

M.S. Ramaiah Institute of Technology  
(Autonomous Institute, Affiliated to VTU)  
Department of Computer Science and Engineering

**Course Name: Database Systems**

**Course Code: CS52**

**Credits: 3:1:0**

**UNIT 2**

**Term: October 2021– February 2022**

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Reference:

Elmasri, R., Shamkant B. Navathe, R.  
*Fundamentals of Database Systems*

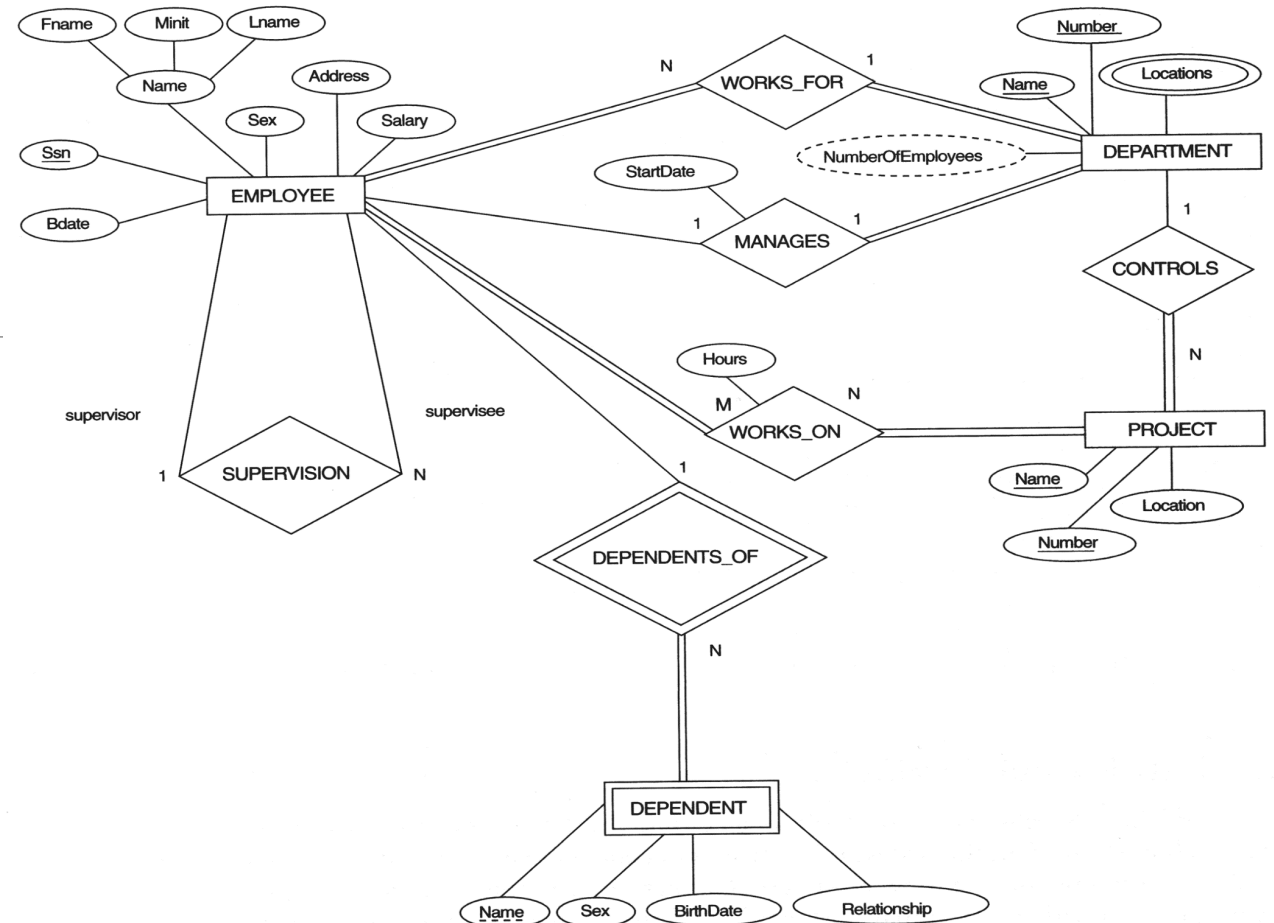
# ER-to-Relational Mapping Algorithm

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- Step 1: Mapping of Regular Entity Types
- Step 2: Mapping of Weak Entity Types
- Step 3: Mapping of Binary 1:1 Relation Types
  - Foreign Key Approach : add key of partial participation E to total participation E
  - Merged Relation Approach: when both participations are total
  - Cross-reference or relationship relation approach:
    - create a third relation R with keys of both Entities
- Step 4: Mapping of Binary 1:N Relationship Types.
- Step 5: Mapping of Binary M:N Relationship Types.
- Step 6: Mapping of Multivalued attributes.
- Step 7: Mapping of N-ary Relationship Types:
  - where  $n > 2$  or degree of the relationship  $\text{type} > 2$

## Step 1: Mapping of Regular Entity Types

- Figure out all the regular/strong entity from the diagram and then create a corresponding relation(table) that includes all the simple attributes.
- Choose one of the attributes as a primary key. If composite, the simple attributes together form the primary key.
- For the given ER-Diagram we have *Employee*, *Department* and *Project* as strong/regular entity, as they are enclosed in single rectangle.
- So, we create respective relations that is depicted in the figure below.



### EMPLOYEE

Fname	Minit	Lname	<u>Ssn</u>	Bdate	Address	Sex	Salary
-------	-------	-------	------------	-------	---------	-----	--------

### DEPARTMENT

Dname	<u>Dnumber</u>
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### PROJECT

Pname	<u>Pnumber</u>	Plocation
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## Step 2: Mapping of Weak Entity Types

- Figure out the weak entity types from the diagram and create a corresponding relation(table) that includes all its simple attributes.
- Add as foreign key all of the primary key attributes in the entity corresponding to the owner entity.
- The primary key is a combination of all the primary key attributes from the owner and the primary key of the weak entity.
- For the given ER-Diagram we have *Dependent* as a weak entity, as it is enclosed in a double rectangle that is indicative of an entity being weak.
- The Dependent relation(table) is created that is shown in the figure below.

### EMPLOYEE

Fname	Minit	Lname	<u>Ssn</u>	Bdate	Address	Sex	Salary
-------	-------	-------	------------	-------	---------	-----	--------

### DEPARTMENT

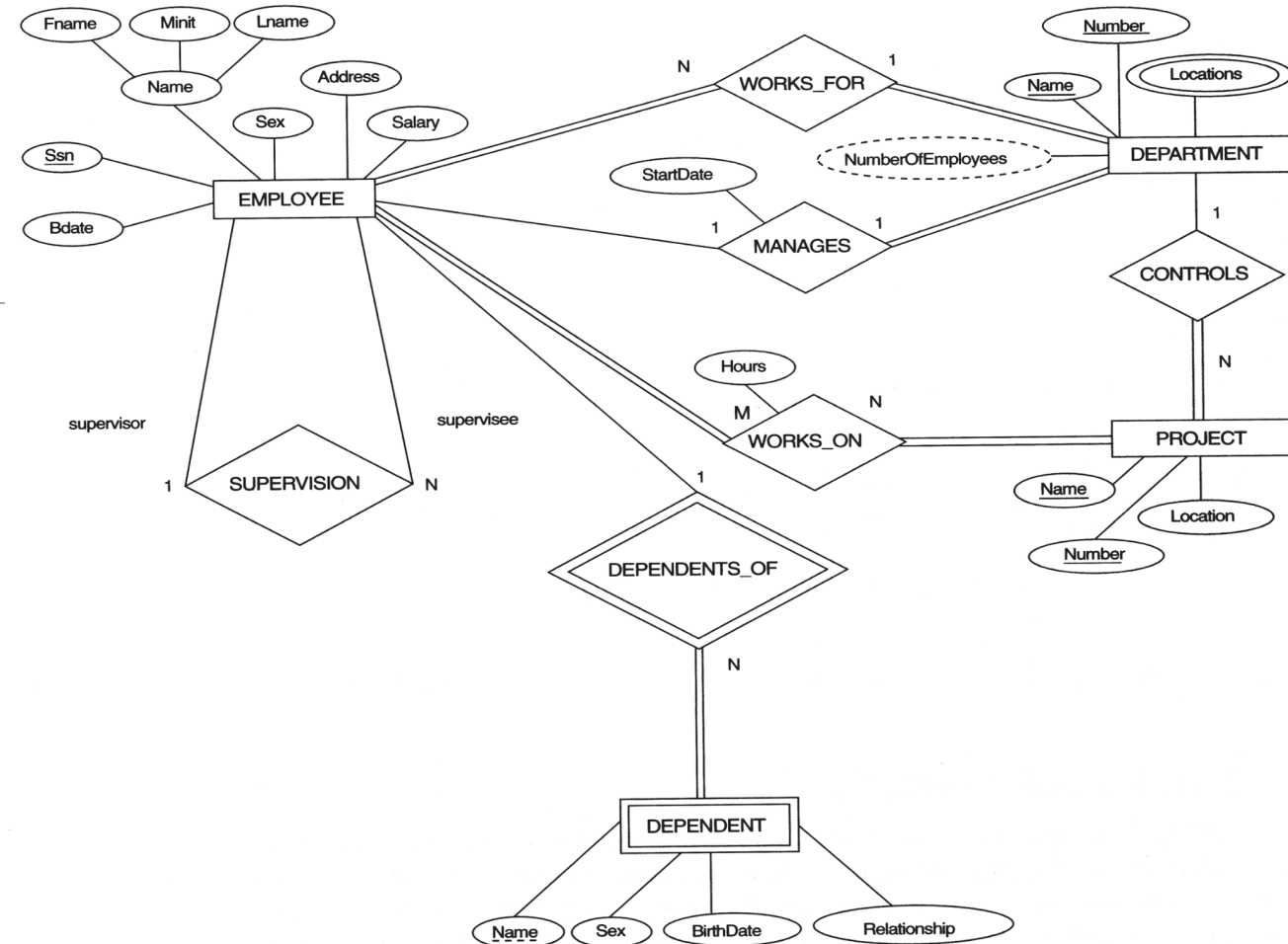
Dname	<u>Dnumber</u>
-------	----------------

### PROJECT

Pname	<u>Pnumber</u>	Plocation
-------	----------------	-----------

### DEPENDENT

<u>Essn</u>	<u>Dependent_name</u>	Sex	Bdate	Relationship
-------------	-----------------------	-----	-------	--------------



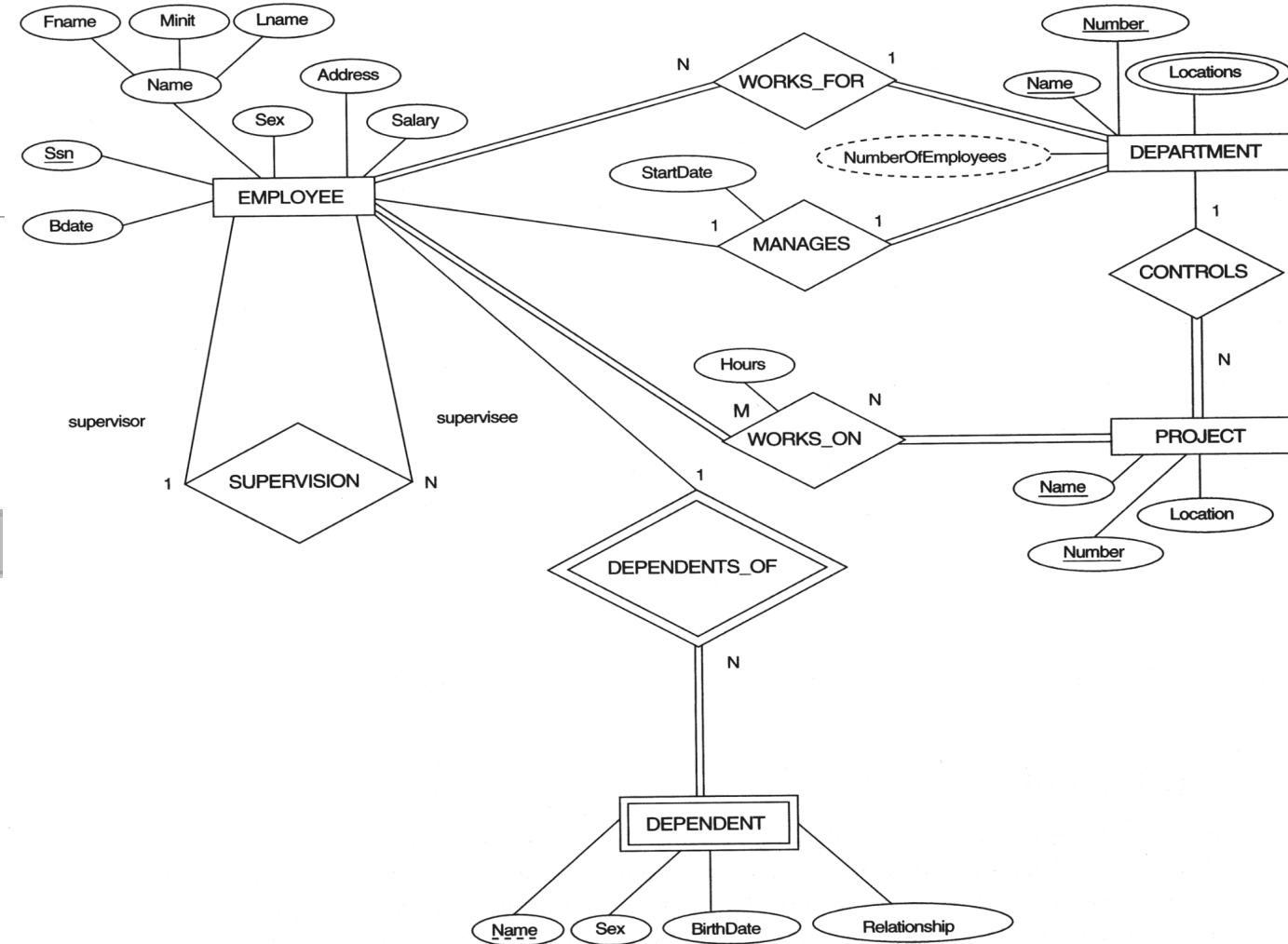
- **Step 3: Mapping of Binary 1:1 Relation Types**
- Now we need to figure out the entities from ER diagram for which there exists a 1-to-1 relationship.

#### EMPLOYEE

Fname	Minit	Lname	<u>Ssn</u>	Bdate	Address	Sex	Salary
-------	-------	-------	------------	-------	---------	-----	--------

#### DEPARTMENT

Dname	<u>Dnumber</u>	Mgr_ssn	Mgr_start_date
-------	----------------	---------	----------------



## Step 4: Mapping of Binary 1:N Relationship Types

- We need to figure out the entities from ER diagram for which there exists a 1-to-N relationship.
- The entities for which there exists a 1-to-N relationship, choose a relation as S as the type at N-side of relationship and other as T.
- Then we add as a foreign key to S all of the primary key attributes of T.

### EMPLOYEE

Fname	Minit	Lname	<u>Ssn</u>	Bdate	Address	Sex	Salary	Super_ssn	Dno
-------	-------	-------	------------	-------	---------	-----	--------	-----------	-----

### DEPARTMENT

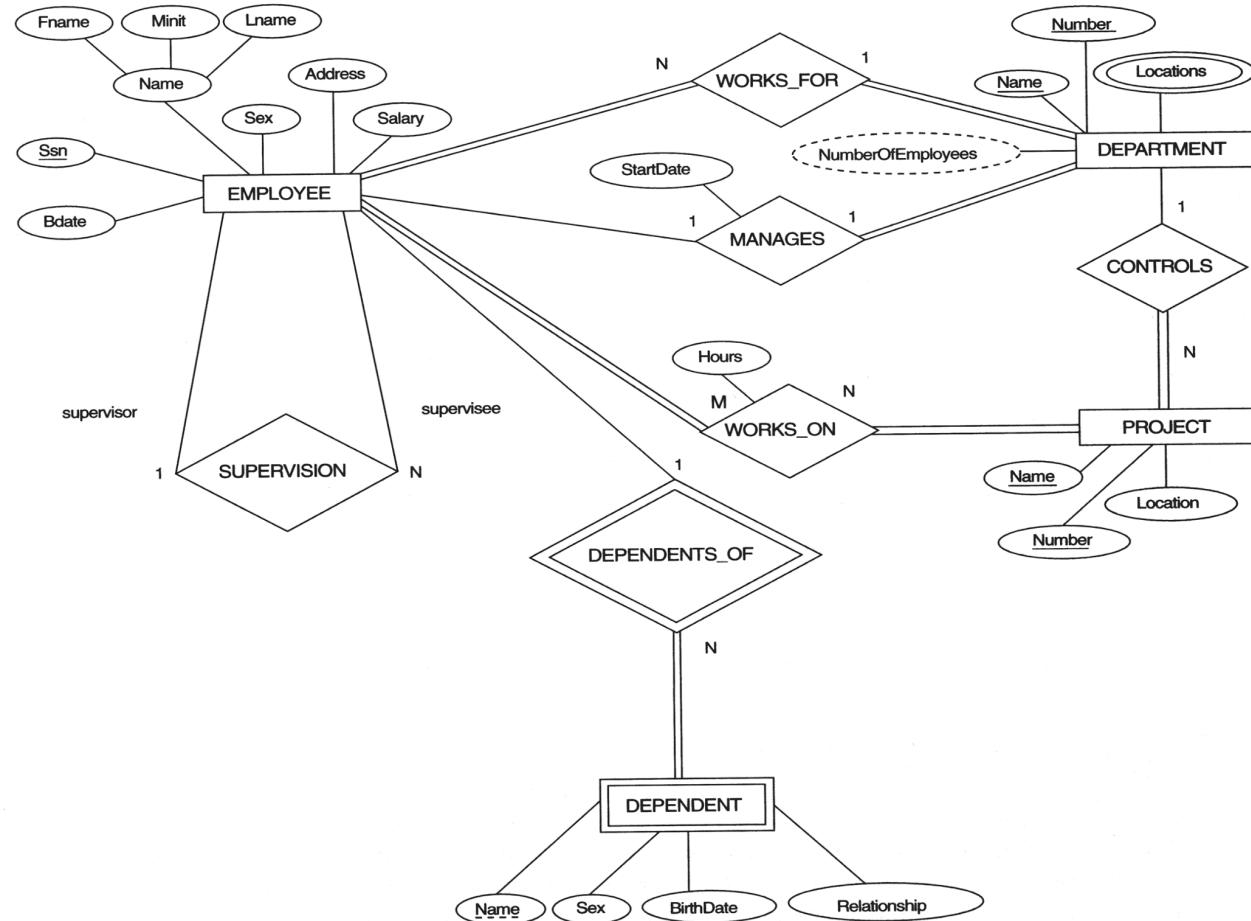
Dname	<u>Dnumber</u>	Mgr_ssn	Mgr_start_date
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### PROJECT

Pname	<u>Pnumber</u>	Plocation	Dnum
-------	----------------	-----------	------

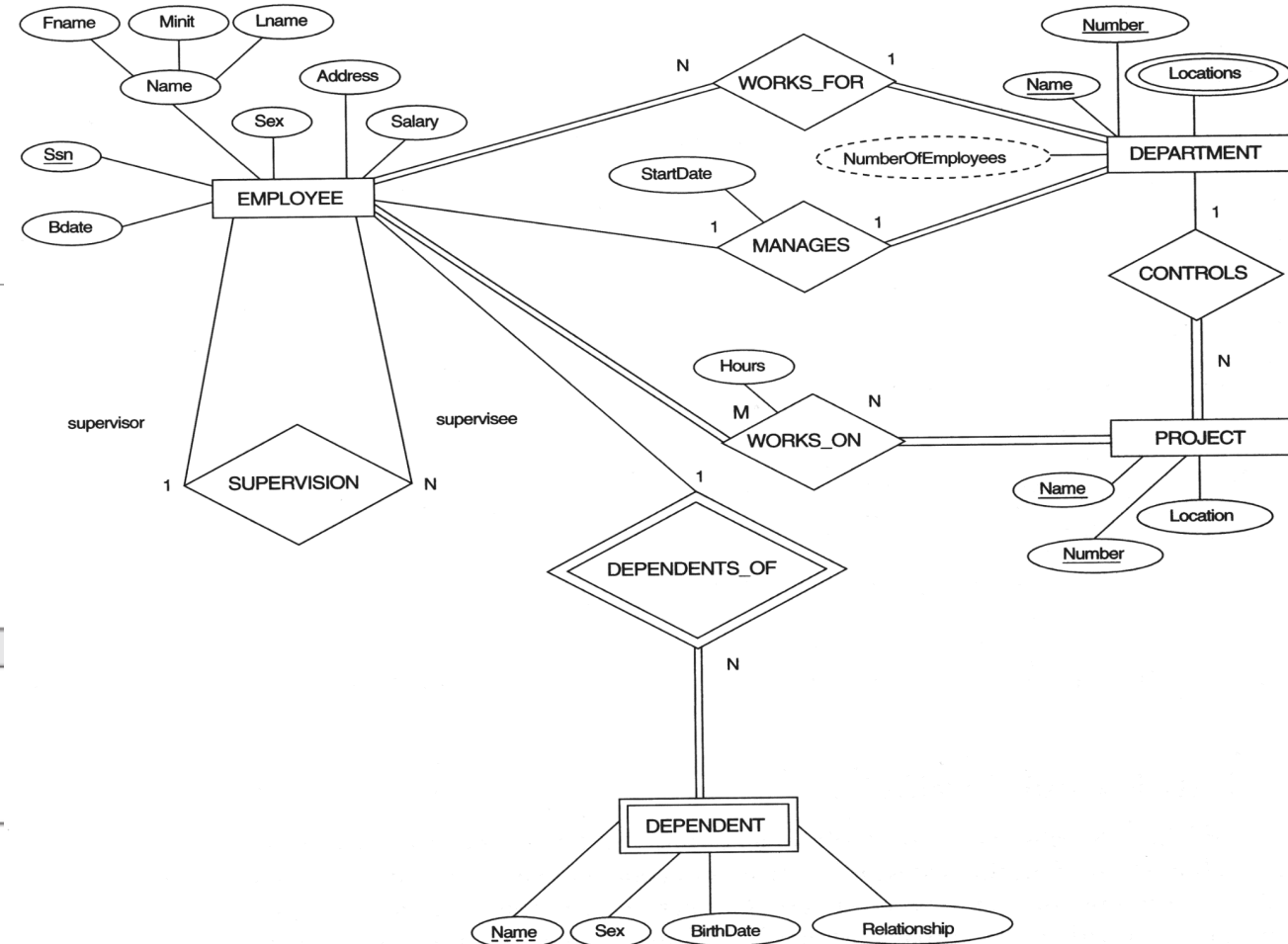
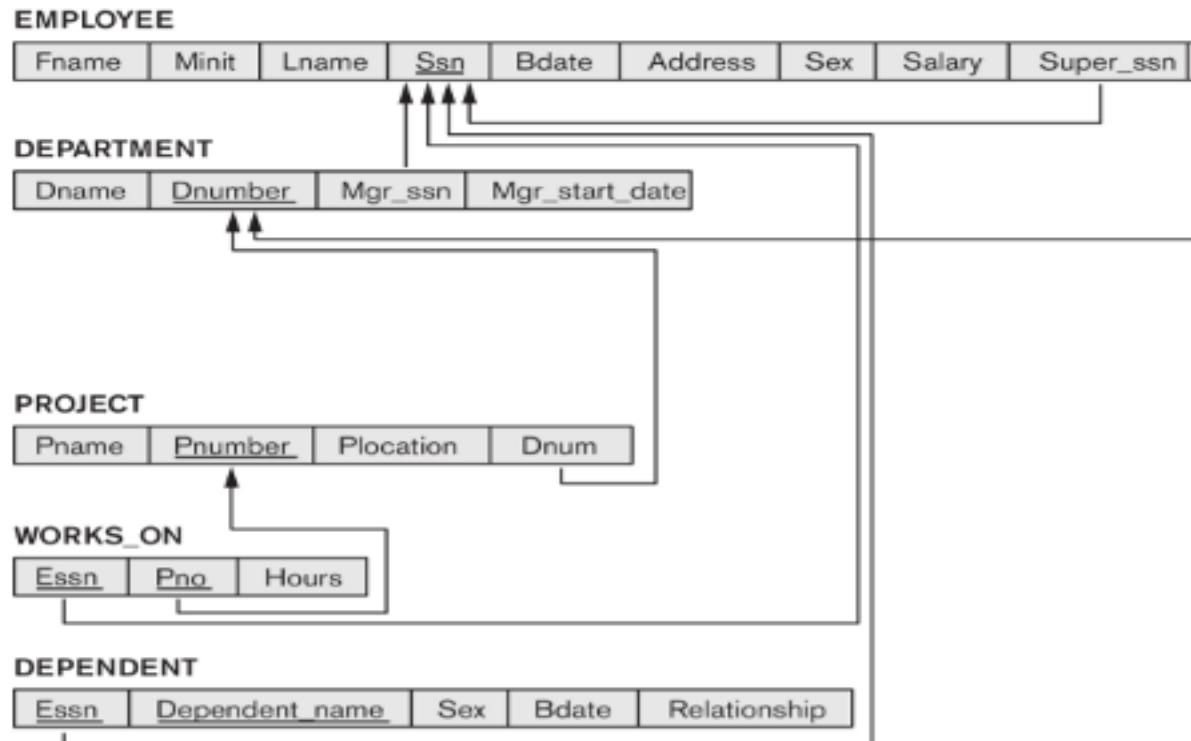
### DEPENDENT

<u>Essn</u>	<u>Dependent_name</u>	Sex	Bdate	Relationship
-------------	-----------------------	-----	-------	--------------



## Step 5: Mapping of Binary M:N Relationship Types

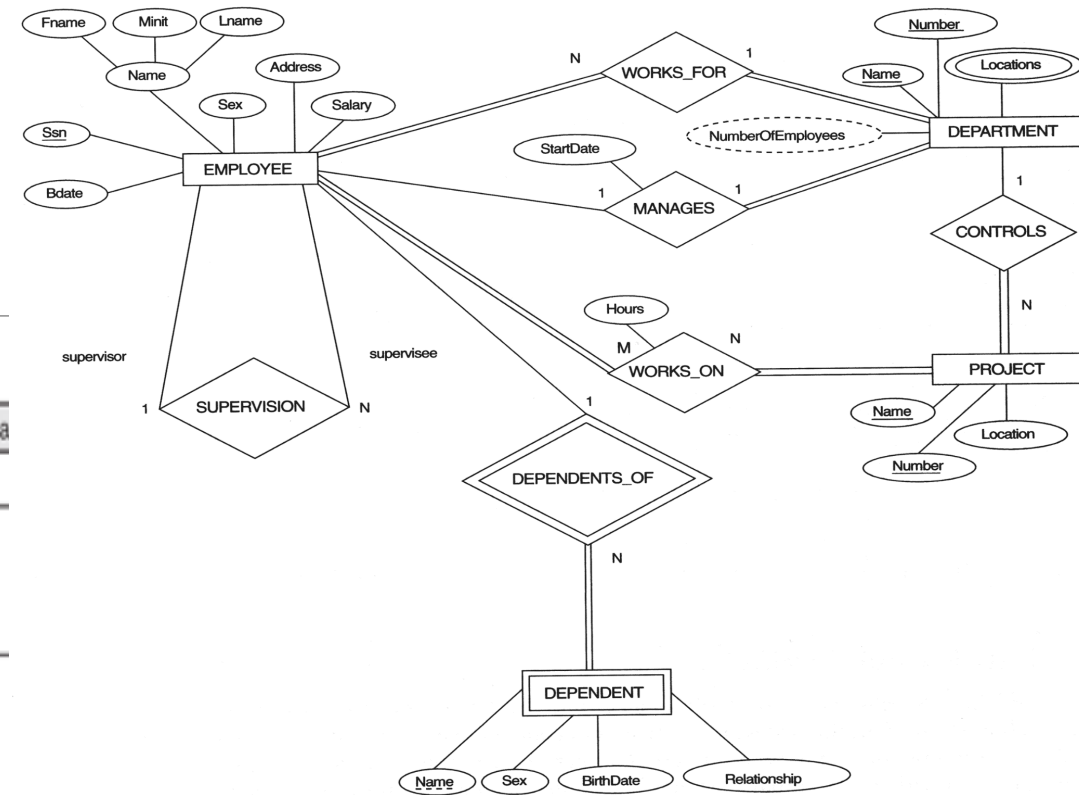
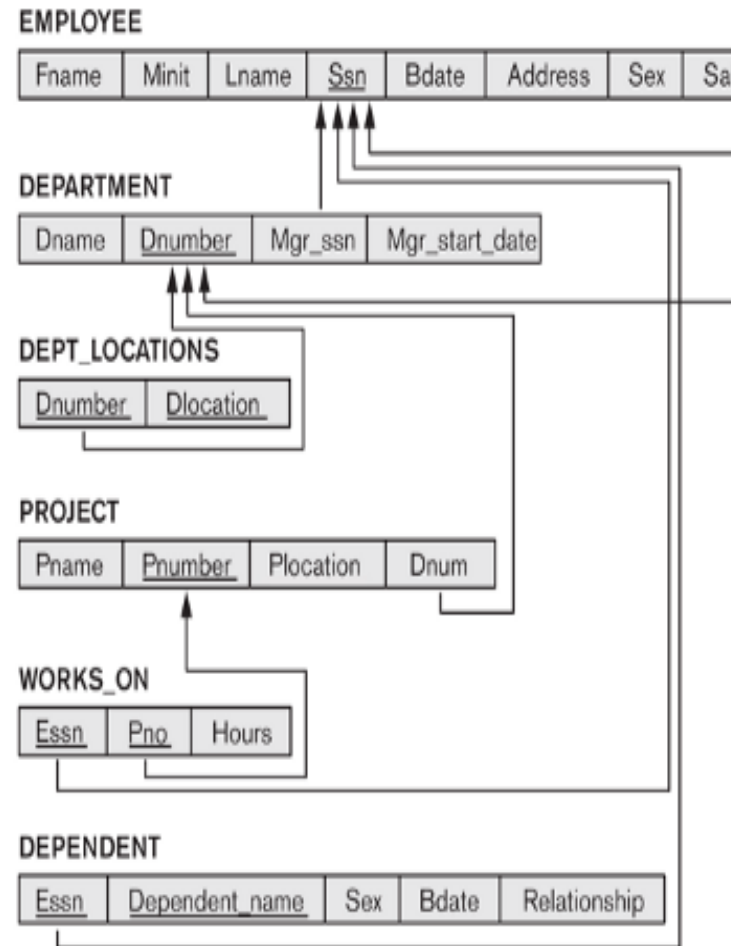
- Now we need to figure out the entities from ER diagram for which there exists an M-to-N relationship.
- Create a new relation(table) S.
- The primary keys of relations(tables) between which M-to-N relationship exists, are added to the new relation S created, that acts as a foreign key.





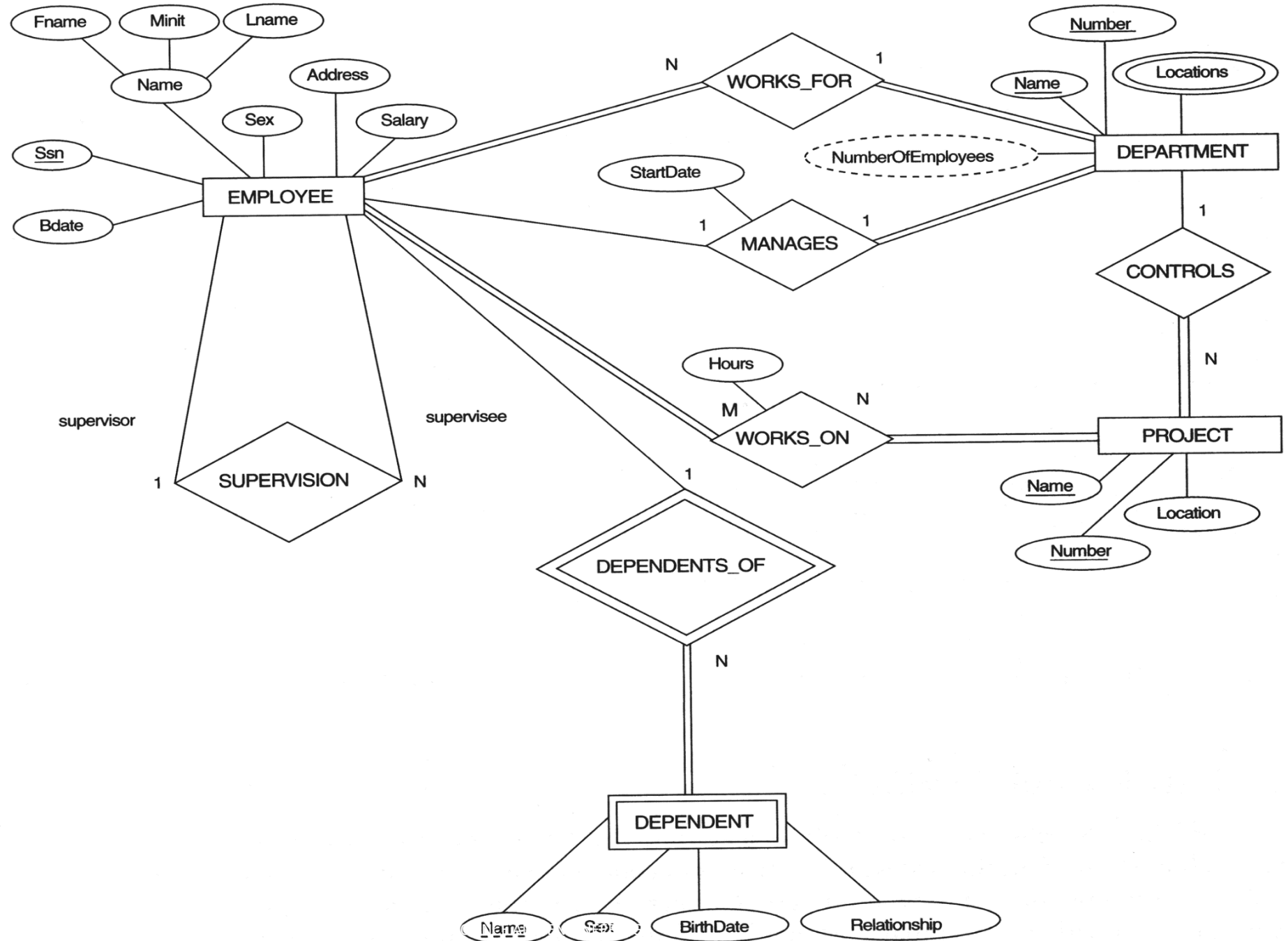
## Step 6: Mapping of Multivalued attributes

- Now identify the relations (tables) that contain multi-valued attributes.
- Then we need to create a new relation S
- In the new relation S we add as foreign keys the primary keys of the corresponding relation.
- Then we add the multi-valued attribute to S; the combination of all attributes in S forms the primary key.





The ER conceptual  
schema diagram for  
the COMPANY  
database



Result of  
mapping the  
COMPANY ER  
schema into a  
relational  
schema.

### EMPLOYEE

Fname	Minit	Lname	<u>Ssn</u>	Bdate	Address	Sex	Salary	Super_ssn	Dno
-------	-------	-------	------------	-------	---------	-----	--------	-----------	-----

### DEPARTMENT

Dname	<u>Dnumber</u>	Mgr_ssn	Mgr_start_date
-------	----------------	---------	----------------

### DEPT\_LOCATIONS

<u>Dnumber</u>	<u>Dlocation</u>
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### PROJECT

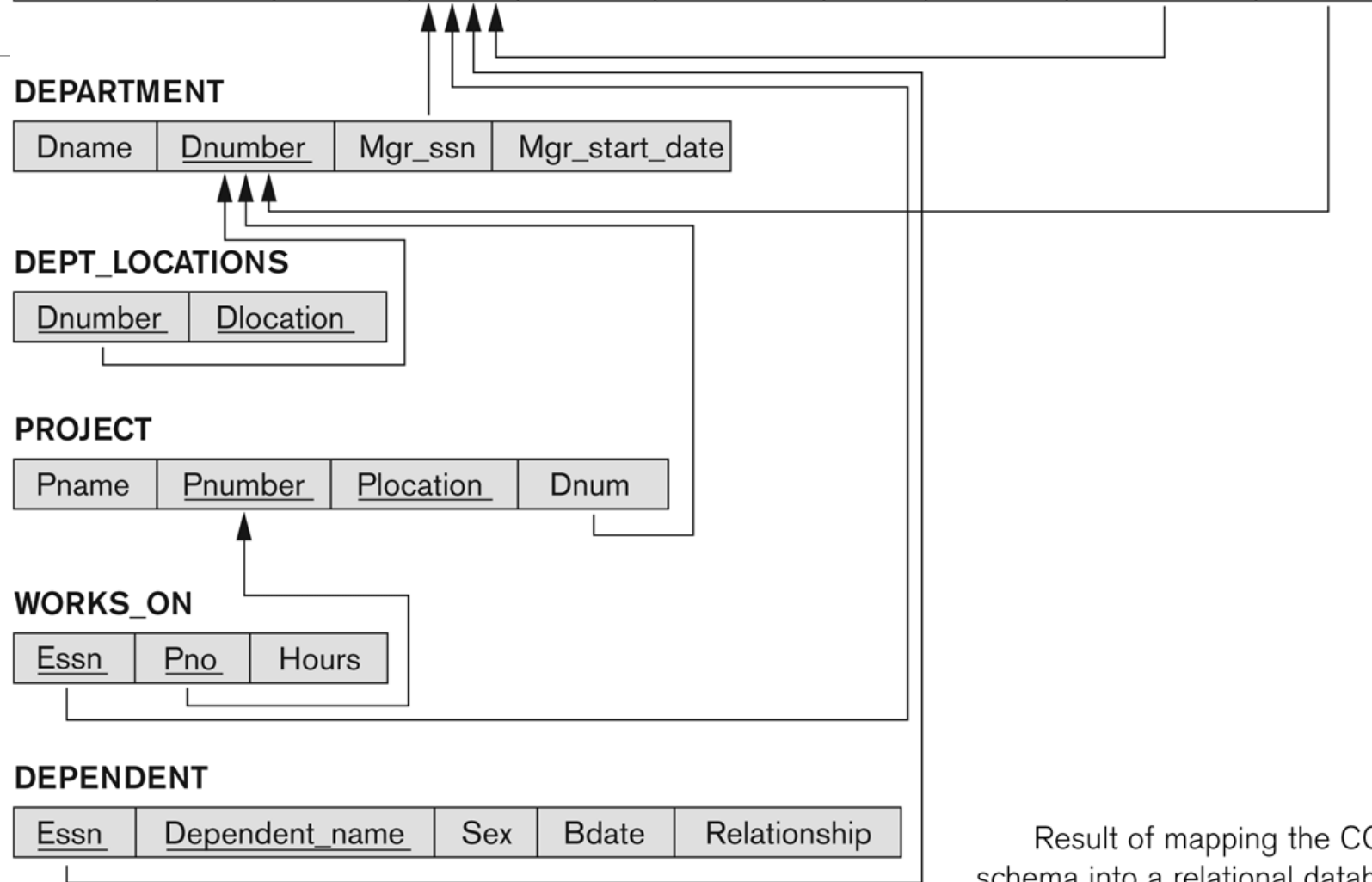
Pname	<u>Pnumber</u>	<u>Plocation</u>	Dnum
-------	----------------	------------------	------

### WORKS\_ON

<u>Essn</u>	<u>Pno</u>	Hours
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### DEPENDENT

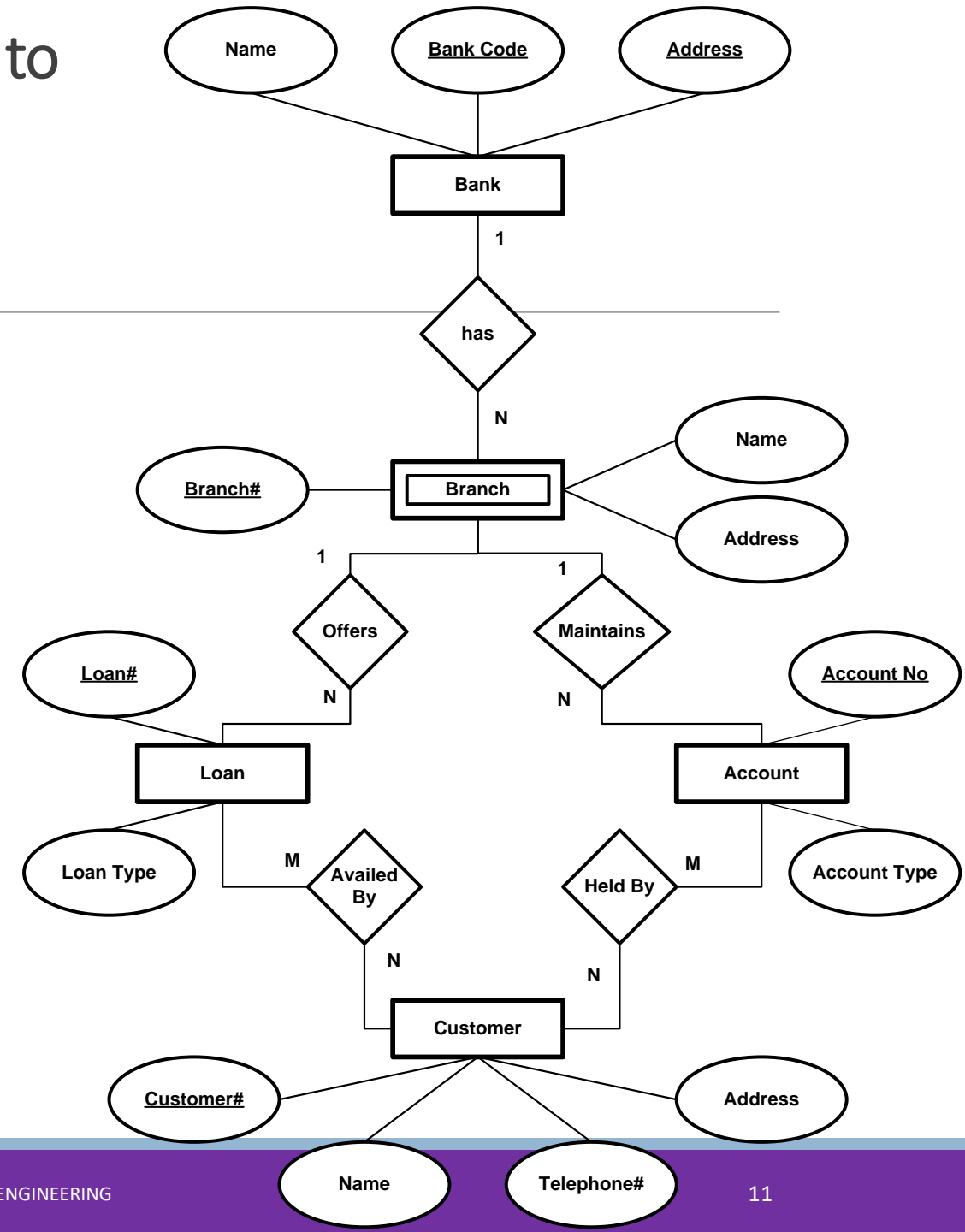
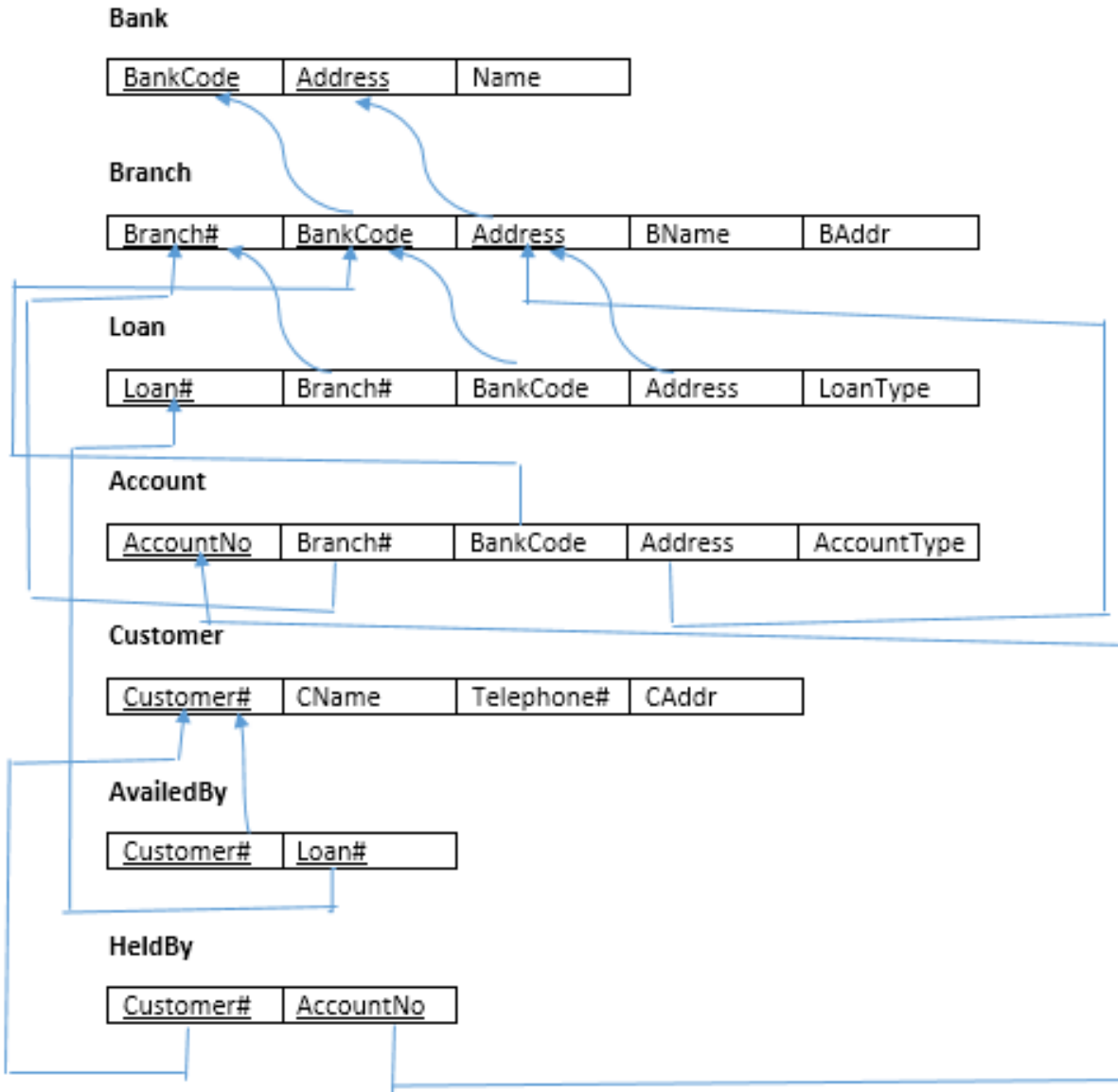
<u>Essn</u>	<u>Dependent_name</u>	Sex	Bdate	Relationship
-------------	-----------------------	-----	-------	--------------



**Figure 7.2**

Result of mapping the COMPANY ER  
schema into a relational database schema.

# Convert the given ER Diagram to relational schema



# Relational Model Concepts

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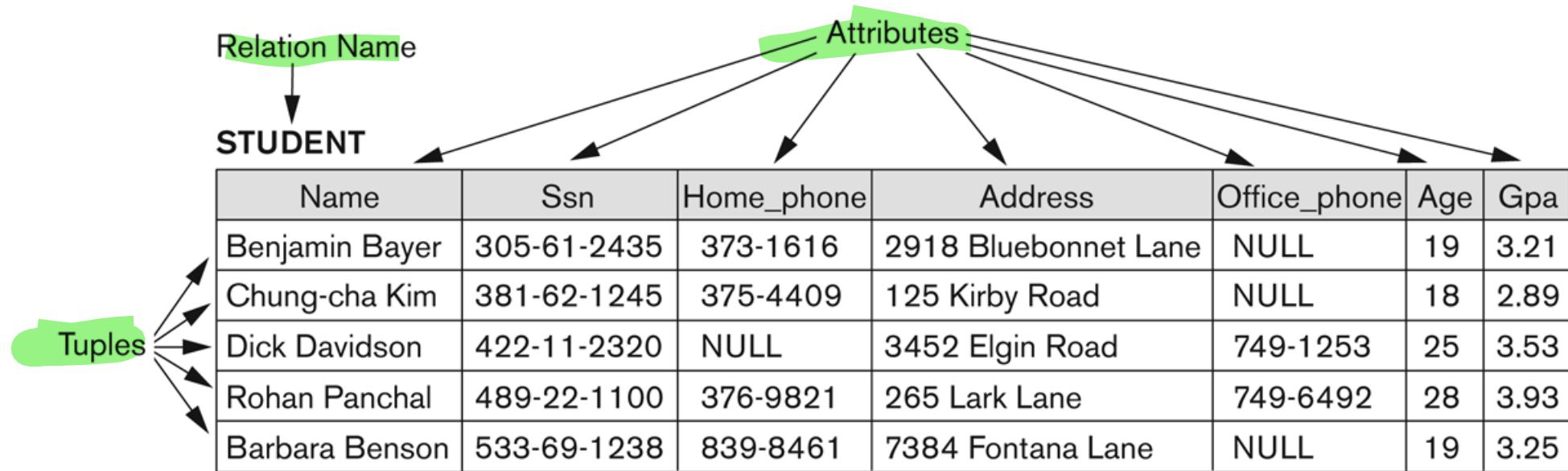
- A Relation is a mathematical concept based on the ideas of sets
- The model was first proposed by Dr. E.F. Codd of IBM Research in 1970 in the following paper:
  - "A Relational Model for Large Shared Data Banks," Communications of the ACM, June 1970
- The above paper caused a major revolution in the field of database management and earned Dr. Codd the ACM Turing Award

# Informal Definitions

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- Informally, a **relation** looks like a **table** of values.
- A **relation** typically contains a **set of rows**.
- The data elements in each **row** represent certain facts that correspond to a real-world **entity or relationship**
  - In the formal model, rows are called **tuples**
- Each **column** has a **column header** that gives an indication of the **meaning of the data items in that column**
  - In the formal model, the column header is called an **attribute name** (or just **attribute**)

# Example of a Relation



**Figure 5.1**

The attributes and tuples of a relation STUDENT.

# Informal Definitions

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- Key of a Relation:
  - Each row has a value of a data item (or set of items) that uniquely identifies that row in the table
    - Called the *key*
  - In the STUDENT table, SSN is the key
  - Sometimes row-ids or sequential numbers are assigned as keys to identify the rows in a table
    - Called *artificial key* or *surrogate key*



# Formal Definitions - Schema

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- The **Schema** (or description) of a Relation:
  - Denoted by  $R(A_1, A_2, \dots, A_n)$
  - R is the **name** of the relation
  - The **attributes** of the relation are  $A_1, A_2, \dots, A_n$
- Example:  
CUSTOMER (Cust-id, Cust-name, Address, Phone#)
  - CUSTOMER is the relation name
  - Defined over the four attributes: Cust-id, Cust-name, Address, Phone#
- Each attribute has a **domain or a set of valid values**.
  - For example, the domain of Cust-id is 6 digit numbers.

# Formal Definitions - Tuple

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- A **tuple** is an **ordered set of values** (enclosed in angled brackets '**< ... >**')
  - **Each value** is derived from an appropriate *domain*.
- A row in the CUSTOMER relation is a **4-tuple** and would consist of **four values**, for example:
  - **<632895, "John Smith", "101 Main St. Atlanta, GA 30332", "(404) 894-2000">**
  - This is called a 4-tuple as it has 4 values
  - A tuple (row) in the CUSTOMER relation.
- A **relation is a set of such tuples** (rows)

# Formal Definitions - Domain

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- A **domain** has a logical definition:
  - Example: “USA\_phone\_numbers” are the **set of 10 digit phone numbers** valid in the U.S.
- A domain also has a **data-type** or a **format defined** for it.
  - The **USA\_phone\_numbers** may have a format: **(ddd)ddd-dddd** where each d is a decimal digit.
  - **Dates** have various formats such as year, month, date formatted as **yyyy-mm-dd**, or as **dd mm,yyyy** etc.
- The **attribute name** designates the **role played by a domain** in a relation:
  - Used to interpret the meaning of the data elements corresponding to that attribute
  - Example: The domain Date may be used to define two attributes named “Invoice-date” and “Payment-date” with different meanings

# Formal Definitions - State

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- The **relation state** is a **subset of the Cartesian product of the domains of its attributes**
  - each domain contains the set of all possible values the attribute can take.
- Example: **attribute Cust-name** is defined over the domain of character strings of maximum **length 25**
  - **dom(Cust-name)** is **varchar(25)**
- The role these strings play in the CUSTOMER relation is that of the *name of a customer*.

# Formal Definitions - Summary

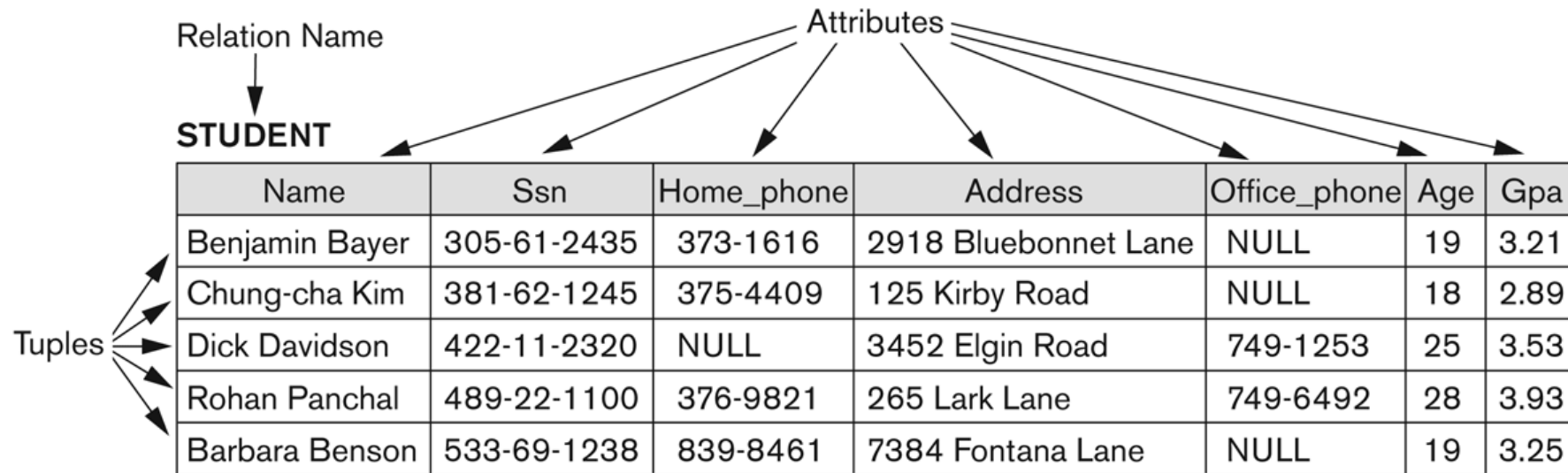
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- Formally,
  - Given  $R(A_1, A_2, \dots, A_n)$
  - $r(R) \subset \text{dom}(A_1) \times \text{dom}(A_2) \times \dots \times \text{dom}(A_n)$
- $R(A_1, A_2, \dots, A_n)$  is the **schema** of the relation
- $R$  is the **name** of the relation
- $A_1, A_2, \dots, A_n$  are the **attributes** of the relation
- $r(R)$ : a **specific state** (or "value" or "population") of relation  $R$  – this is a *set of tuples* (rows)
  - $r(R) = \{t_1, t_2, \dots, t_n\}$  where each  $t_i$  is an  $n$ -tuple
  - $t_i = \langle v_1, v_2, \dots, v_n \rangle$  where each  $v_j$  *element-of*  $\text{dom}(A_j)$

# Definition Summary

<u>Informal Terms</u>		<u>Formal Terms</u>
Table		Relation
Column Header		Attribute
All possible Column Values		Domain
Row		Tuple
Table Definition		Schema of a Relation
Populated Table		State of the Relation

# Example – A relation STUDENT



**Figure 5.1**

The attributes and tuples of a relation STUDENT.



# Characteristics Of Relations

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- Ordering of tuples in a relation  $r(R)$ :
  - The tuples are *not considered to be ordered*, even though they appear to be in the tabular form.
- Ordering of attributes in a relation schema  $R$  (and of values within each tuple):
  - We will consider the attributes in  $R(A_1, A_2, \dots, A_n)$  and the values in  $t = \langle v_1, v_2, \dots, v_n \rangle$  to be ordered .
    - (However, a more general alternative definition of relation does not require this ordering).

# Same state as previous Figure (but with different order of tuples)

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**Figure 5.2**

The relation STUDENT from Figure 5.1 with a different order of tuples.

**STUDENT**

Name	Ssn	Home_phone	Address	Office_phone	Age	Gpa
Dick Davidson	422-11-2320	NULL	3452 Elgin Road	749-1253	25	3.53
Barbara Benson	533-69-1238	839-8461	7384 Fontana Lane	NULL	19	3.25
Rohan Panchal	489-22-1100	376-9821	265 Lark Lane	749-6492	28	3.93
Chung-cha Kim	381-62-1245	375-4409	125 Kirby Road	NULL	18	2.89
Benjamin Bayer	305-61-2435	373-1616	2918 Bluebonnet Lane	NULL	19	3.21

# Characteristics Of Relations

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- Values in a tuple:
  - All values are considered atomic (indivisible).
  - Each value in a tuple must be from the domain of the attribute for that column
    - If tuple  $t = \langle v_1, v_2, \dots, v_n \rangle$  is a tuple (row) in the relation state  $r$  of  $R(A_1, A_2, \dots, A_n)$
    - Then each  $v_i$  must be a value from  $dom(A_i)$
  - A special null value is used to represent values that are unknown or inapplicable to certain tuples.

# Relational Integrity Constraints

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- Constraints are **conditions** that must hold on **all** valid relation states.
- There are three *main types* of constraints in the relational model:
  - **Key** constraints
  - **Entity integrity** constraints
  - **Referential integrity** constraints
- Another implicit constraint is the **domain** constraint
  - Every value in a tuple must be from the *domain of its attribute* (or it could be **null**, if allowed for that attribute)

# Key Constraints

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- **Superkey of R:**
  - Is a set of attributes SK of R with the following condition:
    - No two tuples in any valid relation state  $r(R)$  will have the same value for SK
    - That is, for any distinct tuples  $t_1$  and  $t_2$  in  $r(R)$ ,  $t_1[SK] \neq t_2[SK]$
    - This condition must hold in any valid state  $r(R)$
- **Key of R:**
  - A "minimal" superkey
  - That is, a key is a superkey K such that removal of any attribute from K results in a set of attributes that is not a superkey (does not possess the superkey uniqueness property)

# Key Constraints (continued)

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- Example: Consider the CAR relation schema:
  - CAR(State, Reg#, SerialNo, Make, Model, Year)
  - CAR has two keys:
    - Key1 = {State, Reg#}
    - Key2 = {SerialNo}
  - Both are also superkeys of CAR
  - {SerialNo, Make} is a superkey but *not* a key.
- In general:
  - Any *key* is a *superkey* (but not vice versa)
  - Any set of attributes that *includes a key* is a *superkey*
  - A *minimal* superkey is also a key

# Key Constraints (continued)

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- If a relation has **several candidate keys**, **one is chosen** arbitrarily to be the **primary key**.
  - The primary key attributes are underlined.
- Example: Consider the CAR relation schema:
  - CAR(State, Reg#, SerialNo, Make, Model, Year)
  - We chose SerialNo as the primary key
- The **primary key value is used to *uniquely identify* each tuple** in a relation
  - Provides the tuple identity
- Also **used to *reference* the tuple from another tuple**
  - General rule: **Choose** as **primary key the smallest of the candidate keys** (in terms of size)
  - Not always applicable – choice is sometimes subjective



# CAR table with two candidate keys – LicenseNumber chosen as Primary Key

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**CAR**

<u>License_number</u>	Engine_serial_number	Make	Model	Year
Texas ABC-739	A69352	Ford	Mustang	02
Florida TVP-347	B43696	Oldsmobile	Cutlass	05
New York MPO-22	X83554	Oldsmobile	Delta	01
California 432-TFY	C43742	Mercedes	190-D	99
California RSK-629	Y82935	Toyota	Camry	04
Texas RSK-629	U028365	Jaguar	XJS	04

**Figure 5.4**

The CAR relation, with two candidate keys: License\_number and Engine\_serial\_number.

# Relational Database Schema

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- **Relational Database Schema:**
  - A set  $S$  of relation schemas that belong to the same database.
  - $S$  is the name of the whole **database schema**
  - $S = \{R_1, R_2, \dots, R_n\}$
  - $R_1, R_2, \dots, R_n$  are the names of the individual **relation schemas** within the database  $S$
- Following slide shows a COMPANY database schema with 6 relation schemas

# COMPANY Database Schema

## EMPLOYEE

Fname	Minit	Lname	<u>Ssn</u>	Bdate	Address	Sex	Salary	Super_ssn	Dno
-------	-------	-------	------------	-------	---------	-----	--------	-----------	-----

## DEPARTMENT

Dname	<u>Dnumber</u>	Mgr_ssn	Mgr_start_date
-------	----------------	---------	----------------

## DEPT\_LOCATIONS

<u>Dnumber</u>	<u>Dlocation</u>
----------------	------------------

## PROJECT

Pname	<u>Pnumber</u>	Plocation	Dnum
-------	----------------	-----------	------

## WORKS\_ON

<u>Essn</u>	<u>Pno</u>	Hours
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## DEPENDENT

<u>Essn</u>	<u>Dependent_name</u>	Sex	Bdate	Relationship
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**Figure 5.5**  
Schema diagram for  
the COMPANY  
relational database  
schema.

# Entity Integrity

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- **Entity Integrity:**
  - The *primary key attributes* PK of each relation schema R in S cannot have null values in any tuple of  $r(R)$ .
    - This is because primary key values are used to *identify* the individual tuples.
    - $t[PK] \neq \text{null}$  for any tuple t in  $r(R)$
    - If PK has several attributes, null is not allowed in any of these attributes
  - Note: Other attributes of R may be constrained to disallow null values, even though they are not members of the primary key.

# Referential Integrity

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- A **constraint involving two relations**
  - The previous constraints involve a single relation.
- **Used to specify a relationship among tuples in two relations:**
  - The **referencing relation** and the **referenced relation**.

# Referential Integrity

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- Tuples in the **referencing relation R1** have **attributes FK** (called **foreign key attributes**) that reference the primary key attributes PK of the **referenced relation R2**.
  - A tuple  $t_1$  in  $R_1$  is said to **reference** a tuple  $t_2$  in  $R_2$  if  $t_1[FK] = t_2[PK]$ .
- A **referential integrity constraint** can be **displayed** in a relational database schema as a **directed arc from R1.FK to R2**.

# Referential Integrity (or foreign key) Constraint

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- Statement of the constraint
  - The value in the foreign key column (or columns) FK of the the **referencing relation** R1 can be **either**:
    - (1) a value of an existing primary key value of a corresponding primary key PK in the **referenced relation** R2, or
    - (2) a **null**.
- In case (2), the FK in R1 should **not** be a part of its own primary key.



# Displaying a relational database schema and its constraints

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- Each relation schema can be displayed as a row of attribute names
- The name of the relation is written above the attribute names
- The primary key attribute (or attributes) will be underlined
- A foreign key (referential integrity) constraints is displayed as a directed arc (arrow) from the foreign key attributes to the referenced table
  - Can also point the the primary key of the referenced relation for clarity
- Next slide shows the COMPANY **relational schema diagram**

# Referential Integrity Constraints for COMPANY database

**Figure 5.7**

Referential integrity constraints displayed on the COMPANY relational database schema.

