

# Why Was the AES Encryption Algorithm necessary?

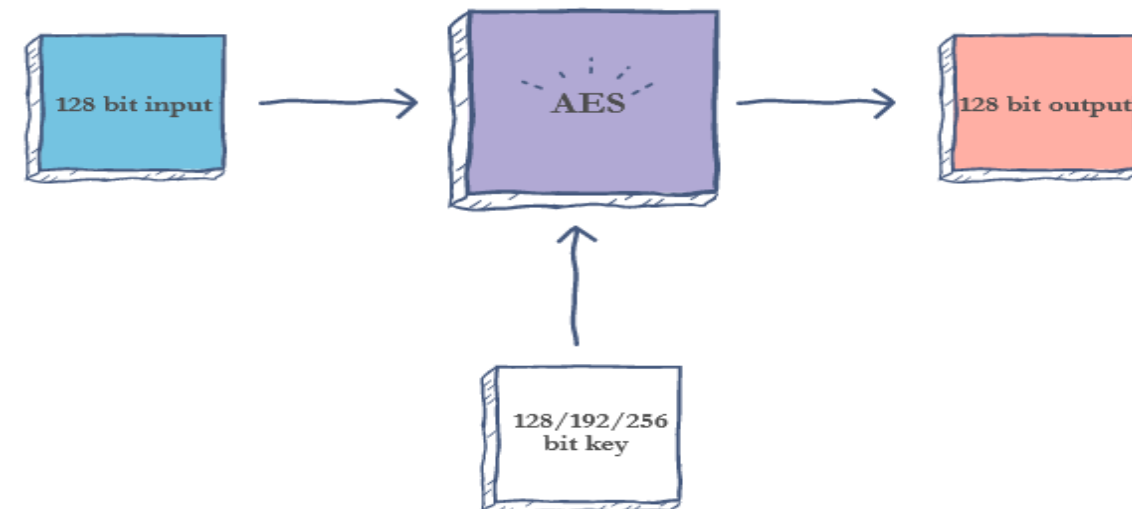
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Chronology of DES Cracking	
Broken for the first time	1997
Broken in 56 hours	1998
Broken in 22 hours and 15 minutes	1999
Capable of broken in 5 minutes	2021

# Introduction

Advanced Encryption Standard (AES) features are as follows:

- Symmetric key symmetric block cipher
- 128-bit block data, 128/192/256-bit keys
- Stronger and faster than Triple-DES



	DES	AES
Developed	1977	2000
Cipher Type	Symmetric block cipher	Symmetric block cipher
Block size	64 bits	128 bits
Key length	56 bits	128/192/256 bits
Security	Rendered insecure	Considered secure

# Introduction

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- AES is an iterative rather than Feistel cipher.
- It is based on ‘substitution–permutation network’.
- It comprises of a series of linked operations, some of which involve replacing inputs by specific outputs (substitutions) and others involve shuffling bits around (permutations).
- AES performs all its computations on bytes rather than bits.

# Introduction

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The Advanced Encryption Standard (AES) published by the National Institute of Standards and Technology (NIST) in December 2001.

- History
- Criteria
- Rounds
- Data Units
- Structure of Each Round

# Introduction

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## History

- In February 2001, NIST announced that a draft of the Federal Information Processing Standard (FIPS) was available for public review and comment.
- Finally, AES was published as FIPS 197 in the Federal Register in December 2001.

# Introduction

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## Criteria

The criteria defined by NIST for selecting AES fall into three areas:

1. Security -128bit key
2. Cost-Computational efficiency and storage requirements
3. Implementation -Flexibility(platform independent)

# Introduction

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## Rounds

- AES is a non Feistel cipher that encrypts and decrypts a block of 128bit data.
- It uses 10,12 or 14 rounds → keysize-128/192/256bits

# Introduction

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## Rounds

AES-128

AES-192

AES-256

But roundkey is

Always 128bits

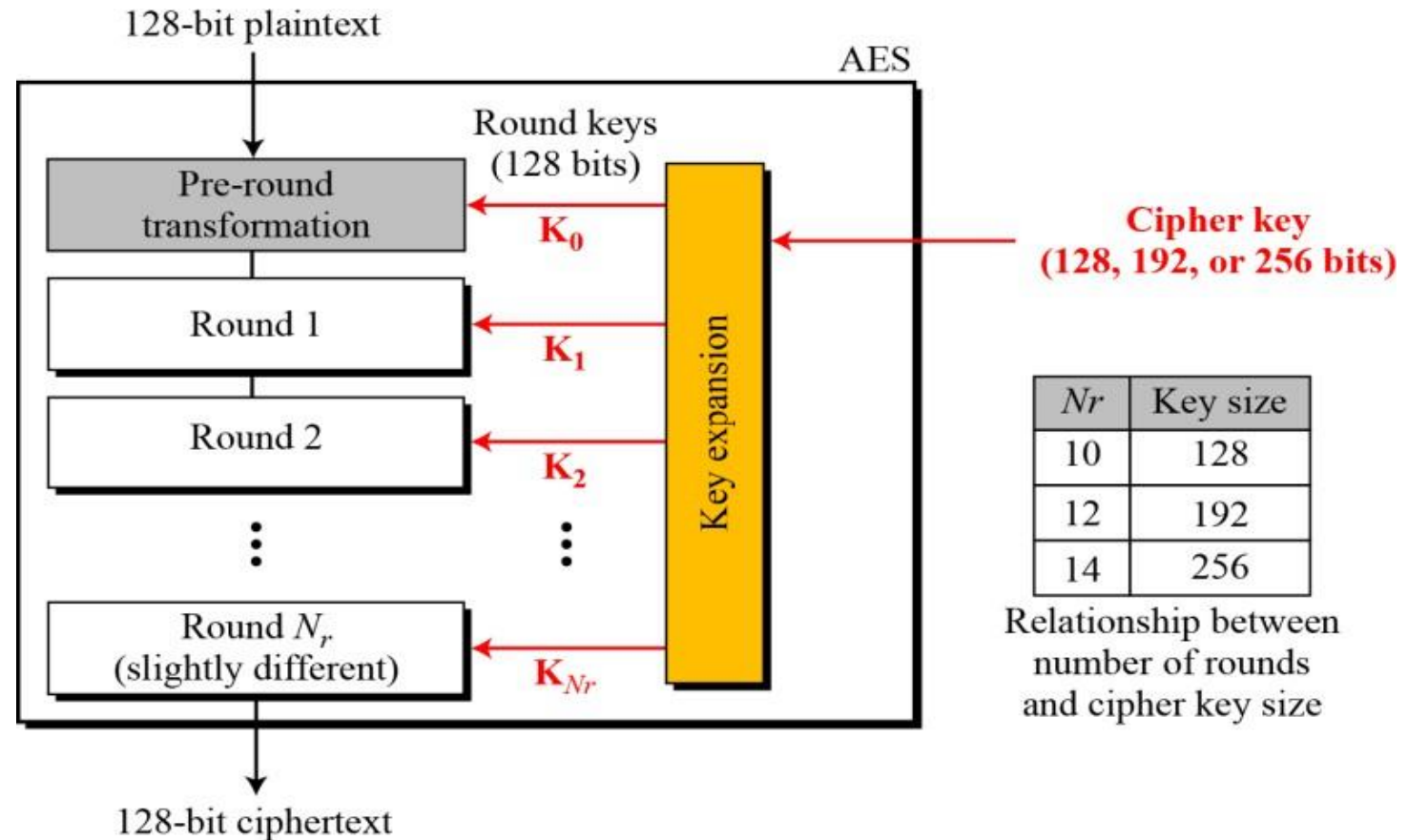


# Introduction

## Rounds

The number of round key is one more than the number of rounds

Number of Round keys =  $N_r + 1$



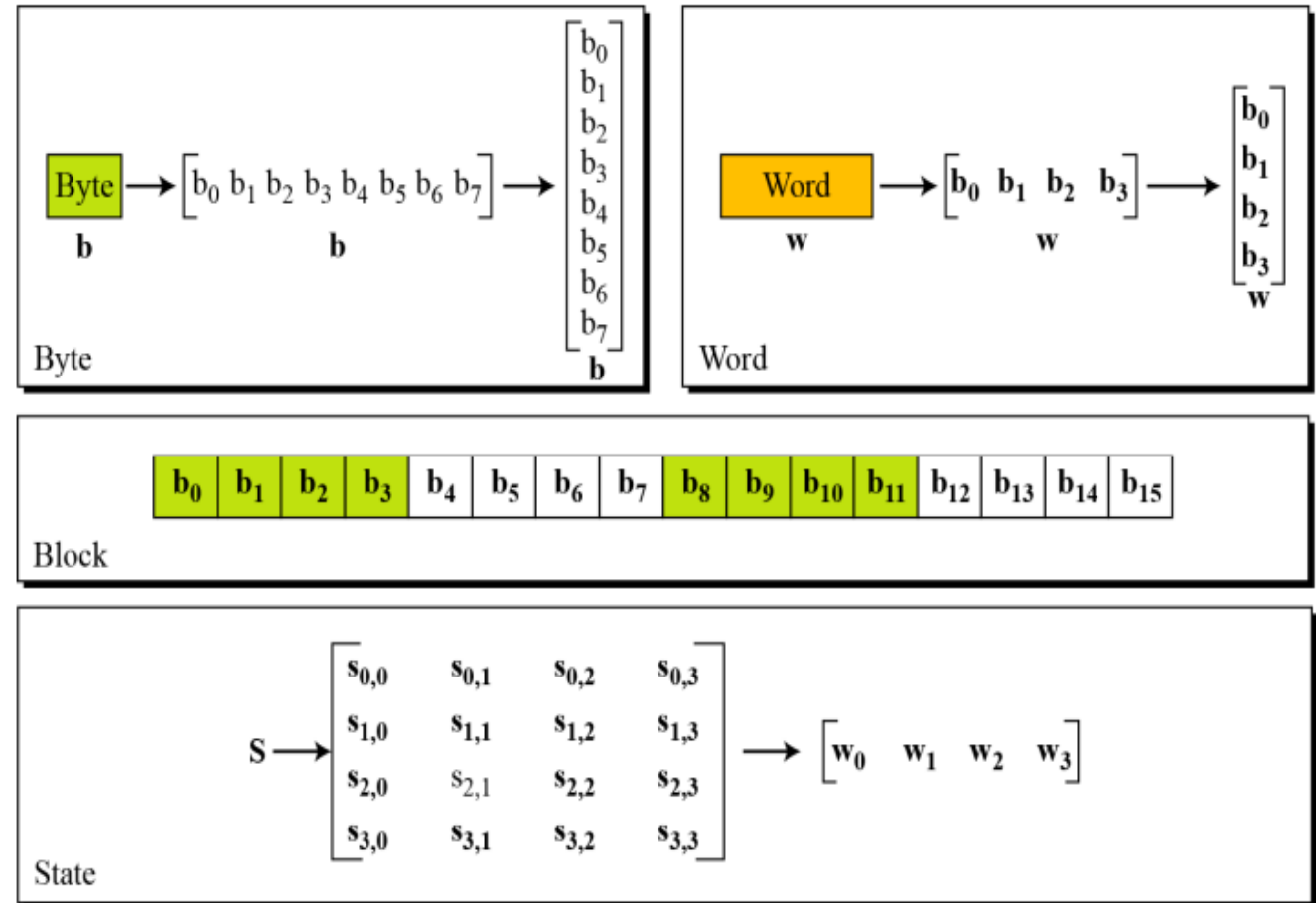
# Introduction

## Data Units

AES uses 5 units of measurement to refer to data

1. Bits
2. Bytes
3. Words
4. Blocks
5. State

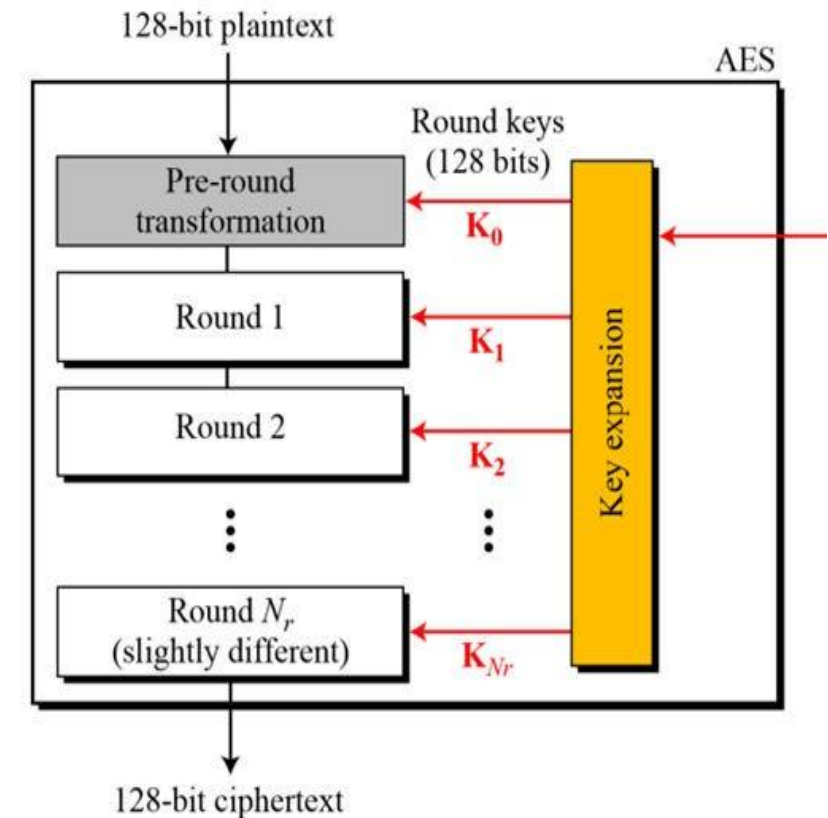
*Data units used in AES*



# Introduction

## Data Units – States

- AES uses several rounds
- Each round is made of several stages – Data blocks are transferred from one stage to other
- At the beginning and end of cipher – data blocks
- Before and after each stage – data block is referred as state



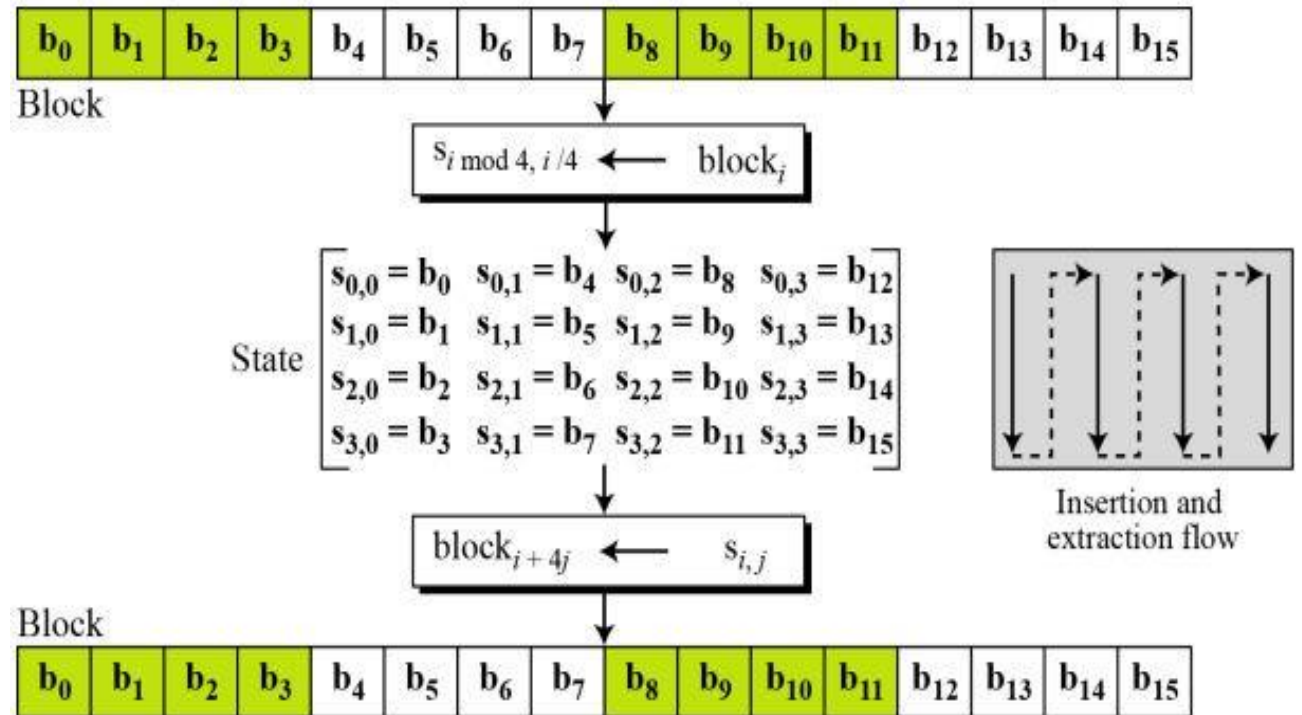
# Introduction

## Data Units – States

- S – State
- T- temporary state
- States are made up of 16bytes
- Matrix (4x4)

0	1	2	3
4	5	6	7
8	9	10	11
12	13	14	15

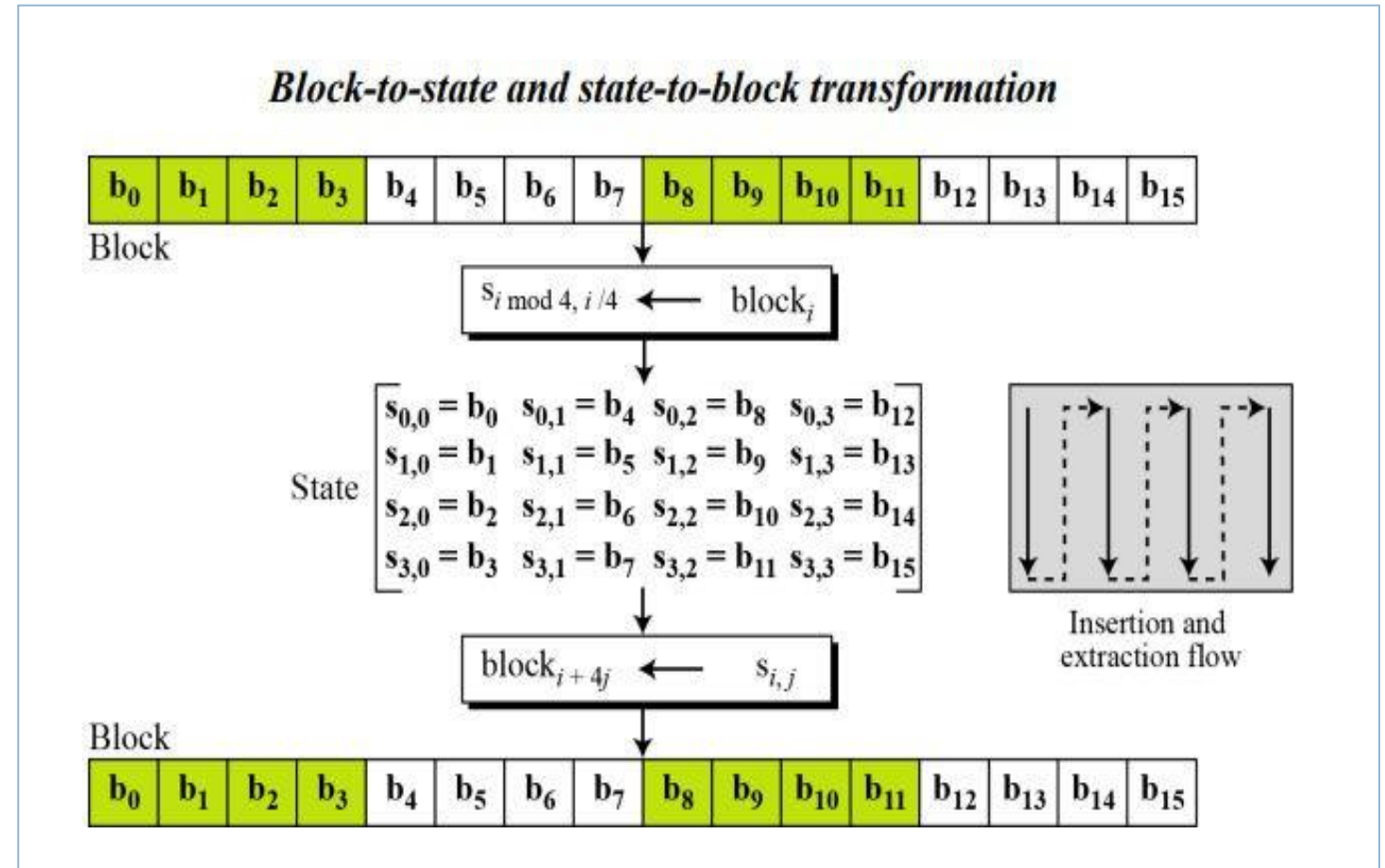
### Block-to-state and state-to-block transformation



# Introduction

## Data Units – States

- State is treated as row matrix(1 x 4) of words



# Introduction

## Example

*Changing plaintext to state*

Text: A E S U S E S A M A T R I X **Z Z**

Hexadecimal: 00 04 12 14 12 04 12 00 0C 00 13 11 08 23 19 19

State:  $\begin{bmatrix} 00 & 12 & 0C & 08 \\ 04 & 04 & 00 & 23 \\ 12 & 12 & 13 & 19 \\ 14 & 00 & 11 & 19 \end{bmatrix}$

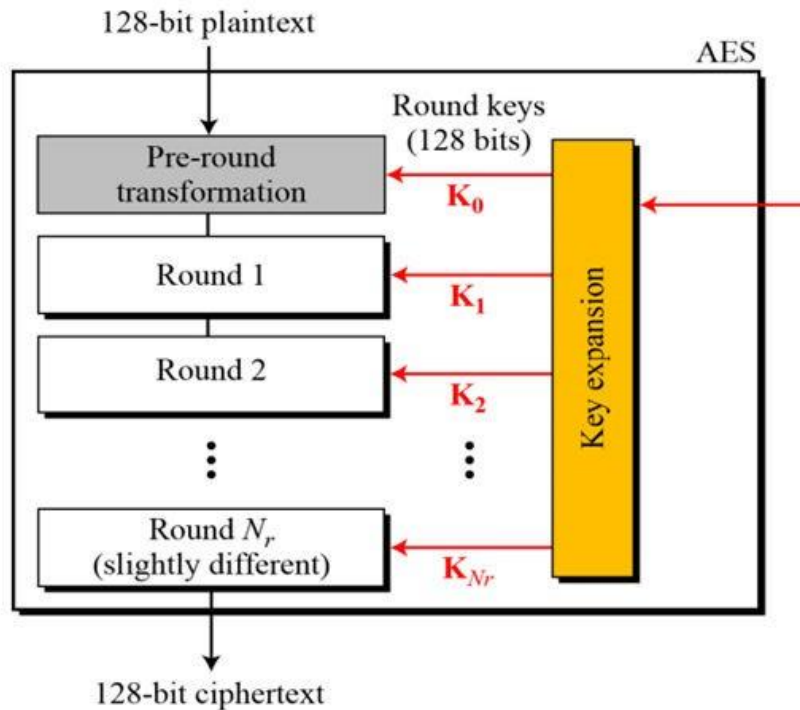
Plaintext →	a	b	c	d	e	f	g	h	i	j	k	l	m	n	o	p	q	r	s	t	u	v	w	x	y	z
Ciphertext →	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O	P	Q	R	S	T	U	V	W	X	Y	Z
Value →	00	01	02	03	04	05	06	07	08	09	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25

Decimal	Hex	Char
0	0	[NULL]
1	1	[START OF HEADING]
2	2	[START OF TEXT]
3	3	[END OF TEXT]
4	4	[END OF TRANSMISSION]
5	5	[ENQUIRY]
6	6	[ACKNOWLEDGE]
7	7	[BELL]
8	8	[BACKSPACE]
9	9	[HORIZONTAL TAB]
10	A	[LINE FEED]
11	B	[VERTICAL TAB]
12	C	[FORM FEED]
13	D	[CARRIAGE RETURN]
14	E	[SHIFT OUT]
15	F	[SHIFT IN]
16	10	[DATA LINK ESCAPE]
17	11	[DEVICE CONTROL 1]
18	12	[DEVICE CONTROL 2]
19	13	[DEVICE CONTROL 3]
20	14	[DEVICE CONTROL 4]
21	15	[NEGATIVE ACKNOWLEDGE]
22	16	[SYNCHRONOUS IDLE]
23	17	[ENG OF TRANS. BLOCK]
24	18	[CANCEL]
25	19	[END OF MEDIUM]
26	1A	[SUBSTITUTE]
27	1B	[ESCAPE]
28	1C	[FILE SEPARATOR]
29	1D	[GROUP SEPARATOR]
30	1E	[RECORD SEPARATOR]
31	1F	[UNIT SEPARATOR]

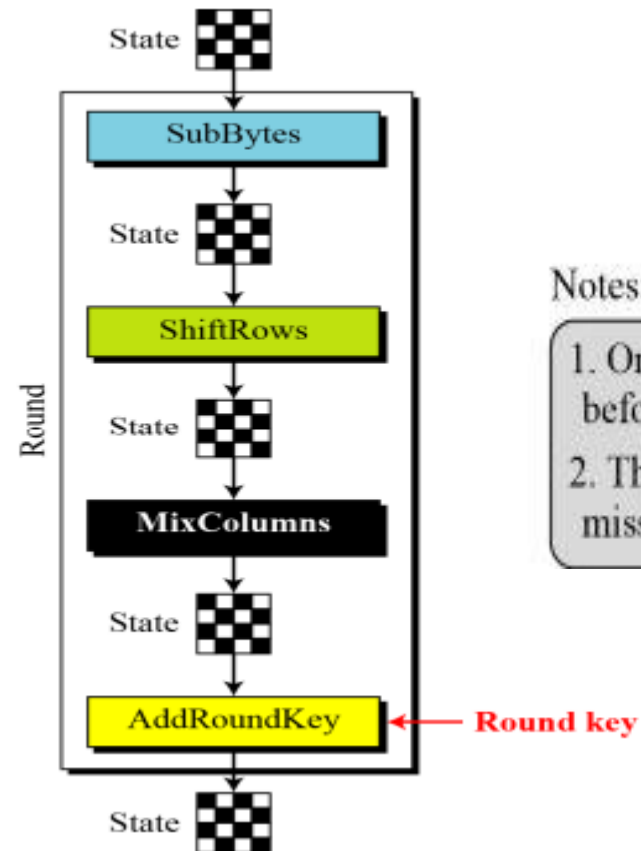


# Introduction

## Structure of Round



### *Structure of each round at the encryption site*



Notes:

1. One AddRoundKey is applied before the first round.
2. The third transformation is missing in the last round.

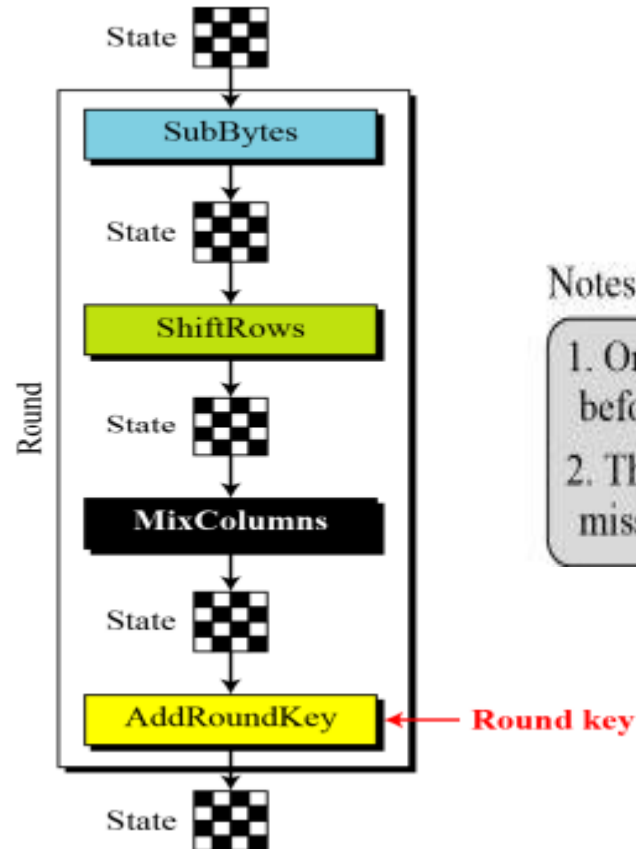
# Introduction

## Structure of Round

### 4 Transformations

1. SubBytes
2. ShiftRows
3. MixColumns
4. Add Round Keys

*Structure of each round at the encryption site*



Notes:

1. One AddRoundKey is applied before the first round.
2. The third transformation is missing in the last round.



# Transformation

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1. SubBytes(Substitution)
2. ShiftRows (Permutation)
3. MixColumns (Mixing)
4. Add Round Keys (Adding)

# Transformation

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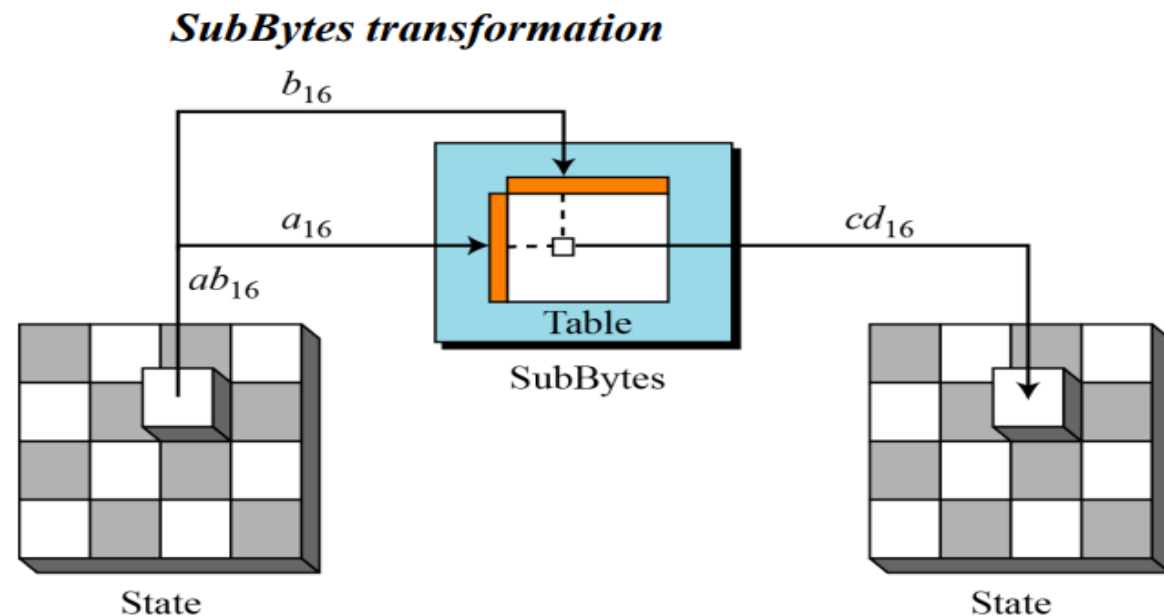
## SubBytes(Substitution)

- AES uses substitution
- Mechanism is different
  1. Substitution done for each byte
  2. Table is used for substitution for each byte
  3. Table Lookup process or mathematical calculation in  $GF(2^8)$  field)

# Transformation

## SubBytes

- SubBytes is used at the encryption site.
- To substitute a byte, we interpret the byte as two hexadecimal digits.
- Left digit –row
- Right digit -column



# Transformation

## SubBytes- Transformation table

*SubBytes transformation table*

	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
0	63	7C	77	7B	F2	6B	6F	C5	30	01	67	2B	FE	D7	AB	76
1	CA	82	C9	7D	FA	59	47	F0	AD	D4	A2	AF	9C	A4	72	C0
2	B7	FD	93	26	36	3F	F7	CC	34	A5	E5	F1	71	D8	31	15
3	04	C7	23	C3	18	96	05	9A	07	12	80	E2	EB	27	B2	75
4	09	83	2C	1A	1B	6E	5A	A0	52	3B	D6	B3	29	E3	2F	84
5	53	D1	00	ED	20	FC	B1	5B	6A	CB	BE	39	4A	4C	58	CF
6	D0	EF	AA	FB	43	4D	33	85	45	F9	02	7F	50	3C	9F	A8
7	51	A3	40	8F	92	9D	38	F5	BC	B6	DA	21	10	FF	F3	D2
8	CD	0C	13	EC	5F	97	44	17	C4	A7	7E	3D	64	5D	19	73
9	60	81	4F	DC	22	2A	90	88	46	EE	B8	14	DE	5E	0B	DB
A	E0	32	3A	0A	49	06	24	5C	C2	D3	AC	62	91	95	E4	79
B	E7	CB	37	6D	8D	D5	4E	A9	6C	56	F4	EA	65	7A	AE	08
C	BA	78	25	2E	1C	A6	B4	C6	E8	DD	74	1F	4B	BD	8B	8A
D	70	3E	B5	66	48	03	F6	0E	61	35	57	B9	86	C1	1D	9E
E	E1	F8	98	11	69	D9	8E	94	9B	1E	87	E9	CE	55	28	DF
F	8C	A1	89	0D	BF	E6	42	68	41	99	2D	0F	B0	54	BB	16

## InvSubBytes-Transformation table

	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
0	52	09	6A	D5	30	36	A5	38	BF	40	A3	9E	81	F3	D7	FB
1	7C	E3	39	82	9B	2F	FF	87	34	8E	43	44	C4	DE	E9	CB
2	54	7B	94	32	A6	C2	23	3D	EE	4C	95	0B	42	FA	C3	4E
3	08	2E	A1	66	28	D9	24	B2	76	5B	A2	49	6D	8B	D1	25
4	72	F8	F6	64	86	68	98	16	D4	A4	5C	CC	5D	65	B6	92
5	6C	70	48	50	FD	ED	B9	DA	5E	15	46	57	A7	8D	9D	84
6	90	D8	AB	00	8C	BC	D3	0A	F7	E4	58	05	B8	B3	45	06
7	D0	2C	1E	8F	CA	3F	0F	02	C1	AF	BD	03	01	13	8A	6B
8	3A	91	11	41	4F	67	DC	EA	97	F2	CF	CE	F0	B4	E6	73
9	96	AC	74	22	E7	AD	35	85	E2	F9	37	E8	1C	75	DF	6E
A	47	F1	1A	71	1D	29	C5	89	6F	B7	62	0E	AA	18	BE	1B
B	FC	56	3E	4B	C6	D2	79	20	9A	DB	C0	FE	78	CD	5A	F4
C	1F	DD	A8	33	88	07	C7	31	B1	12	10	59	27	80	EC	5F
D	60	51	7F	A9	19	B5	4A	0D	2D	E5	7A	9F	93	C9	9C	EF
E	A0	E0	3B	4D	AE	2A	F5	B0	C8	EB	BB	3C	83	53	99	61
F	17	2B	04	7E	BA	77	D6	26	E1	69	14	63	55	21	0C	7D

# Transformation

## Example 1

$$5A_{16} = BE_{16}$$

$$5B_{16} = 39_{16}$$

*SubBytes transformation table*

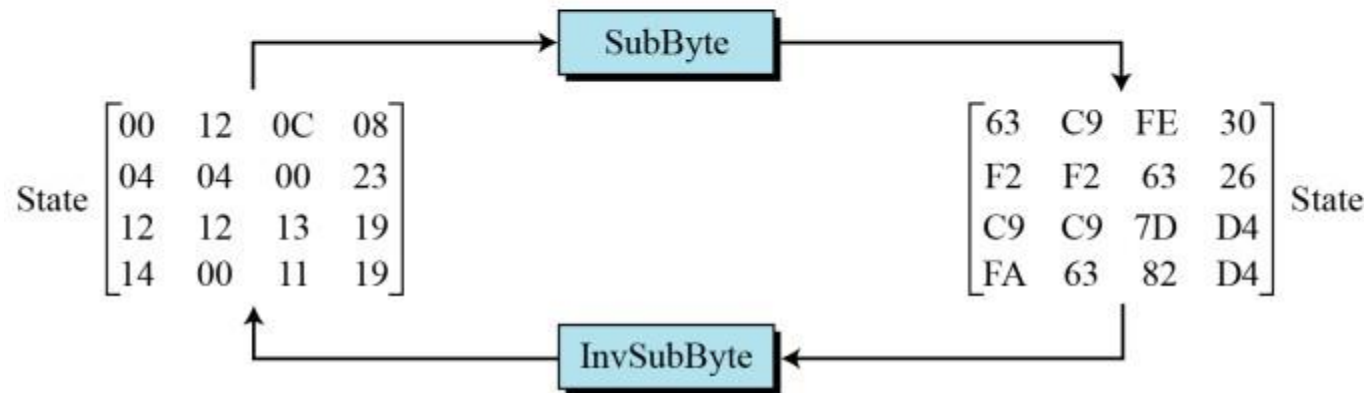
	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
0	63	7C	77	7B	F2	6B	6F	C5	30	01	67	2B	FE	D7	AB	76
1	CA	82	C9	7D	FA	59	47	F0	AD	D4	A2	AF	9C	A4	72	C0
2	B7	FD	93	26	36	3F	F7	CC	34	A5	E5	F1	71	D8	31	15
3	04	C7	23	C3	18	96	05	9A	07	12	80	E2	EB	27	B2	75
4	09	83	2C	1A	1B	6E	5A	A0	52	3B	D6	B3	29	E3	2F	84
5	53	D1	00	ED	20	FC	B1	5B	6A	CB	BE	39	4A	4C	58	CF
6	D0	EF	AA	FB	43	4D	33	85	45	F9	02	7F	50	3C	9F	A8
7	51	A3	40	8F	92	9D	38	F5	BC	B6	DA	21	10	FF	F3	D2
8	CD	0C	13	EC	5F	97	44	17	C4	A7	7E	3D	64	5D	19	73
9	60	81	4F	DC	22	2A	90	88	46	EE	B8	14	DE	5E	0B	DB
A	E0	32	3A	0A	49	06	24	5C	C2	D3	AC	62	91	95	E4	79
B	E7	CB	37	6D	8D	D5	4E	A9	6C	56	F4	EA	65	7A	AE	08
C	BA	78	25	2E	1C	A6	B4	C6	E8	DD	74	1F	4B	BD	8B	8A
D	70	3E	B5	66	48	03	F6	0E	61	35	57	B9	86	C1	1D	9E
E	E1	F8	98	11	69	D9	8E	94	9B	1E	87	E9	CE	55	28	DF
F	8C	A1	89	0D	BF	E6	42	68	41	99	2D	0F	B0	54	BB	16



# Transformation

## Example 2

shows how a state is transformed using the **SubBytes** transformation. The figure also shows that the **InvSubBytes** transformation creates the original one. Note that if the two bytes have the same values, their transformation is also the same.



	0	1	2	3	4	5	6	7	8	9	A	B	C	D	E	F
0	52	09	6A	D5	30	36	A5	38	BF	40	A3	9E	81	F3	D7	FB
1	7C	E3	39	82	9B	2F	FF	87	34	8E	43	44	C4	DE	E9	CB
2	54	7B	94	32	A6	C2	23	3D	EE	4C	95	0B	42	FA	C3	4E
3	08	2E	A1	66	28	D9	24	B2	76	5B	A2	49	6D	8B	D1	25
4	72	F8	F6	64	86	68	98	16	D4	A4	5C	CC	5D	65	B6	92
5	6C	70	48	50	FD	ED	B9	DA	5E	15	46	57	A7	8D	9D	84
6	90	D8	AB	00	8C	BC	D3	0A	F7	E4	58	05	B8	B3	45	06
7	D0	2C	1E	8F	CA	3F	0F	02	C1	AF	BD	03	01	13	8A	6B
8	3A	91	11	41	4F	67	DC	EA	97	F2	CF	CE	F0	B4	E6	73
9	96	AC	74	22	E7	AD	35	85	E2	F9	37	E8	1C	75	DF	6E
A	47	F1	1A	71	1D	29	C5	89	6F	B7	62	0E	AA	18	BE	1B
B	FC	56	3E	4B	C6	D2	79	20	9A	DB	C0	FE	78	CD	5A	F4
C	1F	DD	A8	33	88	07	C7	31	B1	12	10	59	27	80	EC	5F
D	60	51	7F	A9	19	B5	4A	0D	2D	E5	7A	9F	93	C9	9C	EF
E	A0	E0	3B	4D	AE	2A	F5	B0	C8	EB	BB	3C	83	53	99	61
F	17	2B	04	7E	BA	77	D6	26	E1	69	14	63	55	21	0C	7D

# Transformation

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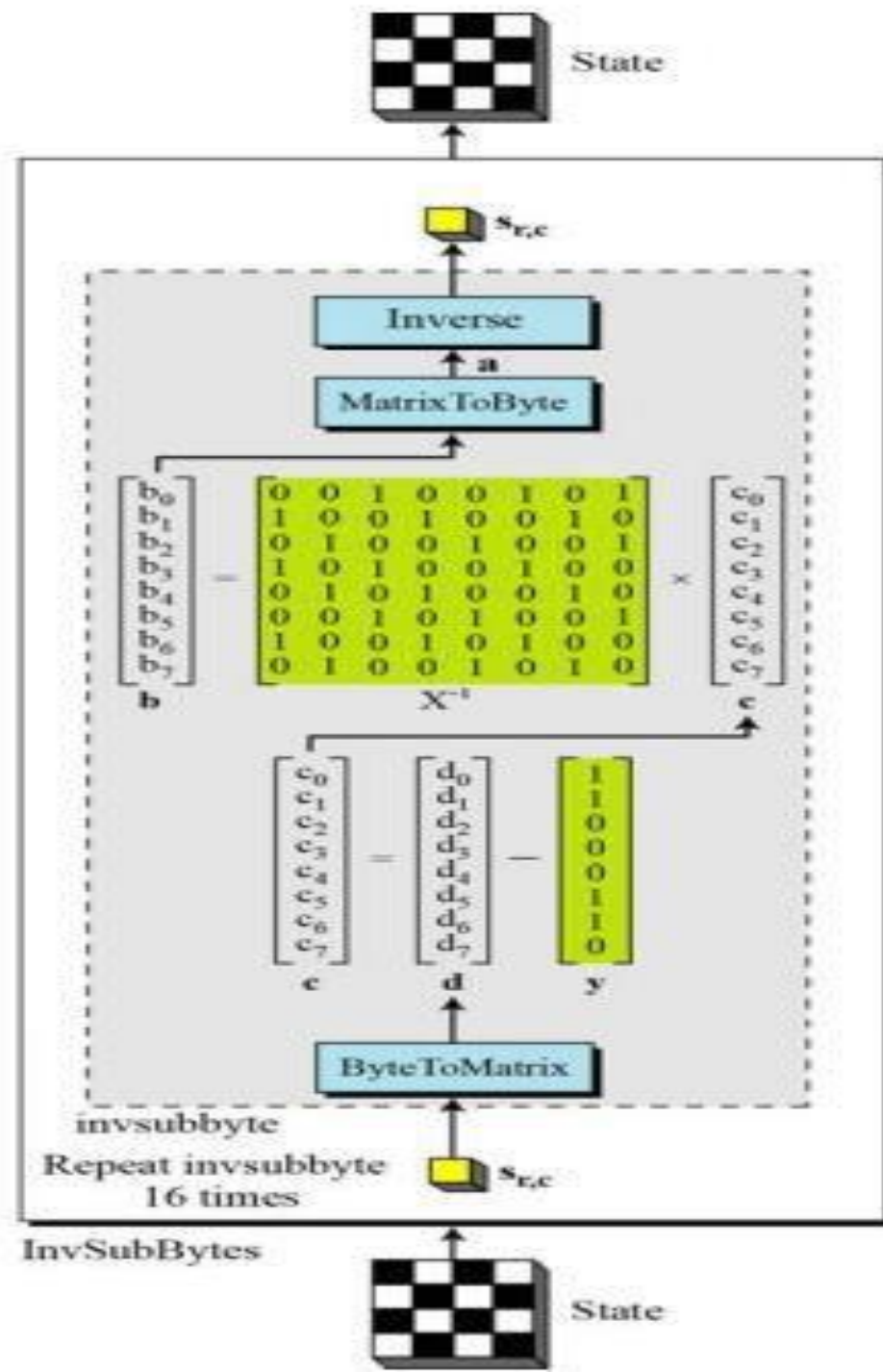
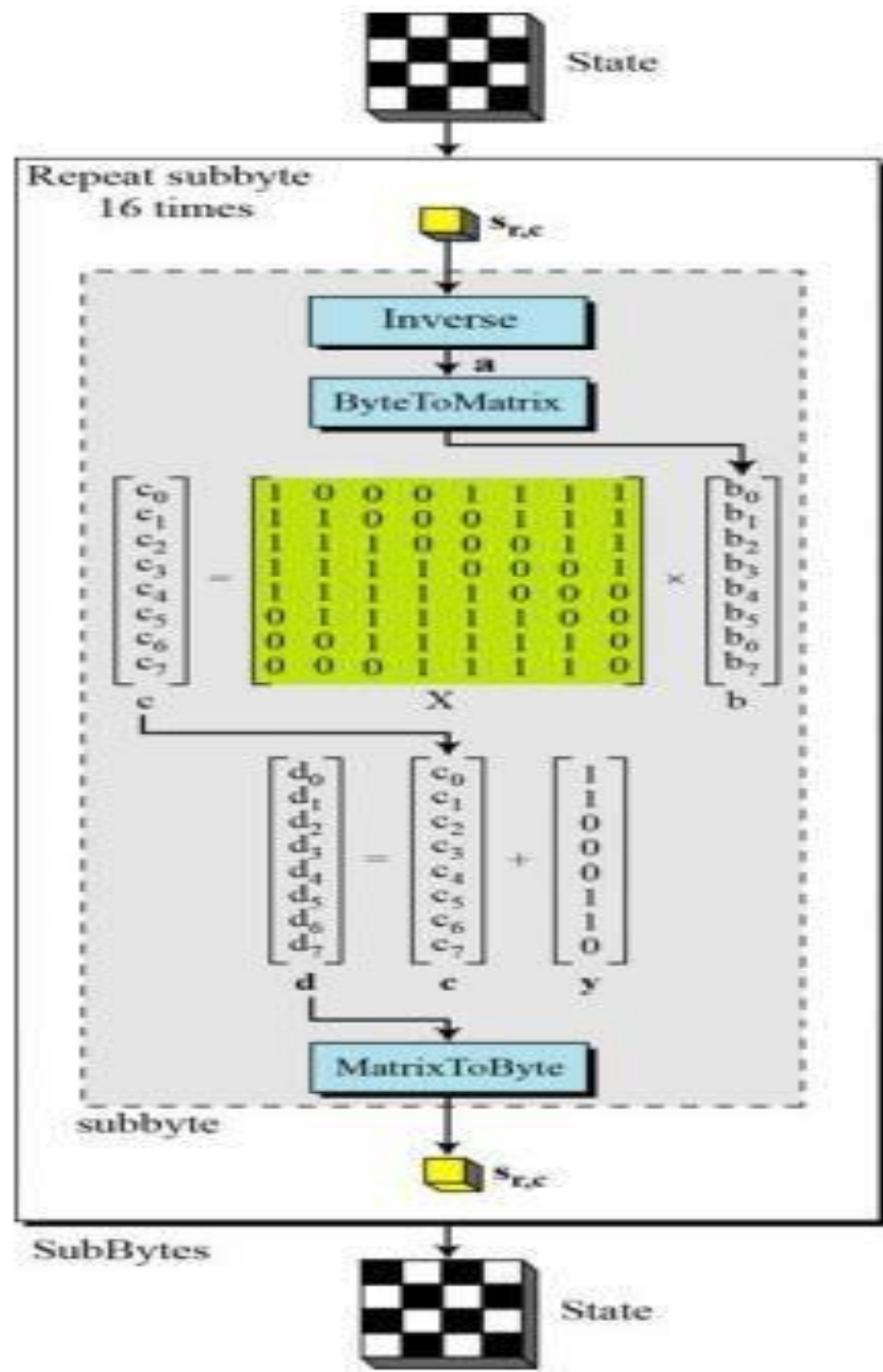
## SubBytes

### *Transformation Using the $GF(2^8)$ Field*

*AES also defines the transformation algebraically using the  $GF(2^8)$  field with the irreducible polynomials  $(x^8 + x^4 + x^3 + x + 1)$*

$$\text{subbyte:} \quad \rightarrow \quad \mathbf{d} = \mathbf{X} (s_{r,c})^{-1} \oplus \mathbf{y}$$

$$\text{invsubbyte:} \quad \rightarrow \quad [\mathbf{X}^{-1}(\mathbf{d} \oplus \mathbf{y})]^{-1} = [\mathbf{X}^{-1}(\mathbf{X} (s_{r,c})^{-1} \oplus \mathbf{y} \oplus \mathbf{y})]^{-1} = [(s_{r,c})^{-1}]^{-1} = s_{r,c}$$





# Transformation

*Pseudocode for SubBytes transformation*

**SubBytes (S)**

```
{  
  for (r = 0 to 3)  
    for (c = 0 to 3)  
       $S_{r,c} = \text{subbyte}(S_{r,c})$   
}
```

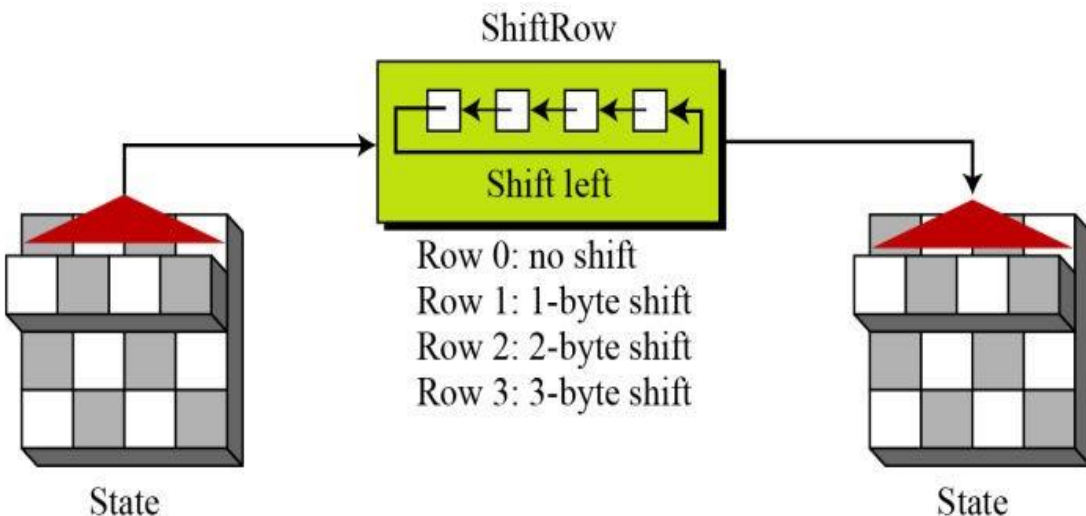
**subbyte (byte)**

```
{  
   $a \leftarrow \text{byte}^{-1}$  // Multiplicative inverse in  $GF(2^8)$  with inverse of 00 to be 00  
  ByteToMatrix (a, b)  
  for (i = 0 to 7)  
  {  
     $\mathbf{c}_i \leftarrow \mathbf{b}_i \oplus \mathbf{b}_{(i+4)\bmod 8} \oplus \mathbf{b}_{(i+5)\bmod 8} \oplus \mathbf{b}_{(i+6)\bmod 8} \oplus \mathbf{b}_{(i+7)\bmod 8}$   
     $\mathbf{d}_i \leftarrow \mathbf{c}_i \oplus \text{ByteToMatrix}(0x63)$   
  }  
  MatrixToByte (d, d)  
  byte  $\leftarrow$  d  
}
```

# Transformation

## ShiftRows (Permutation)

- Another transformation found in a round is shifting, which permutes the bytes.
- Each row is shifted a particular number of times.



[ b0   b1   b2   b3 ]		[ b0   b1   b2   b3 ]
b4   b5   b6   b7	->	b5   b6   b7   b4
b8   b9   b10   b11		b10   b11   b8   b9
[ b12   b13   b14   b15 ]		[ b15   b12   b13   b14 ]

# Transformation

## ShiftRows (Permutation)

- **InvShiftRows** In the decryption, the transformation is called **InvShiftRows** and the shifting is to the right.

*Pseudocode for ShiftRows transformation*

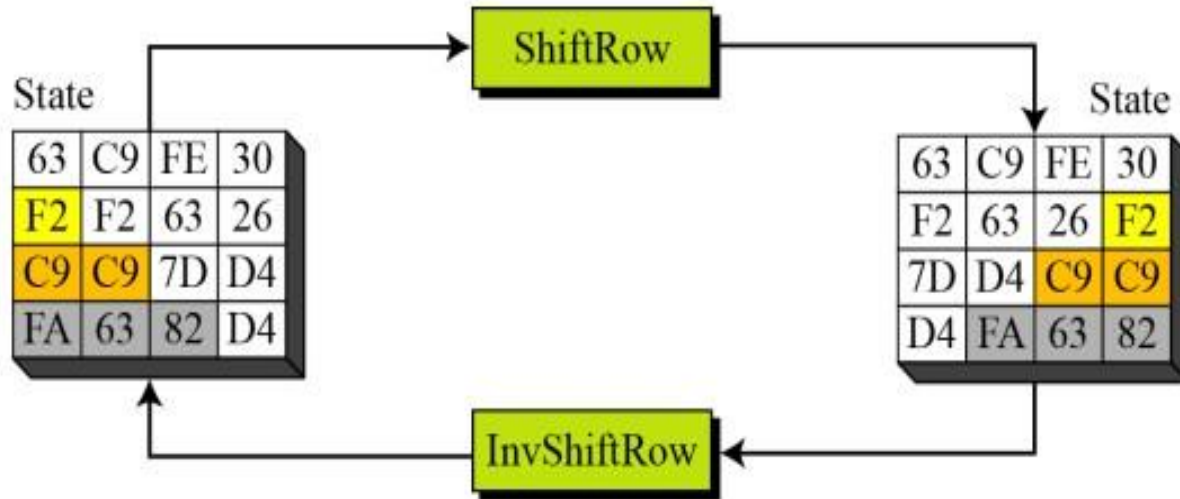
```
ShiftRows (S)
{
  for ( $r = 1$  to 3)
    shiftrow ( $s_r$ ,  $r$ )           //  $s_r$  is the  $r$ th row
}

shiftrow (row,  $n$ )           //  $n$  is the number of bytes to be shifted
{
  CopyRow (row, t)           // t is a temporary row
  for ( $c = 0$  to 3)
     $\mathbf{row}_{(c - n) \bmod 4} \leftarrow \mathbf{t}_c$ 
}
```

# Transformation

## ShiftRows (Permutation)

shows how a state is transformed using ShiftRows transformation. The figure also shows that InvShiftRows transformation creates the original state.



[ b0   b1   b2   b3 ]		[ b0   b1   b2   b3 ]
b4   b5   b6   b7	->	b5   b6   b7   b4
b8   b9   b10   b11		b10   b11   b8   b9
[ b12   b13   b14   b15 ]		[ b15   b12   b13   b14 ]

# Transformation

## MixColumns (Mixing)

- This step is basically a matrix multiplication.
- Each column is multiplied with a specific matrix and thus the position of each byte in the column is changed as a result.

*Mixing bytes using matrix multiplication*

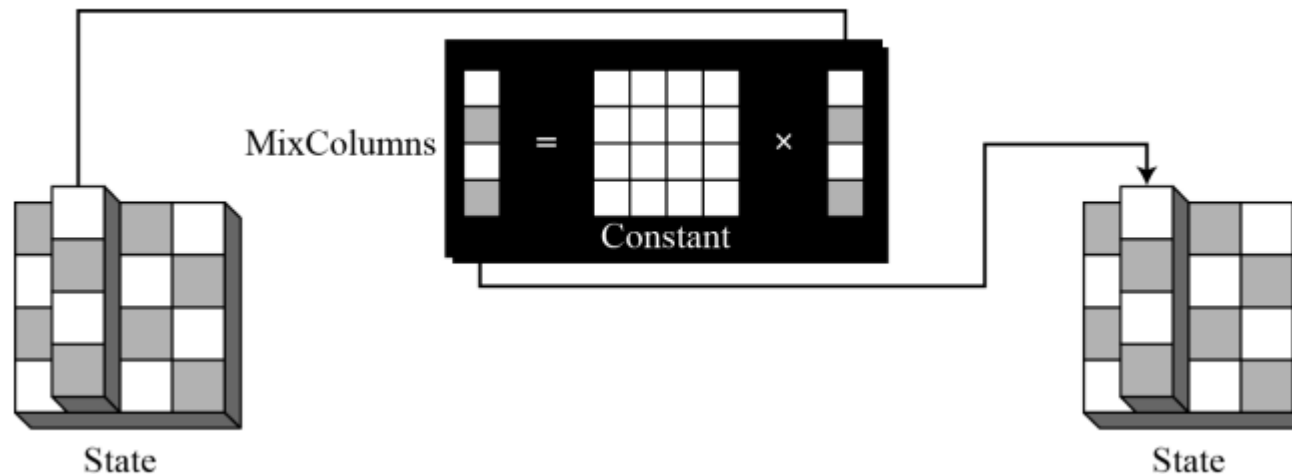
$$\begin{array}{l}
 ax + by + cz + dt \\
 ex + fy + gz + ht \\
 ix + jy + kz + lt \\
 mx + ny + oz + pt
 \end{array}
 \begin{array}{c}
 \rightarrow \\
 \rightarrow \\
 \rightarrow \\
 \rightarrow
 \end{array}
 \begin{bmatrix}
 \text{ } \\
 \text{ } \\
 \text{ } \\
 \text{ }
 \end{bmatrix}
 =
 \begin{bmatrix}
 a & b & c & d \\
 e & f & g & h \\
 i & j & k & l \\
 m & n & o & p
 \end{bmatrix}
 \times
 \begin{bmatrix}
 \mathbf{x} \\
 \mathbf{y} \\
 \mathbf{z} \\
 \mathbf{t}
 \end{bmatrix}$$

New matrix
**Constant matrix**
Old matrix

# Transformation

## MixColumns (Mixing)

- The MixColumns transformation operates at the column level; it transforms each column of the state to a new column.



# Transformation

## MixColumns (Mixing)

*Pseudocode for MixColumns transformation*

```
MixColumns (S)
{
    for (c = 0 to 3)
        mixcolumn (sc)
}

mixcolumn (col)
{
    CopyColumn (col, t)           // t is a temporary column

    col0 ← (0x02) • t0 ⊕ (0x03) • t1 ⊕ t2 ⊕ t3

    col1 ← t0 ⊕ (0x02) • t1 ⊕ (0x03) • t2 ⊕ t3

    col2 ← t0 ⊕ t1 ⊕ (0x02) • t2 ⊕ (0x03) • t3

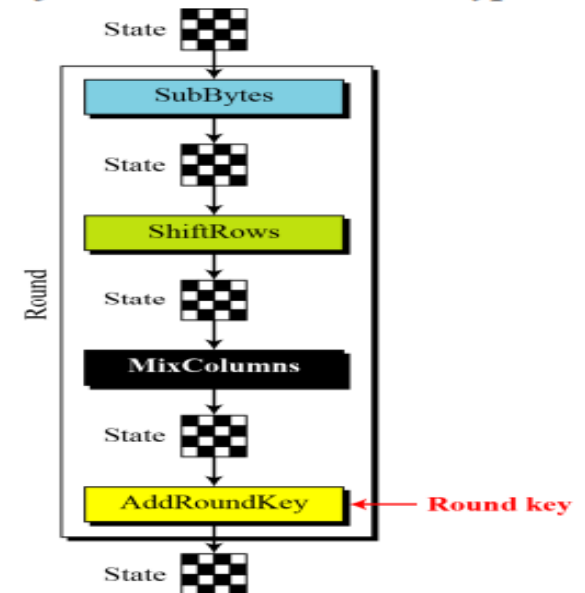
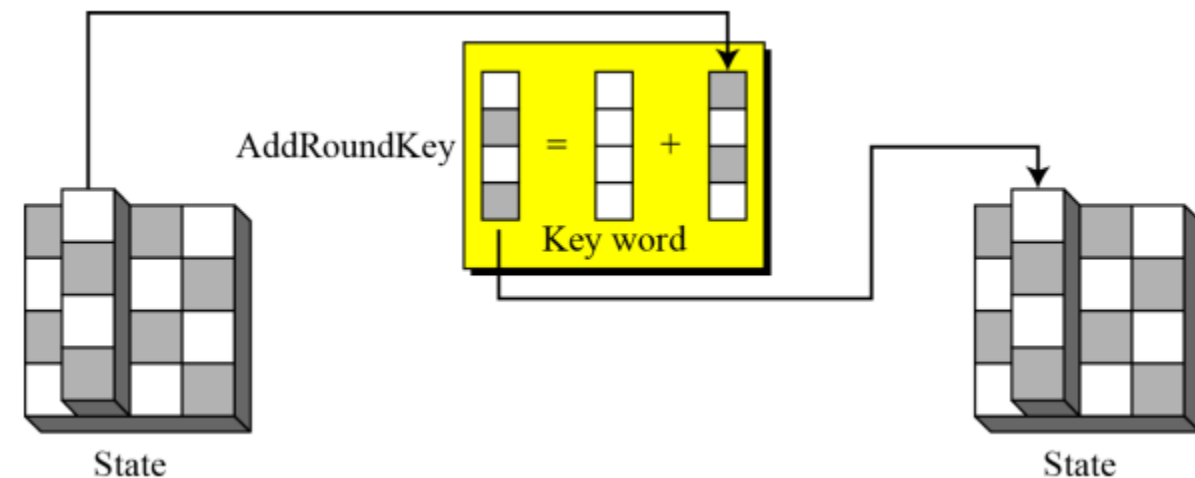
    col3 ← (0x03) • t0 ⊕ t1 ⊕ t2 ⊕ (0x02) • t3
}
```

# Transformation

## Add Round Keys (Adding)

- AddRoundKey proceeds one column at a time.
- AddRoundKey adds a round key word with each state column matrix; the operation in AddRoundKey is matrix addition.

*Structure of each round at the encryption site*





# Transformation

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## Add Round Keys (Adding)

*Pseudocode for AddRoundKey transformation*

**AddRoundKey (S)**

{

  for ( $c = 0$  to 3)

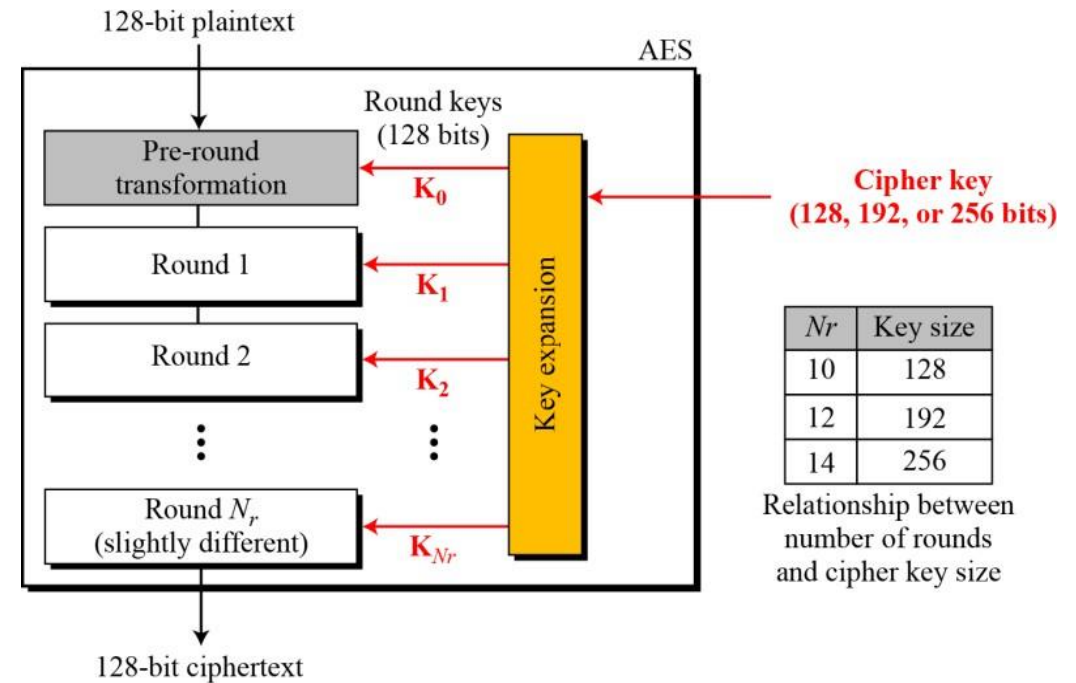
$s_c \leftarrow s_c \oplus w_{\text{round} + 4c}$

}

# Key Expansion

- To create round keys for each round, AES uses a key-expansion process.

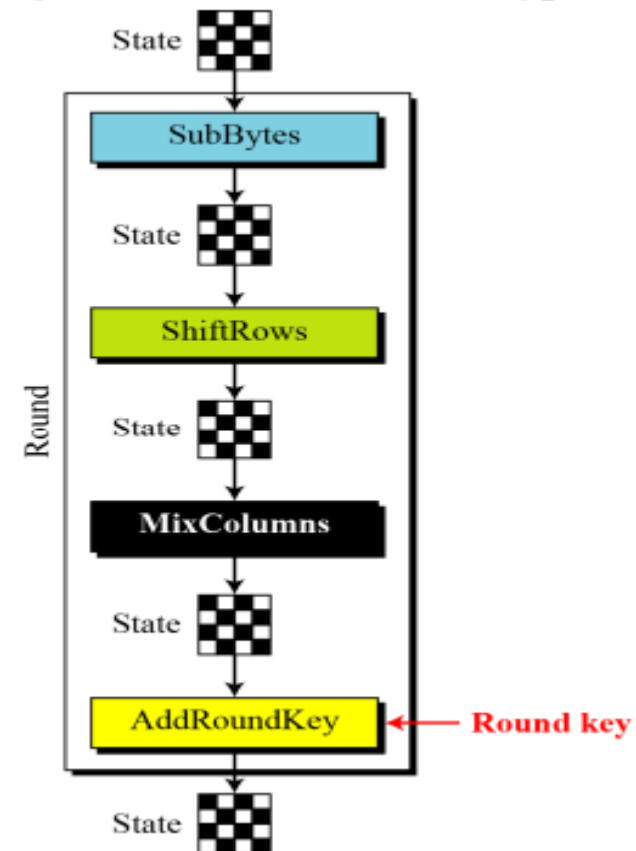
- If the number of rounds is  $N_r$ , the key-expansion routine creates  $N_r + 1$  128-bit round keys from one single 128-bit cipher key



# Key Expansion

- First round key is used for pre-round transformation
- Remaining all for every round transformation 4<sup>th</sup>

*Structure of each round at the encryption site*



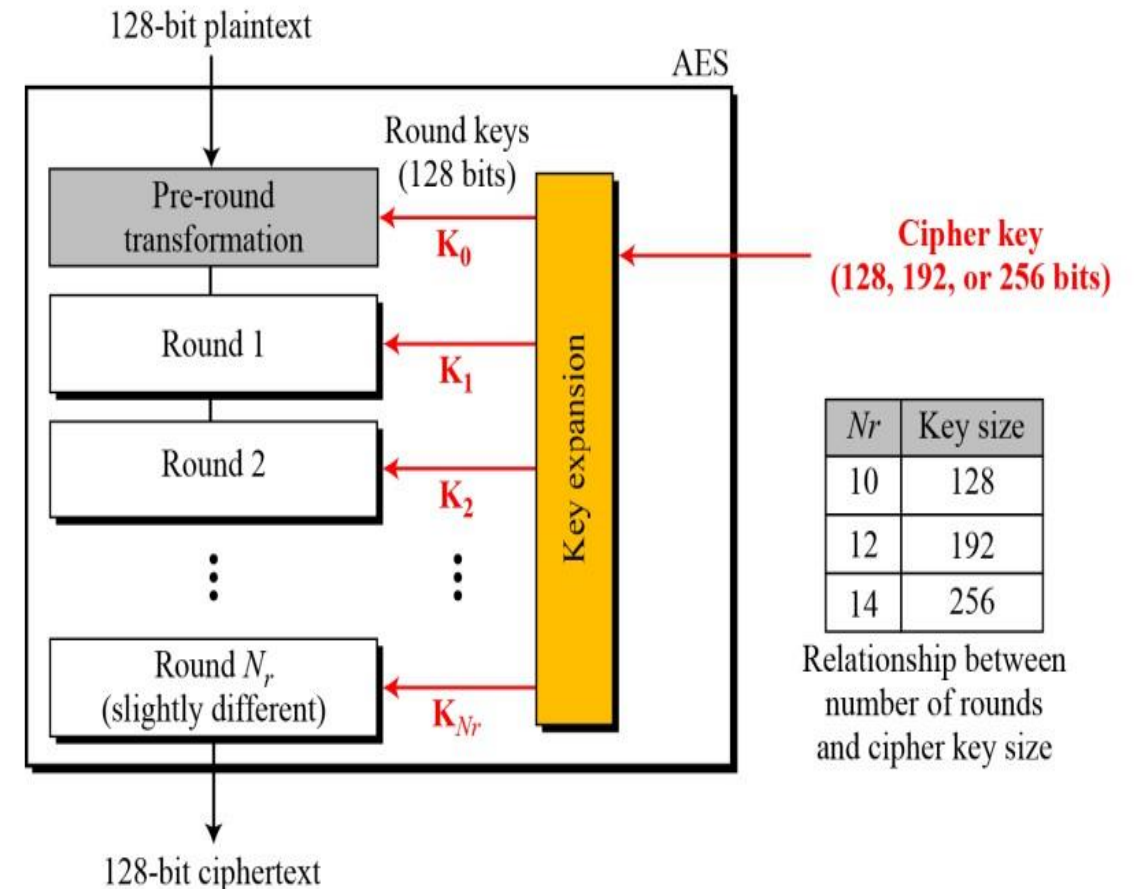
# Key Expansion

Key-expansion creates round key word by word, where a word is an array of 4 bytes.

- Key Expansion in AES-128
- Key Expansion in AES-192 and AES-256
- Key-Expansion Analysis

*Words for each round*

Round	Words			
Pre-round	$w_0$	$w_1$	$w_2$	$w_3$
1	$w_4$	$w_5$	$w_6$	$w_7$
2	$w_8$	$w_9$	$w_{10}$	$w_{11}$
...	...			
$N_r$	$w_{4N_r}$	$w_{4N_r+1}$	$w_{4N_r+2}$	$w_{4N_r+3}$



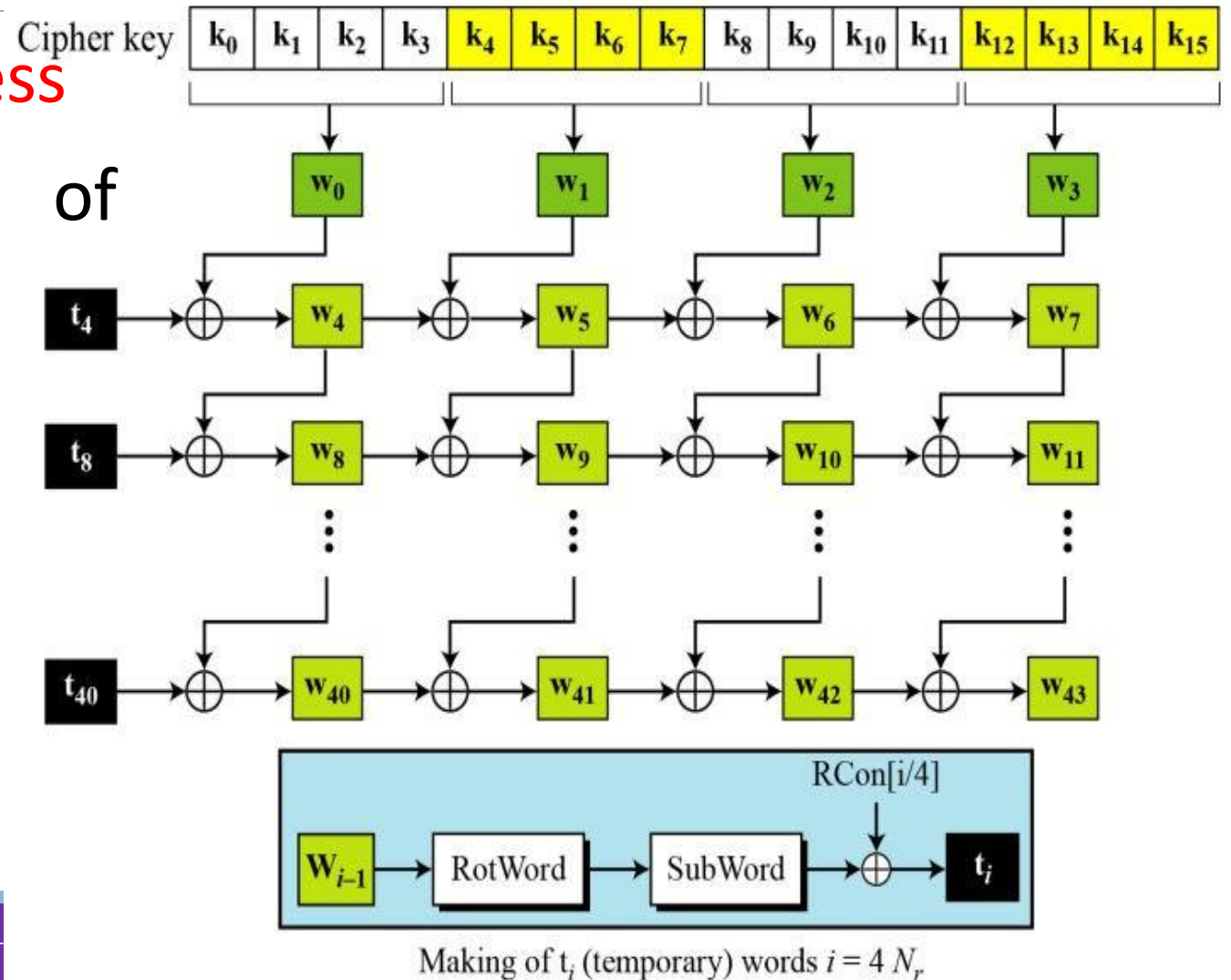
# Key Expansion

## Key Expansion in AES-128 process

1. Cipher key is an array of 16bytes( $k_0$  to  $k_{15}$ )

The first 4 words( $w_0, w_1, w_2, w_3$ ) are made from cipher key

- $k_0$  to  $k_3 \rightarrow w_0$
- $k_4$  to  $k_7 \rightarrow w_1$
- $k_8$  to  $k_{11} \rightarrow w_2$
- $k_{12}$  to  $k_{15} \rightarrow w_3$



# Key Expansion

## Key Expansion in AES-128 process

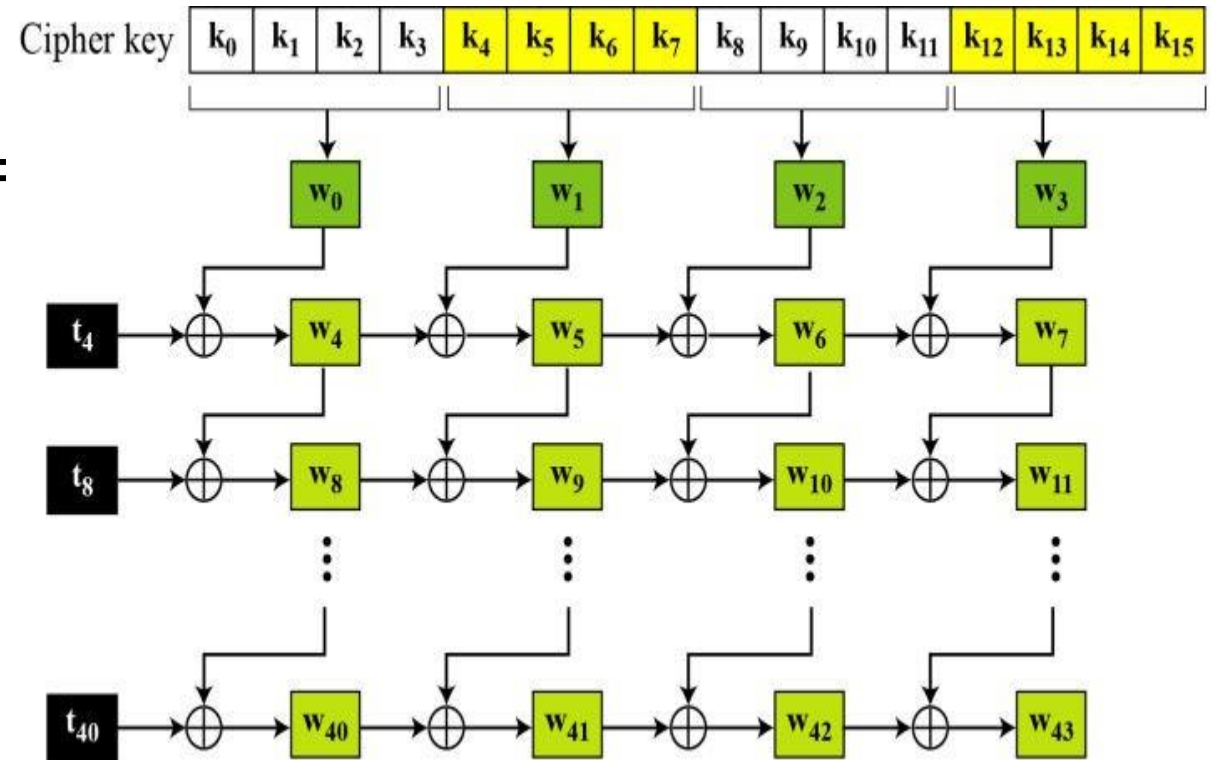
2. The rest of the words ( $w_i$  for  $i$  : are made as follows

i) if  $(i \bmod 4) \neq 0$ ,  $w_i = w_{i-1} \oplus w_{i-4}$

ii) if  $(i \bmod 4) = 0$ ,  $w_i = t \oplus w_{i-4}$

Temporary word  $t$

$t_i = \text{subword}(\text{Rotword}(w_{i-1})) \oplus \text{Rcon}_{i/4}$



# Key Expansion

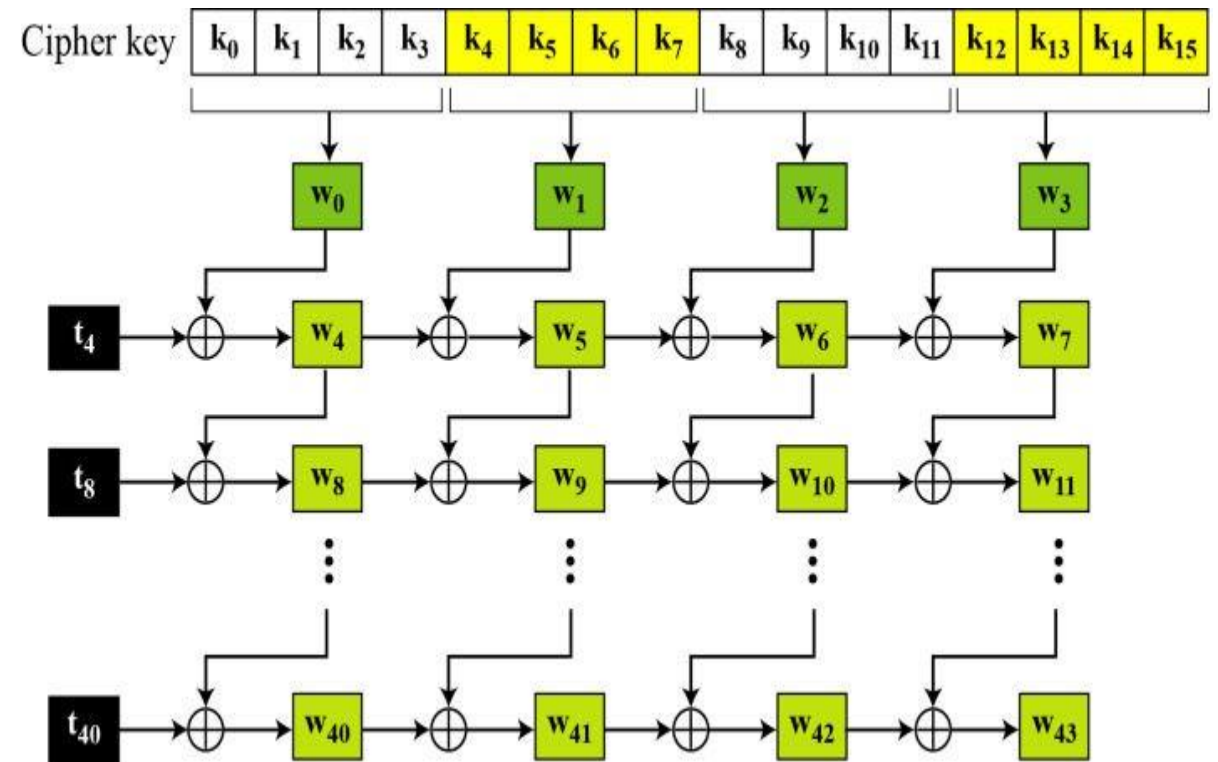
$$t_i = \text{subword}(\text{Rotword}(w_{i-1})) \oplus \text{Rcon}_{i/4}$$

**Rotword** : Applied to only one row

Rotate word routine takes a word as an array of 4bytes and shifts each byte to the left with wrapping.

**Subword** : Applied to 4 bytes.

Substitute word routine takes each byte in the word and substitute another byte for it.



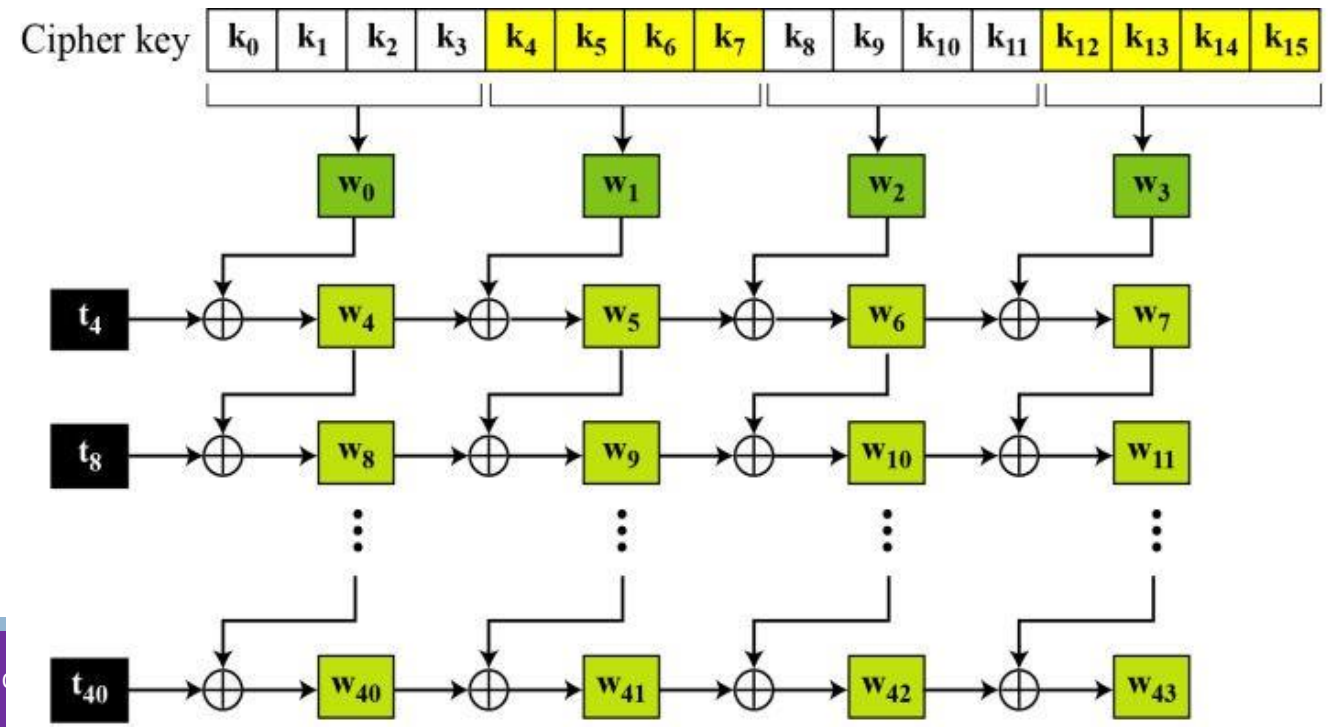


# Key Expansion

$$t_i = \text{subword}(\text{Rotword}(w_{i-1})) \oplus \text{Rcon}_{i/4}$$

Rcon : Round constant is a 4byte value in which the rightmost 3bytes are always zero

Round	Constant (RCon)	Round	Constant (RCon)
1	( <u>01</u> 00 00 00) <sub>16</sub>	6	( <u>20</u> 00 00 00) <sub>16</sub>
2	( <u>02</u> 00 00 00) <sub>16</sub>	7	( <u>40</u> 00 00 00) <sub>16</sub>
3	( <u>04</u> 00 00 00) <sub>16</sub>	8	( <u>80</u> 00 00 00) <sub>16</sub>
4	( <u>08</u> 00 00 00) <sub>16</sub>	9	( <u>1B</u> 00 00 00) <sub>16</sub>
5	( <u>10</u> 00 00 00) <sub>16</sub>	10	( <u>36</u> 00 00 00) <sub>16</sub>





# Key Expansion

The key-expansion routine can either use the table when calculating the words or use the GF(2<sup>8</sup>) field to calculate the leftmost byte dynamically, as shown below

RC <sub>1</sub>	→ $x^{1-1}$	= $x^0$	mod <i>prime</i>	= 1	→ 00000001	→ 01 <sub>16</sub>
RC <sub>2</sub>	→ $x^{2-1}$	= $x^1$	mod <i>prime</i>	= $x$	→ 00000010	→ 02 <sub>16</sub>
RC <sub>3</sub>	→ $x^{3-1}$	= $x^2$	mod <i>prime</i>	= $x^2$	→ 00000100	→ 04 <sub>16</sub>
RC <sub>4</sub>	→ $x^{4-1}$	= $x^3$	mod <i>prime</i>	= $x^3$	→ 00001000	→ 08 <sub>16</sub>
RC <sub>5</sub>	→ $x^{5-1}$	= $x^4$	mod <i>prime</i>	= $x^4$	→ 00010000	→ 10 <sub>16</sub>
RC <sub>6</sub>	→ $x^{6-1}$	= $x^5$	mod <i>prime</i>	= $x^5$	→ 00100000	→ 20 <sub>16</sub>
RC <sub>7</sub>	→ $x^{7-1}$	= $x^6$	mod <i>prime</i>	= $x^6$	→ 01000000	→ 40 <sub>16</sub>
RC <sub>8</sub>	→ $x^{8-1}$	= $x^7$	mod <i>prime</i>	= $x^7$	→ 10000000	→ 80 <sub>16</sub>
RC <sub>9</sub>	→ $x^{9-1}$	= $x^8$	mod <i>prime</i>	= $x^4 + x^3 + x + 1$	→ 00011011	→ 1B <sub>16</sub>
RC <sub>10</sub>	→ $x^{10-1}$	= $x^9$	mod <i>prime</i>	= $x^5 + x^4 + x^2 + x$	→ 00110110	→ 36 <sub>16</sub>

# Key Expansion

## Key Expansion in AES-128 - Algorithm

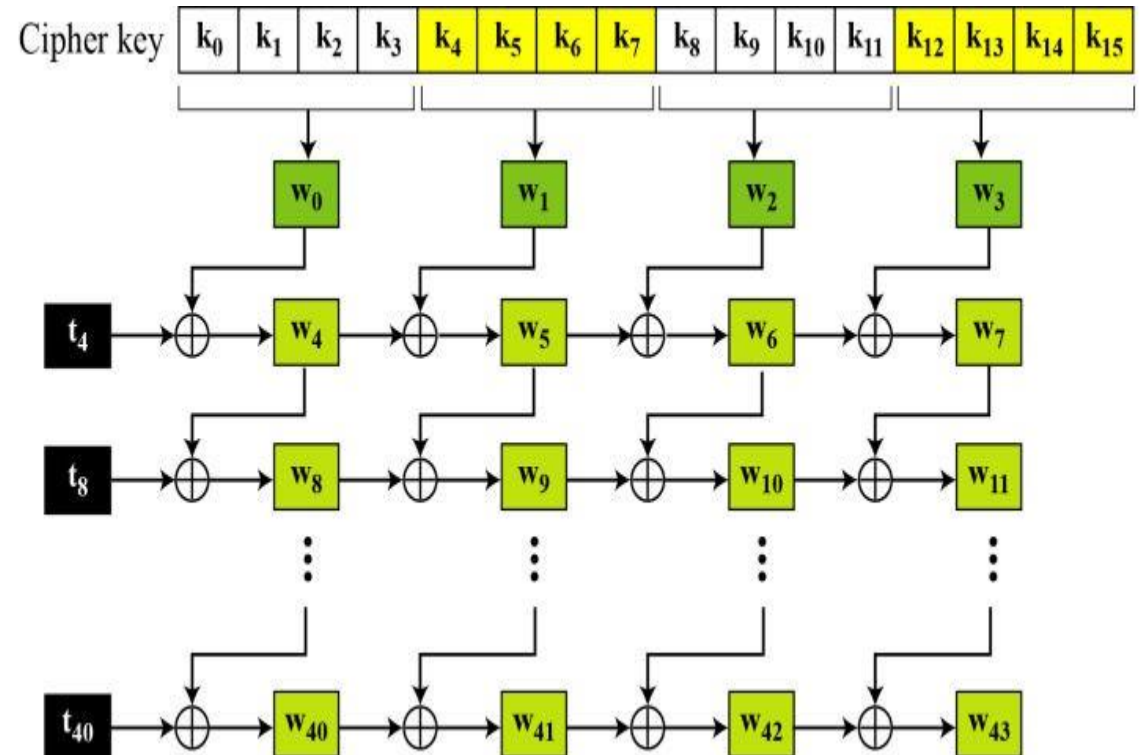
```
KeyExpansion ([key0 to key15], [w0 to w43])  
{  
    for (i = 0 to 3)  
        wi ← key4i + key4i+1 + key4i+2 + key4i+3  
  
    for (i = 4 to 43)  
    {  
        if (i mod 4 ≠ 0)    wi ← wi-1 + wi-4  
        else  
        {  
            t ← SubWord (RotWord (wi-1)) ⊕ RConi/4  
            wi ← t + wi-4  
        }  
    }  
}
```

# Key Expansion

Table 7.5 shows how the keys for each round are calculated assuming that the 128-bit cipher key agreed upon by Alice and Bob is  $(24\ 75\ A2\ B3\ 34\ 75\ 56\ 88\ 31\ E2\ 12\ 00\ 13\ AA\ 54\ 87)_{16}$ .

**Table 7.5** Key expansion example

Round	Values of $t$ 's	First word in the round	Second word in the round	Third word in the round	Fourth word in the round
—		$w_{00} = 2475A2B3$	$w_{01} = 34755688$	$w_{02} = 31E21200$	$w_{03} = 13AA5487$
1	AD20177D	$w_{04} = 8955B5CE$	$w_{05} = BD20E346$	$w_{06} = 8CC2F146$	$w_{07} = 9F68A5C1$
2	470678DB	$w_{08} = CE53CD15$	$w_{09} = 73732E53$	$w_{10} = FFB1DF15$	$w_{11} = 60D97AD4$
3	31DA48D0	$w_{12} = FF8985C5$	$w_{13} = 8CFAAB96$	$w_{14} = 734B7483$	$w_{15} = 2475A2B3$
4	47AB5B7D	$w_{16} = B822deb8$	$w_{17} = 34D8752E$	$w_{18} = 479301AD$	$w_{19} = 54010FFA$
5	6C762D20	$w_{20} = D454F398$	$w_{21} = E08C86B6$	$w_{22} = A71F871B$	$w_{23} = F31E88E1$
6	52C4F80D	$w_{24} = 86900B95$	$w_{25} = 661C8D23$	$w_{26} = C1030A38$	$w_{27} = 321D82D9$
7	E4133523	$w_{28} = 62833EB6$	$w_{29} = 049FB395$	$w_{30} = C59CB9AD$	$w_{31} = F7813B74$
8	8CE29268	$w_{32} = EE61ACDE$	$w_{33} = EAFE1F4B$	$w_{34} = 2F62A6E6$	$w_{35} = D8E39D92$
9	0A5E4F61	$w_{36} = E43FE3BF$	$w_{37} = 0EC1FCF4$	$w_{38} = 21A35A12$	$w_{39} = F940C780$
10	3FC6CD99	$w_{40} = DBF92E26$	$w_{41} = D538D2D2$	$w_{42} = F49B88C0$	$w_{43} = 0DDB4F40$



# Key Expansion

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Round	Constant (RCon)	Round	Constant (RCon)
1	( <u>01</u> 00 00 00) <sub>16</sub>	6	( <u>20</u> 00 00 00) <sub>16</sub>
2	( <u>02</u> 00 00 00) <sub>16</sub>	7	( <u>40</u> 00 00 00) <sub>16</sub>
3	( <u>04</u> 00 00 00) <sub>16</sub>	8	( <u>80</u> 00 00 00) <sub>16</sub>
4	( <u>08</u> 00 00 00) <sub>16</sub>	9	( <u>1B</u> 00 00 00) <sub>16</sub>
5	( <u>10</u> 00 00 00) <sub>16</sub>	10	( <u>36</u> 00 00 00) <sub>16</sub>

$$t_i = \text{subword}(\text{Rotword}(w_{i-1})) \oplus \text{Rcon}_{i/4}$$

$$t_4 = \text{subword}(\text{Rotword}(w_{4-1})) \oplus \text{Rcon}_{4/4}$$

$$t_4 = \text{subword}(\text{Rotword}(w_3)) \oplus \text{Rcon}_1$$

$$\text{Rotword}(13AA5487) = AA548713$$

$$\text{Subword}(AA548713) = AC20177D$$

$$t_4 = AC20177D \oplus \text{Rcon}_1$$

$$= AC20177D \oplus 01\ 00\ 00\ 00 \rightarrow AD20177D$$



# Key Expansion –AES 192 and AES 256

Key-expansion algorithms in the AES-192 and AES-256 versions are very similar to the key expansion algorithm in AES-128, with the following differences:

1. In AES-192, the words are generated in groups of six instead of four.
  - a. The cipher key creates the first six words ( $w_0$  to  $w_5$ ).
  - b. If  $i \bmod 6 \neq 0$ ,  $w_i \leftarrow w_{i-1} + w_{i-6}$ ; otherwise,  $w_i \leftarrow t + w_{i-6}$ .
2. In AES-256, the words are generated in groups of eight instead of four.
  - a. The cipher key creates the first eight words ( $w_0$  to  $w_7$ ).
  - b. If  $i \bmod 8 \neq 0$ ,  $w_i \leftarrow w_{i-1} + w_{i-8}$ ; otherwise,  $w_i \leftarrow t + w_{i-8}$ .
  - c. If  $i \bmod 4 = 0$ , but  $i \bmod 8 \neq 0$ , then  $w_i = \text{SubWord}(w_{i-1}) + w_{i-8}$ .

# Key expansion analysis

The key-expansion mechanism in AES has been designed to provide several features that thwart the cryptanalyst.

1. Even if Eve knows only part of the cipher key or the values of the words in some round keys, she still needs to find the rest of the cipher key before she can find all round keys. This is because of the nonlinearity produced by SubWord transformation in the key-expansion process.
2. Two different cipher keys, no matter how similar to each other, produce two expansions that differ in at least a few rounds.
3. Each bit of the cipher key is diffused into several rounds. For example, changing a single bit in the cipher key, will change some bits in several rounds.
4. The use of the constants, the RCons, removes any symmetry that may have been created by the other transformations.
5. There are no serious weak keys in AES, unlike in DES.
6. The key-expansion process can be easily implemented on all platforms.
7. The key-expansion routine can be implemented without storing a single table; all calculations can be done using the  $GF(2^8)$  and  $GF(2)$  fields.

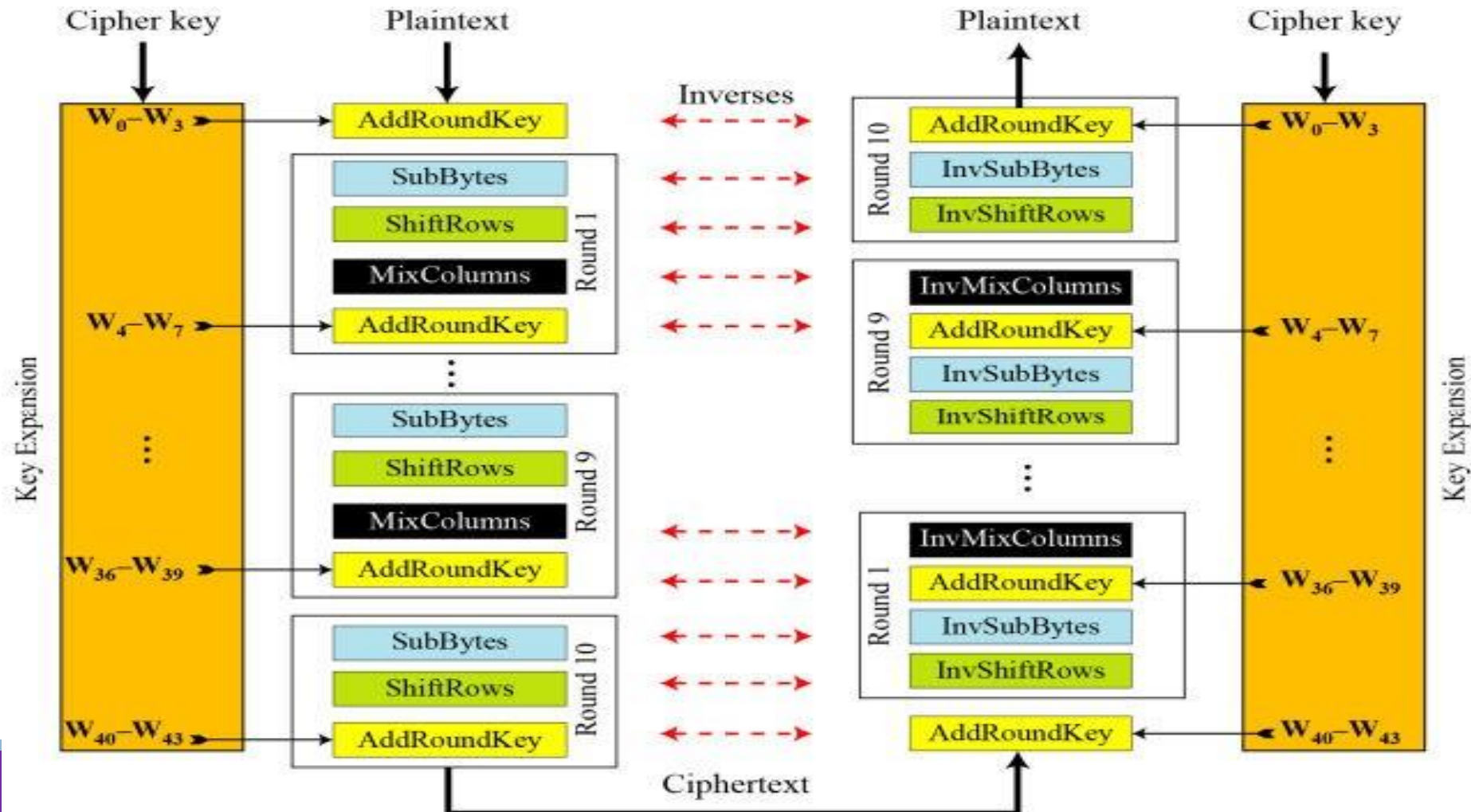
# The AES Ciphers

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- AES uses four types of transformations for encryption and decryption.
- Encryption algorithm is referred to as the cipher
- Decryption algorithm as the inverse cipher.
- Two different design for implementation
  - Original Design
  - Alternative Design



# The AES Ciphers – Original design





# The AES Ciphers –Original design

*The code for the AES-128 version of this design is shown in Algorithm*

*Pseudocode for cipher in the original design*

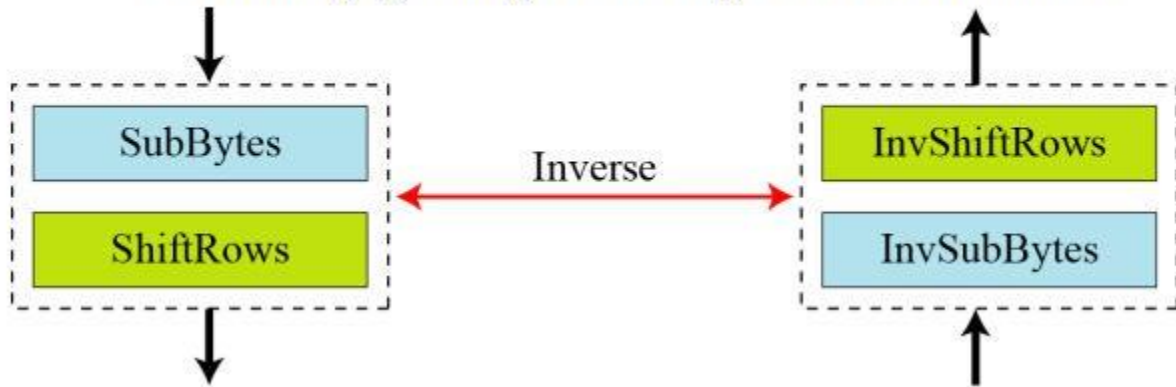
```
Cipher (InBlock [16], OutBlock[16], w[0 ... 43])
{
    BlockToState (InBlock, S)

    S ← AddRoundKey (S, w[0...3])
    for (round = 1 to 10)
    {
        S ← SubBytes (S)
        S ← ShiftRows (S)
        if (round ≠ 10) S ← MixColumns (S)
        S ← AddRoundKey (S, w[4 × round, 4 × round + 3])
    }

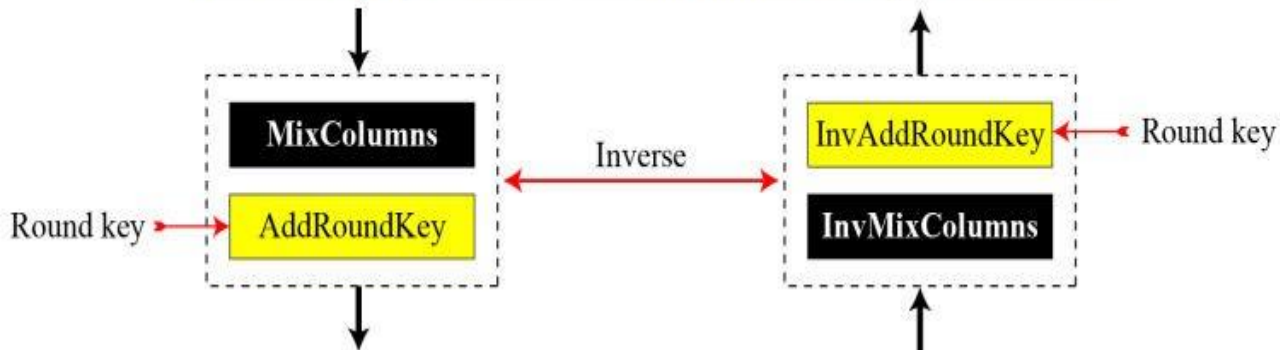
    StateToBlock (S, OutBlock);
}
```

# The AES Ciphers –Alternative Design

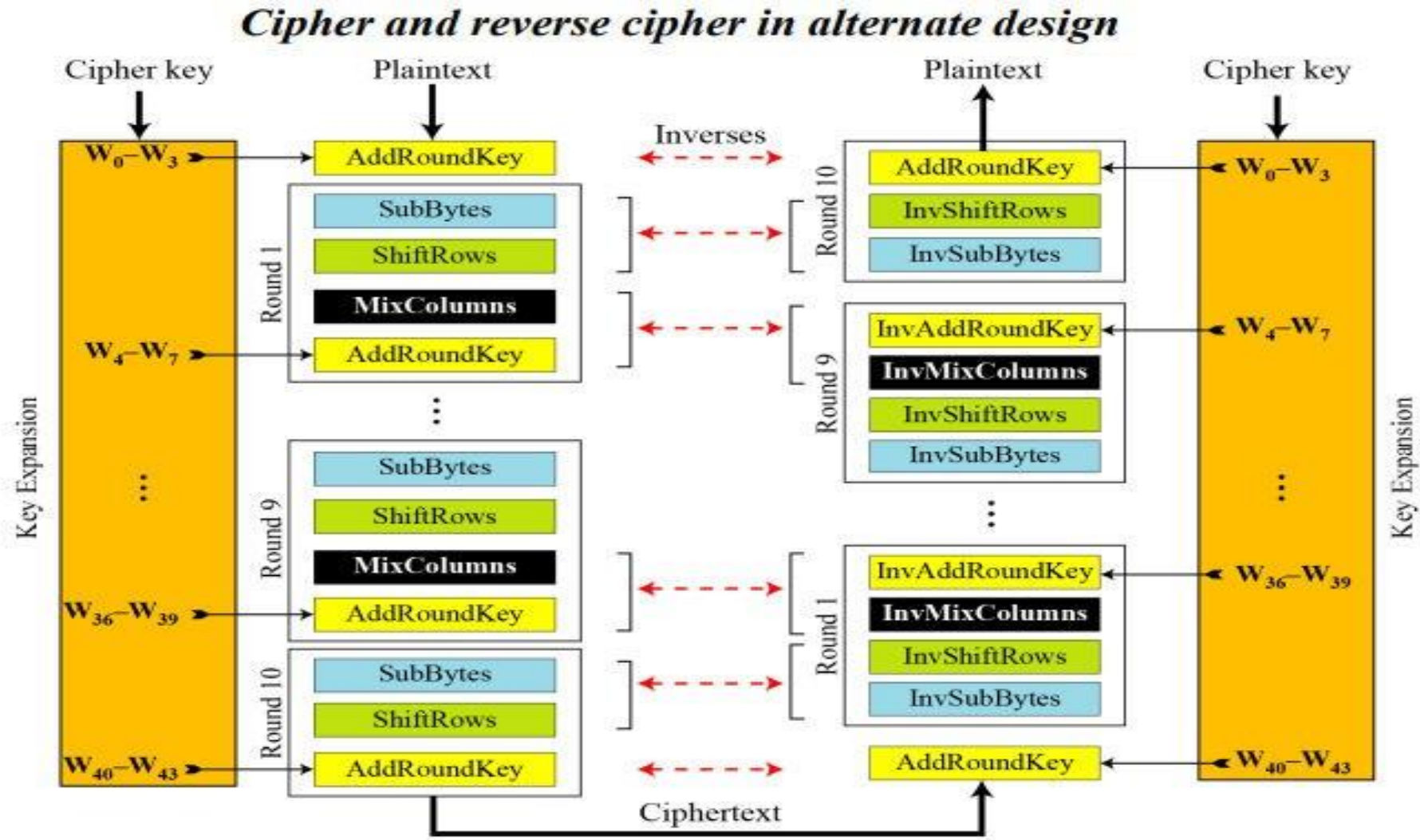
*Invertibility of SubBytes and ShiftRows combinations*



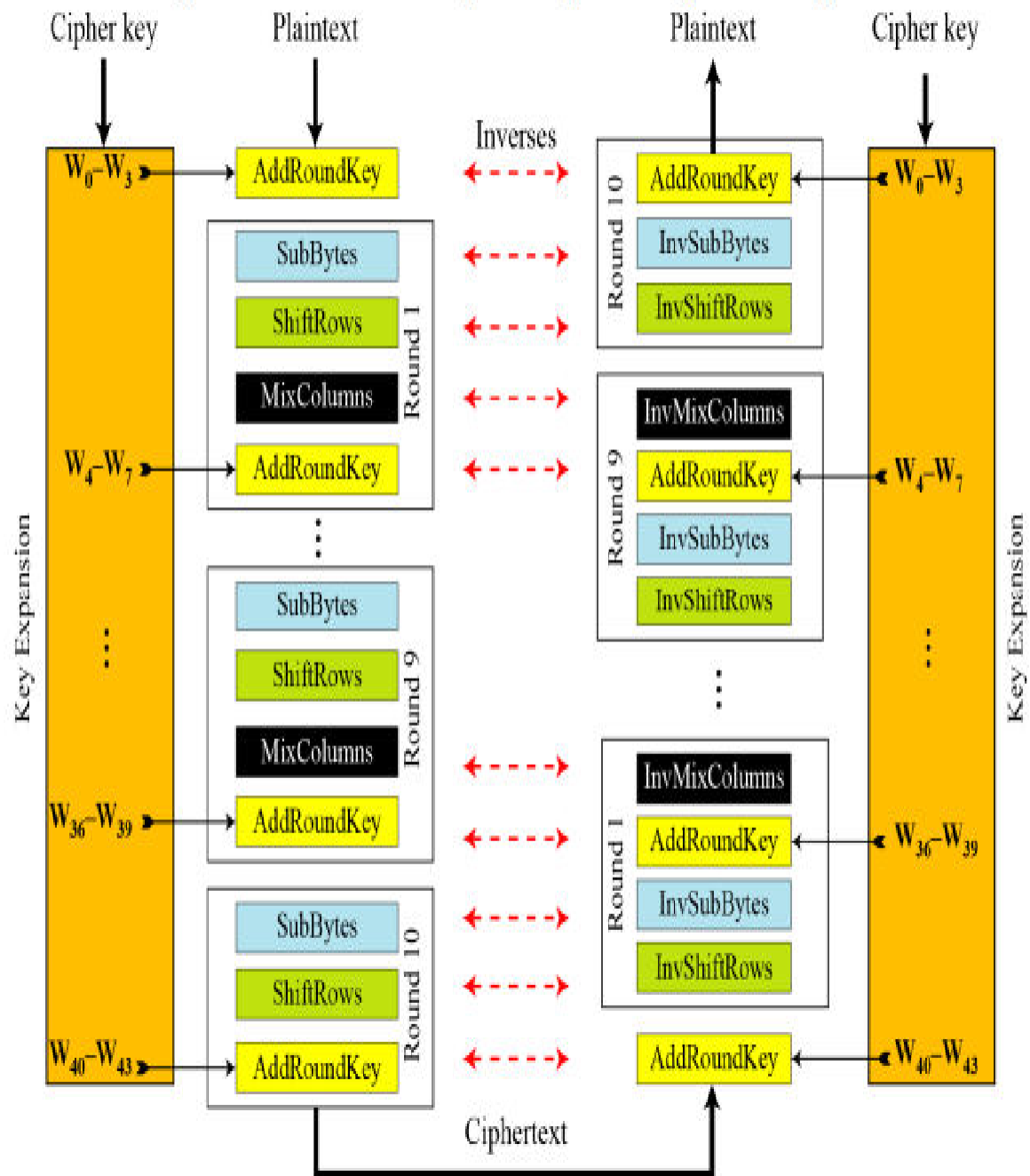
*Invertibility of MixColumns and AddRoundKey combination*



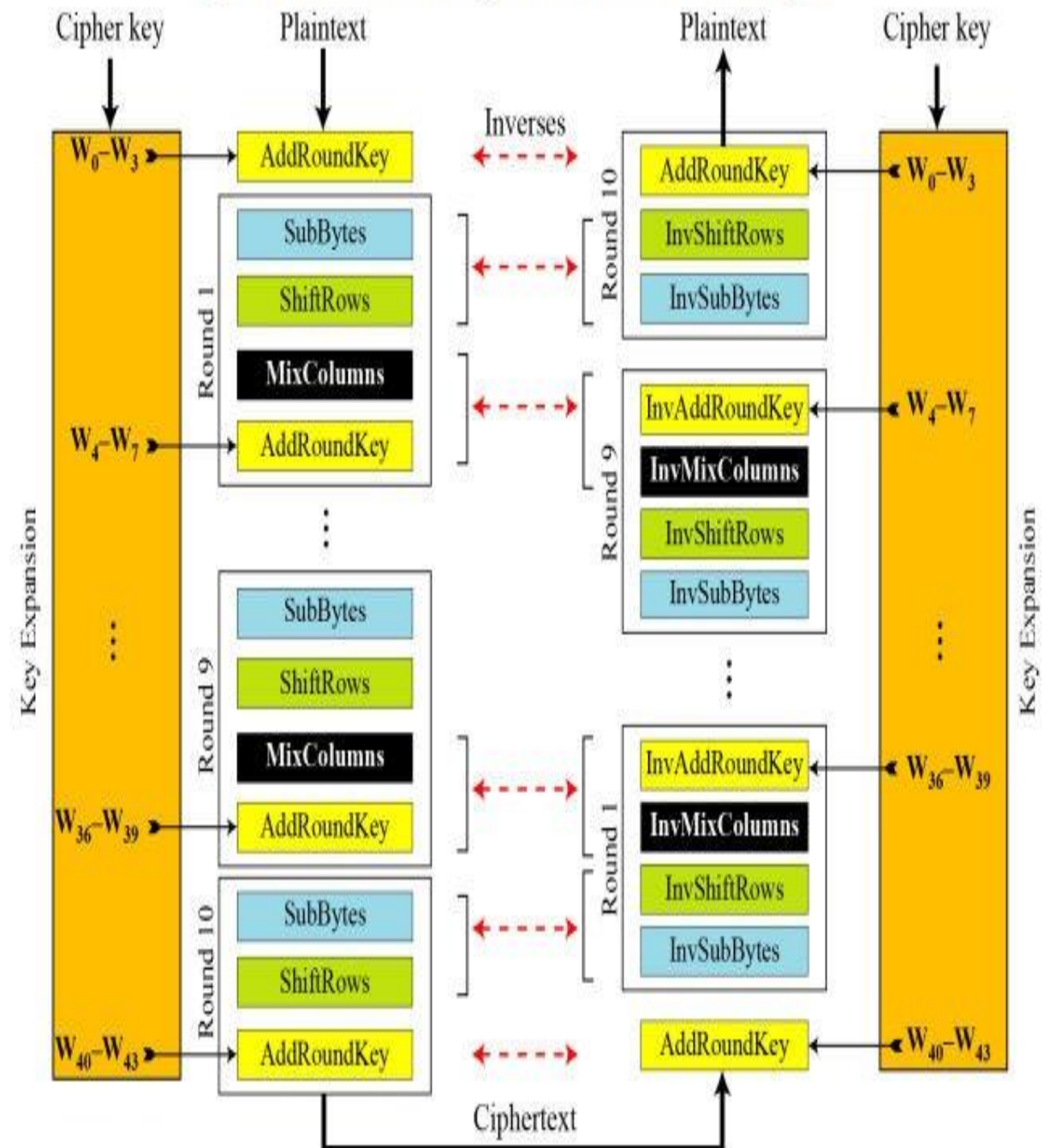
# The AES Ciphers –Alternative Design



## Ciphers and inverse ciphers of the original design



## Cipher and reverse cipher in alternate design



# Analysis of AES

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This section is a brief review of the three characteristics of AES.

- Security
- Implementation
- Simplicity and Cost

# Analysis of AES

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## Security

- Brute-Force Attack :AES is definitely more secure than DES due to the larger-size key.
- Statistical Attacks :Numerous tests have failed to do statistical analysis of the ciphertext.
- Differential and Linear Attacks :There are no differential and linear attacks on AES as yet.



# Analysis of AES

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## Implementation

AES can be implemented in software, hardware, and firmware.

The implementation can use table lookup process or routines that use a well-defined algebraic structure.

# Analysis of AES

---

## Simplicity and Cost

The algorithms used in AES are so simple that they can be easily implemented using cheap processors and a minimum amount of memory.