

Playlist Link:

<https://www.youtube.com/playlist?list=PL1QH9gyQXfguPNDTsnG90W2kBDQpYLDQr>

Transition Diagrams:

Relational Ops:

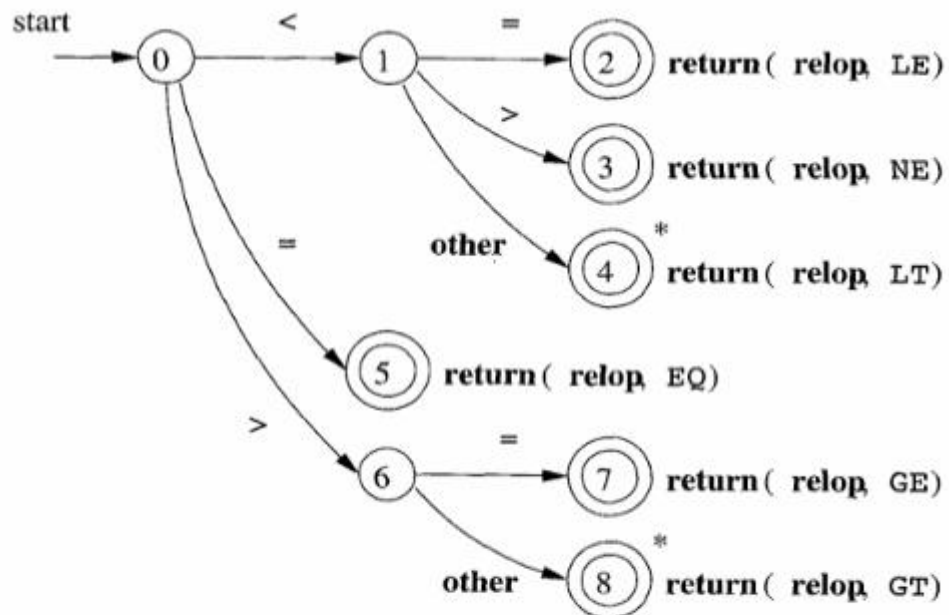
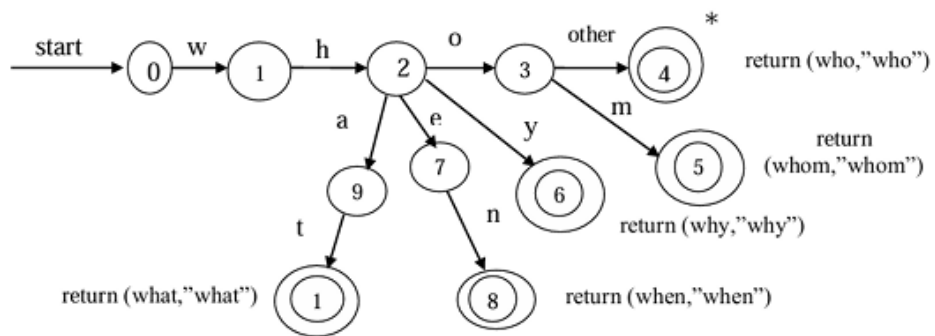
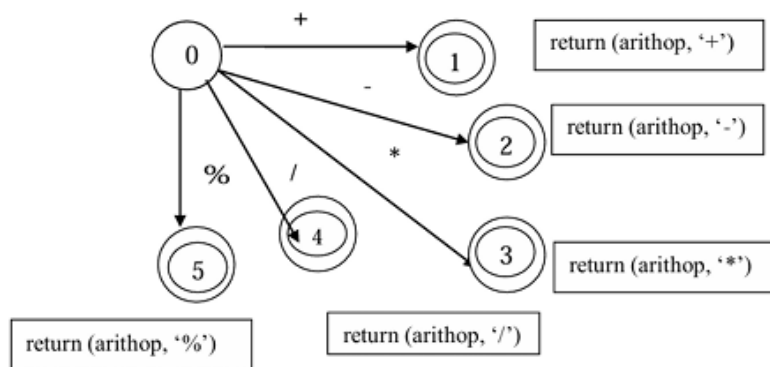


Figure 3.13: Transition diagram for **relop**

Arithmetic Ops:



Arithmetic operators



Count Tokens:

Ex 1:

```
int main ( ) → 4
{
    int i;      5
                8
    for ( i = 0; i < 5; i++ ) 2 1
    {
        int i = 102; 2 2
                    2 7
        printf ( " %d the value of i: ", i )
        i++; 3 7
    }
    return 0; 4 1
}
```

(42)

```
main ( ) ⇒ 3
{
    x = a + b * c; 1 2
    int x, a, b, c; 2 1
    y = x + a; 2 7
}
```

(28)

```

    main() => 3
    { ✓      4
        int x = 10, y <= 10; (13)
        printf("%d %d %d", x); 20
    } (21)

```

```

    main() (4)
    {
        char *c = "string"; 10
        float b = 100.74; 15
        char d = 'e'; 20
        int f = 200; 25
        in t f = 200; 31
        in /* comment */ t f = 200; 37
        ch ar d = 'e'; 37+6=43
        ch /* comment */ ar d = 'e';
    }

```

Eliminating Left Recursion:

Left = $\{ \beta, \beta\alpha, \beta\alpha^2 \}$

$$\underline{A} \rightarrow \underline{A}\alpha \mid \beta$$

\Downarrow

$$\boxed{A \rightarrow \beta A'}$$

$$A' \rightarrow \epsilon \mid \alpha A' \Rightarrow \alpha^*$$

$S \rightarrow \underline{S}(\underline{\beta} \mid \underline{S} \underline{\alpha} \underline{S}) \mid \underline{\beta}$

\underline{A} \underline{A} α β

$S \rightarrow \beta S'$

$S' \rightarrow \epsilon \mid \beta S S S'$

$E \rightarrow \underline{E} \underline{+T} \mid \underline{T}$

\underline{A} \underline{A} α β

$E \rightarrow T E'$

$E' \rightarrow \epsilon \mid + T E'$

Eliminating Left Factoring:

Left factoring.

$\checkmark ND \Rightarrow Det$

$$A \rightarrow \underline{\alpha} \beta_1 \mid \underline{\alpha} \beta_2 \mid \underline{\alpha} \beta_3 \mid \alpha \beta_4$$

Common prefix

$A \rightarrow \alpha A'$

$A' \rightarrow \beta_1 \mid \beta_2 \mid \beta_3 \mid \beta_4$

$S \rightarrow \underline{\beta} \underline{S} \underline{S'} \mid a$

$S' \rightarrow \epsilon \mid es$

$E \rightarrow b$

$S \rightarrow \underline{\beta} \underline{S} \underline{S'} \mid \underline{\beta} \underline{S} \underline{S'} \underline{es} \mid a$

$E \rightarrow b$

$A \rightarrow \alpha \beta_1$

$B \rightarrow \alpha \beta_2$

$S \rightarrow \underline{b} \underline{S} (\underline{S} \underline{a} \underline{a} \underline{S}) \mid \underline{b} \underline{S} \underline{S} \underline{a} \underline{S} \underline{b} \mid \underline{b} \underline{S} \underline{b} \mid a$

$S \rightarrow \underline{b} \underline{S} \underline{S} \underline{S'} \mid a$

$S' \rightarrow \underline{S} \underline{a} \underline{a} \underline{S} \mid \underline{S} \underline{a} \underline{S} \underline{b} \mid b$

$S' \rightarrow S a S'' \mid b$

$S'' \rightarrow a S \mid S b$

$S \rightarrow \underline{a} (\underline{S} \underline{S} \underline{b} \underline{S}) \mid \underline{a} \underline{S} \underline{a} \underline{S} \underline{b} \mid \underline{a} \underline{b} \underline{b} \mid b$

① $S \rightarrow a S' \mid b$

$S' \rightarrow \underline{S} \underline{S} \underline{b} \underline{S} \mid \underline{S} \underline{a} \underline{S} \underline{b} \mid b$

② $S' \rightarrow S S'' \mid b b$

③ $S'' \rightarrow S b S \mid a S b$

$$S \rightarrow \underline{a} \mid \underline{a}b \mid \underline{a}bc \mid \underline{a}bcd$$

$$S \rightarrow aS'$$

$$x S' \rightarrow \epsilon \mid \underline{b} \mid \underline{b}c \mid \underline{b}cd$$

$$S' \rightarrow \epsilon \mid bS''$$

$$x S'' \rightarrow \epsilon \mid \underline{c} \mid \underline{c}d$$

$$S'' \rightarrow \epsilon \mid cS'''$$

$$S''' \rightarrow \epsilon \mid d$$

First and Follow Rules:

First

First(A) gives set of terminals that begins in all strings derived from A.

Follow

Follow(A) gives set of all terminals that follow immediately to the right of A.

1. if $A \rightarrow a\alpha$, $\alpha \in (V \cup T)^*$
 $\text{First}(A) = \{a\}$
2. if $A \rightarrow \epsilon$ then $\text{First}(A) = \{\epsilon\}$
3. if $A \rightarrow BC$ then
 $\rightarrow \text{First}(A) = \text{First}(B)$
 if $\text{First}(B)$ doesn't contain ϵ .
 $\rightarrow \text{First}(A) = \text{First}(B) \cup \text{First}(C)$
 if $\text{First}(B)$ contains ϵ .

1. if S is start symbol then $\text{Follow}(S) = \{\$ \}$.
2. if $A \rightarrow \alpha B \beta$, then $\text{Follow}(B) = \text{First}(\beta)$
 if $\text{First}(\beta)$ doesn't contain ϵ .
3. if $A \rightarrow \alpha B$, then $\text{Follow}(B) = \text{Follow}(A)$.

Ex 1:

$S \rightarrow a B D h$	First	Follow
$B \rightarrow c C$	$\{a\}$	$\{\$, \epsilon\}$
$C \rightarrow b C \mid \epsilon$	$\{c\}$	$\{g, f, h\}$
$D \rightarrow E F$	$\{b, \epsilon\}$	$\{g, f, h\}$
$E \rightarrow g \mid \epsilon$	$\{g, f, \epsilon\}$	$\{h\}$
$F \rightarrow f \mid \epsilon$	$\{g, \epsilon\}$	$\{f, h\}$
	$\{f, \epsilon\}$	$\{h\}$

Ex 2:

$\overleftarrow{E} \rightarrow TE'$	First $\{id, c\}$	Follow $\{\$, \rangle\}$
$E' \rightarrow \epsilon \mid +TE'$	$\{\epsilon, +\}$	$\{\$, \rangle\}$
$\overleftarrow{T} \rightarrow \underline{F}T'$	$\{id, c\}$	$\{+, \$, \rangle\}$
$T' \rightarrow \epsilon \mid \times FT'$	$\{\epsilon, \times\}$	$\{+, \$, \rangle\}$
$F \rightarrow \underline{id} \mid (E)$	$\{id, c\}$	$\{\times, +, \$, \rangle\}$
$T \rightarrow c(T)$		

Ex 3:

$S \rightarrow Bb \mid Cd$	First $\{a, b, c, d\}$	Follow $\{\$\}$
$B \rightarrow aB \mid \epsilon$	$\{a, \epsilon\}$	$\{b\}$
$C \rightarrow cC \mid \epsilon$	$\{c, \epsilon\}$	$\{d\}$

Ex 4:

$S \rightarrow \underline{A}a\underline{A}b \mid BbBa$	First $\{a, b\}$	Follow $\{\$\}$
$A \rightarrow \epsilon$	$\{\epsilon\}$	$\{a, b\}$
$B \rightarrow \epsilon$	$\{\epsilon\}$	$\{b, a\}$

LL(1):

STEPS:

1. Find first and follow of all
2. Construct a Matrix with Variables on Left and Terminals on Top
3. For each individual broken production $A \rightarrow a$, check if the $\text{first}(a)$ contains null, if no then fill the production under $M[A, \text{first}(a)]$
4. If yes, fill it in $M[A, \text{follow}(A)]$
5. Now for the stack part, enter the $\$$ (final state).
6. Compare against input string's pointer alphabet, check the production from matrix M and replace that top of the sstack state with the reversed order of the production (because it's a Stack). Increment the I/S Ptr.
7. If the top of the stack is a terminal and matches the input string's pointer, POP.
8. Repeat until $\$$ is left.

LR(0):

1. Create a new augmented grammar $S' \rightarrow S$
2. Find Closure of the new AG.
3. Closure is basically adding a $.$ Ex: $S' \rightarrow .S$, and since the $.$ has a State again, add the productions of the state next to $.$ and keep repeating until you can no longer do it.
4. Apply Goto(I_0 , all possible), for each and construct the DFA state diagram. GOTO is moving the $.$ one step further and finding closure on that new state.
5. After State diagram, construct a Matrix M with the numbers of state on the left and the Headers Action (containing terminals) and Goto (containing Variables (state: S, T, A, B , etc))
6. Now using the state Diagram, for each LR Item I_0, I_1, I_2, \dots , fill the action side with Shifts if $I_0 \rightarrow I_1$ is via a , then under $M[I_0, a]$ fill S_1 .
7. Fill the Goto side with the state number directly, ex: If $I_0 \rightarrow I_2$ is via A , then under $M[I_0, A]$, fill 2
8. If it's the final Item, then fill all the actions, with the no. of production (you can label each individual production as 1,2,3,etc) as R1 etc

Ex: if the state I6 is final item, and it contains A->ab., and it is 3rd production, then fill all actions with R3.

9. Now for the stack shit, fill the stack with 0 .

10. The I/Str ptr is at first position, check the state over the M[0,ptr] if its a Shift, then push the PTR alphabet first and then the Shift Nukmber in matrix. Increment PTR and continue.

11. If its a reduce operation, then u should find the length of the No of Reduce production's and POP those no of elements. Add the Left hand (State) of the production to the stack. And now find the transition of the added state with the Number below it.

12. Repeat until u find Accept.

SLR(1):

1. Same as LR0 until the state diagram is being constructed.

2. While adding the Reduce in Matrix, make sure it gets added only in the positions where the Follow(the reduced production's left State) is present. Not the entire action row for that state.

3. Stack shit same as LR0.

CALR(1):

1. A new LR(0) iTem, it will have the Augmented Grammar + a Look ahead symbol. Ex: S'-> . S, \$ Here \$ is look ahead symbol, comma ',' is a separator.

2. The look ahead symbol while calculating closure is done as follows.... The first(next elements following the newly added Closure States), will be the new look ahead for that transition.

Ex: S'-> .S, \$

Next the follow of the elements to the next of the . and the state i.e First(\$)

S->.AA, \$

now next we need to add A's production (assume $A \rightarrow a \mid b$), here since we have A after .A, we need to calculate $\text{first}(A\$)$, which is $a \mid b$.

$A \rightarrow .ab, a \mid b$.

If there is nothing then add \$

3. now continue the same, like that for LR0, but when adding the reduce in actions for final elements, add it to the elements in the LOOK AHEAD of the Final state only.

4. Same stack shit.

LALR(1):

Steps:

1. Same as CALR 1
2. Merge the states which have the same LR(0) items (ignore Look ahead symbols).
3. Basically if 4th and 6th have same LR0 items, then replace them by a new 4,6th state, write r4 r6 as r46 and so on.

Parsers

Non Recursive Descent Parser (Top-Down Parser):

LL(1) (Left-right Leftmost 1 by 1 character read):

Ex 1:

Non Recursive Descent parser.

Predictive parser or LL(1)

	First	Follow	M	id	+	*	()	\$
$E \rightarrow TE'$	$\{id, (\}$	$\{ \$,) \}$	E	$E \rightarrow TE'$			$E \rightarrow TE'$		
$E' \rightarrow \epsilon + TE'$	$\{ \epsilon, + \}$	$\{ \$,) \}$	E'						
$T \rightarrow FT'$	$\{id, (\}$	$\{ +, \$,) \}$	T						
$T' \rightarrow \epsilon * FT'$	$\{ \epsilon, * \}$	$\{ +, \$,) \}$	T'						
$F \rightarrow id (E)$	$\{id, (\}$	$\{ *, +, \$,) \}$	F						

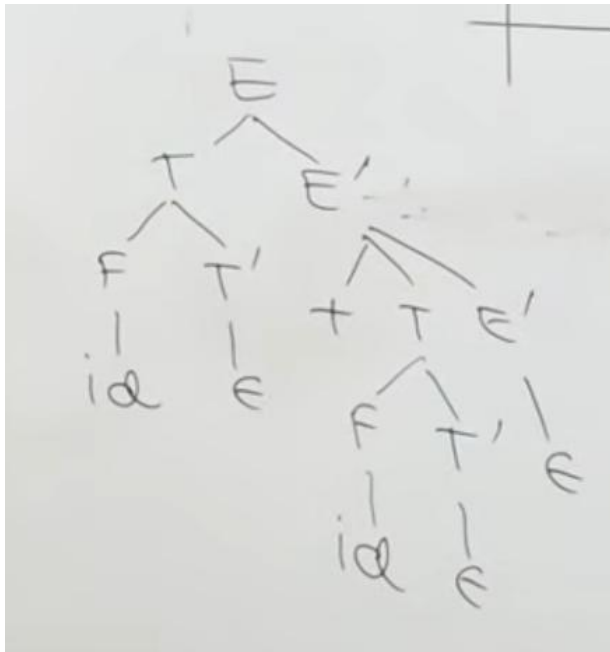
$E \rightarrow TE'$
 $A \quad \alpha \quad id, ($

1. Add $A \rightarrow \alpha$ under $M[A, a]$ where $a \in \text{First}(\alpha)$
2. Add $A \rightarrow \alpha$ under $M[A, a]$ where $a \in \text{Follow}(A)$ if $\text{First}(\alpha)$ contains ϵ .

Non Recursive Descent parser.

Predictive parser or LL(1)

Stack	Input	Production	M	id	+	*	()	\$
\$E	id+id\$	$E \rightarrow TE'$	E	$E \rightarrow TE'$			$E \rightarrow TE'$		
\$E'T	id+id\$	$T \rightarrow FT'$	E'						
\$E'T'F	id+id\$	$F \rightarrow id$	E'		$E' \rightarrow +TE'$			$E' \rightarrow \epsilon$	$E' \rightarrow \epsilon$
\$E'T'id	id+id\$	POP	T	$T \rightarrow FT'$			$T \rightarrow FT'$		
\$E'T'	+id\$	$T' \rightarrow \epsilon$	T'						
\$E'	+id\$	$E' \rightarrow +TE'$	T'		$T' \rightarrow \epsilon$	$T' \rightarrow *FT'$		$T' \rightarrow \epsilon$	$T' \rightarrow \epsilon$
\$E'T+	+id\$	POP	F	$F \rightarrow id$			$F \rightarrow (E)$		
\$E'T	id\$	$T \rightarrow FT'$							
\$E'T'F	id\$	$F \rightarrow id$							
\$E'T'id	id\$	POP							
\$E'T'	\$	$T' \rightarrow \epsilon$							
\$E'	\$	$E' \rightarrow \epsilon$							
\$	\$	Accept							



Ex 2:

	FPast	Follow		a	b	c	f	g	h	\$
$S \rightarrow aBDh$	$\{a\}$	$\{\$ \}$	M							
$\rightarrow cC$	$\{c\}$	$\{g, f, h\}$	S	$S \rightarrow aBDh$						
$\rightarrow bC e$	$\{b, e\}$	$\{g, f, h\}$	B			$B \rightarrow cC$				
$\rightarrow EF$	$\{g, f, e\}$	$\{h\}$	C		$C \rightarrow bC$		$C \rightarrow e$	$C \rightarrow e$	$C \rightarrow e$	
$\rightarrow g e$	$\{g, e\}$	$\{f, h\}$	D				$D \rightarrow EF$	$D \rightarrow EF$	$D \rightarrow EF$	
$F \rightarrow f e$	$\{f, e\}$	$\{h\}$	E				$E \rightarrow e$	$E \rightarrow g$	$E \rightarrow e$	
			F				$F \rightarrow f$		$F \rightarrow e$	

LL(1) parsing Table.

$C \rightarrow e$
 $A \rightarrow \alpha$
 $F(\alpha) = e$
 $F \rightarrow e$

$D \rightarrow EF$
 $D \rightarrow F$
 \downarrow
 $\{g, e\}$
 $\{f, e\}$

Stack	input	Production	M	a	b	c	f	g	h	\$
\$ S	acbh\$	$S \rightarrow aBDh$	S	$S \rightarrow aBDh$						
\$ hDBa	acbh\$	POP	B			$B \rightarrow cC$				
\$ hDB	cbh\$	$B \rightarrow cC$	C		$C \rightarrow bC$		$C \rightarrow \epsilon$	$C \rightarrow \epsilon$	$C \rightarrow \epsilon$	
\$ hDCc	cbh\$	POP	D				$D \rightarrow \epsilon F$	$D \rightarrow \epsilon F$	$D \rightarrow \epsilon F$	
\$ hDC	bh\$	$C \rightarrow bC$	E				$E \rightarrow \epsilon$	$E \rightarrow g$	$E \rightarrow \epsilon$	
\$ hDCb	bh\$	POP	F				$F \rightarrow f$		$F \rightarrow \epsilon$	
\$ hDC	h\$	$C \rightarrow \epsilon$								
\$ hD	h\$	$D \rightarrow \epsilon F$								
\$ hFE	h\$	$E \rightarrow \epsilon$								
\$ hF	h\$	$F \rightarrow \epsilon$								
\$ h	h\$	POP								
\$	\$	Accept								

LL(1) parsing Table.

Fast method: Check whether Grammar is LL(1)

LL(1) Grammar: Each cell $M[A, a]$ has 0 or 1 production.

Non-LL(1) Grammar: At least one cell $M[A, a]$ has 2 or more productions.
This is called a **conflict**.

Slow method (faster if only asked if Grammar is LL(1) or not)

check given Grammar is LL(1) or not.

1. If G doesn't contain ϵ .

$$A \rightarrow \alpha_1 | \alpha_2 | \alpha_3$$

$$\text{First}(\alpha_1) \cap \text{First}(\alpha_2) = \emptyset$$

$$\text{First}(\alpha_2) \cap \text{First}(\alpha_3) = \emptyset$$

$$\text{First}(\alpha_3) \cap \text{First}(\alpha_1) = \emptyset$$

2. If G contains ϵ .

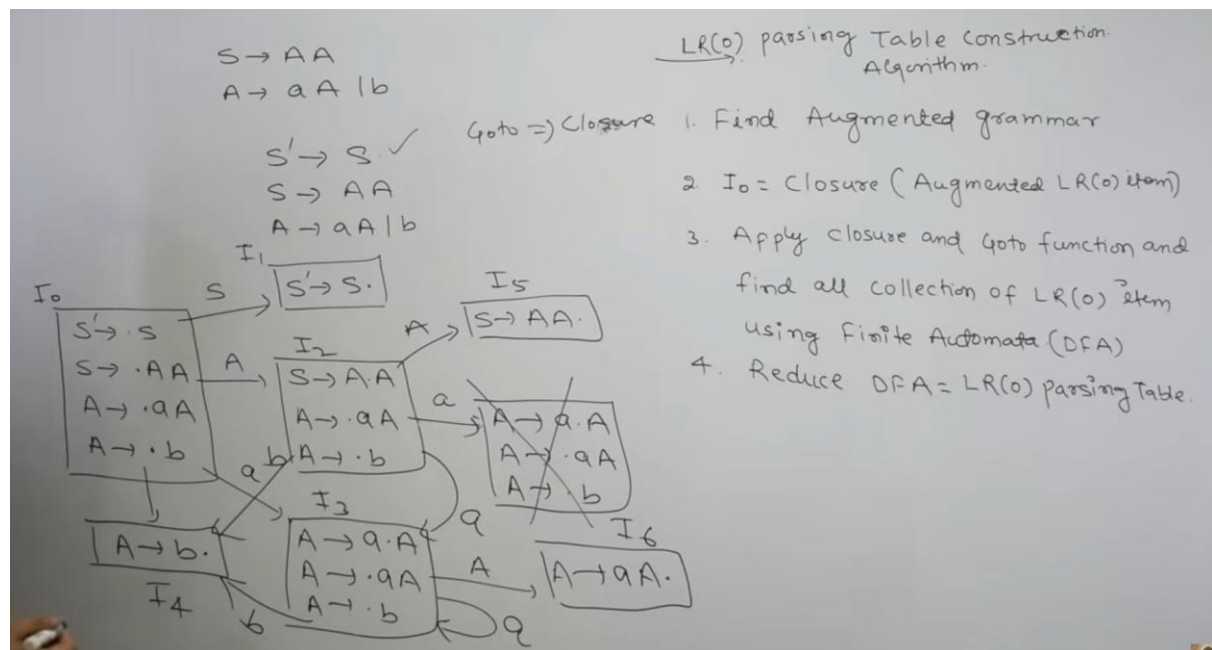
$$A \rightarrow \alpha_1 | \alpha_2 | \epsilon$$

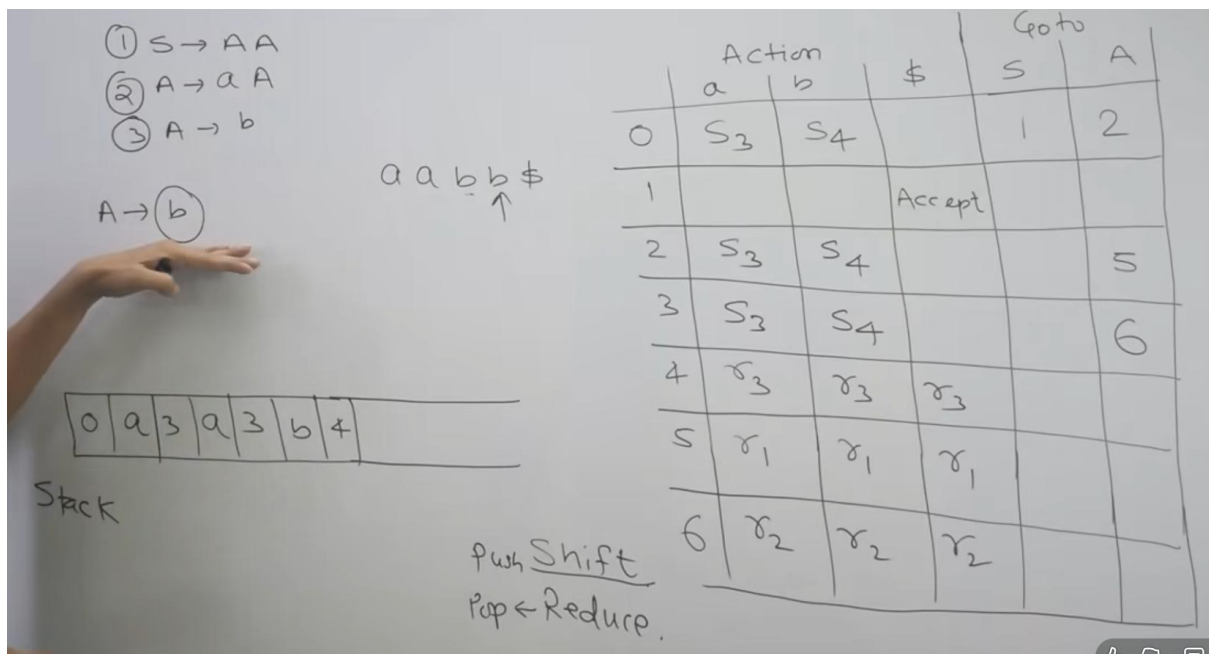
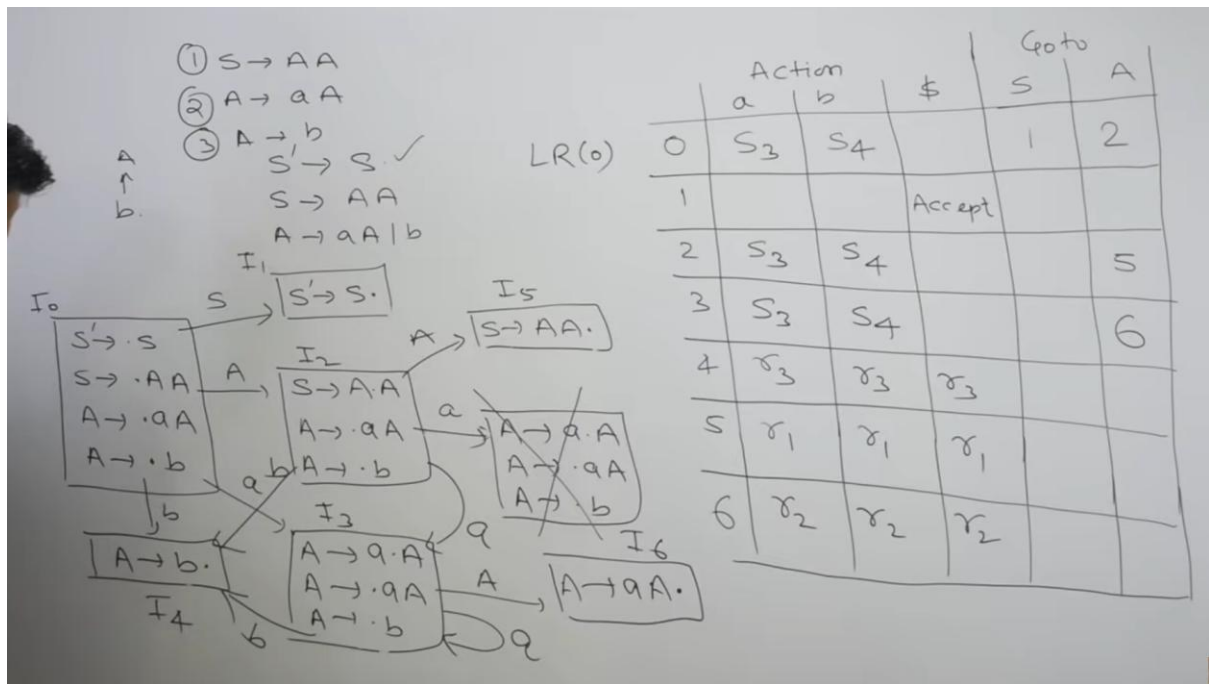
$$\text{First}(\alpha_1) \cap \text{First}(\alpha_2) = \emptyset$$

$$\text{First}(\alpha_1) \cap \text{Follow}(A) = \emptyset$$

$$\text{First}(\alpha_2) \cap \text{Follow}(A) = \emptyset$$

LR(0) (Left to right read, Rightmost Derivation in Reverse order):

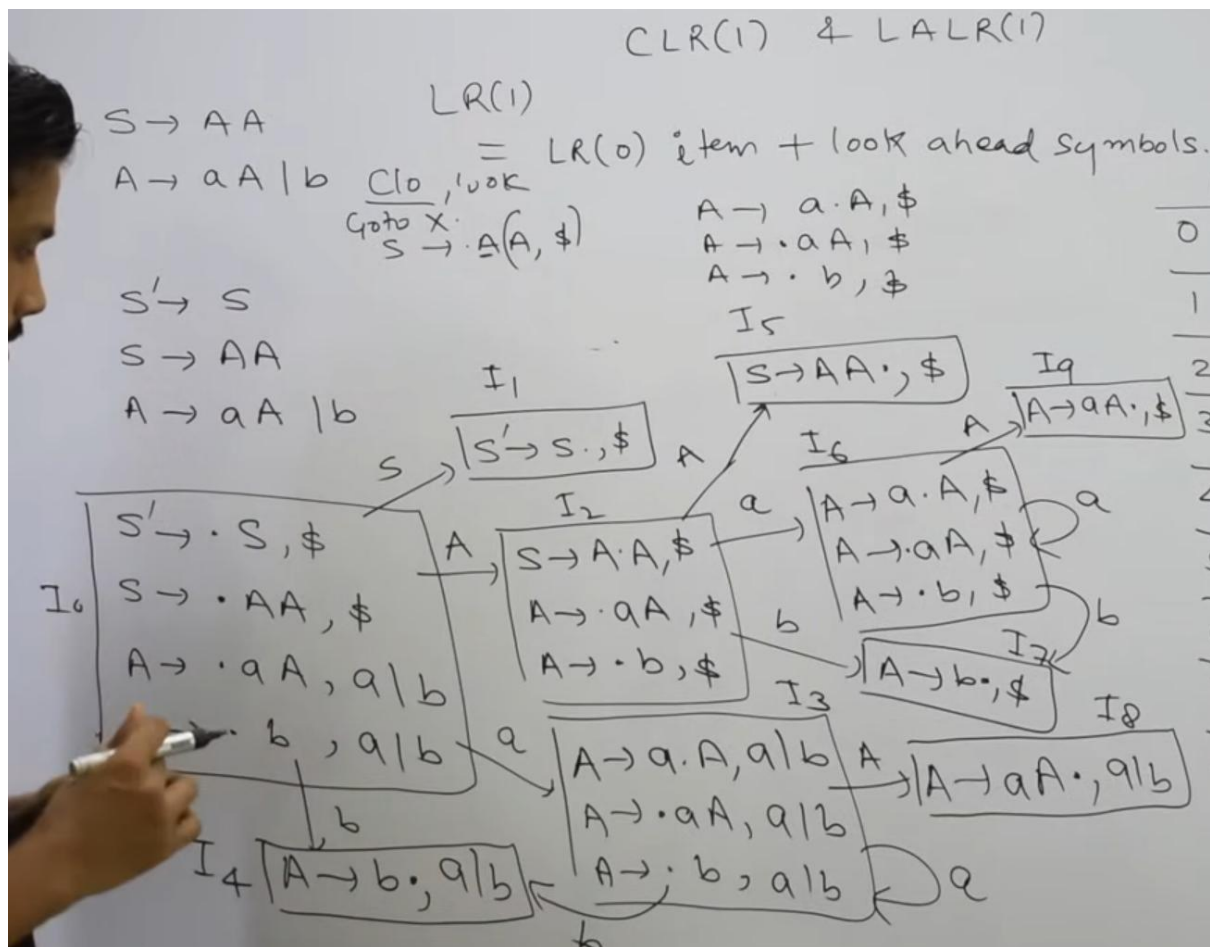




CALR(1) Canonical Form Items:

LR(0) Item + Look Ahead Symbols (Follow of everything ahead of .X)

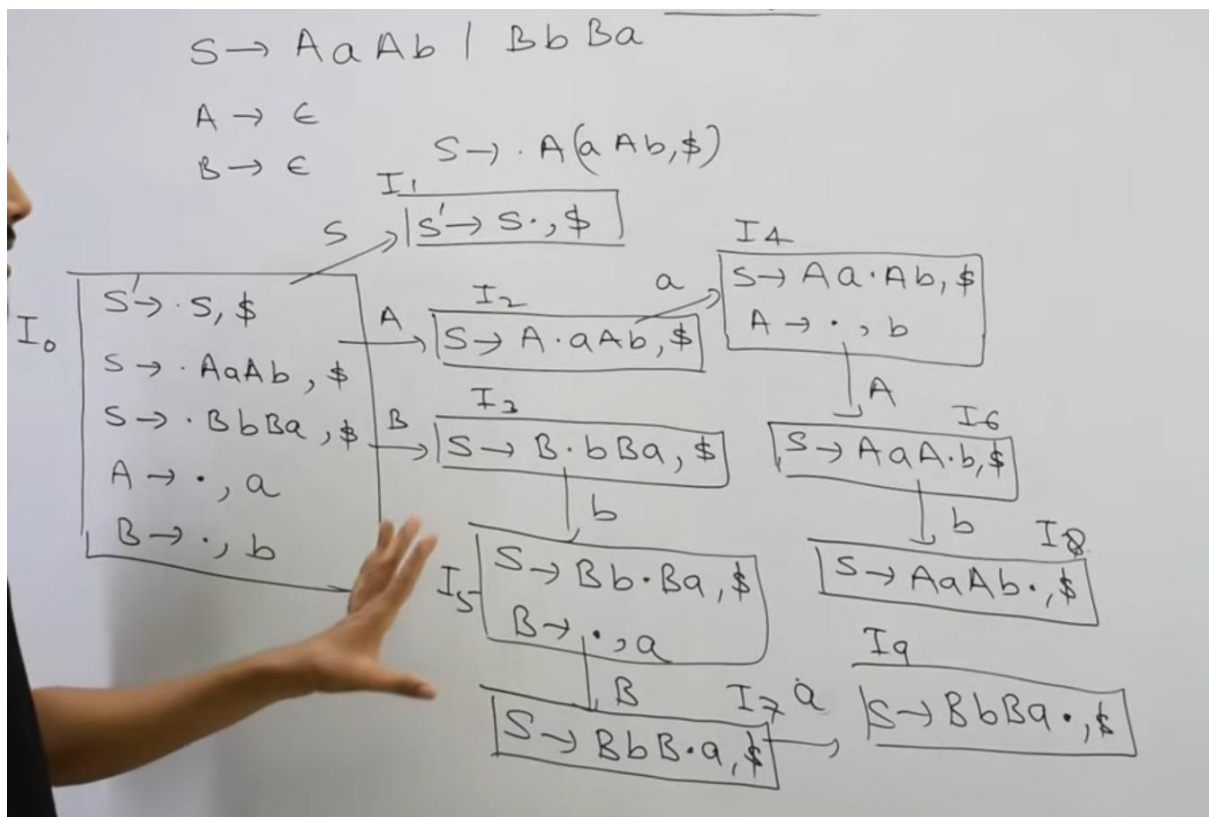
Ex 1: $S \rightarrow \cdot Aa$, \$



Filling of table same as LR(0), but here the Reduce will be filled in Look Ahead Symbols of Final States (Reduced states)

states.	ACTION			GOTO	
	a	b	\$	S	A
0	S ₃	S ₄		1	2
1			Accept		
2	S ₆	S ₇			5
\$ 3	S ₃	S ₄			8
4	r ₃	r ₃			
5			r ₁		
6	S ₆	S ₇			9
7			r ₃		
b 8	r ₂	r ₂			
9			r ₂		

Ex 2:

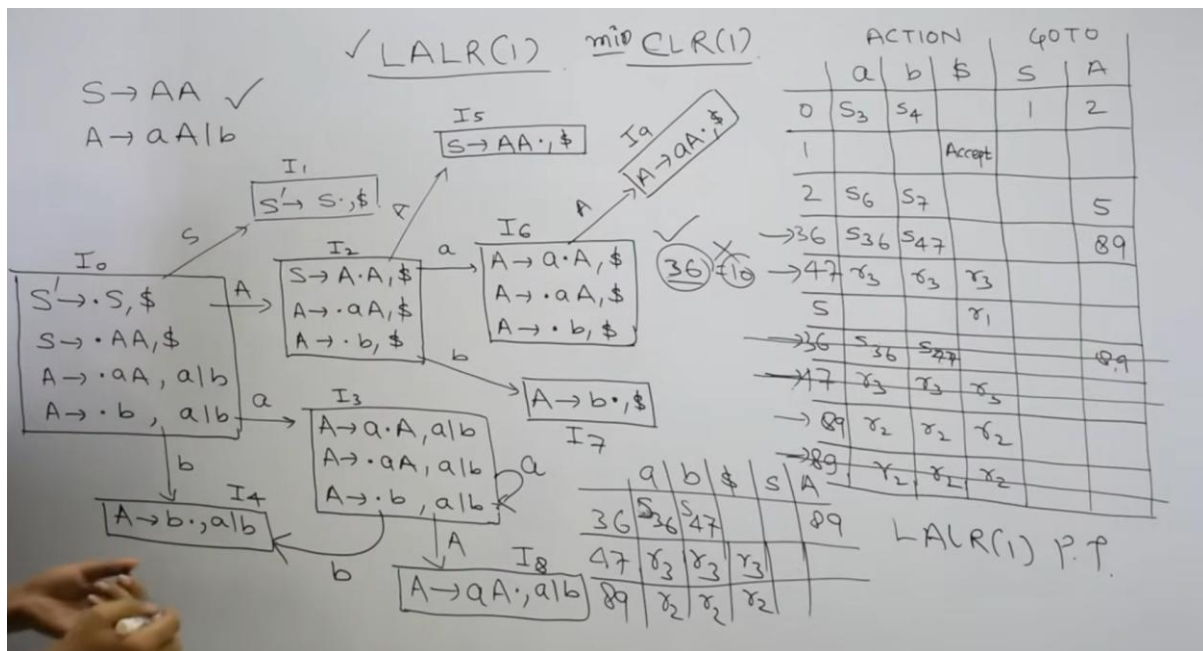


	ACTION			GOTO		
	a	b	\$	S	A	B
0	r ₃	r ₄		1	2	3
1			Accept			
2	s ₄					
3		s ₅				
4		r ₃			6	
5	r ₄					7
6		s ₈				
7	s ₉					
8			r ₁			
9			r ₂			

LALR(1):

Same as CALR(1) steps, merge the states that have the same LR(0) items (look ahead symbols may be different), and then fill the rows with the productions and then eliminate the repeated merge state. If there's no Conflicts (SR, RR) in any cell, then its valid.

Ex 1:



Ex 2:

