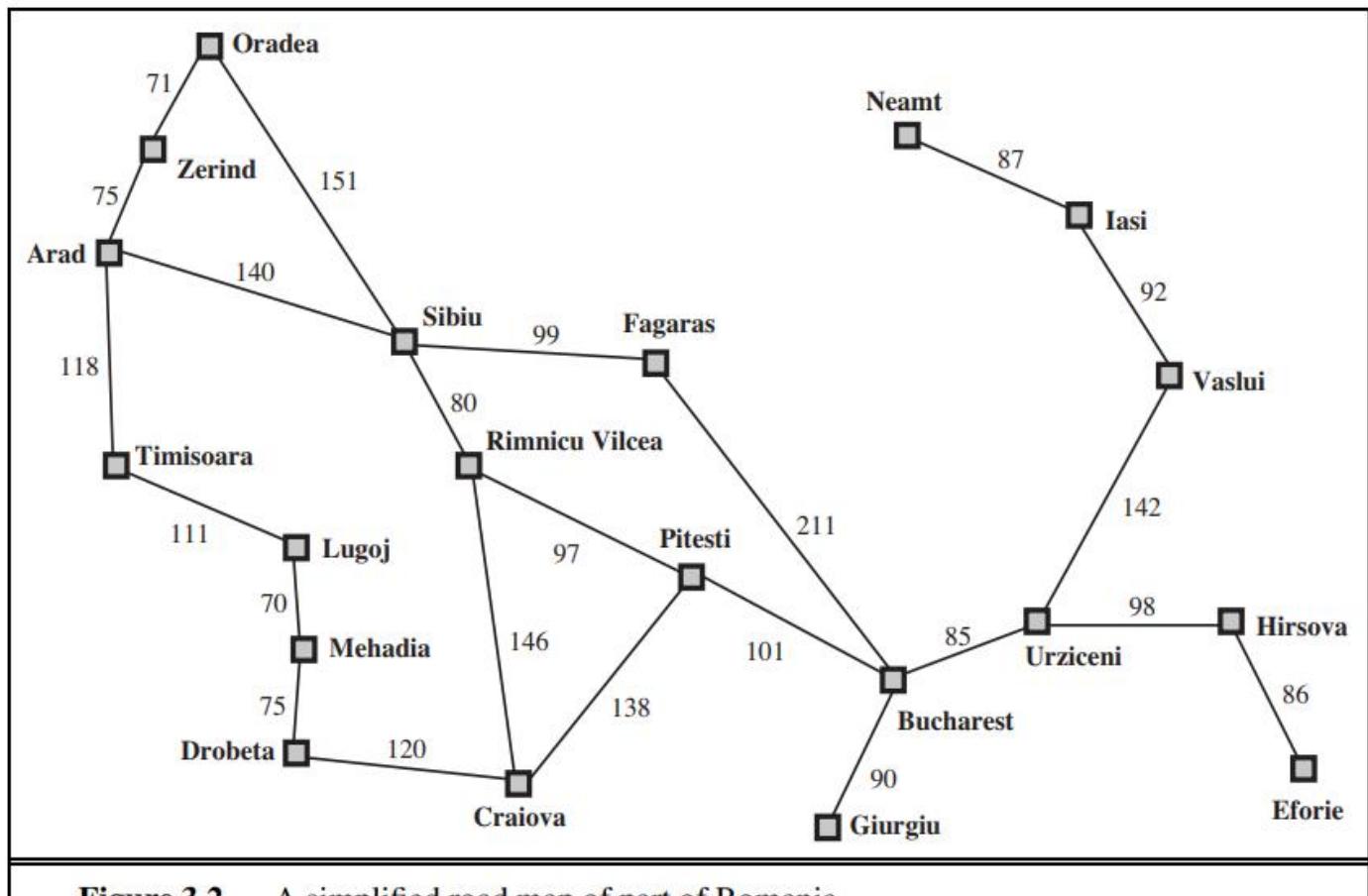
# Well-defined problems and solutions

- **TRANSITION MODEL**

Together, the initial state, actions, and transition model implicitly define the State Space of the problem

The state space forms a directed network or graph in which the nodes are states and the links between nodes are actions.

A path in the state space is a sequence of states connected by a sequence of actions.



**Figure 3.2** A simplified road map of part of Romania.

# Well-defined problems and solutions

---

- Goal Test

Determines whether a given state is a goal state.

The agent's goal in Romania is the singleton set  $\{\text{In(Bucharest)}\}$ .

Example: In chess, the goal is to reach a state called “checkmate,” where the opponent’s king is under attack and can’t escape

# Well-defined problems and solutions

---

- Path cost

The problem-solving agent chooses a cost function that reflects its own performance measure.

Path cost function assigns a numeric cost to each path.

Cost of a path can be described as the sum of the costs of the individual actions along the path.

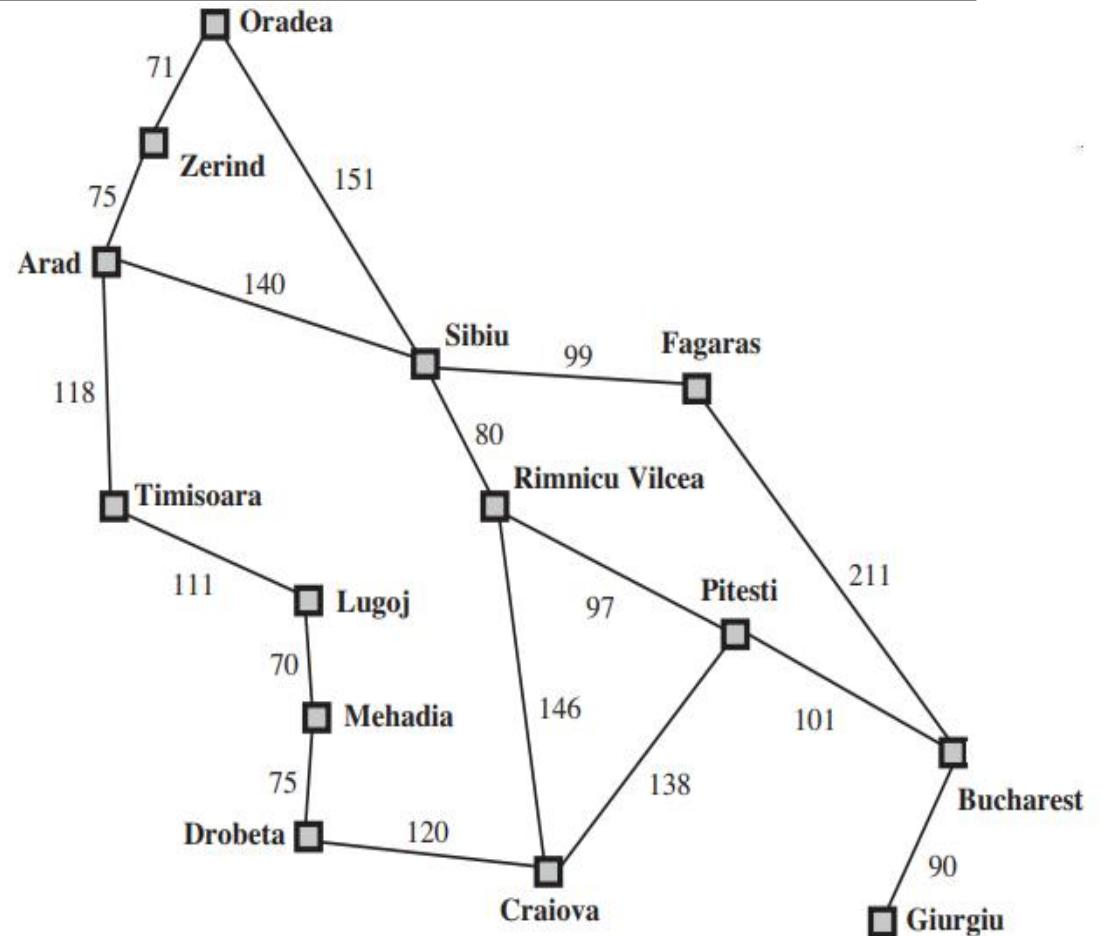
The step cost of taking action  $a$  in state  $s$  to reach state  $s'$  is denoted by  $c(s, a, s')$ .

# Well-defined problems and solutions

- Path cost

Example :

Agent – Arad to Bucharest,  
time is of the essence, so the  
cost of a path might be its  
length in kilometers.



# Summarize Well-defined problems and solutions

---

Together a problem is defined by

- Initial state
- Actions
- Successor function
- Goal test
- Path cost function

The ***solution*** of a problem is then

- *a path from the initial state to a state satisfying the goal test*

***Optimal*** solution

- the solution with lowest path cost among all solutions

# Formulating problems

---

We proposed a formulation of the problem - **Arad to Bucharest** in terms of the initial state, actions, transition model, goal test, and path cost.

This formulation seems reasonable, but it is still a model—an abstract mathematical description

Abstract of State description

# Formulating problems

---

State of the world includes so many things: the traveling companions, the current radio program, the scenery out of the window, the proximity of law enforcement officers, the distance to the next rest stop, the condition of the road, the weather, and so on

All these considerations are left out of our state descriptions because they are irrelevant to the problem of finding a route to Bucharest.

The process of removing detail from a representation is called **Abstraction.**

# Example problems

---

Two main varieties of problem faced in AI games.

## Toy problems

- those intended to illustrate or exercise various problem-solving methods
- E.g., puzzle, chess, etc.

## Real-world problems

- tend to be more difficult and whose solutions people actually care about
- E.g., Design, planning, etc.

# Example problems

---

## Toy problems - Vacuum world

- States: The state is determined by both the agent location and the dirt locations.

A larger environment with  $n$  locations has  $n \cdot 2^n$  states.

Thus, there are  $2 \times 2^2 = 8$  possible world states.

- Initial state: Any state can be designated as the initial state.
- Actions: Left, Right, and Suck.

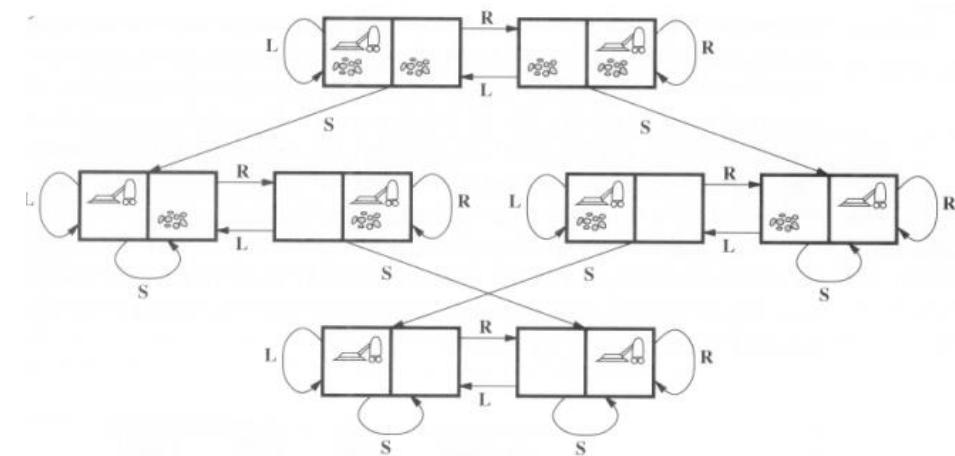
# Example problems

---

## Toy problems - Vacuum world

- Transition model: The actions have their expected effects, except that moving Left in the leftmost square, moving Right in the rightmost square, and Sucking in a clean square have no effect.

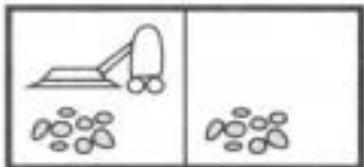
The complete state space is shown in Figure



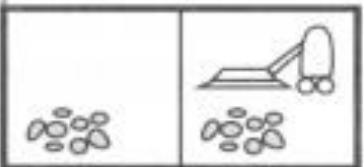
# Toy problems

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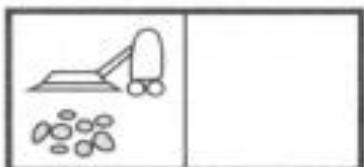
1



2



3



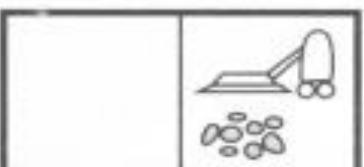
4



5



6



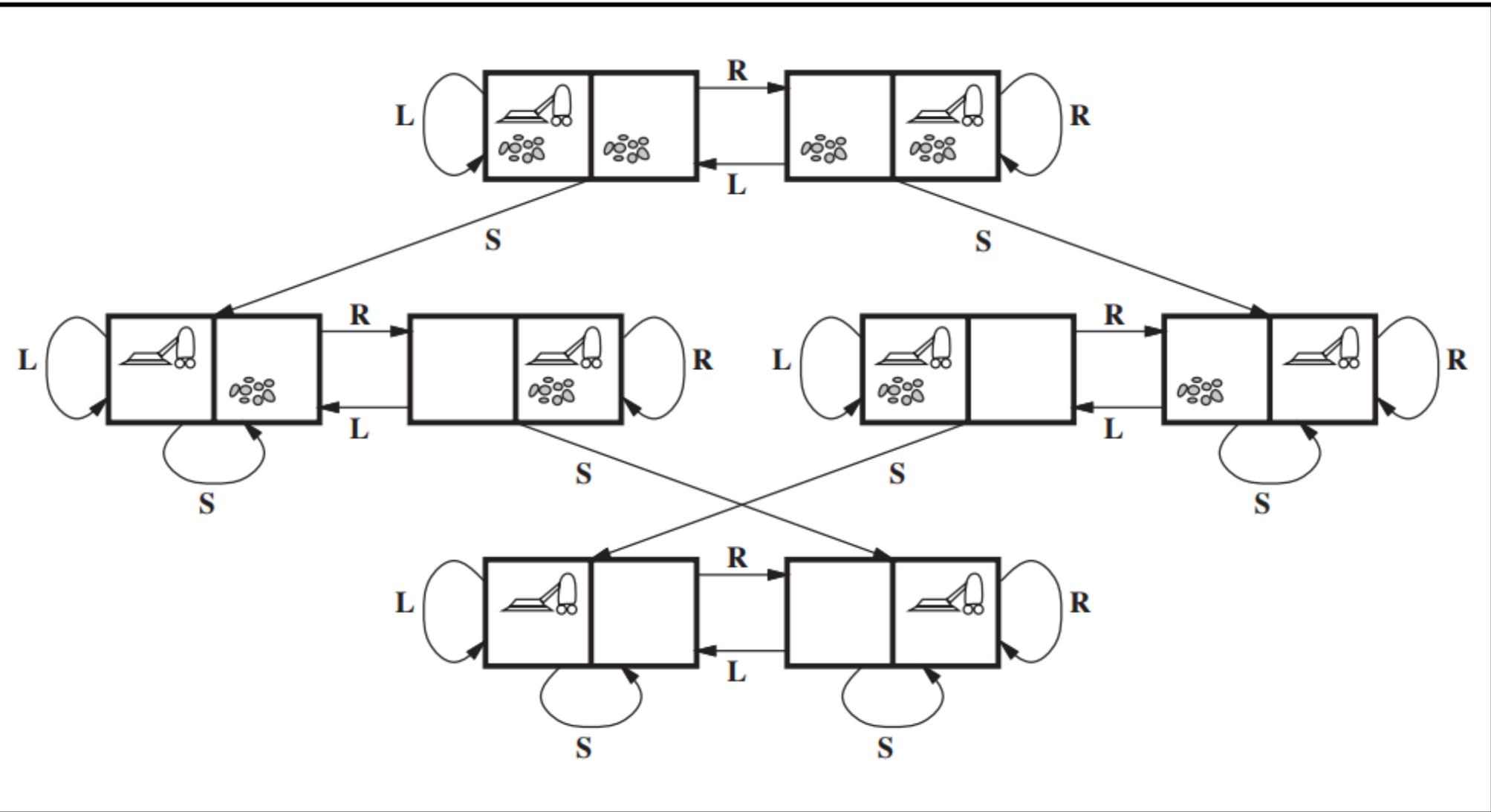
7



8



- Number of states: 8
- Initial state: Any
- Number of actions: 3
  - left, right, suck
- Goal: clean up all dirt
  - Goal states: {7, 8}
- Path Cost:
  - Each step costs 1



**Figure 3.3** The state space for the vacuum world. Links denote actions: L = *Left*, R = *Right*, S = *Suck*.

# Example problems

---

## Toy problems -8 Puzzle

The 8-puzzle belongs to the family of sliding-block puzzles, which are often used as test problems for new search algorithms in AI.

- It consists of 3 x 3 board with 8 numbered tiles and a blank space
- A tile adjacent to the blank space can slide into the blank space.
- The objective is to reach the specified goal state.

7	2	4
5		6
8	3	1

Start State

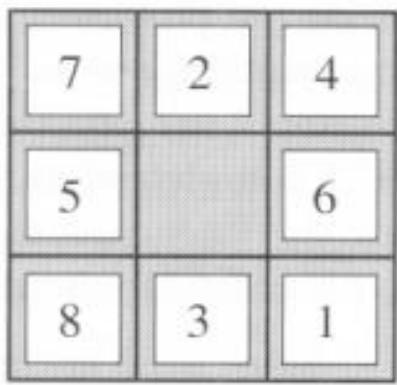
	1	2
3	4	5
6	7	8

Goal State

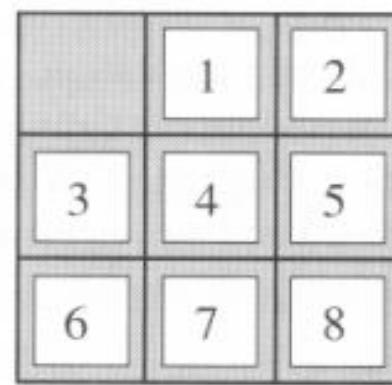
# Example problems

---

- Initial state: Any state can be designated as the initial state.
- Actions: Movements of the blank space Left, Right, Up, or Down.
- Transition model: Given a state and action, this returns the resulting state  
For example, if we apply Left to the start state in Figure, the resulting state has the 5 and the blank switched.
- Goal test: This checks whether the state matches the goal configuration
- Path cost: Each step costs 1, so the path cost is the number of steps in the path.



Start State



Goal State

# Example problems

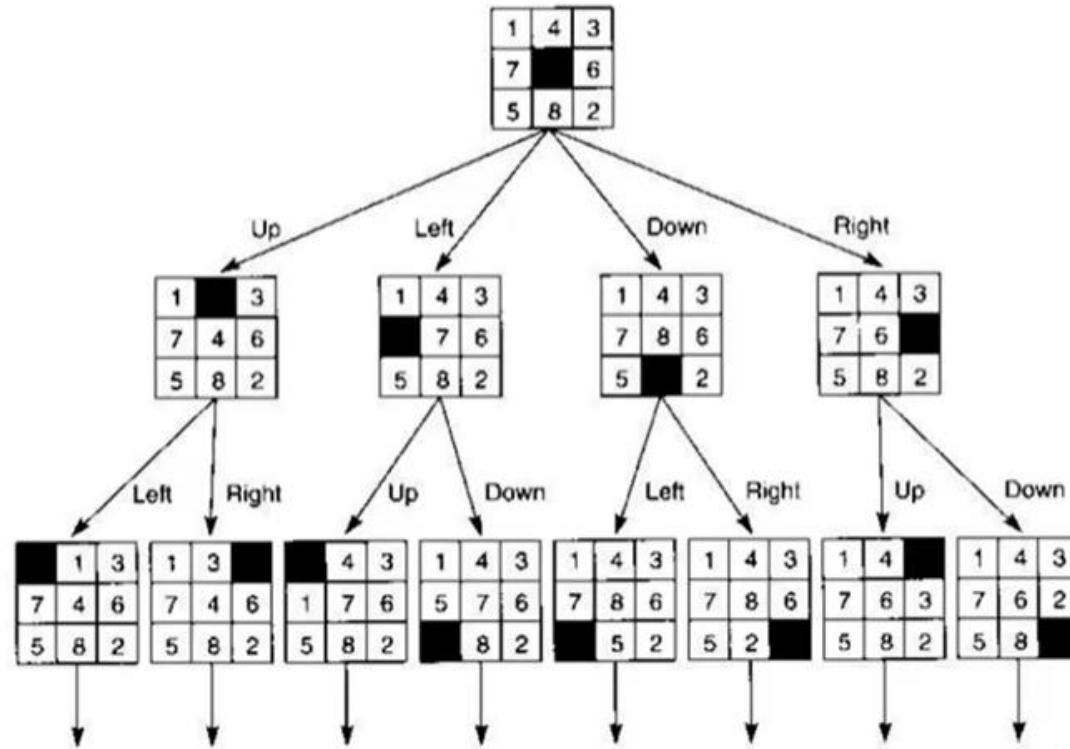
The 8-puzzle has  $9!/2 = 181, 440$  reachable states and is easily solved.

2	1	6
4		8
7	5	3

**Initial State**

1	2	3
8		4
7	6	5

**Goal State**

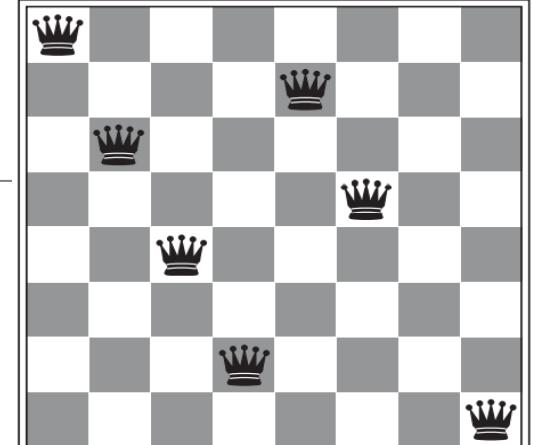


# Example problems

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## Toy problems - 8-queens

- n queens puzzle of placing 8 queens on an  $n \times n$  chessboard
- 8 chess queens on an  $8 \times 8$  chessboard such that none of them is able to capture any other using the standard chess queen's moves.
- Any queen is assumed to be able to attack any other.
- Thus, a solution requires that no two queens share the same row, column, or diagonal.



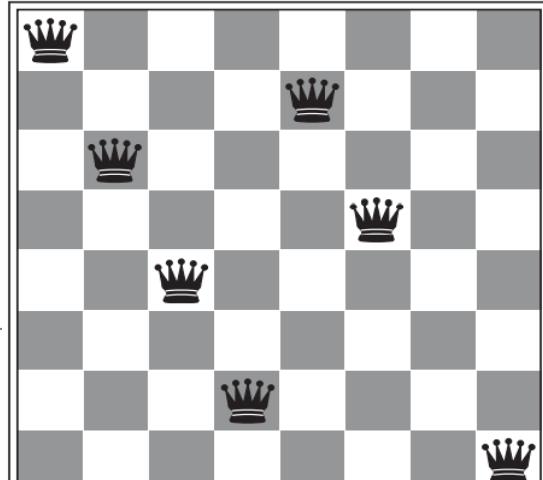
# Example problems

## Toy problems - 8-queens

There are two main kinds of formulation.

An incremental formulation involves operators that augment the state description, starting with an empty state; for the 8-queens problem, this means that each action adds a queen to the state.

A complete-state formulation starts with all 8 queens on the board and moves them around.



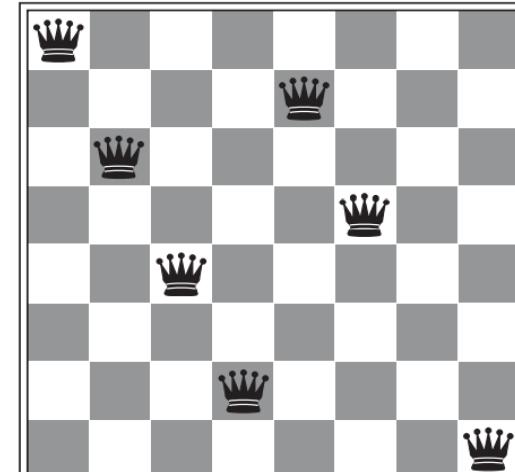
# Example problems

---

Toy problems - 8-queens

As per the incremental formulation :

- **States:** Any arrangement of 0 to 8 queens on the board is a state.
- **Initial state:** No queens on the board.
- **Actions:** Add a queen to any empty square.
- **Transition model:** Returns the board with a queen added to the specified square.
- **Goal test:** 8 queens are on the board, none attacked.



# Example problems

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## Real-world problems

- Route-finding algorithms are used in a variety of applications.
- Others, such as routing video streams in computer networks, military operations planning, and airline travel-planning systems, involve much more complex specifications.

# Example problems

---

## Real-world problems

1. Airline travel problems
2. Touring problems
3. Traveling salesperson problem
4. A VLSI layout
5. Robot navigation
6. Automatic assembly sequencing

# Example problems

---

## 1. Airline travel problems

- **States:** Each state obviously includes a location (e.g., an airport) and the current time. Furthermore, because the cost of an action (a flight segment) may depend on previous segments, their fare bases, and their status as domestic or international, the state must record extra information about these “historical” aspects.
- **Initial state:** This is specified by the user’s query.
- **Actions:** Take any flight from the current location, in any seat class, leaving after the current time, leaving enough time for within-airport transfer if needed.
- **Transition model:** The state resulting from taking a flight will have the flight’s destination as the current location and the flight’s arrival time as the current time.
- **Goal test:** Are we at the final destination specified by the user?
- **Path cost:** This depends on monetary cost, waiting time, flight time, customs and immigration procedures, seat quality, time of day, type of airplane, frequent-flier mileage awards, and so on.

# 2.Touring problems

Are closely related to route-finding problems

Problem - “Visit every city at least once, starting and ending in Bucharest”.

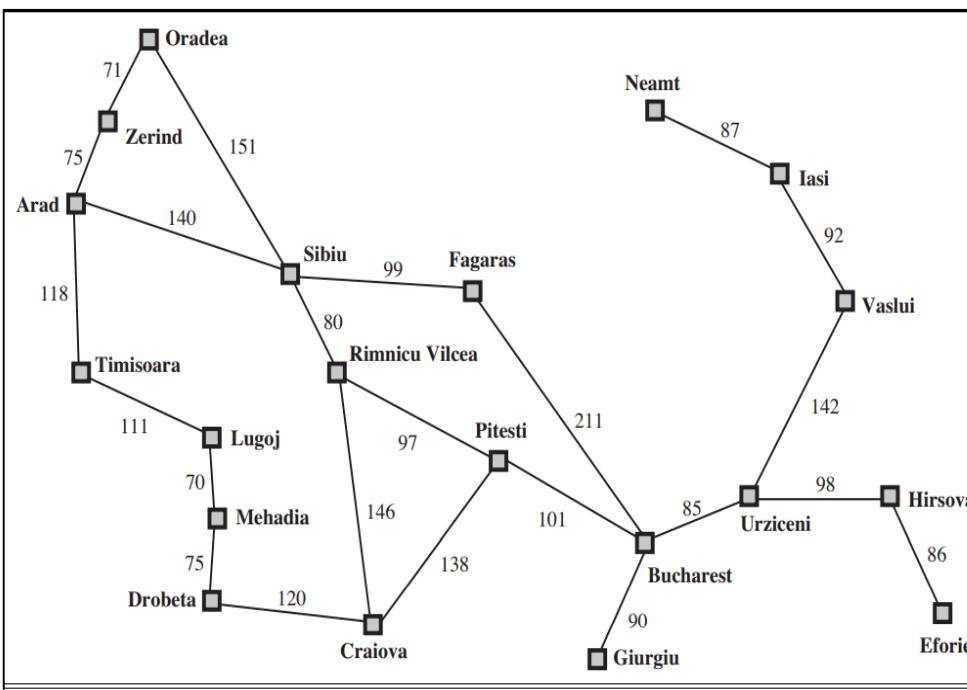


Figure 3.2 A simplified road map of part of Romania.

In(Bucharest), Visited({Bucharest}),  
 In(Vaslui), Visited({Bucharest, Urziceni, Vaslui})

# 3. Traveling salesperson problem

---

Is a touring problem in which each city must be visited exactly once.

The aim is to find the shortest tour.

The problem is known to be NP-hard, but an enormous amount of effort has been expended to improve the capabilities of TSP algorithms.

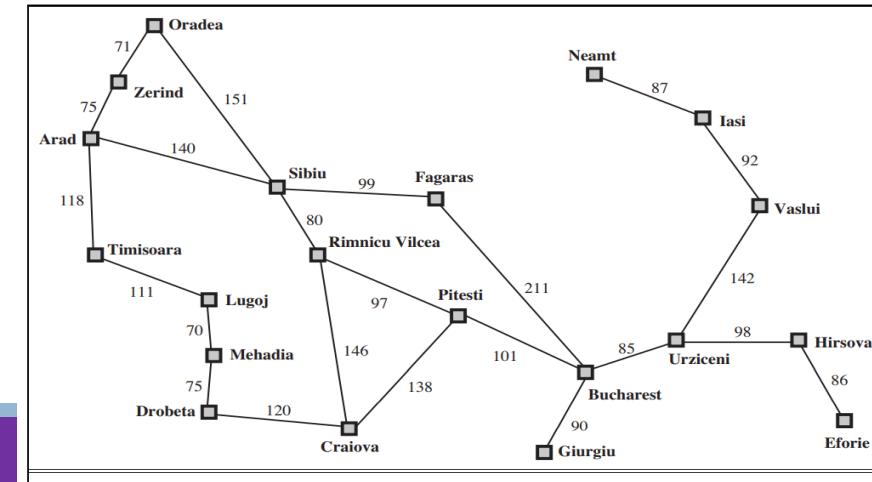


Figure 3.2 A simplified road map of part of Romania.

# Unit I

---

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The Structure of Agents

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Problem-Solving Agents

Example Problems

Searching for Solution

Uniformed Search Strategies

Informed Search Strategies

Heuristic Functions

# Searching for solutions

# Searching for solutions

---

All problems are transformed

- as a search tree generated by the initial state and successor function

Finding out a solution is done by

- Searching through the state space
- Represent state space with Tree and Graph

# Search tree

---

## Initial state

- The root of the search tree is a **search node**

## Expanding

- applying successor function to the current state thereby generating a new set of states

## Leaf nodes

- a node with no children in the tree.

The set of all leaf nodes available for expansion at any given point is called the **Frontier( Open list)** .

The process of expanding nodes on the frontier continues until either a solution is found or there are no more states to expand.

Figure shows the first few steps in growing the search tree for finding a route from Arad to Bucharest.

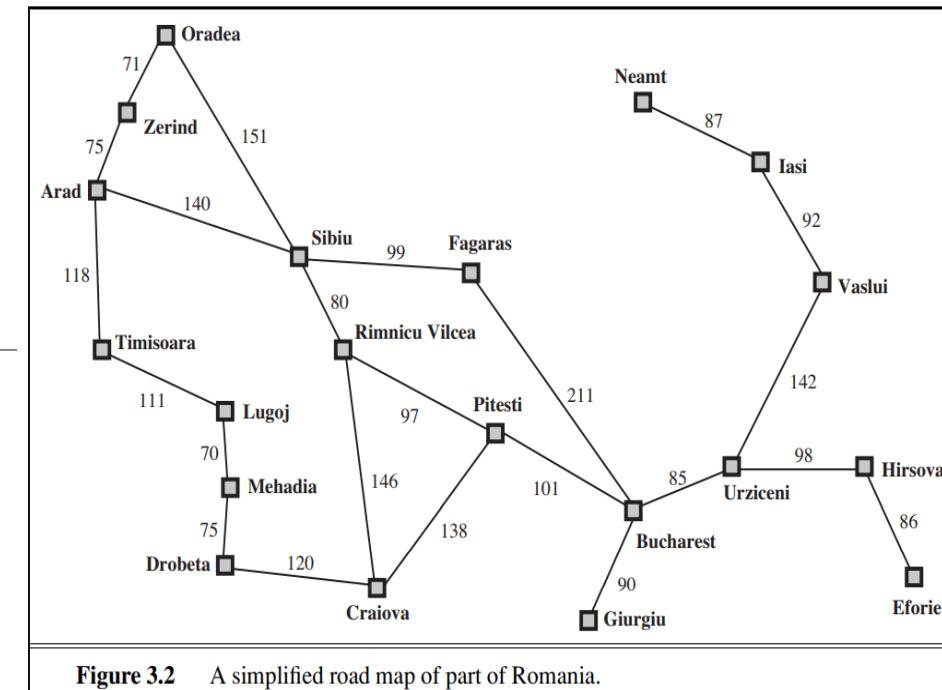
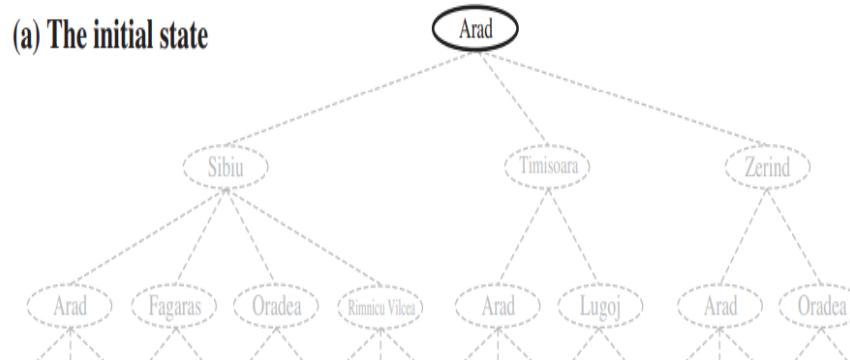
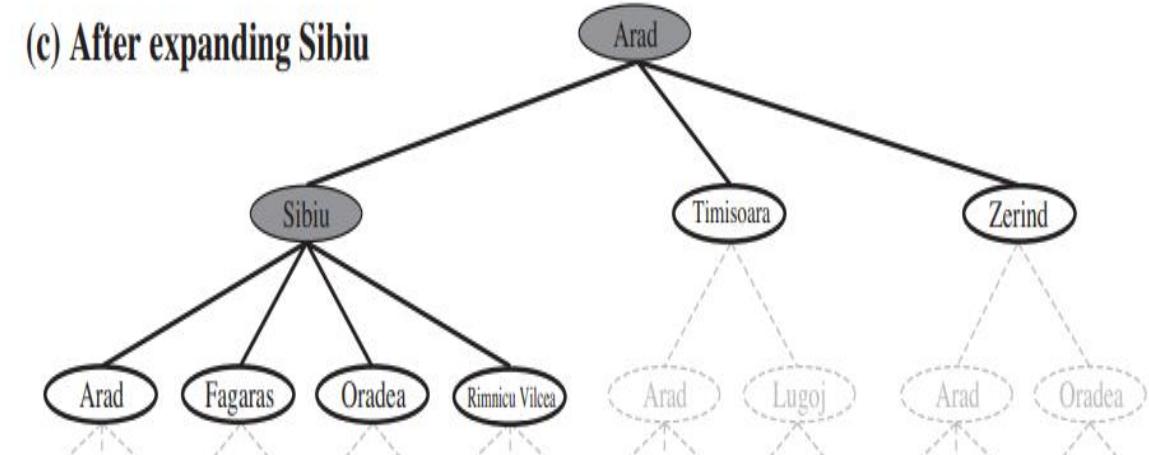
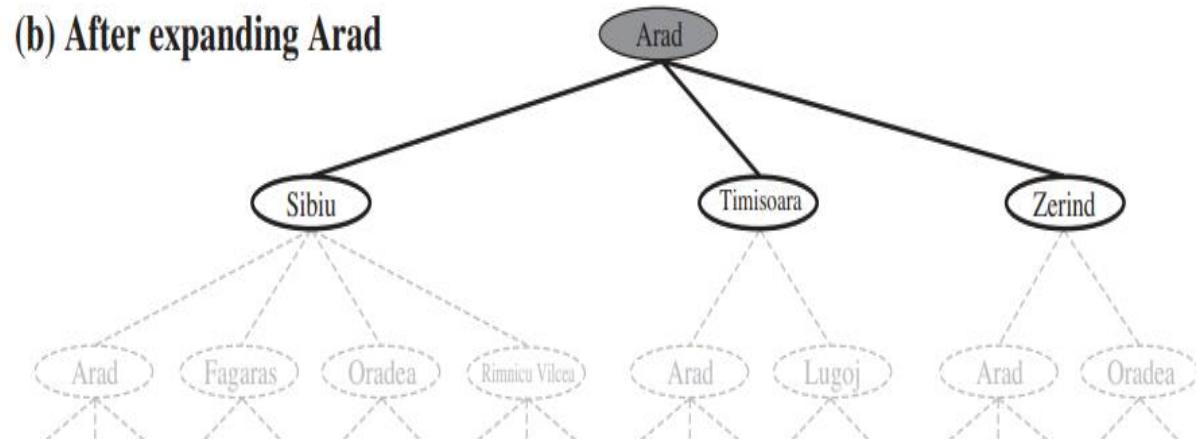


Figure 3.2 A simplified road map of part of Romania.



# Search algorithms share this basic structure.

They vary primarily according to how they choose which state to expand next—the so-called search strategy

**function** TREE-SEARCH(*problem*) **returns** a solution, or failure

initialize the frontier using the initial state of *problem*

**loop do**

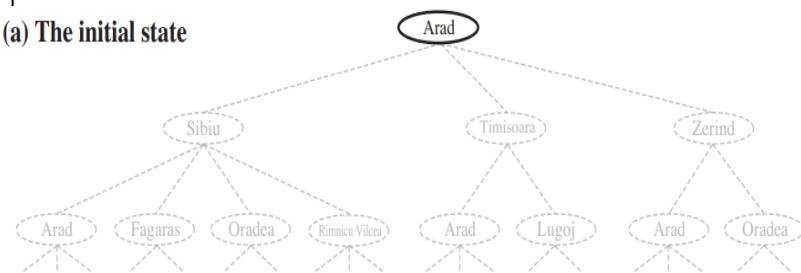
**if** the frontier is empty **then return** failure

    choose a leaf node and remove it from the frontier

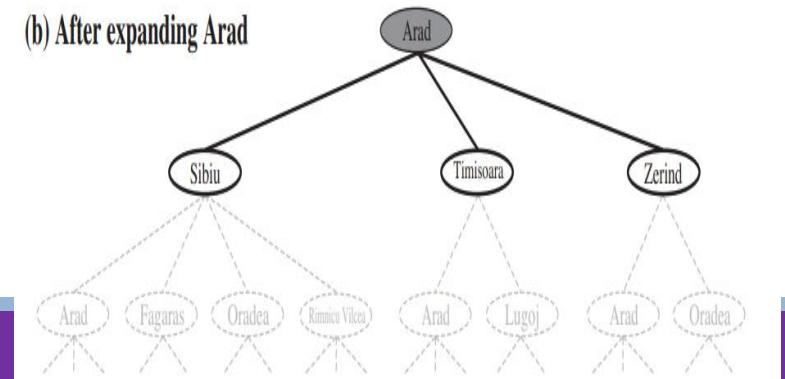
**if** the node contains a goal state **then return** the corresponding solution

    expand the chosen node, adding the resulting nodes to the frontier

(a) The initial state

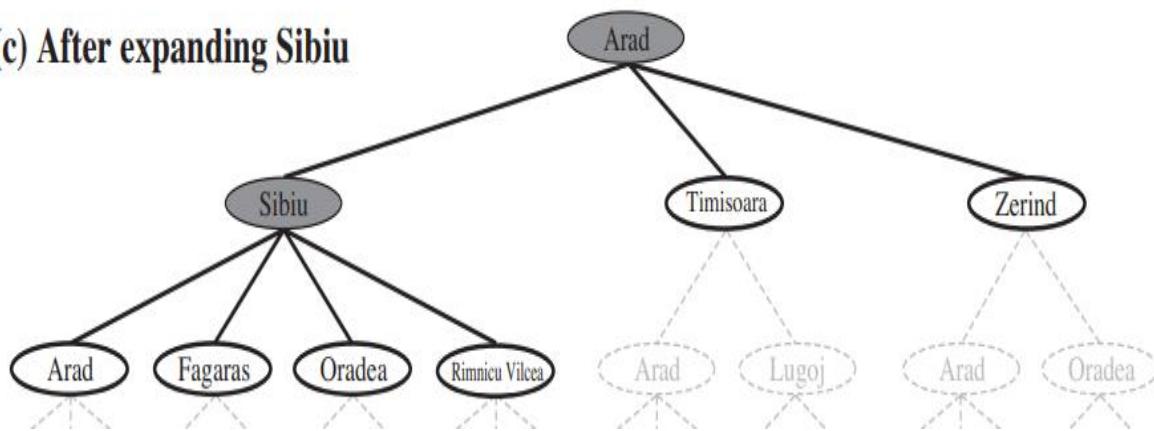


(b) After expanding Arad



# Search algorithms share this basic structure.

(c) After expanding Sibiu



In(Arad) is a repeated state in the search tree, generated in this case by a **loopy path**.

Loops can cause certain algorithms to fail, making otherwise solvable problems unsolvable

Loopy paths are a special case of redundant paths

**redundant paths are unavoidable.**

The way to avoid exploring redundant paths is to remember where one has been.

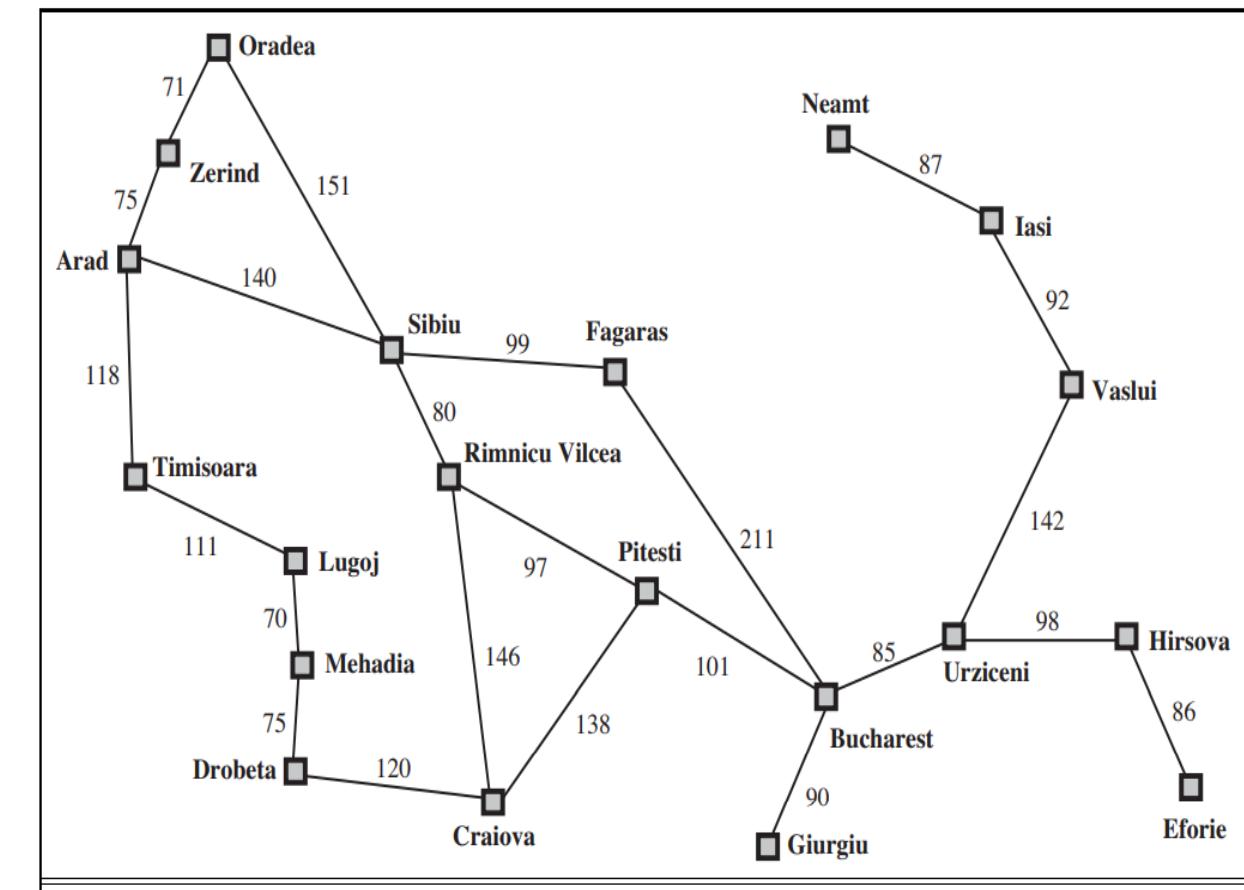


Figure 3.2 A simplified road map of part of Romania.

# Search algorithms share this basic structure.

---

To do this, we augment the TREE-SEARCH algorithm with a data structure called the explored set (also known as the closed list), which remembers every expanded node.

Newly generated nodes that match previously generated nodes—ones in the explored set or the frontier—can be discarded instead of being added to the frontier.

The new algorithm, called GRAPH-SEARCH, is shown in figure

**function** TREE-SEARCH(*problem*) **returns** a solution, or failure

initialize the frontier using the initial state of *problem*

**loop do**

**if** the frontier is empty **then return** failure

    choose a leaf node and remove it from the frontier

**if** the node contains a goal state **then return** the corresponding solution

    expand the chosen node, adding the resulting nodes to the frontier

**function** GRAPH-SEARCH(*problem*) **returns** a solution, or failure

initialize the frontier using the initial state of *problem*

**initialize the explored set to be empty**

**loop do**

**if** the frontier is empty **then return** failure

    choose a leaf node and remove it from the frontier

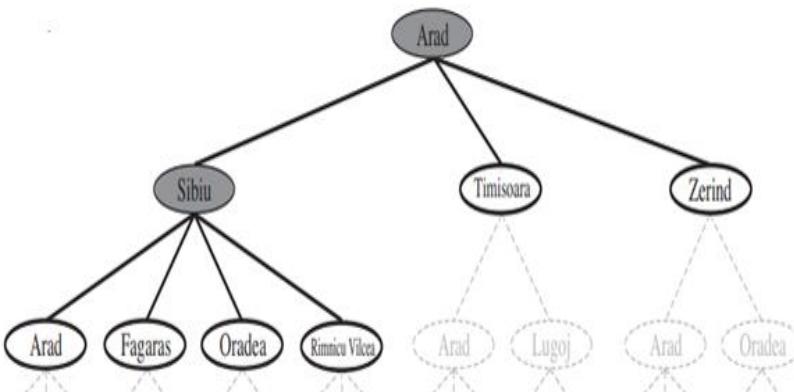
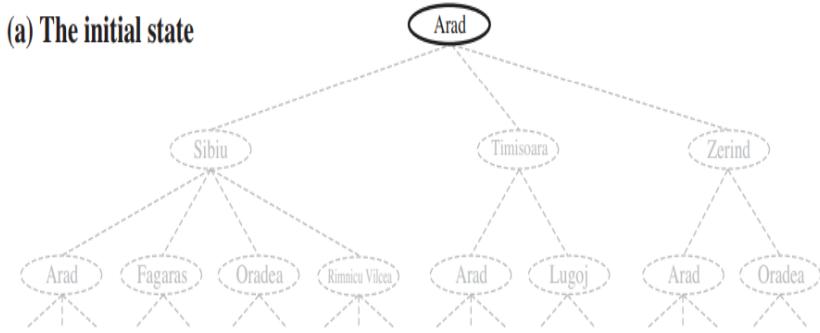
**if** the node contains a goal state **then return** the corresponding solution

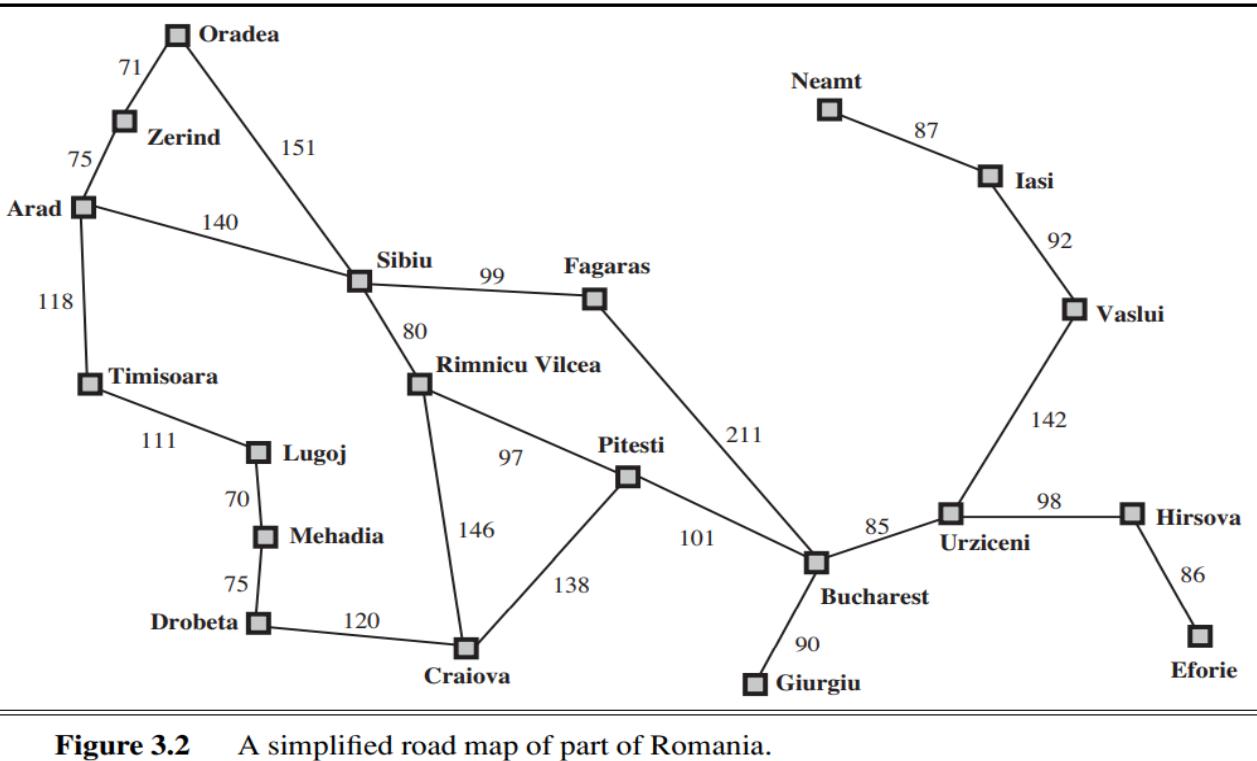
**add the node to the explored set**

    expand the chosen node, adding the resulting nodes to the frontier

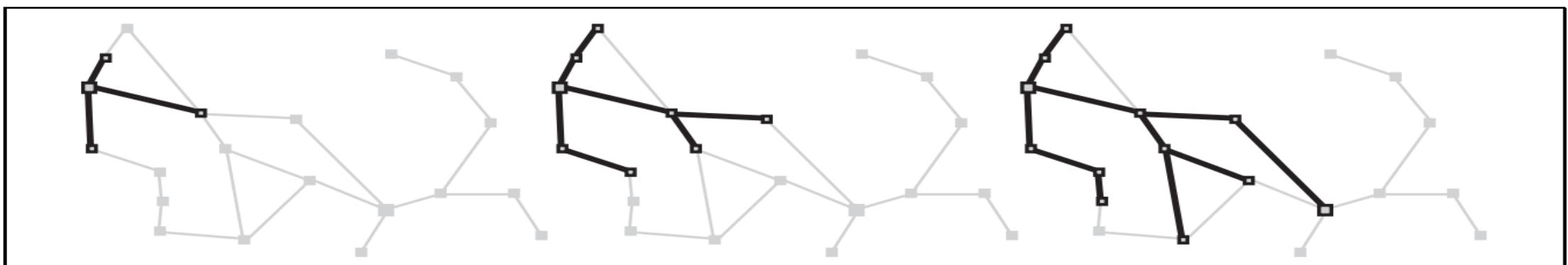
**only if not in the frontier or explored set**

(a) The initial state





**Figure 3.2** A simplified road map of part of Romania.



**Figure 3.8** A sequence of search trees generated by a graph search on the Romania problem of Figure 3.2. At each stage, we have extended each path by one step. Notice that at the third stage, the northernmost city (Oradea) has become a dead end: both of its successors are already explored via other paths.

# Rectangular grid Problem

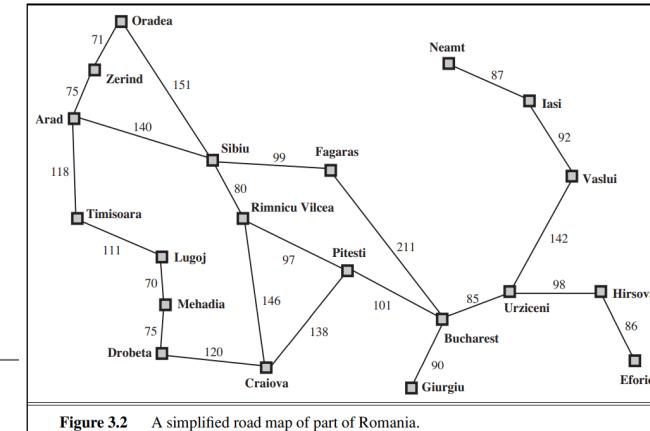


Figure 3.2 A simplified road map of part of Romania.

Route finding on a rectangular grid is important example in computer games.

In grid, each state has four successors, so a search tree of depth  $d$  that includes repeated states has  $4^d$  leaves; but there are only about  $2d^2$  distinct states within  $d$  steps of any given state.

For  $d = 20$ , this means about a trillion nodes but only about 800 distinct states.

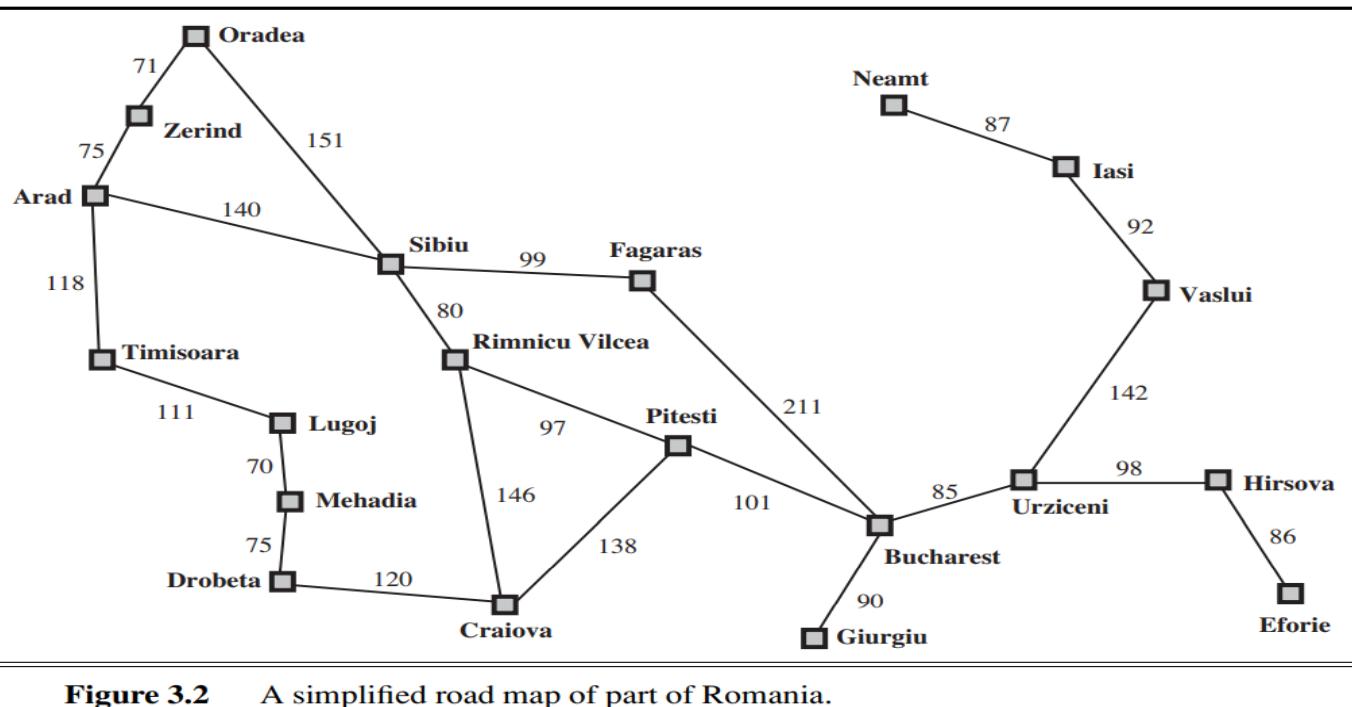
# Graph search algorithm

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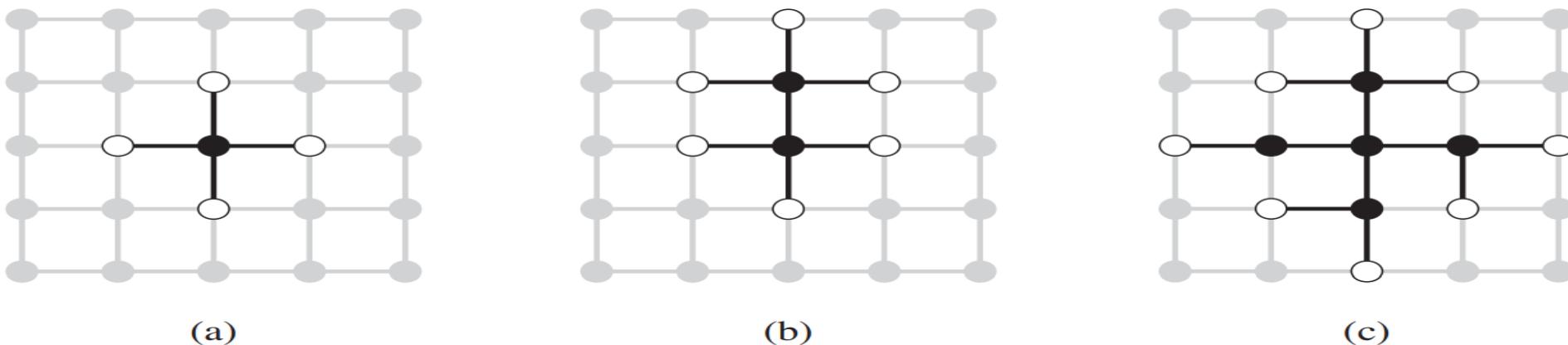
The algorithm has another nice property:

The frontier separates the state-space graph into the explored region and the unexplored region, so that every path from the initial state to an unexplored state has to pass through a state in the frontier.

This property is illustrated in next Figure.



**Figure 3.2** A simplified road map of part of Romania.



**Figure 3.9** The separation property of GRAPH-SEARCH, illustrated on a rectangular-grid problem. The frontier (white nodes) always separates the explored region of the state space (black nodes) from the unexplored region (gray nodes). In (a), just the root has been expanded. In (b), one leaf node has been expanded. In (c), the remaining successors of the root have been expanded in clockwise order.

# Infrastructure for search algorithms

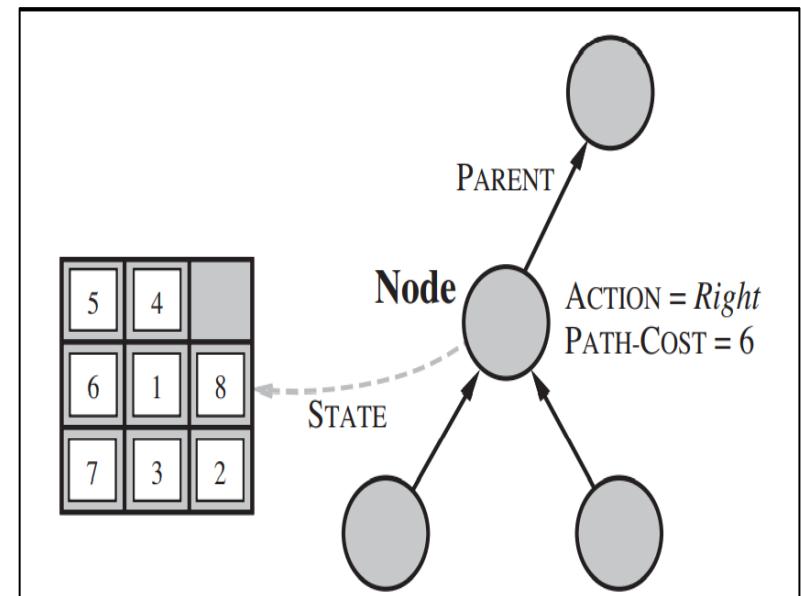
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- Search algorithms require a data structure to keep track of the search tree that is being constructed.
- For each node  $n$  of the tree, we have a structure that **contains four components**
  - $n.\text{STATE}$ : the state in the state space to which the node corresponds;
  - $n.\text{PARENT}$ : the node in the search tree that generated this node;
  - $n.\text{ACTION}$ : the action that was applied to the parent to generate the node;
  - $n.\text{PATH-COST}$ : the cost, traditionally denoted by  $g(n)$ , of the path from the initial state to the node, as indicated by the parent pointers.

# The node data structure is depicted in Figure

Nodes are the data structures from which the search tree is constructed. Each has a parent, a state, and various bookkeeping fields. Arrows point from child to parent.

- $n.\text{STATE}$ : the state in the state space to which the node corresponds;
- $n.\text{PARENT}$ : the node in the search tree that generated this node;
- $n.\text{ACTION}$ : the action that was applied to the parent to generate the node;
- $n.\text{PATH-COST}$ : the cost, traditionally denoted by  $g(n)$ , of the path from the initial state to the node, as indicated by the parent pointers.



The function CHILD-NODE takes a parent node and an action and returns the resulting child node:

---

```
function CHILD-NODE(problem, parent, action) returns a node
  return a node with
    STATE = problem.RESULT(parent.STATE, action),
    PARENT = parent, ACTION = action,
    PATH-COST = parent.PATH-COST + problem.STEP-COST(parent.STATE, action)
```

# Data structure -Queue

---

We need to put Nodes somewhere.

The frontier needs to be stored in such a way that the search algorithm can easily choose the next node to expand according to its preferred strategy.

The appropriate data structure for this is a queue.

The operations on a queue are as follows:

- **EMPTY?(queue)** returns true only if there are no more elements in the queue.
- **POP(queue)** removes the first element of the queue and returns it.
- **INSERT(element, queue)** inserts an element and returns the resulting queue.

# Data structure -Queue

---

Three common Queue variants are

- First-in First-out (FIFO) : pops the oldest element of the queue
- Last-in First-out(LIFO) : pops the newest element of the queue
- Priority queue: pops the element of the queue with the highest priority according to some ordering function.

# Measuring problem-solving performance

---

The evaluation of a search strategy in 4 ways:

- **Completeness:**
  - is the strategy guaranteed to find a solution when there is one?
- **Optimality:**
  - does the strategy find the highest-quality solution when there are several different solutions?
- **Time complexity:**
  - how long does it take to find a solution?
- **Space complexity:**
  - how much memory is needed to perform the search?

# Measuring problem-solving performance

---

Graph is an explicit data structure that is input to the search program.

The typical measure is the size of the state space graph,  $|V| + |E|$

where V is the set of vertices (nodes) of the graph

E is the set of edges (links).

In AI, the graph is often represented implicitly by the initial state, actions, and transition model

# Measuring problem-solving performance

---

In AI, complexity is expressed with 3 quantities

- **b**, branching factor, maximum number of successors of any node
- **d**, the depth of the shallowest goal node.
- **m**, the maximum length of any path in the state space

Time and Space is measured in

- Time - number of nodes generated during the search
- Space -maximum number of nodes stored in memory

# Measuring problem-solving performance

---

For effectiveness of a search algorithm

- we can just consider the total cost
- **The total cost** = path cost ( $g$ ) of the solution found + search cost
  - search cost = time necessary to find the solution

Tradeoff:

- (long time, optimal solution with least  $g$ )
- vs. (shorter time, solution with slightly larger path cost  $g$ )

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---

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**Uniformed Search Strategies**

**Informed Search Strategies**

Heuristic Functions

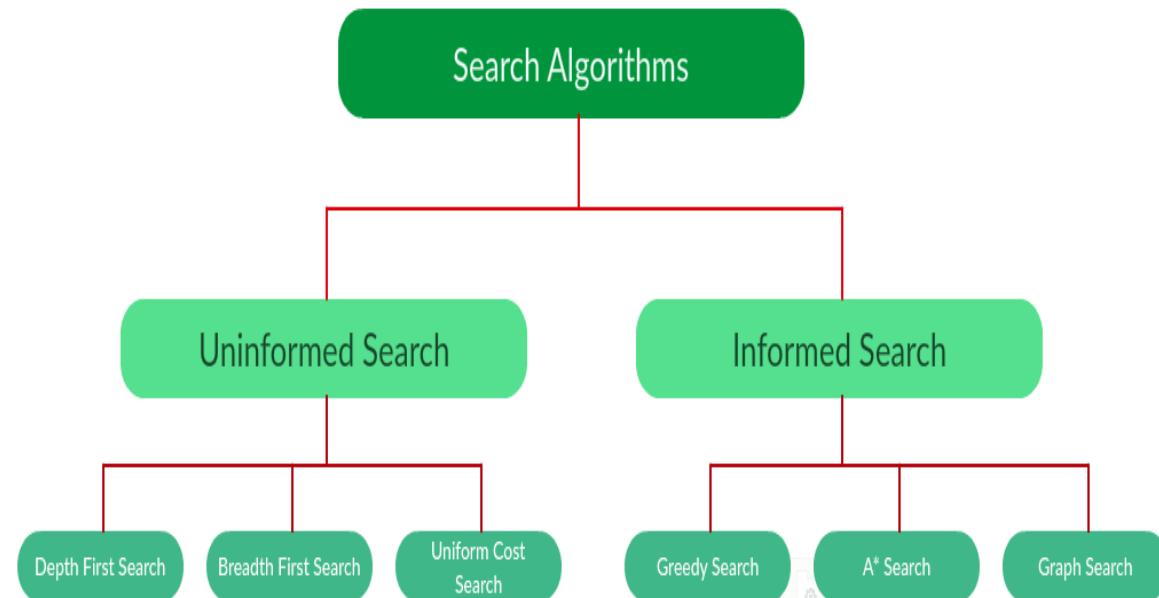
# Search strategies

## Uninformed search (Blind search)

- No information about the number of steps or the path cost from the current state to the goal
- Search the state space **blindly**

## Informed search, or heuristic search

- A cleverer strategy that searches toward the goal, based on the information from the current state so far



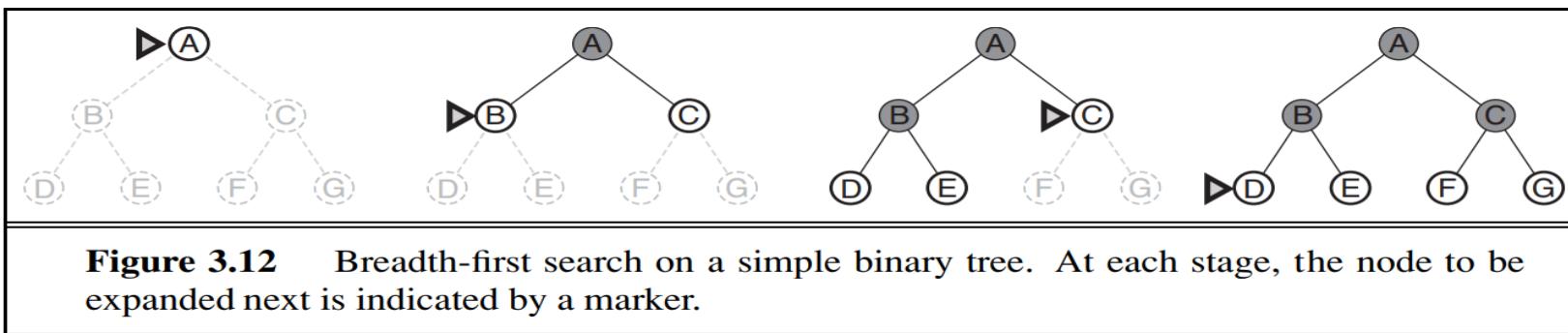
# Uninformed search strategies

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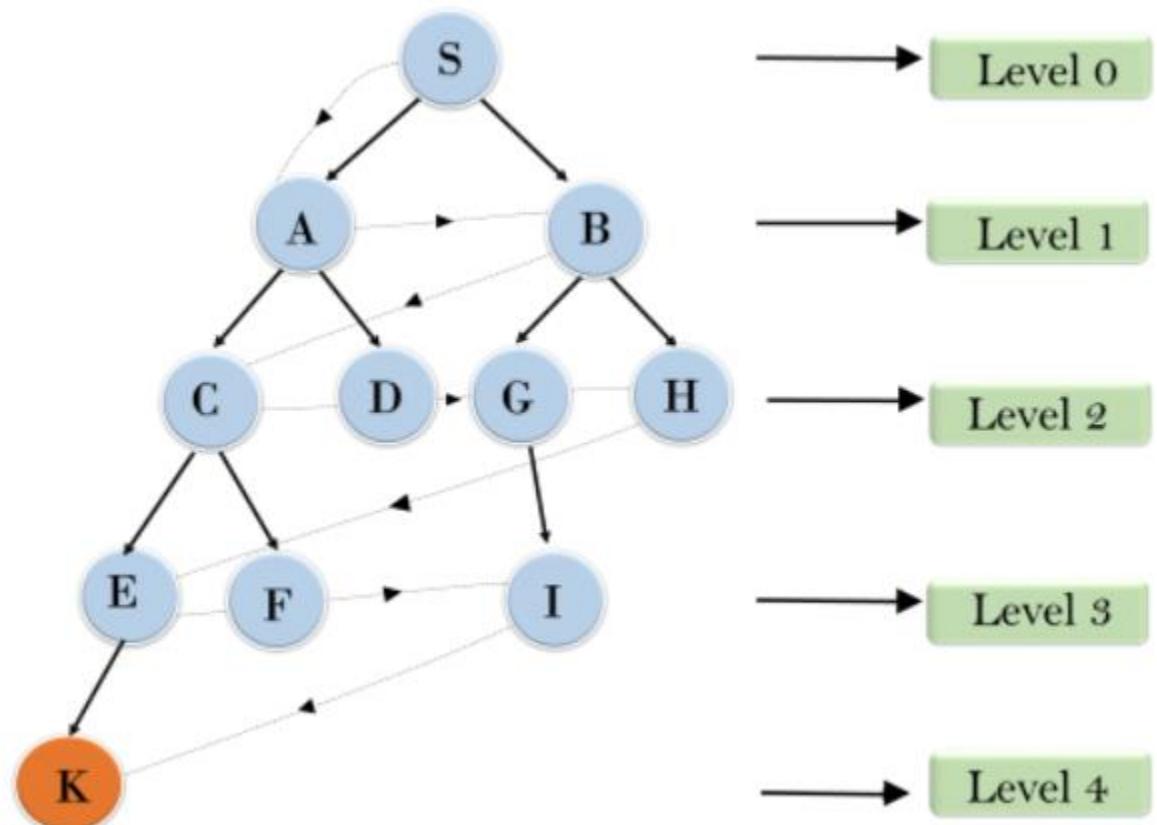
- 1. Breadth-first search
- 2. Uniform-cost search
- 3. Depth-first search
- 4. Depth-limited search
- 5. Iterative deepening depth-first search
- 6. Bidirectional search
- Comparing uninformed search strategies

# Breadth-first search

- Breadth-first search is the most common search strategy for **traversing a tree or graph**. This algorithm **searches breadthwise in a tree or graph**, so it is called breadth-first search.
- BFS algorithm starts searching **from the root node of the tree and expands all successor node at the current level** before moving to nodes of next level.
- Breadth-first search implemented using **FIFO queue** data structure.



# Example:Breadth-first search



S--->A--->B--->C--->D--->G--->H--->E--->F--->I--->K

# Breadth-first search

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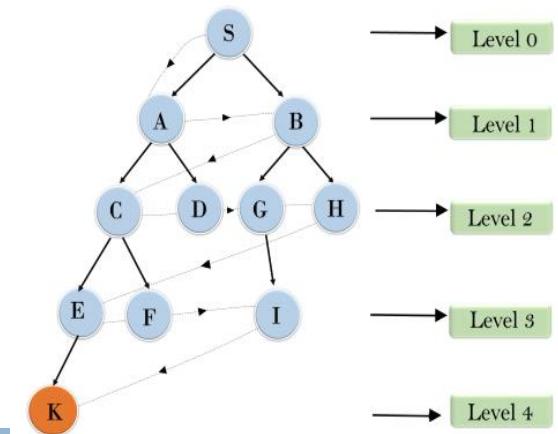
```
function BREADTH-FIRST-SEARCH(problem) returns a solution, or failure
  node  $\leftarrow$  a node with STATE = problem.INITIAL-STATE, PATH-COST = 0
  if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
  frontier  $\leftarrow$  a FIFO queue with node as the only element
  explored  $\leftarrow$  an empty set
  loop do
    if EMPTY?(frontier) then return failure
    node  $\leftarrow$  POP(frontier) /* chooses the shallowest node in frontier */
    add node.STATE to explored
    for each action in problem.ACTIONS(node.STATE) do
      child  $\leftarrow$  CHILD-NODE(problem, node, action)
      if child.STATE is not in explored or frontier then
        if problem.GOAL-TEST(child.STATE) then return SOLUTION(child)
        frontier  $\leftarrow$  INSERT(child, frontier)
```

# Properties of breadth-first search

- Completeness: BFS is complete, which means if the shallowest goal node is at some finite depth, then BFS will find a solution.
- Optimality : BFS is optimal if path cost is a non-decreasing function of the depth of the node.
- Time complexity: Number of nodes traversed in BFS until the shallowest Node. Where the **d= depth of shallowest solution** and **b is a node at every state.**

$$b + b^2 + b^3 + \dots + b^d = O(b^d)$$

- Space complexity: Memory size to store every level of the tree is  $O(b^d)$



# Breadth-first search

---

## Advantages:

- BFS will provide a solution if any solution exists.
- If there are more than one solutions for a given problem, then BFS will provide the minimal solution which requires the least number of steps.

## Disadvantage

- It requires lots of memory since each level of the tree must be saved into memory to expand the next level.
- BFS needs lots of time if the solution is far away from the root node.

# Uniform cost search

---

**Breadth-first** finds the shallowest goal state

- but not necessarily be the least-cost solution
- work only if all step costs are equal

## Uniform cost search

- modifies breadth-first strategy by always expanding the lowest-cost node
- The lowest-cost node is measured by the path cost  $g(n)$

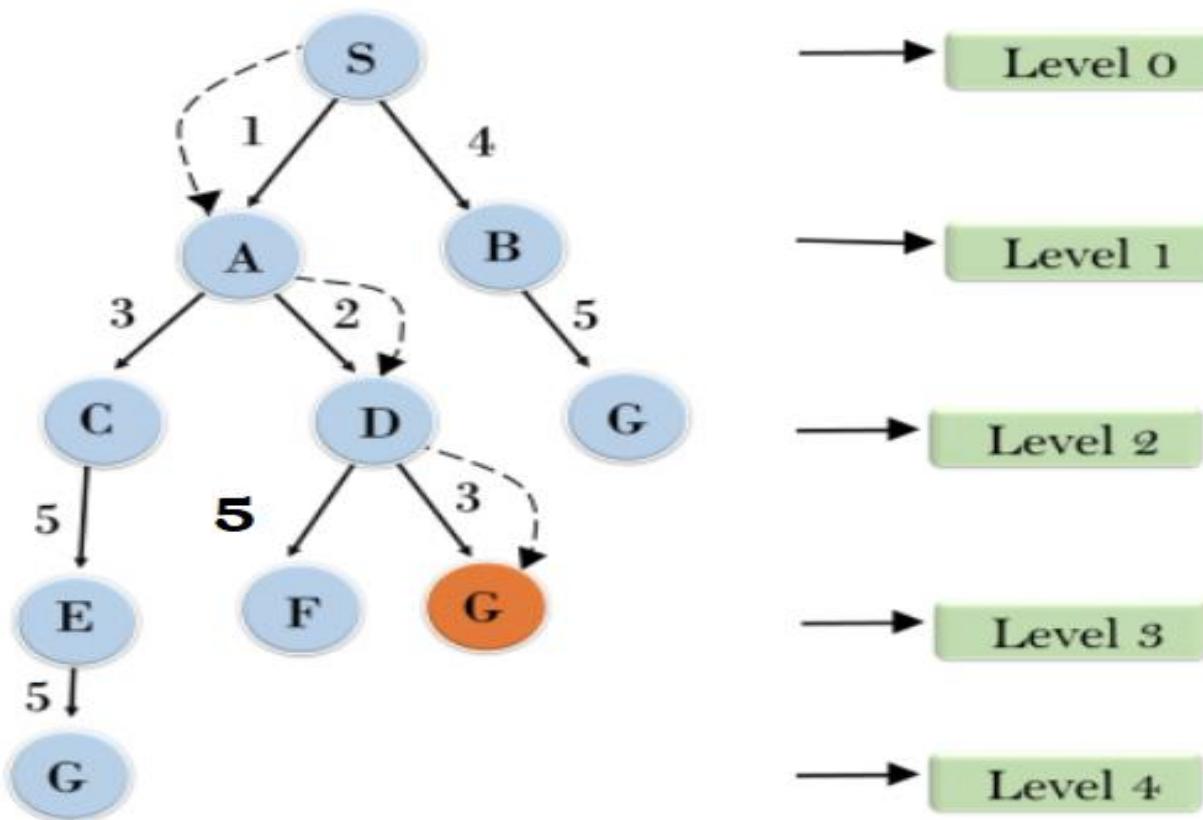
# Uniform cost search

---

- Uniform-cost search is a searching algorithm used for traversing a weighted tree or graph.
- This algorithm comes into play when a different cost is available for each edge.
- The primary goal of the uniform-cost search is to find a path to the goal node which has the lowest cumulative cost.
- Uniform-cost search expands nodes according to their path costs from the root node.
- A uniform-cost search algorithm is implemented by the priority queue.

# Example: Uniform cost search

---



# Uniform cost search

---

```
function UNIFORM-COST-SEARCH(problem) returns a solution, or failure
  node  $\leftarrow$  a node with STATE = problem.INITIAL-STATE, PATH-COST = 0
  frontier  $\leftarrow$  a priority queue ordered by PATH-COST, with node as the only element
  explored  $\leftarrow$  an empty set
  loop do
    if EMPTY?(frontier) then return failure
    node  $\leftarrow$  POP(frontier) /* chooses the lowest-cost node in frontier */
    if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
    add node.STATE to explored
    for each action in problem.ACTIONS(node.STATE) do
      child  $\leftarrow$  CHILD-NODE(problem, node, action)
      if child.STATE is not in explored or frontier then
        frontier  $\leftarrow$  INSERT(child, frontier)
      else if child.STATE is in frontier with higher PATH-COST then
        replace that frontier node with child
```

# Uniform cost search

---

- Completeness: Is complete, as if there is a solution, UCS will find it.
- Optimality : Is optimal as it only selects a path with the lowest path cost.
- Time complexity:

Let  $C^*$  is Cost of the optimal solution,

$\varepsilon$  is each step to get closer to the goal node.

Then the number of steps is  $= C^*/\varepsilon + 1$ .

Here we have taken  $+1$ , as we start from state 0 and end to  $C^*/\varepsilon$ .

Worst-case time complexity of Uniform-cost search is  $O(b^{1 + [C^*/\varepsilon]})$ .

- Space complexity: Worst-case space complexity of Uniform-cost search is  $O(b^{1 + [C^*/\varepsilon]})$ .

# Uniform cost search

---

## Advantages:

- Uniform cost search is optimal because at every state the path with the least cost is chosen.

## Disadvantages:

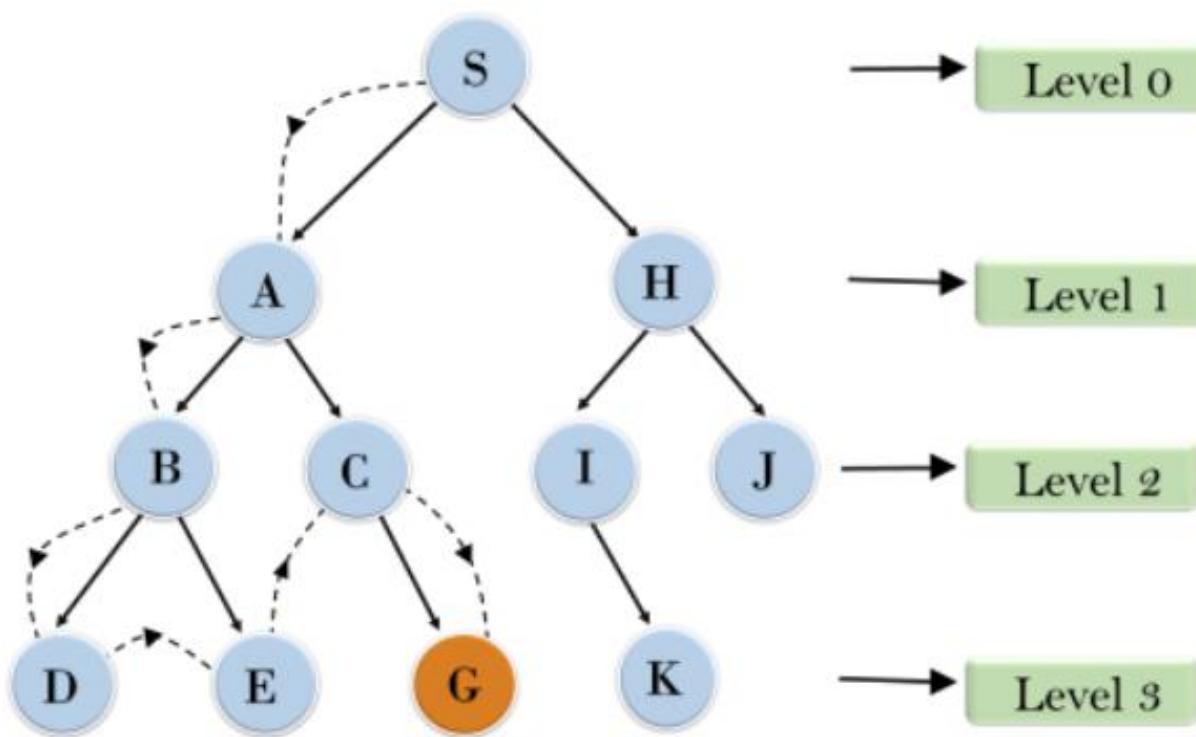
- It does not care about the number of steps involved in searching and only concerned about path cost. Due to which this algorithm may be stuck in an infinite loop.

# Depth-first search

---

- Depth-first search is a recursive algorithm **for traversing a tree or graph data structure.**
- It is called the depth-first search because it **starts from the root node and follows each path to its greatest depth node** before moving to the next path.
- DFS uses a **STACK**.

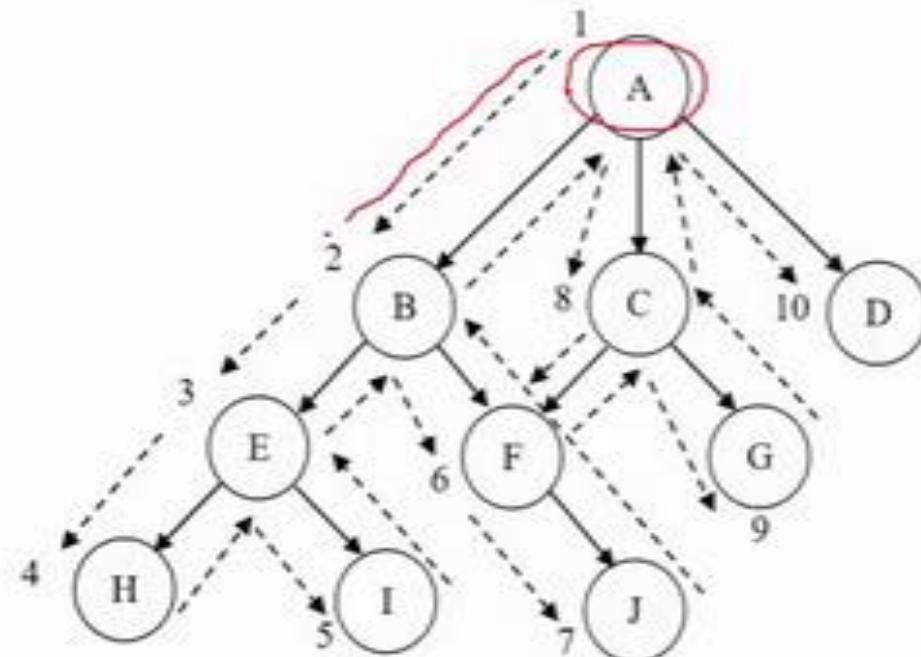
# Example: Depth-first search



# Example: Depth-first search

Q) Apply the depth first search algorithm on the following graph , where the start state is (A) and the desired goal state is (G),show the successive values of open and closed ,and the traversed path

Iteration #	X	open	closed
0	-	[A]	[]
1	A	[BCD]	[A]
2	B	[EFCD]	[BA]
3	E	[HIFCD]	[EBA]
4	H	[IFCD]	[HEBA]
5	I	[FCD]	[IHEBA]
6	F	[JCD]	[FIHEBA]
7	J	[CD]	[JFIHEBA]
8	C	[GD]	[CJFIHEBA]
9	G	G is the goal	



# Depth-first search

---

- Completeness: Is complete within finite state space as it will expand every node within a limited search tree.
- Optimal: Is non-optimal, as it may generate a large number of steps or high cost to reach to the goal node.
- Time Complexity: Time complexity of DFS will be equivalent to the node traversed by the algorithm. It is given by:  $O(b^m)$ 

Where, m= maximum depth of any node and this can be much larger than d
- Space Complexity: DFS algorithm needs to store only single path from the root node, hence space complexity of DFS is equivalent to the size of the fringe set, which is  $O(bm)$ .

# Depth-first search

---

## Advantage:

- DFS requires very **less memory** as it only needs to store a stack of the nodes on the path from root node to the current node.
- It takes **less time to reach to the goal node** than BFS algorithm (if it traverses in the right path).

## Disadvantage:

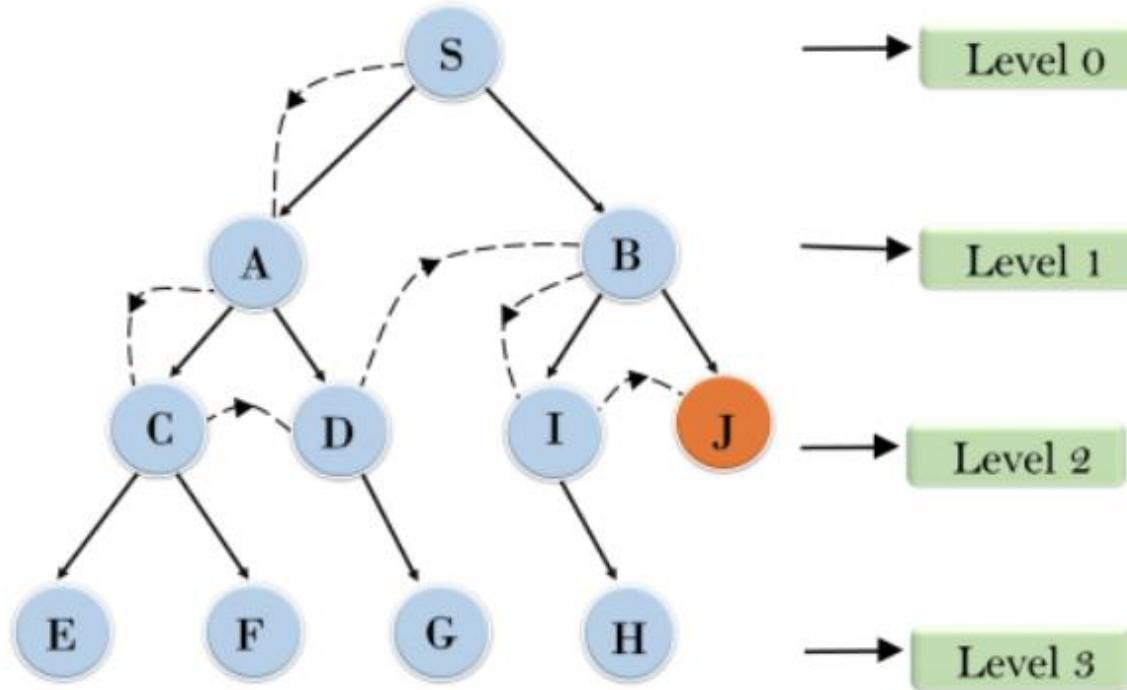
- There is the possibility that many states keep re-occurring, and there is **no guarantee of finding the solution**.
- DFS algorithm goes for deep down searching and sometime it may **go to the infinite loop**

# Depth-Limited Search Algorithm

---

- A depth-limited search algorithm is similar to DFS with **a predetermined limit**.
- Depth-limited search can solve the drawback of the infinite path in the Depth-first search.
- In this algorithm, the **node at the depth limit will treat as it has no successor nodes further**.
- Depth-limited search can be terminated with two Conditions of failure:
  - Standard failure value: It indicates that problem does not have any solution.
  - Cutoff failure value: It defines no solution for the problem within a given depth limit.

# Example: Depth-Limited Search Algorithm



# Depth-Limited Search Algorithm

---

```
function DEPTH-LIMITED-SEARCH(problem, limit) returns a solution, or failure/cutoff
  return RECURSIVE-DLS(MAKE-NODE(problem.INITIAL-STATE), problem, limit)

function RECURSIVE-DLS(node, problem, limit) returns a solution, or failure/cutoff
  if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
  else if limit = 0 then return cutoff
  else
    cutoff_occurred?  $\leftarrow$  false
    for each action in problem.ACTIONS(node.STATE) do
      child  $\leftarrow$  CHILD-NODE(problem, node, action)
      result  $\leftarrow$  RECURSIVE-DLS(child, problem, limit - 1)
      if result = cutoff then cutoff_occurred?  $\leftarrow$  true
      else if result  $\neq$  failure then return result
    if cutoff_occurred? then return cutoff else return failure
```

# Properties of Depth-limited search

---

Completeness: Is complete if the solution is above the depth-limit.

Optimal: Depth-limited search can be viewed as a special case of DFS, and it is also not optimal even if  $\ell > d$ .

Time Complexity: Time complexity of DLS algorithm is  $O(b^\ell)$ .

Space Complexity: Space complexity of DLS algorithm is  $O(b\ell)$ .

# Depth-limited search

---

Advantages:

- Depth-limited search is **Memory efficient**.

Disadvantages:

- Depth-limited search also has a disadvantage of **incompleteness**.
- It may **not be optimal** if the problem has more than one solution.

# Iterative deepening depth-first search

---

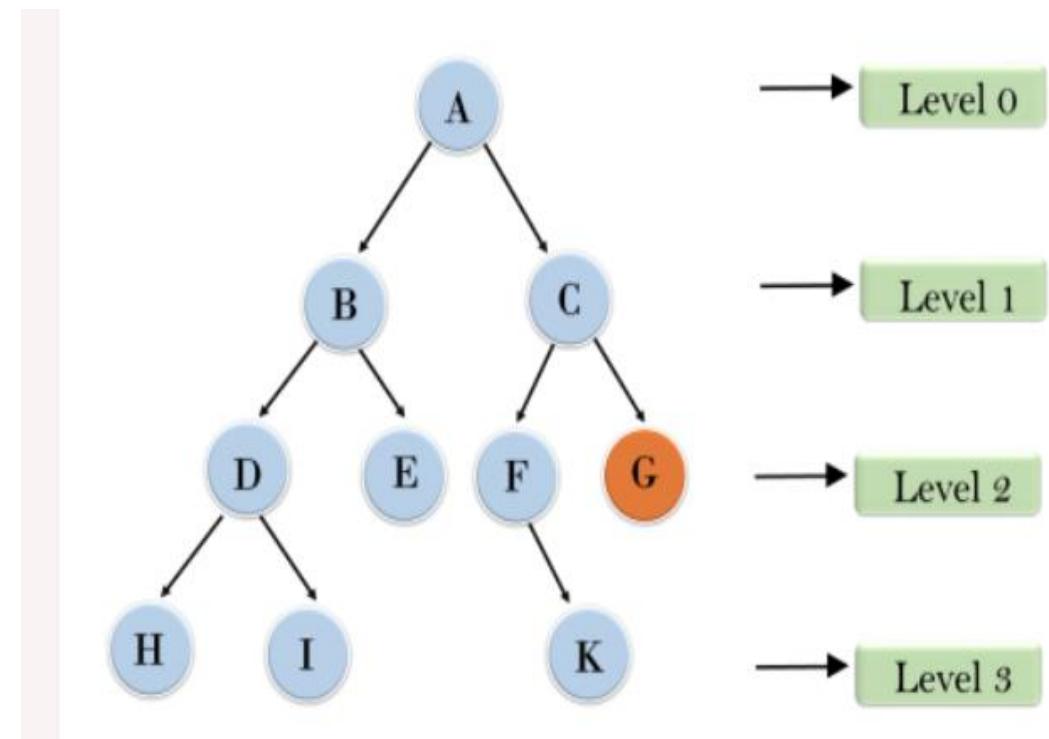
- It is a combination of DFS and DLS algorithms.
- This search algorithm **finds out the best depth limit** and does it by gradually **increasing the limit until a goal is found**.
- This Search algorithm combines the benefits of Breadth-first search's fast search and depth-first search's memory efficiency.
- The iterative search algorithm **is useful uninformed search when search space is large, and depth of goal node is unknown**.

# Example: Iterative deepening depth-first search

1'st Iteration----> A **d=0**

2'nd Iteration----> A -> B -> C **d=1**

3'rd Iteration---->A, B, D, E, C, F, G **d=2**



# Iterative deepening depth-first search

---

```
function ITERATIVE-DEEPENING-SEARCH(problem) returns a solution, or failure
    for depth = 0 to  $\infty$  do
        result  $\leftarrow$  DEPTH-LIMITED-SEARCH(problem, depth)
        if result  $\neq$  cutoff then return result
```

# Iterative deepening search (Analysis)

---

## Advantages:

- It combines the benefits of BFS and DFS search algorithm in terms of **fast search and memory efficiency**.

## Disadvantages:

- The main drawback is that it repeats all the work of the previous phase.

# Properties of iterative deepening search

---

- Completeness: Is complete if the branching factor is finite.
- Optimal: **Is optimal** if path cost is a non-decreasing function of the depth of the node.
- Time Complexity: Let's suppose b is the branching factor and depth is d then the worst-case time complexity is  **$O(b^d)$** .
- Space Complexity: The space complexity is  **$O(bd)$** .

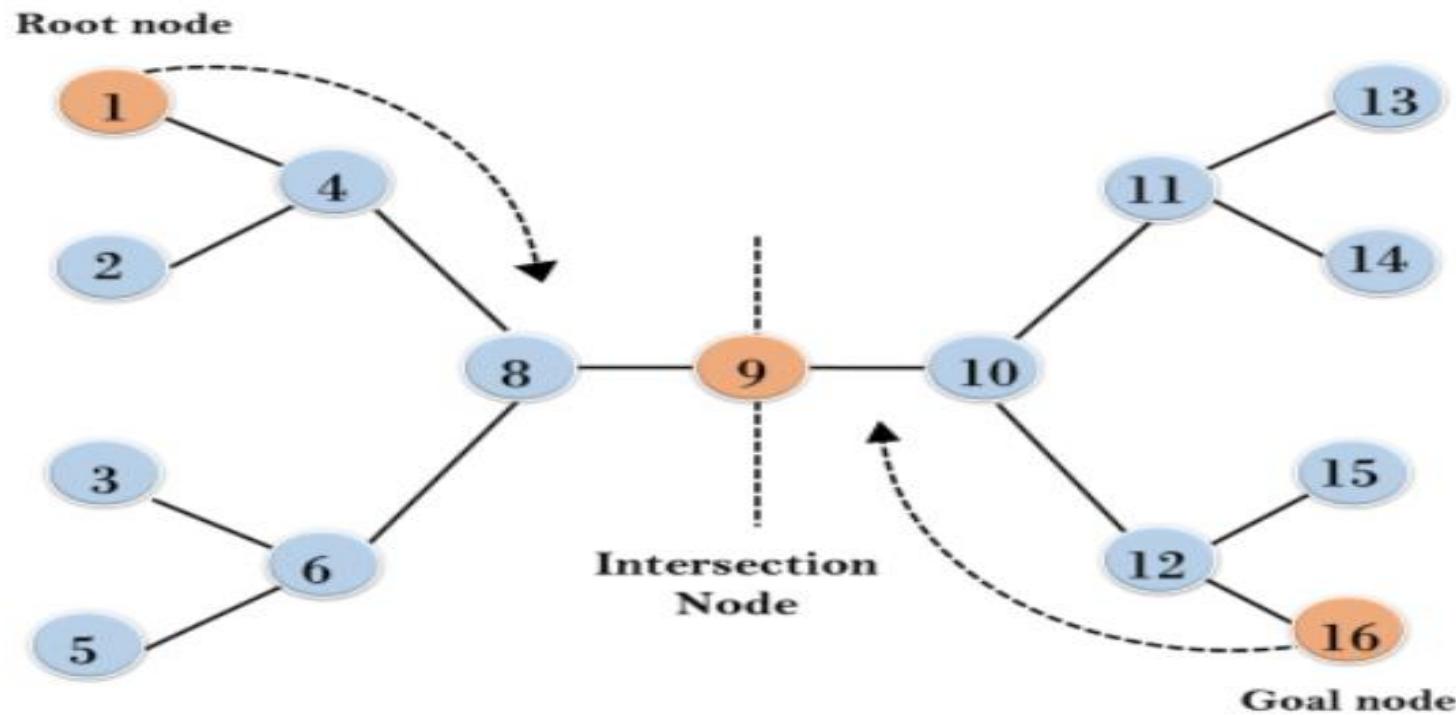
# Bidirectional search

---

- Bidirectional search divides one single search graph with two small subgraphs in which one starts the search from an initial vertex and other starts from goal vertex.
- Bidirectional search algorithm runs two simultaneous searches,
  - one from initial state called as **forward-search** and
  - other from goal node called as **backward-search**, to find the goal node.
- The search stops when these two graphs intersect each other.
- Bidirectional search can use search techniques such as BFS, DFS, DLS, etc.

# Example Bidirectional search

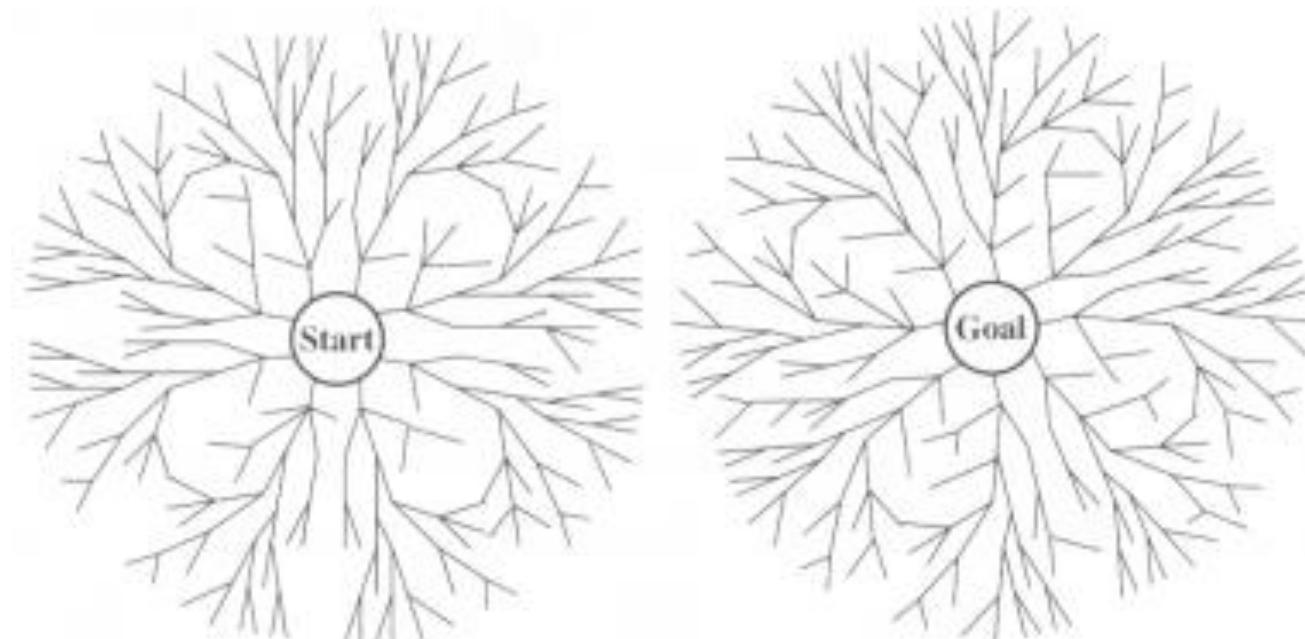
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# Bidirectional search

---

A schematic view of a bidirectional search that is about to succeed when a branch from the start node meets a branch from the goal node.



# Bidirectional search

---

Completeness: Is complete if we use BFS in both searches.

Optimal: Is Optimal.

Time Complexity: Time complexity of bidirectional search using BFS is  $O(b^{d/2})$ .

Space Complexity: Space complexity of bidirectional search is  $O(b^{d/2})$ .

# Bidirectional search

---

Advantages:

- Bidirectional search **is fast.**
- Bidirectional search **requires less memory**

Disadvantages:

- Implementation of the bidirectional search tree **is difficult.**
- In bidirectional search, one should know the **goal state in advance.**

# Comparing search strategies

Criterion	Breadth-First	Uniform-Cost	Depth-First	Depth-Limited	Iterative Deepening	Bidirectional (if applicable)
Complete?	Yes <sup>a</sup>	Yes <sup>a,b</sup>	No	No	Yes <sup>a</sup>	Yes <sup>a,d</sup>
Time	$O(b^d)$	$O(b^{1+\lfloor C^*/\epsilon \rfloor})$	$O(b^m)$	$O(b^\ell)$	$O(b^d)$	$O(b^{d/2})$
Space	$O(b^d)$	$O(b^{1+\lfloor C^*/\epsilon \rfloor})$	$O(bm)$	$O(b\ell)$	$O(bd)$	$O(b^{d/2})$
Optimal?	Yes <sup>c</sup>	Yes	No	No	Yes <sup>c</sup>	Yes <sup>c,d</sup>

**Figure 3.21** Evaluation of tree-search strategies.  $b$  is the branching factor;  $d$  is the depth of the shallowest solution;  $m$  is the maximum depth of the search tree;  $\ell$  is the depth limit. Superscript caveats are as follows: <sup>a</sup> complete if  $b$  is finite; <sup>b</sup> complete if step costs  $\geq \epsilon$  for positive  $\epsilon$ ; <sup>c</sup> optimal if step costs are all identical; <sup>d</sup> if both directions use breadth-first search.

# Informed search strategies

---

The informed search algorithm is more useful for large search space.

Informed search algorithm uses the idea of heuristic, so it is also called Heuristic search.

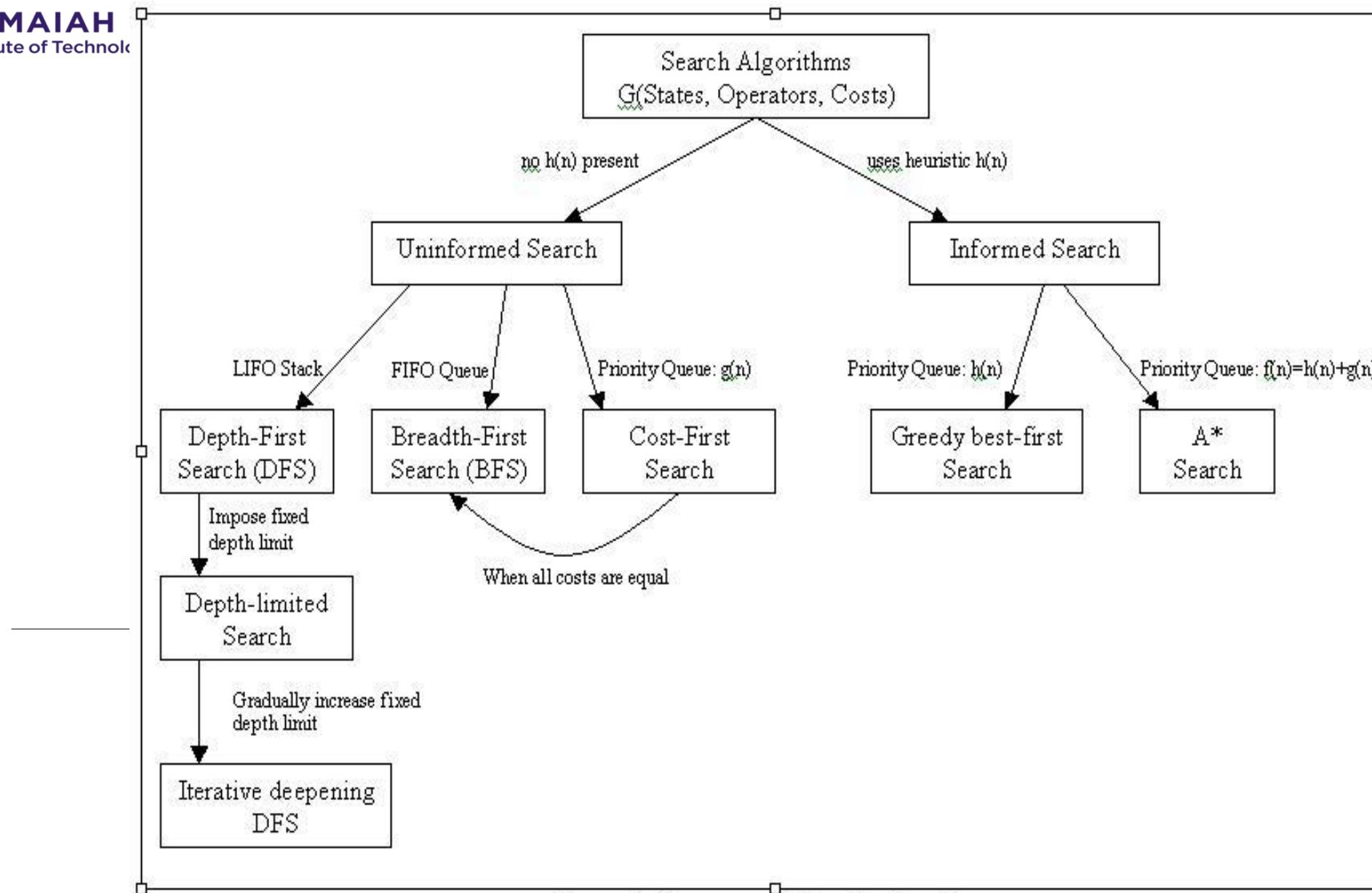


Figure 4: Taxonomy of Search Algorithms

# Outline

---

Best-first search

Greedy best-first search

A\* search

Heuristics

A search strategy is defined by picking the **order of node expansion**

# Informed search algorithms

---

## Informed Search

- Also called heuristic search
- Use problem-specific knowledge
- Search strategy: a node is selected for exploration based on an
  - evaluation function,
  - Estimate of desirability

## Evaluation function generally consists of two parts

- The path cost from the initial state to a node  $n$ ,  $g(n)$ (optional)
- The estimated cost of the cheapest path from a node  $n$  to a goal node, the heuristic function, $h(n)$ .  
If the node  $n$  is a goal state  $\rightarrow h(n)=0$   
Can't be computed from the problem definition (need experience)

# Informed search strategies

---

- **Heuristics function:** Heuristic is a function which is used in Informed Search, and it finds the most promising path.
- It takes the current state of the agent as its input and produces the estimation of how close agent is from the goal.
- It is represented by  $h(n)$ , and it calculates the cost of an optimal path between the pair of states.
- The value of the heuristic function is always positive.

# Informed search strategies

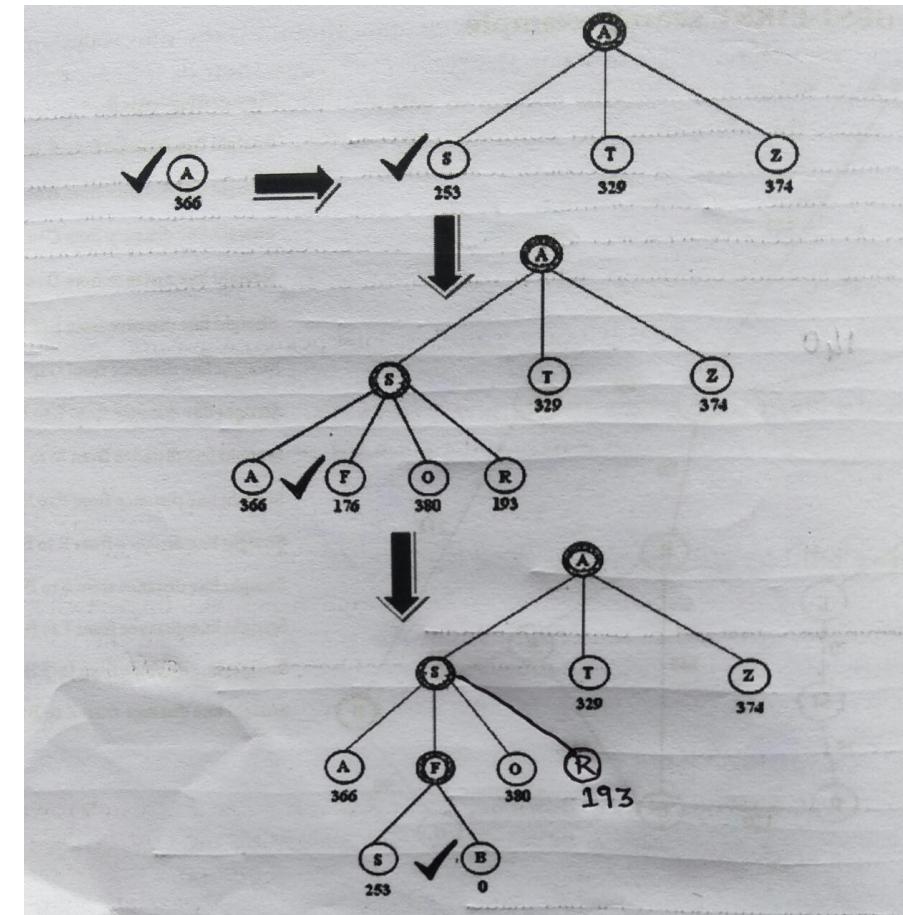
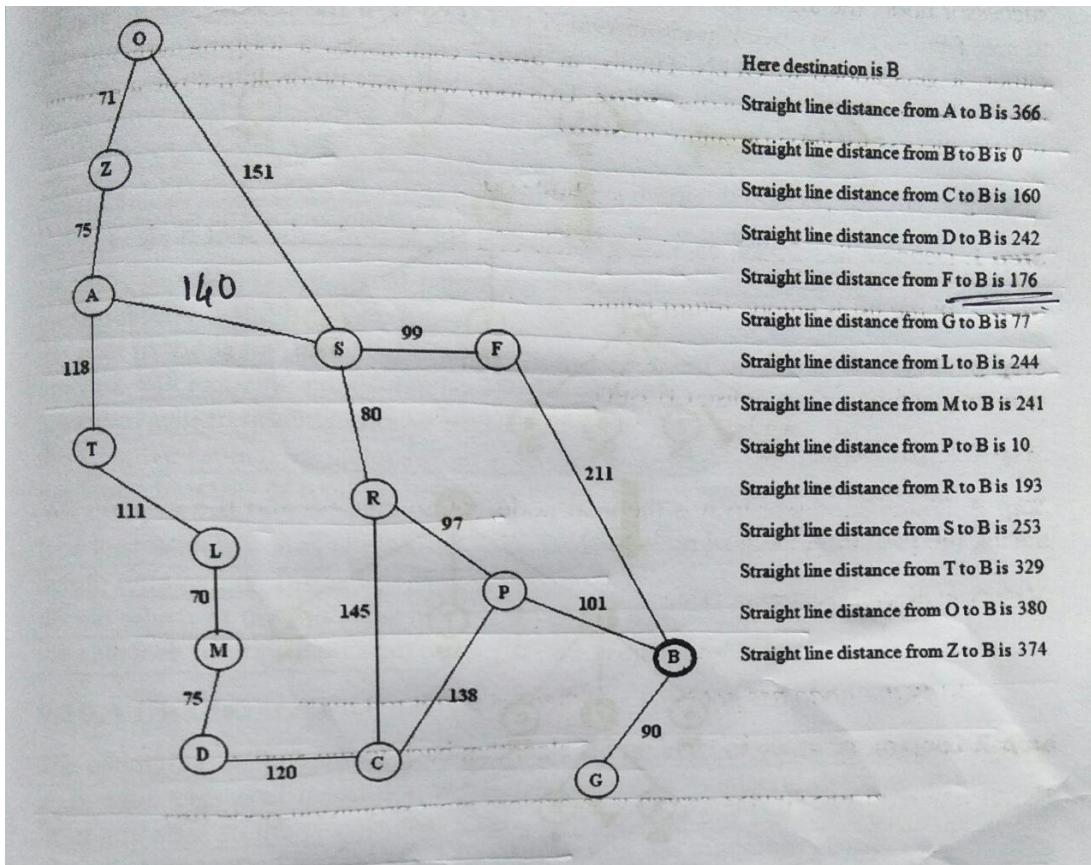
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- Heuristic search algorithms **expands nodes based on their heuristic value  $h(n)$ .**
- It maintains two lists, OPEN and CLOSED list.
- In the CLOSED list, it places those nodes which have already expanded
- In the OPEN list, it places nodes which have yet not been expanded.
- On each iteration, each node  $n$  with the lowest heuristic value is expanded and generates all its successors and  $n$  is placed to the closed list.
- The algorithm continues until a goal state is found.
  - **Best First Search Algorithm(Greedy search)**
  - **A\* Search Algorithm**

# Best First Search Example

A is the start state

B is the Goal State



# Best First Search Algorithm

**Step 1.** Define a list, OPEN, consisting solely of a single node, the start node, s.

**Step 2.** IF the list is empty, return failure.

**Step 3.** Remove from the list the node n with the best score (the node where f is the minimum), and move it to a list, CLOSED.

**Step 4.** Expand node n.

**Step 5.** IF any successor to n is the goal node, return success and the solution (by tracing the path from the goal node to s).

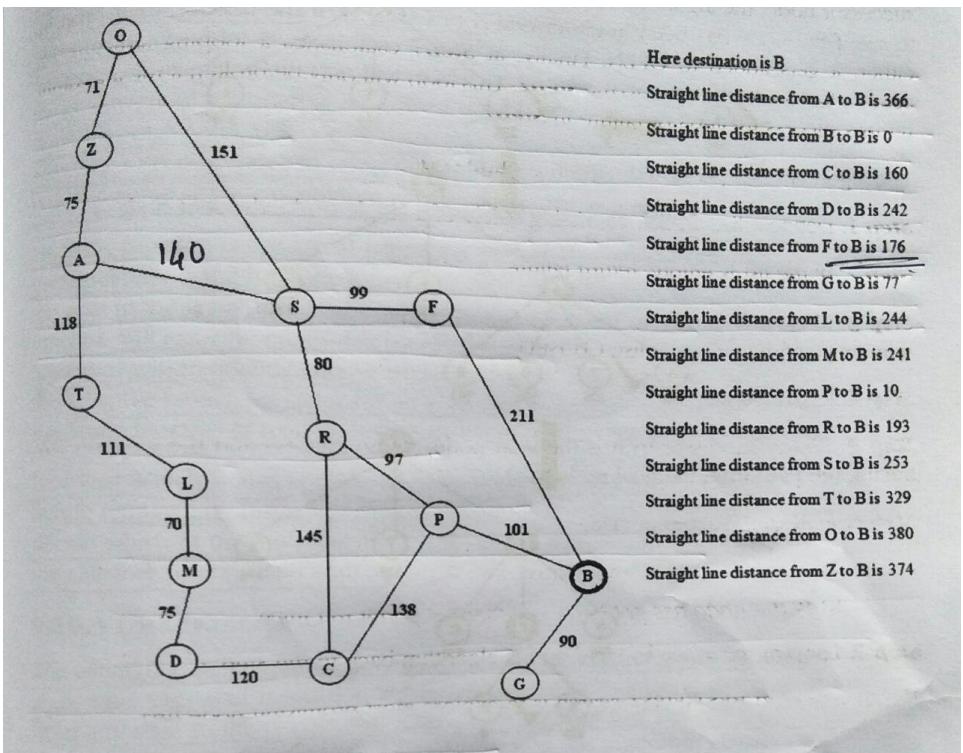
**Step 6.** FOR each successor node:

a) apply the evaluation function, f, to the node.

b) IF the node has not been in either list, add it to OPEN.

**Step 7.** Looping structure by sending the algorithm back to the Step 2.

# Best First Search Example Tracing



Start Node: A

Goal Node: B

Step 1: OPEN = {A}  $\begin{matrix} 366 \\ \{ \} \end{matrix}$

CLOSED = {}

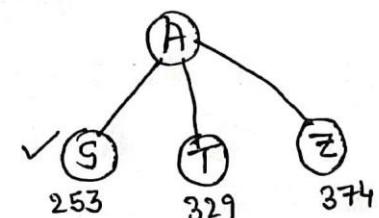
Step 2: List OPEN is not empty.

Step 3: Remove 'A' from OPEN and put it in CLOSED

OPEN = {}

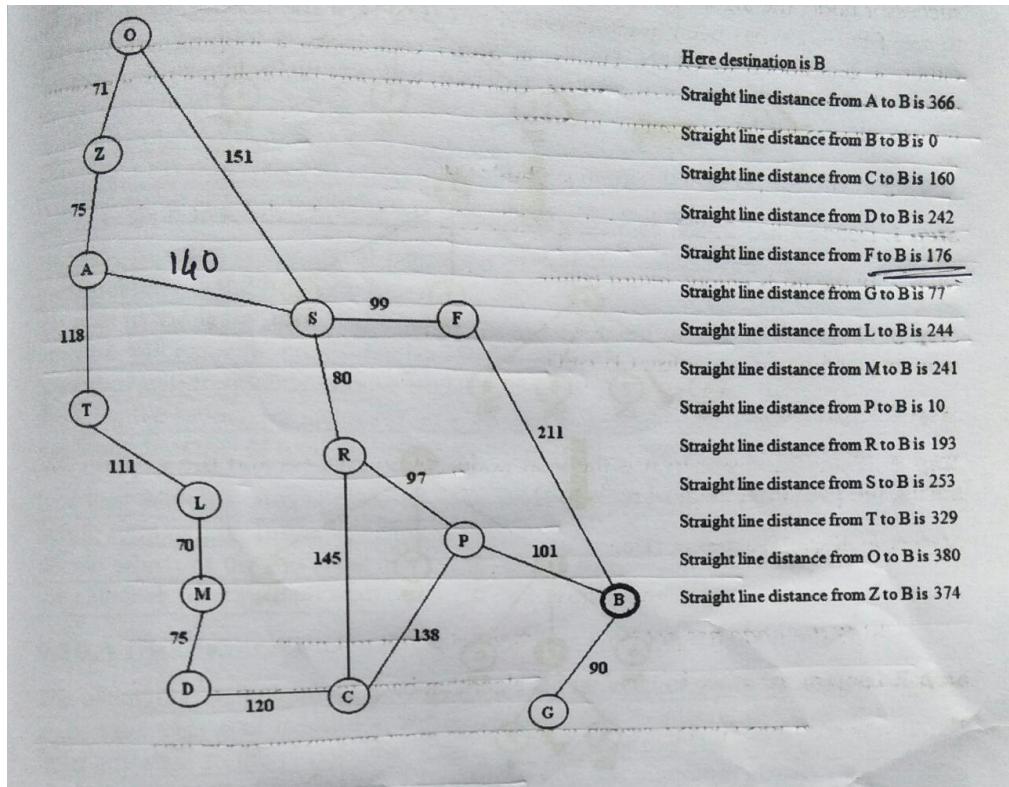
CLOSED = {A}

Step 4: Expand 'A'



Step 5: No successor of A ( $\{S, T, Z\}$ ) is goal state.

# Best First Search Example Tracing



Step 6: For each successor node,

1. S

OPEN = {S}  
253

CLOSED = {A}

2. T

OPEN = {S, T}  
253 329

CLOSED = {A}

3. Z

OPEN = {S, T, Z}  
253 329 374

CLOSED = {A}

Step 7: Control back to Step 2.

Step 2: List OPEN is not empty.

Step 3: Remove S (best score - 253) from OPEN and store it in CLOSED.

OPEN = {T, Z}  
329 374

CLOSED = {A, S}

# Best First Search Algorithm (For reference to solve problem)

**Step 1.** Define a list, OPEN, consisting solely of a single node, the start node, s.

**Step 2.** IF the list is empty, return failure.

**Step 3.** Remove from the list the node n with the best score (the node where f is the minimum), and move it to a list, CLOSED.

**Step 4.** Expand node n.

**Step 5.** IF any successor to n is the goal node, return success and the solution (by tracing the path from the goal node to s).

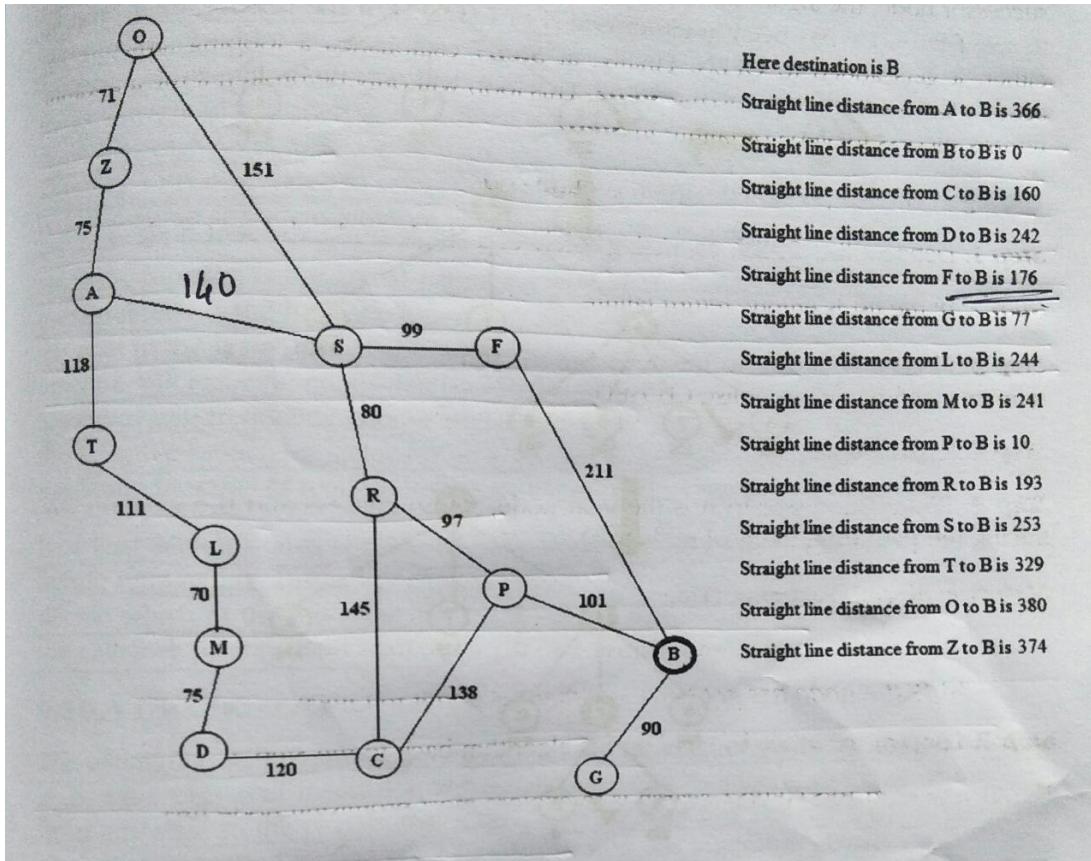
**Step 6.** FOR each successor node:

a) apply the evaluation function, f, to the node.

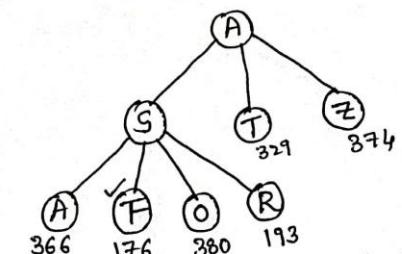
b) IF the node has not been in either list, add it to OPEN.

**Step 7.** Looping structure by sending the algorithm back to the Step 2.

# Best First Search Example Tracing



Step 4: Expand 'S'



Step 5: No successor of 'S' ( $\{A, F, O, R\}$ ) is goal state.

Step 6: For each successor node,

1. A (It is in CLOSED list already considered)

2. F

$$OPEN = \{T, Z, F\} \quad CLOSED = \{A, Z\}$$

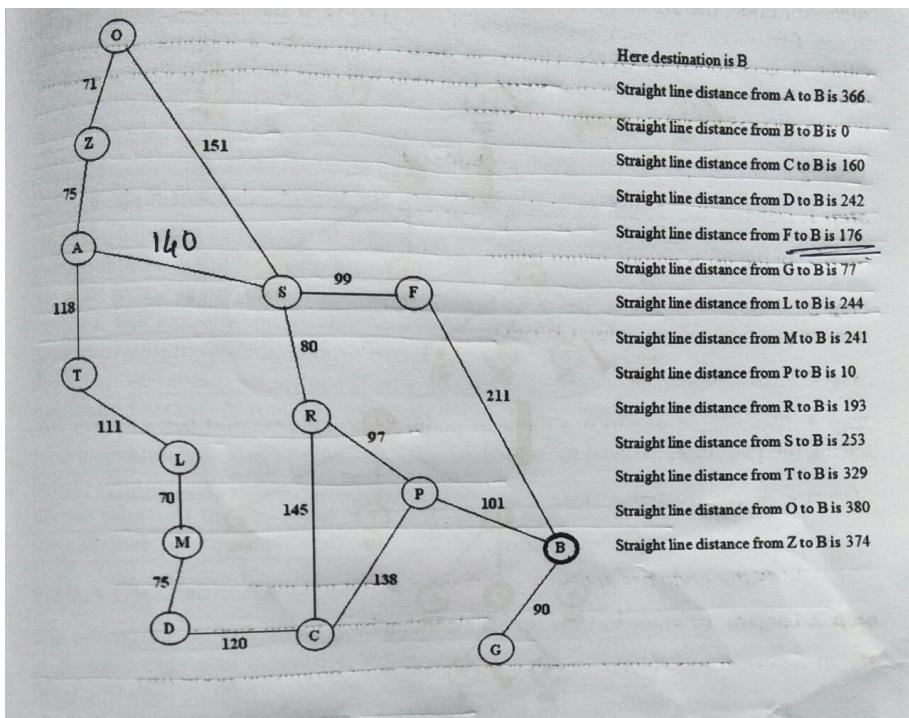
3. O

$$OPEN = \{T, Z, F, O\} \quad CLOSED = \{A, Z\}$$

4. R

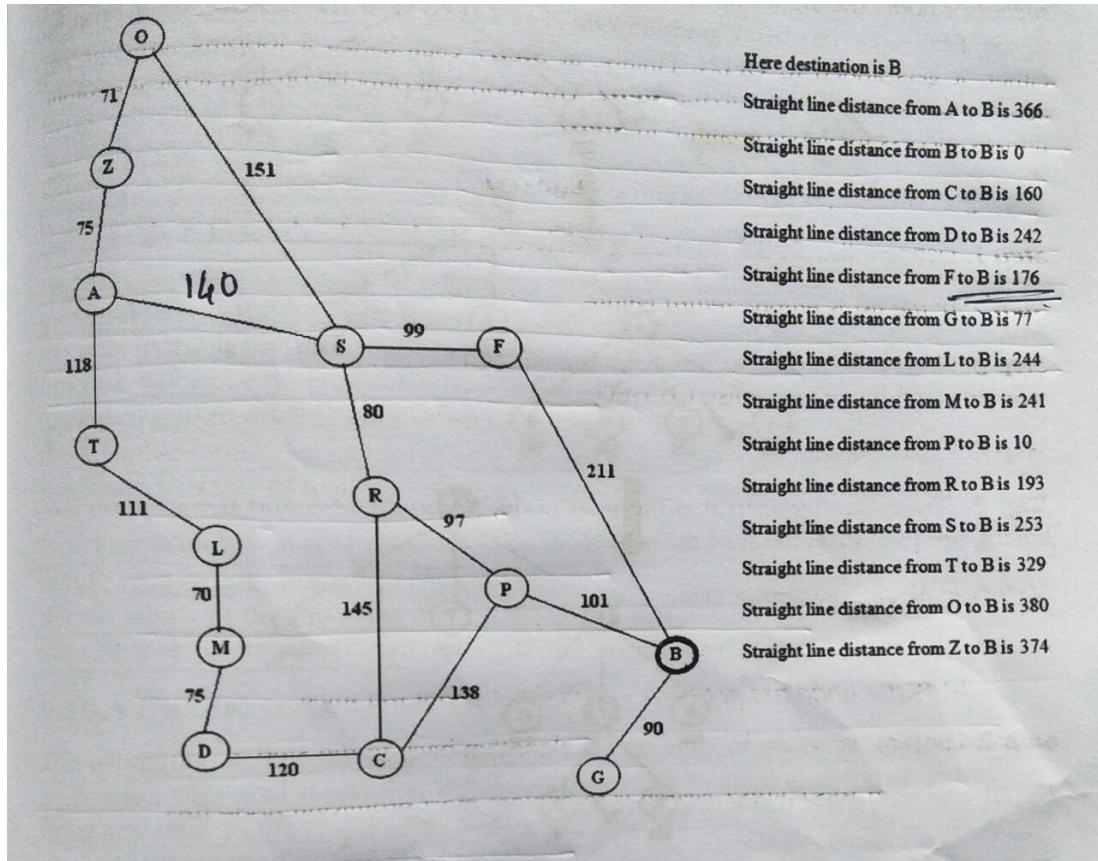
$$OPEN = \{T, Z, F, O, R\} \quad CLOSED = \{A, Z\}$$

# Best First Search Example Tracing



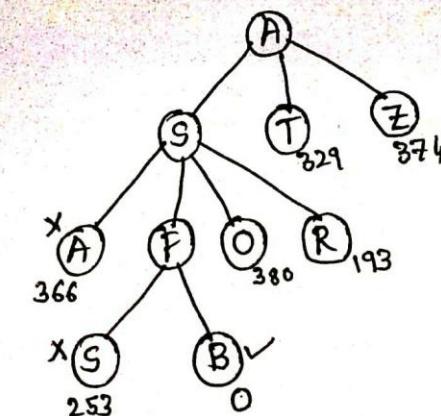
- Step 7: control back to Step 2.
- Step 2: List OPEN is not empty.
- Step 3: Remove F (best score - 176) from OPEN  
and store it in CLOSED
- $OPEN = \{T, Z, O, R\}$        $CLOSED = \{A, Z, F\}$
- $329 \quad 374 \quad 380 \quad 193$

# Best First Search Example Tracing



CS Scanned with CamScanner

Step 4: Expand node F



Step 5: Successor of F, B is the goal node.  
return success and the solution path  
 $\{A \rightarrow S \rightarrow F \rightarrow B\}$

# Properties of Best First Search

---

## Complete?

No – can get stuck in loops.

## Time?

$O(b^m)$ , but a good heuristic can give dramatic improvement.

b – branching factor, m – depth

## Space?

$O(b^m)$  - keeps all nodes in memory.

## Optimal?

No.

# Greedy best-first search

---

- It is the combination of DFS and BFS.
- With the help of best-first search, at each step, we can choose the most promising node, we expand the node which is closest to the goal node and the closest cost is estimated by heuristic function, i.e.
- The greedy best first algorithm is implemented by the priority queue.
- A key component of these algorithms is a heuristic function denoted  $h(n)$
- Thus, it evaluates nodes by using just the heuristic function

$$f(n) = h(n)$$

$h(n)$ = estimated cost from node n to the goal.

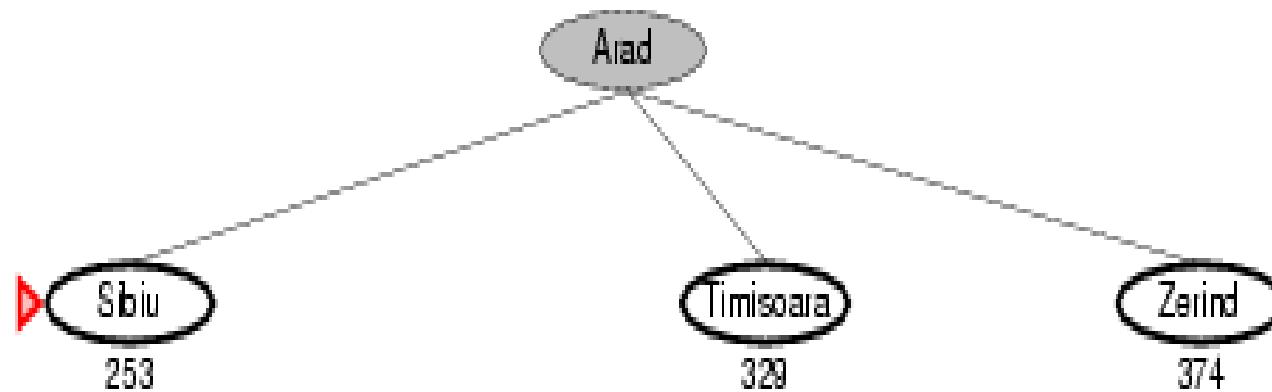
# Greedy best-first search example

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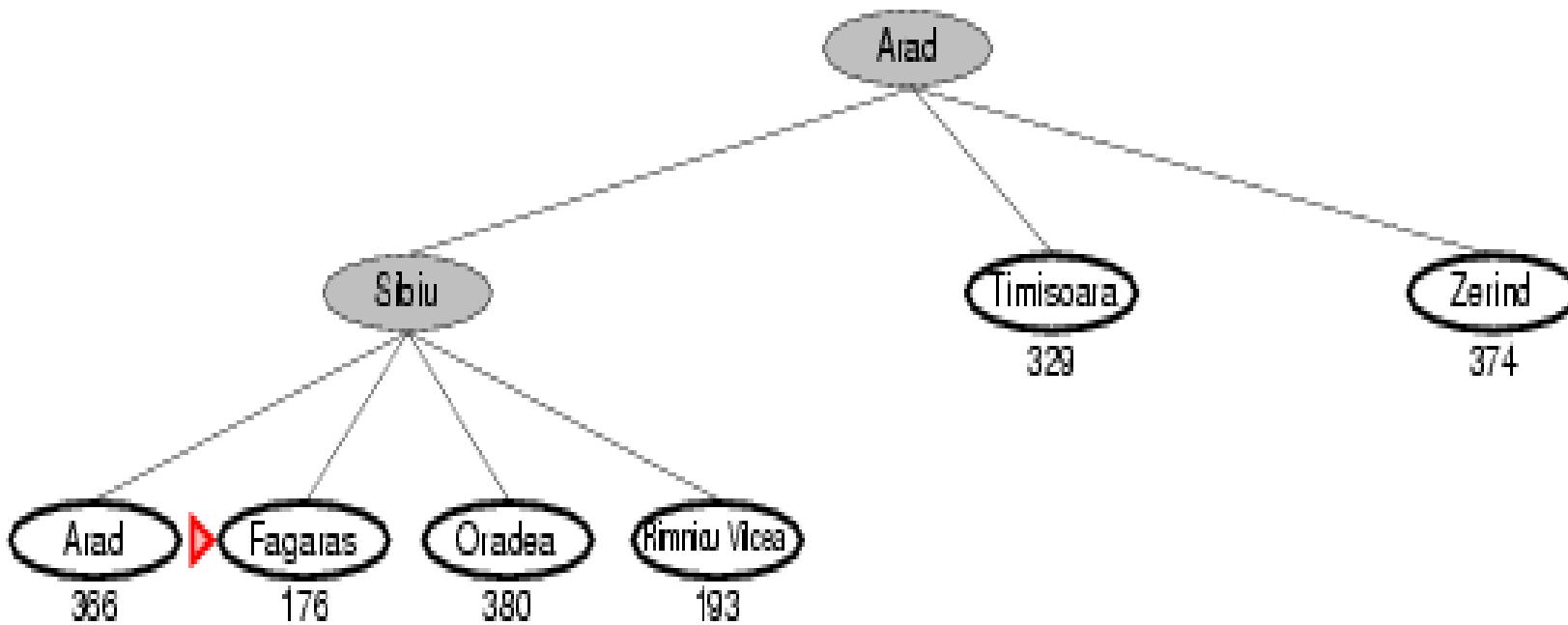
# Greedy best-first search example

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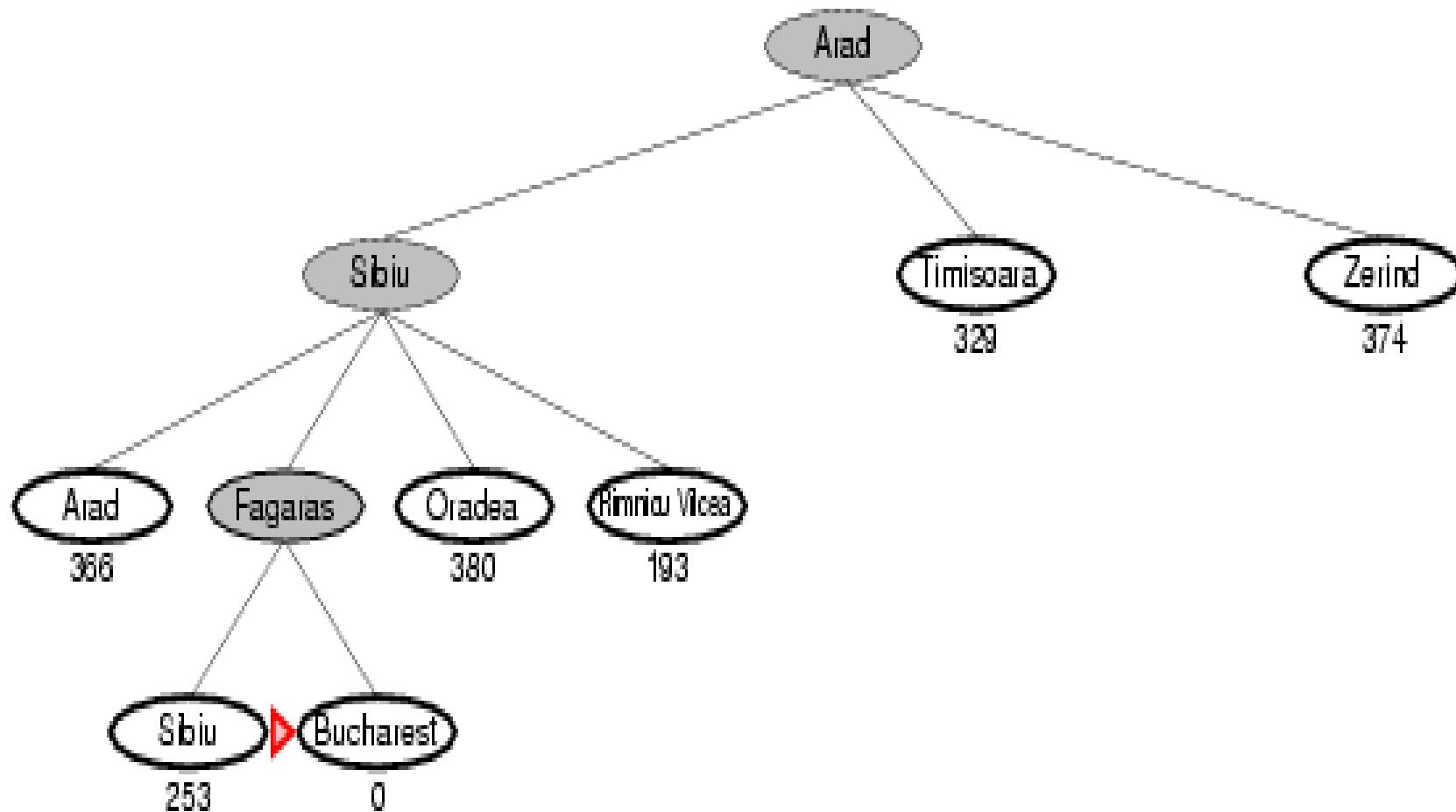
# Greedy best-first search example

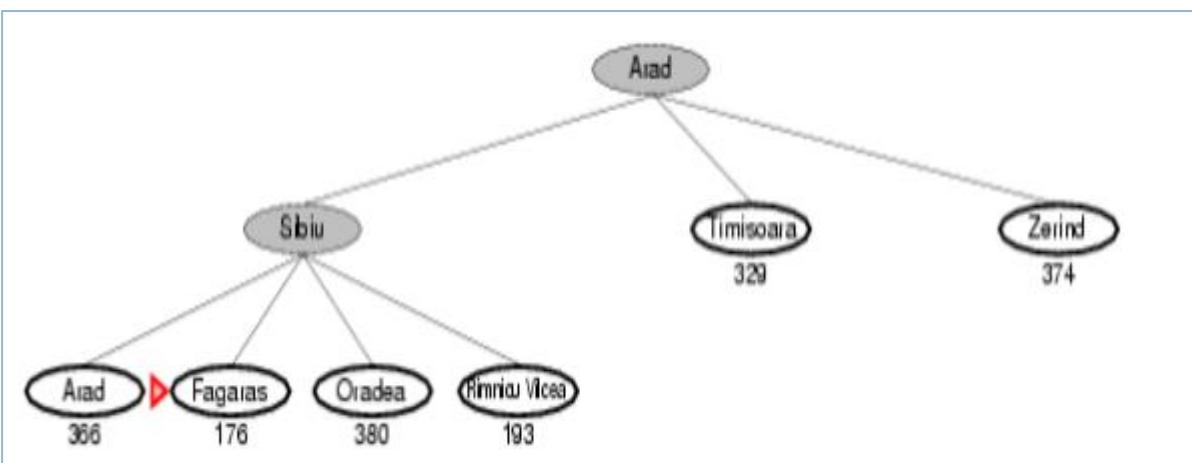
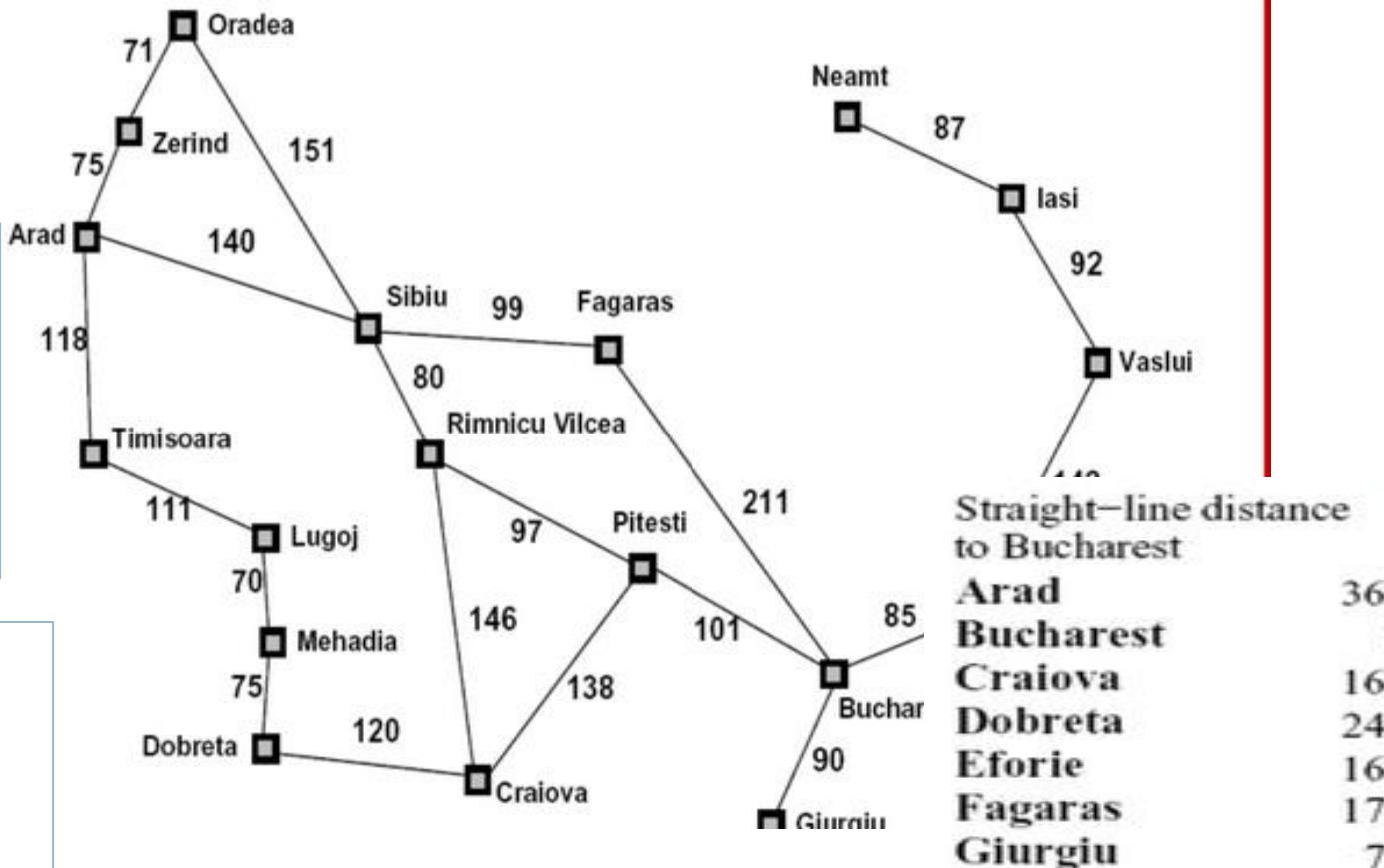
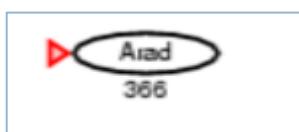
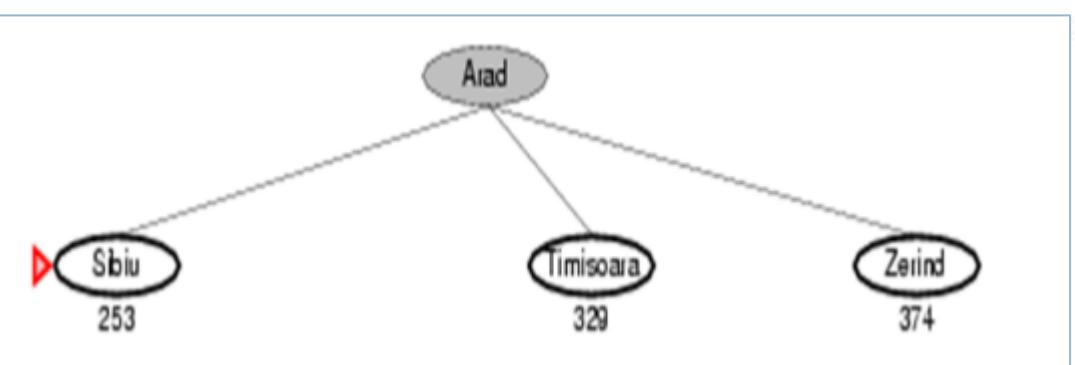
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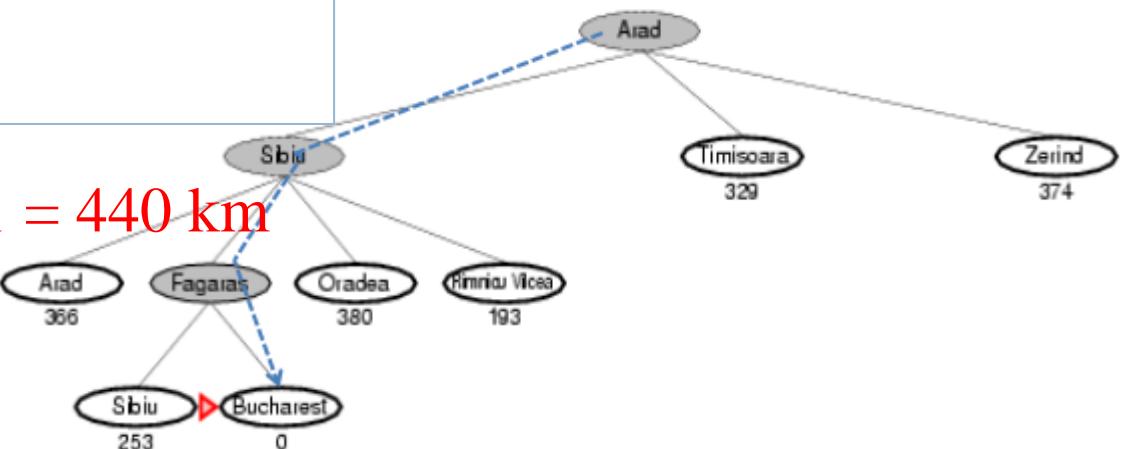
# Greedy best-first search example

---





Total path cost =  $140 + 99 + 211 = 440$  km



# Example :Greedy best-first search

---

- **But, the path Arad-Sibiu-Fagaras-Bucharest is sub-optimal**
  - **Total path cost =  $140 + 99 + 211 = 440$  km**
- **The optimal path is:**
  - Arad-Sibiu-Rimnicu Vilcea-Pitesti-Bucharest
  - **Path cost =  $140 + 80 + 97 + 101 = 418$  km**
- **Best-first search can be improved by taking the actual cost to a state n into account**
  - **The new search strategy is called A\***

# Example :Greedy best-first search

---

Limitation : It may not find the optimal solution

- Only takes estimated cost i.e.,  $h(n)$  from the current state to the goal state
- Does not take the actual cost i.e.,  $g(n)$  from the start state to the current state

# Properties of Greedy best-first search

---

- Time Complexity: The worst case time complexity of Greedy best first search is  $O(b^m)$ .
- Space Complexity: The worst case space complexity of Greedy best first search is  $O(b^m)$ . Where, m is the maximum depth of the search space.
- Complete: Greedy best-first search is also **incomplete**, even if the given state space is finite.
- Optimal: Greedy best first search algorithm is **not optimal**.

# Greedy best-first search

---

## Advantages

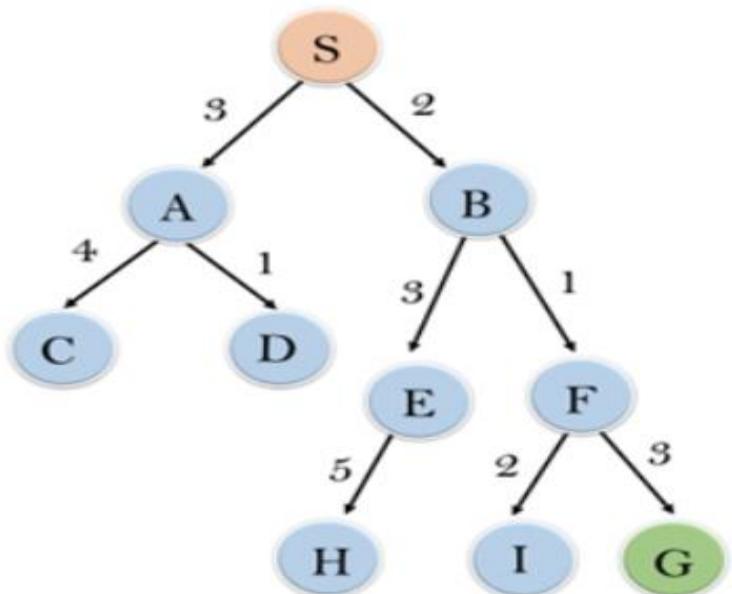
- Best first search can switch between BFS and DFS by gaining the advantages of both the algorithms.
- This algorithm is more efficient than BFS and DFS algorithms.

## Disadvantages

- It can behave as an unguided depth-first search in the worst case scenario.
- It can get stuck in a loop as DFS.
- This algorithm is not optimal.

# Example :Greedy best-first search

Final solution path will be S----> B----->F-----> G = 2+1+3 =6



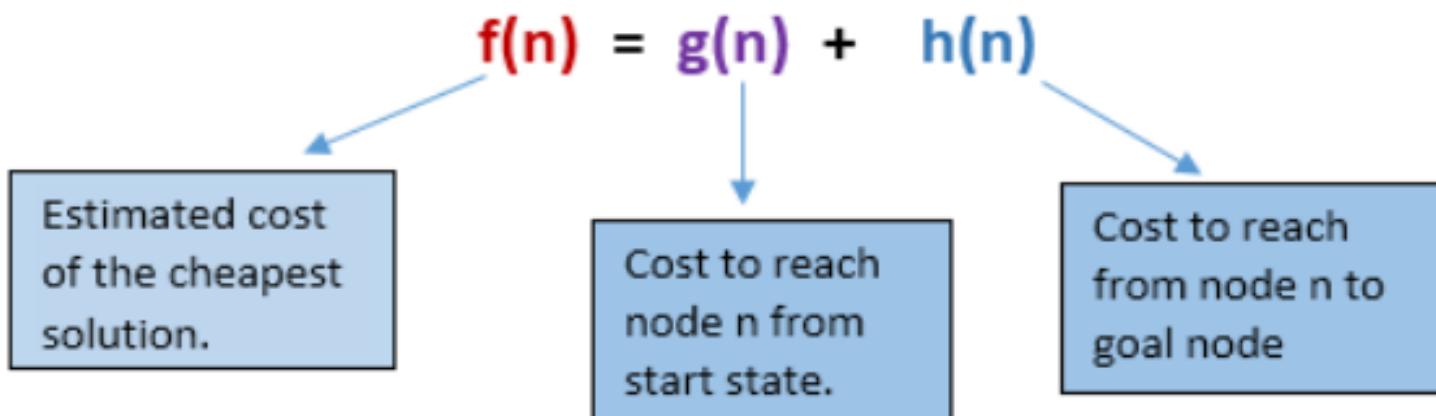
node	H (n)
A	12
B	4
C	7
D	3
E	8
F	2
H	4
I	9
S	13
G	0

Open list	Closed list
[S]	[ ]
[ B, A]	[ S ]
[F,E,A]	[ S,B ]
[G,E,I,A]	[S,B,F ]
	[S,B,F,G ]
	2+1+3=6

# A\* search

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- A\* search is the most commonly known form of best-first search.
- It uses heuristic function  $h(n)$ , and cost to reach the node  $n$  from the start state  $g(n)$ .
- A\* search algorithm finds the shortest path through the search space using the heuristic function.
- In A\* search algorithm, we use search heuristic as well as the cost to reach the node.



# A\* search

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- A\* Search Algorithm is a simple and efficient search algorithm that can be used to find the optimal path between two nodes in a graph.
- It will be used for the shortest path finding.
- It is an extension of Dijkstra's shortest path algorithm (Dijkstra's Algorithm).
- The A\* Search Algorithm also uses a heuristic function that provides additional information regarding how far away from the goal node we are.

The implementation of A\* Algorithm involves maintaining two lists- OPEN and CLOSED.

- OPEN contains those nodes that have been evaluated by the heuristic function but have not been expanded into successors yet.
- CLOSED contains those nodes that have already been visited.

# A\* search

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**Step1:** Place the starting node in the OPEN list.

**Step 2:** Check if the OPEN list is empty or not, if the list is empty then return failure and stops.

**Step 3:** Select the node from the OPEN list which has the smallest value of evaluation function ( $g+h$ ), if node n is goal node then return success and stop, otherwise

**Step 4:** Expand node n and generate all of its successors, and put n into the closed list. For each successor  $n'$ , check whether  $n'$  is already in the OPEN or CLOSED list, if not then compute evaluation function for  $n'$  and place into Open list.

**Step 5:** Else if node  $n'$  is already in OPEN and CLOSED, then it should be attached to the back pointer which reflects the lowest  $g(n')$  value.

**Step 6:** Return to Step 2.

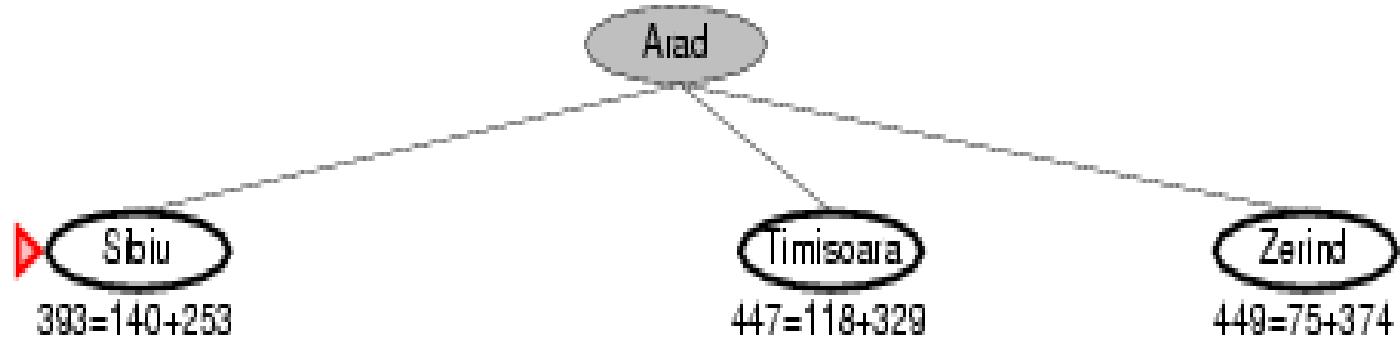
# A\* search example

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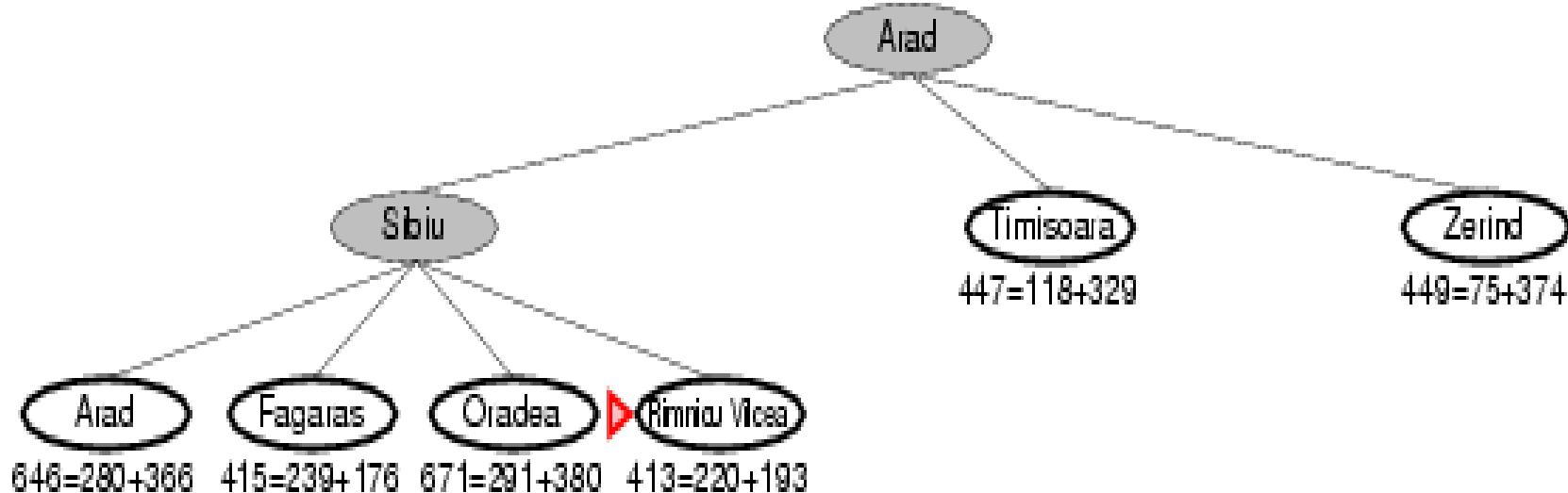
# A\* search example

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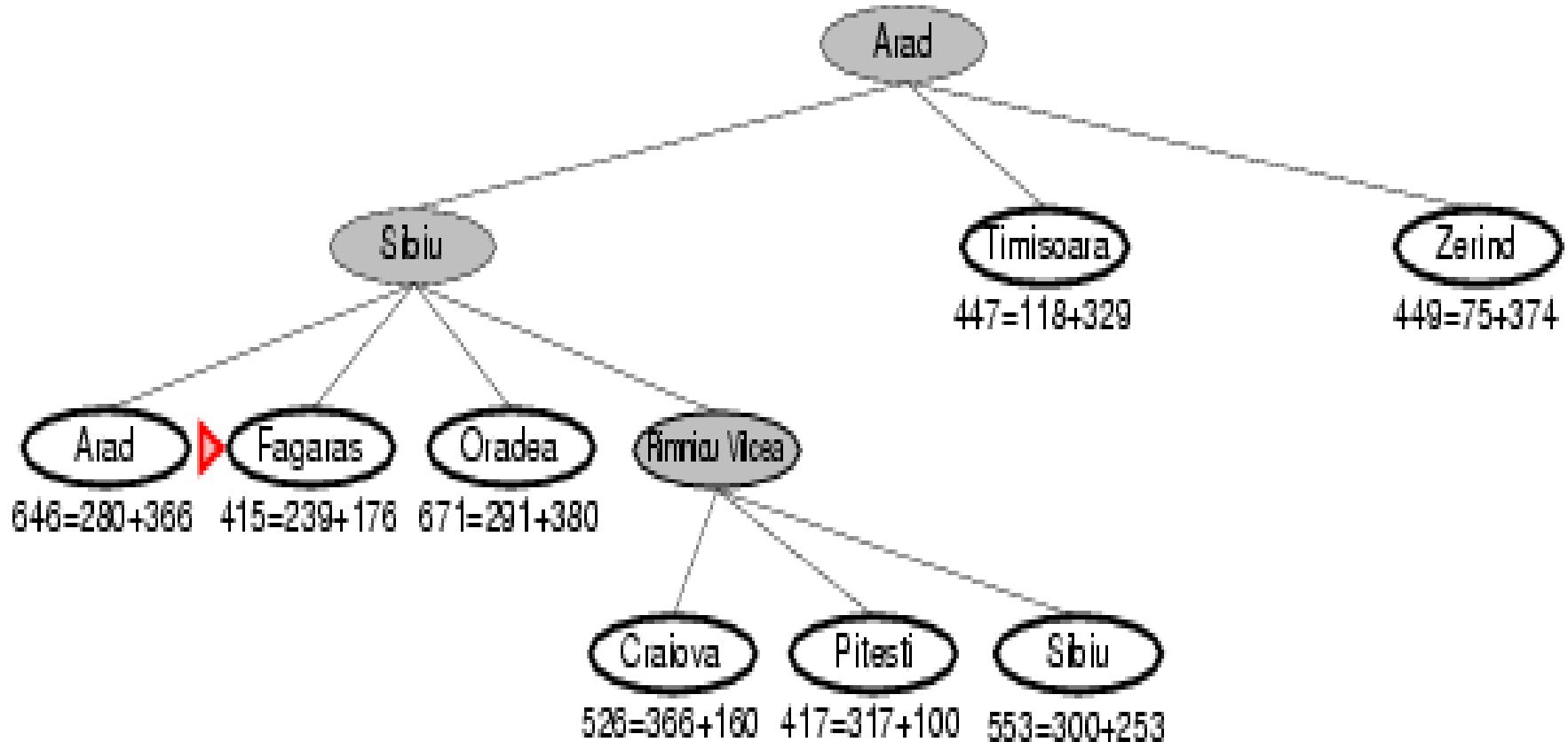


# A\* search example

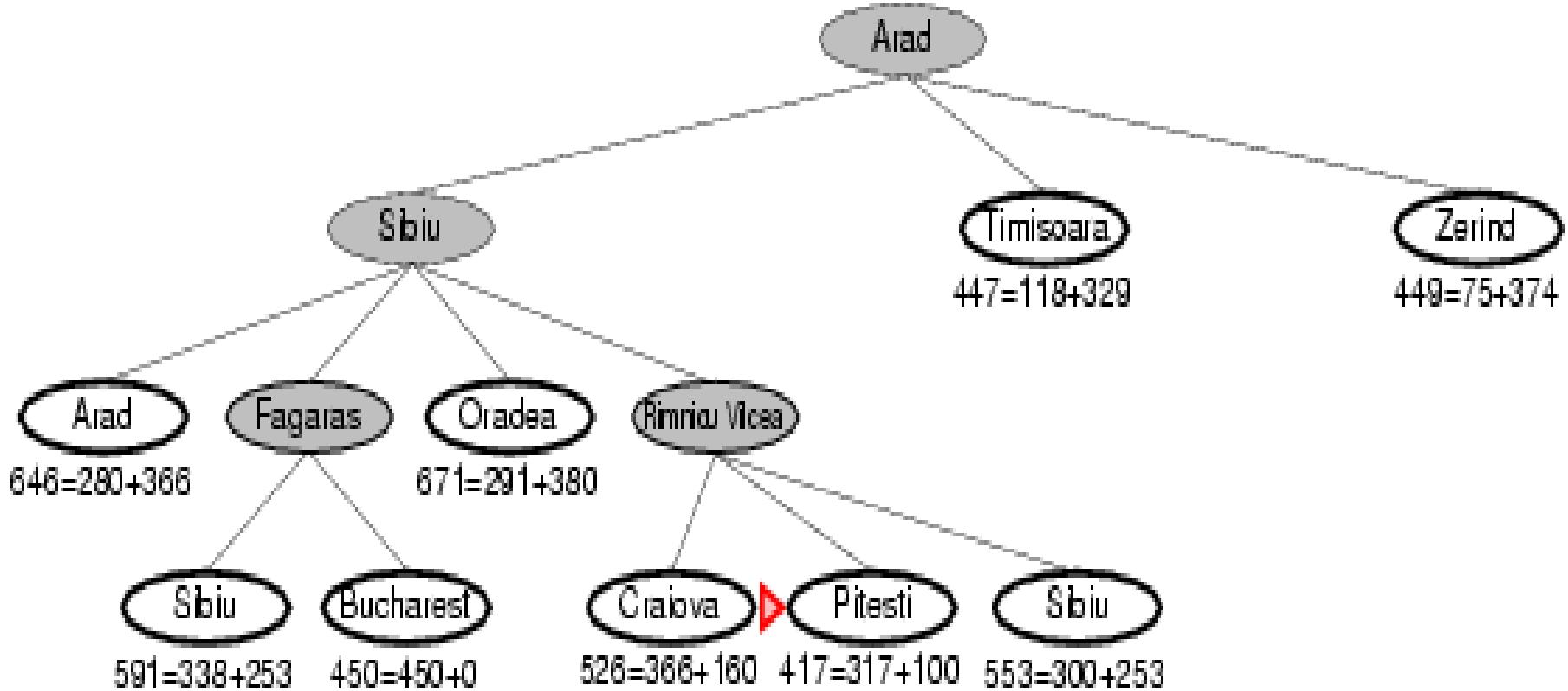
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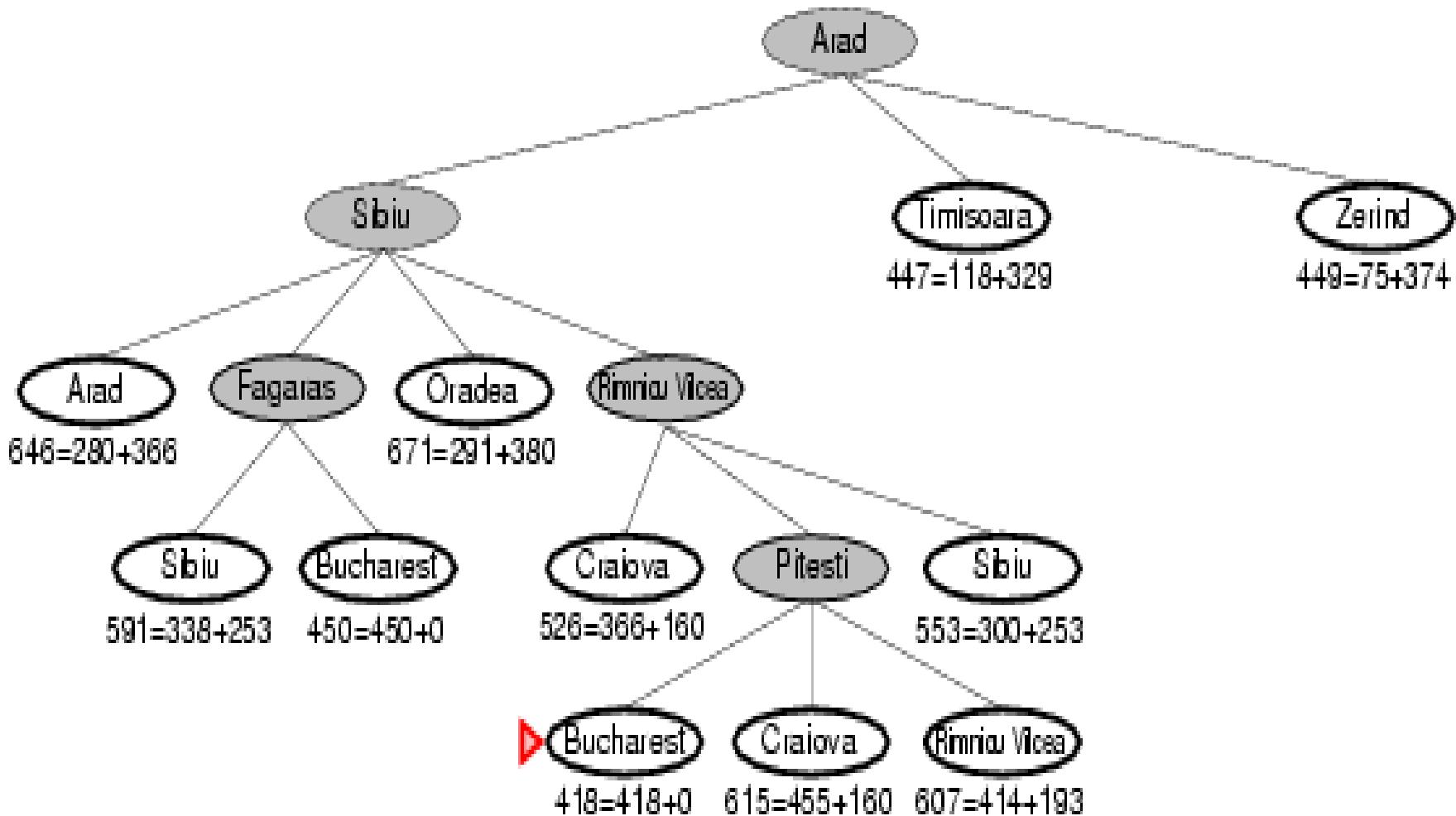
# A\* search example



# A\* search example

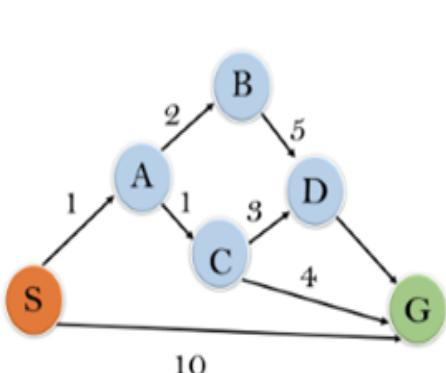


# A\* search example



# A\* search

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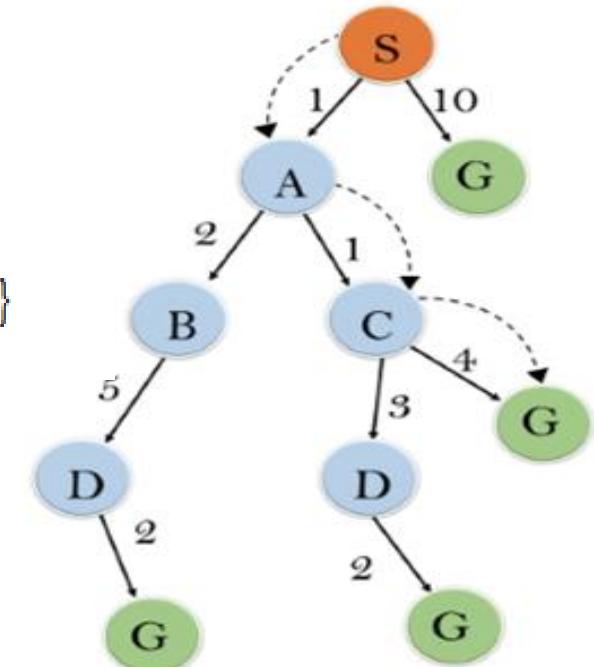
State	$h(n)$
S	5
A	3
B	4
C	2
D	6
G	0

**Initialization:**  $\{(S, 5)\}$

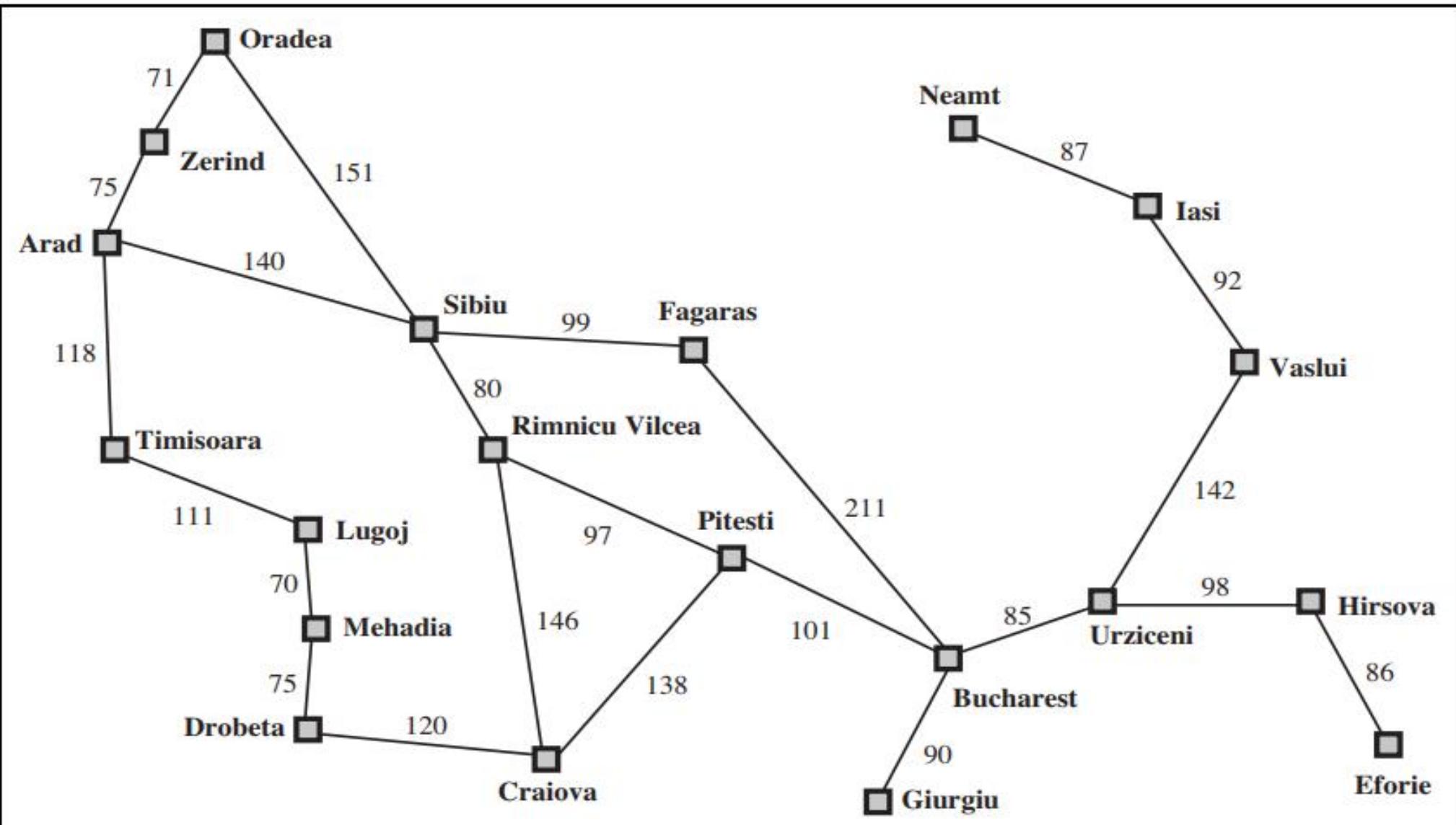
**Iteration1:**  $\{(S \rightarrow A, 4), (S \rightarrow G, 10)\}$

**Iteration2:**  $\{(S \rightarrow A \rightarrow C, 4), (S \rightarrow A \rightarrow B, 7), (S \rightarrow G, 10)\}$

**Iteration3:**  $\{(S \rightarrow A \rightarrow C \rightarrow G, 6), (S \rightarrow A \rightarrow C \rightarrow D, 11), (S \rightarrow A \rightarrow B, 7), (S \rightarrow G, 10)\}$



**Iteration 4** will give the final result, as **S---->A---->C---->G** it provides the optimal path with cost 6.



**Figure 3.2** A simplified road map of part of Romania.



# Examples: A\*

Heuristic Table

A 24	F 145	K 108	P 65
B 28	G 123	L 51	Q 11
C 70	H 95	N 58	
D 95	I 77	O 10	
E 118	J 57	M 0	

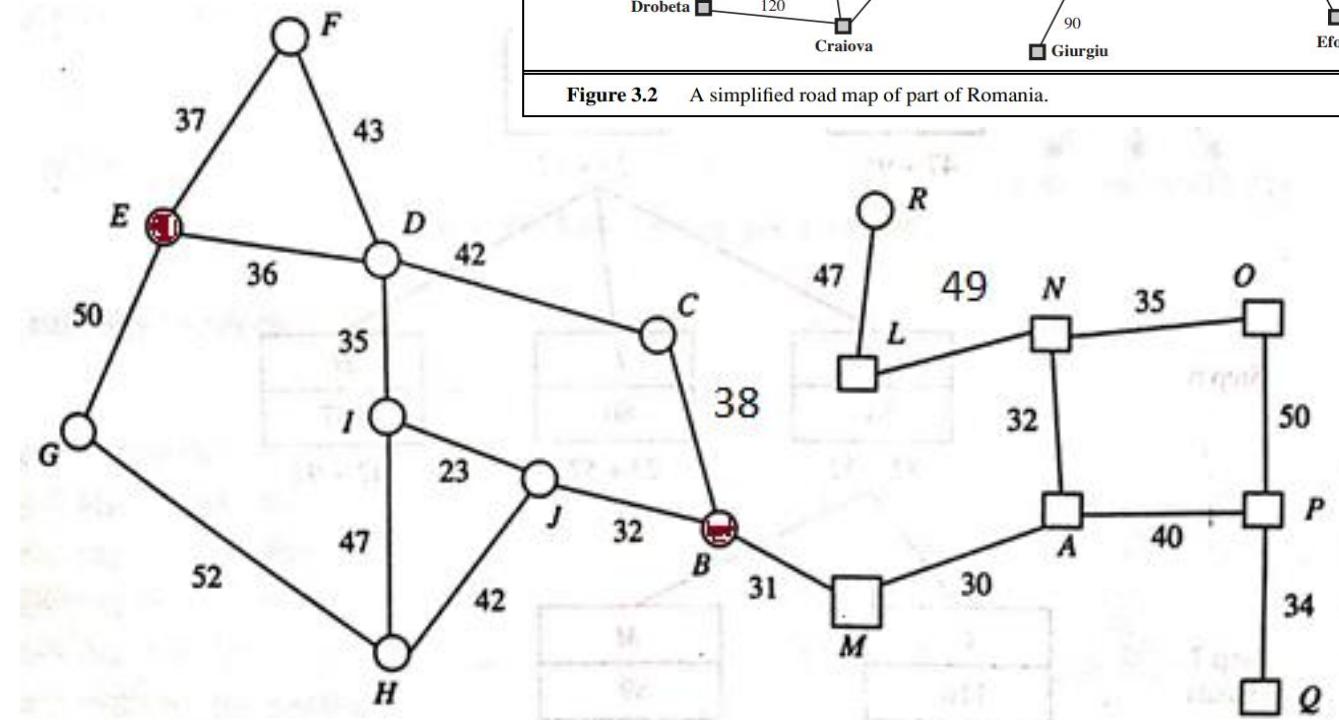


Figure 3.2 A simplified road map of part of Romania.

# A\* Search Problem 2

**Example 3.1** The example given below determines an optimal path to travel from one corner to another corner of a country using other heuristic functions.

Figure 3.12 shows the road map of different cities  $A, B, C, D, E, F, G, H, I, J, K, L, M, N, O, P, Q$ , i.e. all 17 cities in a hypothetical country. The heuristic function SLD is straight-line distance as shown in Table 3.1. Another function  $g(n)$  is the distances shown in Figure 3.13 between two cities.  $f(n) = g(n) + h(n)$ . In Figure 3.11, the expansion of root node first and consequently the node with the lowest  $f(n)$  successively we

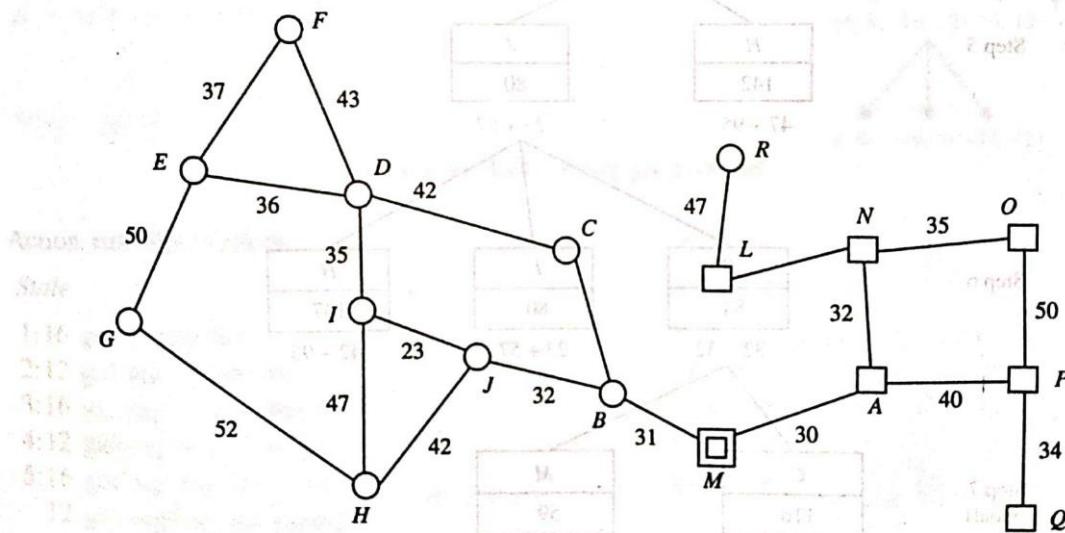


Figure 3.12 Road map of a country.

Start state: E  
 Goal state: M

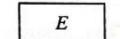
Table 3.1 SLD for Figure 3.10

A 24	F 145	K 108	P 65
B 28	G 123	L 51	Q 11
C 70	H 95	N 58	
D 95	I 77	O 10	
E 118	J 57	M 0	

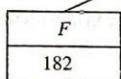
obtain a optimal path between the cities corresponding to nodes  $E$  and  $M$  respectively. At the node in the block upper character shows the name of the city and the lower number shows the heuristic function  $f(n)$ .

**Step 1  
(Initial)**

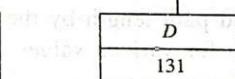

$$118 = 0 + 118$$

**Step 2**


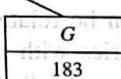
$$36 + 95$$


**Step 3**

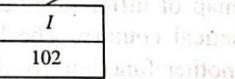
$$37 + 145$$



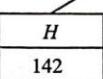
$$36 + 95$$



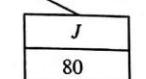
$$50 + 123$$

**Step 4**


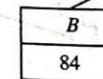
$$35 + 77$$


**Step 5**


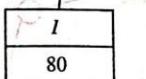
$$47 + 95$$



$$23 + 57$$

**Step 6**


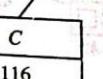
$$32 + 52$$



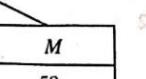
$$23 + 57$$



$$42 + 95$$

**Step 7  
(Goal)**


$$46 + 70$$



$$31 + 28$$

Figure 3.13 Finding optimal path between two cities.

# Properties of A\*

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Complete? Yes (unless there are infinitely many nodes with  $f \leq f(G)$  )

Time? Exponential

Space? Keeps all nodes in memory

Optimal? Yes

# Properties of A\* search

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**Complete:** A\* algorithm is complete as long as Branching factor is finite. Cost at every action is fixed.

**Optimal:** A\* search algorithm is optimal if it follows below two conditions:

- **Admissible:** the first condition requires for optimality is that  $h(n)$  should be an admissible heuristic for A\* tree search. An admissible heuristic is optimistic in nature.
- **Consistency:** Second required condition is consistency for only A\* graph-search.

**Time Complexity:**  $O(b^d)$ , where b is the branching factor.

**Space Complexity:**  $O(b^d)$

# A\* search

---

## Advantages

- A\* search algorithm is the best algorithm than other search algorithms.
- A\* search algorithm is optimal and complete.
- This algorithm can solve very complex problems.

## Disadvantages

- It does not always produce the shortest path as it mostly based on heuristics and approximation.
- A\* search algorithm has some complexity issues.
- The main drawback of A\* is memory requirement as it keeps all generated nodes in the memory, so it is not practical for various large-scale problems.

# Evaluation / Heuristic Function

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- Evaluation function  $f(n) = g(n) + h(n)$ 
  - $g(n)$  = exact cost so far to reach  $n$
  - $h(n)$  = estimated cost to goal from  $n$
  - $f(n)$  = estimated total cost of cheapest path through  $n$  to goal
- Uniform Cost Search:  $f(n) = g(n)$
- Greedy (best-first) Search:  $f(n) = h(n)$
- A\* Search:  $f(n) = g(n) + h(n)$

# Heuristic Functions

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- The 8-puzzle was one of the earliest heuristic search problems
- If we want to find the shortest solutions , we need a heuristic function that never overestimates the number of steps to the goal.

## 2 commonly used methods

- **h1 = the number of misplaced tiles.**
- h1 is an admissible heuristic because it is clear that any tile that is out of place must be moved at least once
- **h2 = the sum of the distances of the tiles from their goal positions.**
- Called also the city block distance or **Manhattan distance**.
- h2 is also admissible because all any move can do is move one tile one step closer to the goal.

# Heuristic Functions

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The state of 8-puzzle is the different permutation of tiles within the frame.

The operations are the permissible moves up, down, left, right.

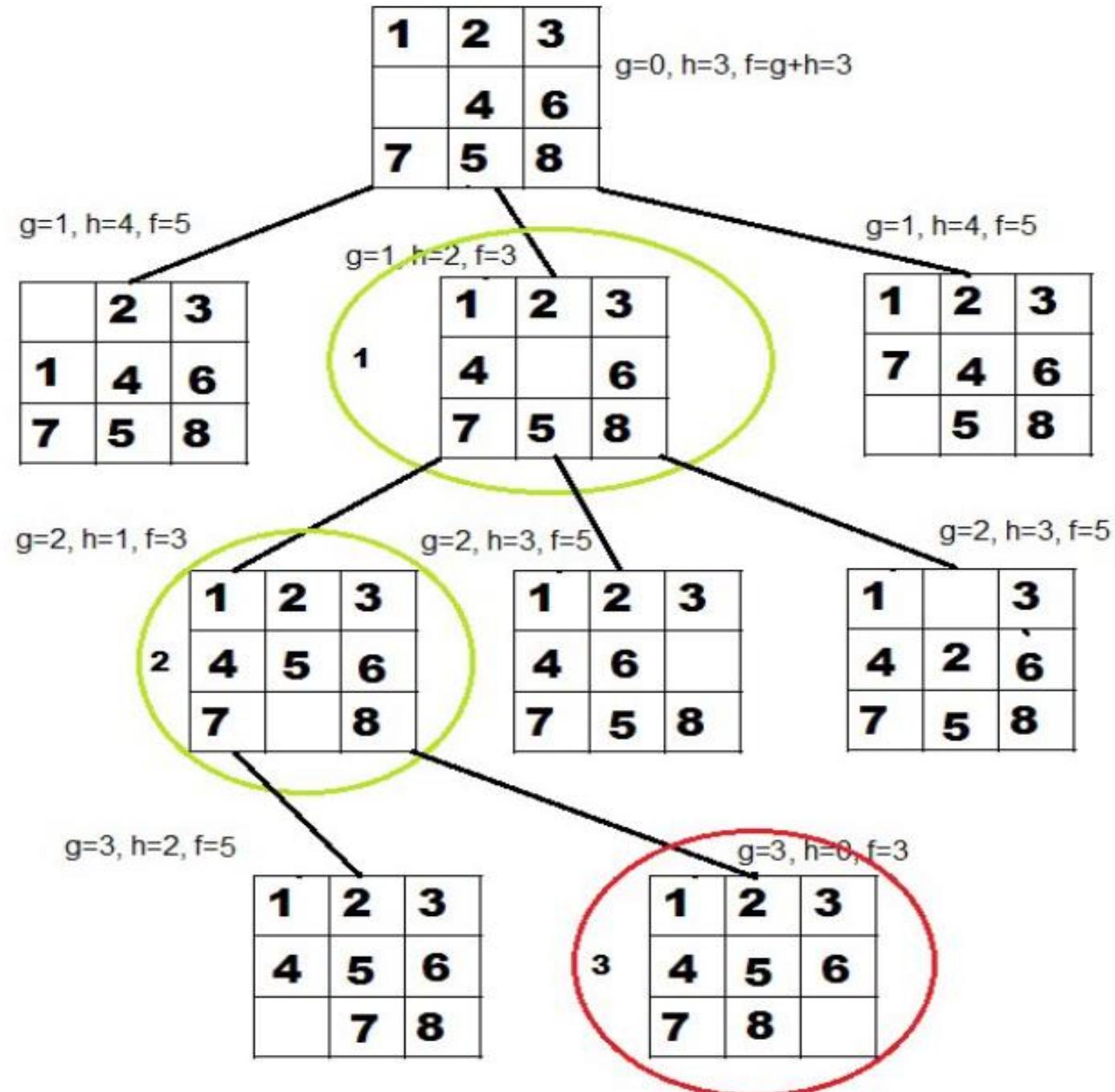
Here at each step of the problem a function  $f(x)$  will be defined which is the combination of  $g(x)$  and  $h(x)$ .  
i.e.  $F(x)=g(x) + h(x)$

Where

$g(x)$ : how many steps in the problem you have already done or the current state from the initial state.

$h(x)$ : Number of ways through which you can reach at the goal state from the current state or Is the heuristic estimator that compares the current state with the goal state note down how many states are displaced from the initial or the current state.

After calculating the  $f$  value at each step finally take the smallest  $f(x)$  value at every step and choose that as the next current state to get the goal



### Manhattan priority Function

1	2	3	4	5	6	7	8		
4	5	6							
7	8								

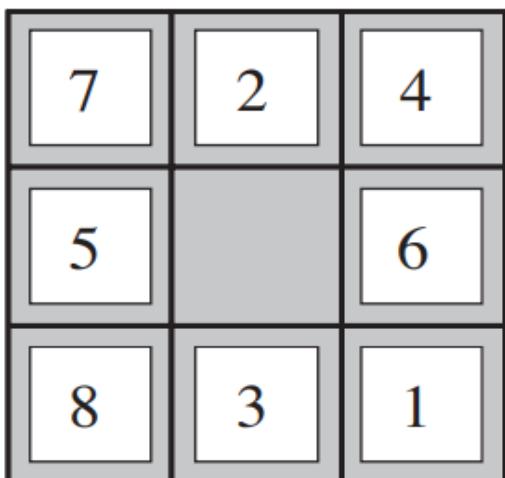
1	2	3	4	5	6	7	8		
1	0	0	1	1	0	0	1	4	
0	0	0	0	1	0	0	1	2	
0	0	0	1	1	0	1	1	4	

# Heuristic Functions

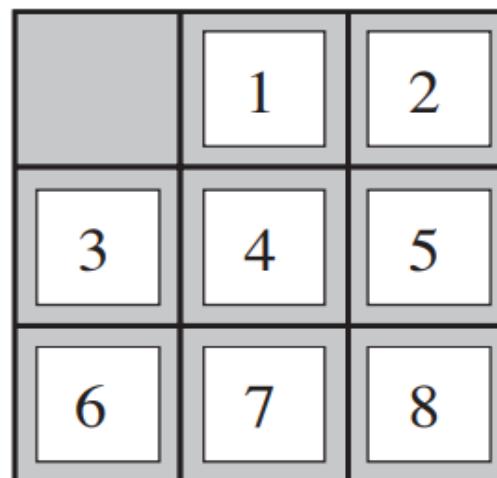
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The 8-puzzle was one of the earliest heuristic search problems.

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Start State



Goal State

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A typical instance of the 8-puzzle. The solution is 26 steps long.

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# Heuristic Functions

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## The effect of heuristic accuracy on performance

- **Branching factor  $b^*$**
- **Total number of nodes generated by a particular problem is  $N$**
- **Solution depth is  $d$**
- **$b^*$  is the branching factor that a uniform tree of depth  $d$  would have to have in order to contain  $N + 1$  nodes.**
- **Thus,  $N + 1 = 1 + b^* + (b^*)^2 + \dots + (b^*)^d$ .**

THANK YOU