

Binary Search Fix

Let's go through this code line by line and break it down for better understanding.

◆ Problem Statement Recap

We are given an $m \times n$ matrix. Our goal is to **sort each diagonal in ascending order** while keeping the relative positions of the diagonals intact.

A **diagonal** in a matrix is a set of elements that move **down-right** (`row++` , `col++`) starting from some cell.

◆ Example

📌 Input Matrix

```
3 3 1 1
2 2 1 2
1 1 1 2
```

📌 Output Matrix (after sorting each diagonal)

```
1 1 1 1
1 2 2 2
1 2 3 3
```

◆ Step-by-Step Code Walkthrough

◆ **Function:** `diagonalSort(int[][] mat)`

This function initiates the diagonal sorting process.

```
java
```

```
public int[][] diagonalSort(int[][] mat) {
    int n = mat.length;        // Number of rows
    int m = mat[0].length;     // Number of columns
```

- ✓ `n` stores the total number of rows in the matrix.
- ✓ `m` stores the total number of columns in the matrix.

◆ First Loop: Sorting Diagonals from the First Row (`row = 0`)

java

```
// row = 0
for(int col = 0 ; col < m ; col++){
    sort(mat , 0 , col , n , m);
}
```

💡 What does this loop do?

- It starts at `row = 0` (first row).
- Iterates through each column (`col = 0` to `m-1`).
- Calls `sort(mat, 0, col, n, m)`, which sorts the diagonal starting from `(0, col)`.

Example

Start Position	Extracted Diagonal
<code>(0,0)</code> → <code>(1,1)</code> → <code>(2,2)</code>	<code>[3, 2, 1]</code>
<code>(0,1)</code> → <code>(1,2)</code> → <code>(2,3)</code>	<code>[3, 1, 2]</code>
<code>(0,2)</code> → <code>(1,3)</code>	<code>[1, 2]</code>
<code>(0,3)</code>	<code>[1]</code>

- ✓ This ensures all diagonals starting from the first row are covered.

◆ Second Loop: Sorting Diagonals from the First Column (`col = 0`)

java

```
// col = 0;
for(int row = 1 ; row < n ; row++){
    sort(mat , row , 0 , n , m);
}
```

💡 What does this loop do?

- It starts at `col = 0` (first column).
- Iterates through each row (`row = 1` to `n-1`).
- Calls `sort(mat, row, 0, n, m)`, which sorts the diagonal starting from `(row, 0)`.

Example

Start Position	Extracted Diagonal
<code>(1,0) → (2,1)</code>	<code>[2, 1]</code>
<code>(2,0)</code>	<code>[1]</code>

- ✅ This ensures all diagonals starting from the first column are covered.
- ✅ The `(0,0)` diagonal is already covered in the first loop, so we start from `row = 1`.

♦ Function: `sort(int[][] mat, int row, int col, int n, int m)`

This function sorts a single diagonal starting from `(row, col)`.

java

```
public void sort(int[][] mat , int row , int col , int n , int m){
    List<Integer> values = new ArrayList<>();
}
```

- ✅ Creates an empty list `values` to store diagonal elements.

♦ Step 1: Extract Diagonal Elements

java

```
int r = row , c = col;

while(r < n && c < m){
    values.add(mat[r][c]);
    r++;
    c++;
}
```

💡 What happens here?

- `(r, c)` starts at `(row, col)`.
- Moves **down-right** (`r++`, `c++`).
- Stores diagonal elements in `values`.

Example

Starting from `(0,0)`:

ini

```
values = [3, 2, 1]
```

Starting from `(0,1)`:

ini

```
values = [3, 1, 2]
```

♦ Step 2: Sort the Extracted Values

java

```
Collections.sort(values);
```

✅ Sorts the diagonal elements in **ascending order**.

For `(0,0) → (1,1) → (2,2)`, we get:

less

Before Sorting: [3, 2, 1]

After Sorting: [1, 2, 3]

◆ Step 3: Write Back the Sorted Values

java

```
r = row;
c = col;
int index = 0;

while(r < n && c < m){
    mat[r][c] = values.get(index++);
    r++;
    c++;
}
```

💡 What happens here?

- Starts at (row, col).
- Writes back the sorted values into the matrix along the diagonal.

Example

For diagonal (0,0) → (1,1) → (2,2):

makefile

Original: [3, 2, 1]

Sorted: [1, 2, 3]

✅ This replaces the **original** matrix values with the sorted diagonal.

◆ Final Sorted Matrix

```
1 1 1 1
1 2 2 2
1 2 3 3
```

◆ Time Complexity Analysis

For an $m \times n$ matrix:

1. Extracting a diagonal $\rightarrow O(D)$
2. Sorting a diagonal $\rightarrow O(D \log D)$
3. Writing back $\rightarrow O(D)$

Since there are $(n + m - 1)$ diagonals, total complexity:

mathematica

```
O((n + m) * D log D)
```

🔥 Final Summary

- 1 First loop covers diagonals from the first row.
 - 2 Second loop covers diagonals from the first column (except $(0, 0)$).
 - 3 Sort function:
 - Extracts diagonal elements
 - Sorts them
 - Writes them back into the matrix
- ✓ Every diagonal is sorted independently.
- ✓ Final result maintains diagonal order but sorts the elements.

Would You Like a Step-by-Step Visual Diagram?

I can illustrate it for better clarity! 