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AI1103-Assignment 1

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Download all python codes from

https://github.com/Shambu-K/Assignment-1/blob/main/assignment-1.py

and latex-tikz codes from

https://github.com/Shambu-K/Assignment-1/blob/main/Assignment-1.tex

QUESTION

(4.6) Find the probability of throwing at most 2 sixes in 6 throws of a single die.

SOLUTION

Let X represent the number of sixes in six throws of a dice

 $X \in \{0,1,2,3,4,5,6\}$

By Binomial distribution formula,

$$P(X = k) = {}^{n}C_{k}p^{k}(1 - p)^{n-k}$$

Here,

Symbol	Meaning
k	no. of sixes in six throws of a dice
n	no. of throws $= 6$
p	Pr of getting 6 in single throw= $\frac{1}{6}$

TABLE 0: This table gives the meaning of each symbol used in the formula

To find the probability of getting atmost two sixes in six throws of a single dice:

$$Pr(X \le 2) = Pr(X = 0) + Pr(X = 1) + Pr(X = 2)$$

(0.0.1)

$$\Pr(X = 0) = {}^{6}C_{0} \times \left(\frac{1}{6}\right)^{0} \times \left(\frac{5}{6}\right)^{6-0}$$
 (0.0.2)

$$\Pr(X = 1) = {}^{6}C_{1} \times \left(\frac{1}{6}\right)^{1} \times \left(\frac{5}{6}\right)^{6-1}$$
 (0.0.3)

$$\Pr(X = 2) = {}^{6}C_{2} \times \left(\frac{1}{6}\right)^{2} \times \left(\frac{5}{6}\right)^{6-2}$$
 (0.0.4)

$$\Pr(X \le 2) = \left(\frac{5^6}{6^6}\right) \times 1 + \left(\frac{5^5}{6^6}\right) \times 6 + \left(\frac{5^4}{6^6}\right) \times 15$$
(0.0.5)

= 0.937714

(0.0.6)