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AI1103-Assignment 1

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Download all python codes from

https://github.com/Shambu-K/Assignment-1/blob/main/assignment-1.py

and latex-tikz codes from

https://github.com/Shambu-K/Assignment-1/blob/main/Assignment-1.tex

PROBLEM

(4.6) Find the probability of throwing at most 2 sixes in 6 throws of a single die.

Solution

Let X represent the number of sixes in six throws of a dice

 $X \in \{0, 1, 2, 3, 4, 5, 6\}$

By Binomial distribution formula,

$$P(X = k) = \binom{n}{k} p^k (1 - p)^{n-k}$$
 (0.0.1)

Here,

Symbol	Meaning
k	no. of sixes in six throws of a dice
n	no. of throws i.e. 6
p	probablility of getting a six in a single throw of dice = $\frac{1}{6}$

To find the probability of getting atmost two sixes in six throws of a single dice:

$$P(X \le 2) = P(X = 0) + P(X = 1) + P(X = 2)$$
(0.0.2)

$$P(X = 0) = {6 \choose 0} \times (\frac{1}{6})^0 \times (\frac{5}{6})^{6-0} (0.0.3)$$

$$P(X = 1) = {6 \choose 1} \times (\frac{1}{6})^1 \times (\frac{5}{6})^{6-1}$$
 (0.0.4)

$$P(X=2) = \binom{6}{2} \times (\frac{1}{6})^2 \times (\frac{5}{6})^{6-2}$$
 (0.0.5)

$$P(X \le 2) = \frac{5^6}{6^6} \times 1 + \frac{5^5}{6^6} \times 6 + \frac{5^4}{6^6} \times 15$$
 (0.0.6)

$$P(X \le 2) = 0.937714 \tag{0.0.7}$$