

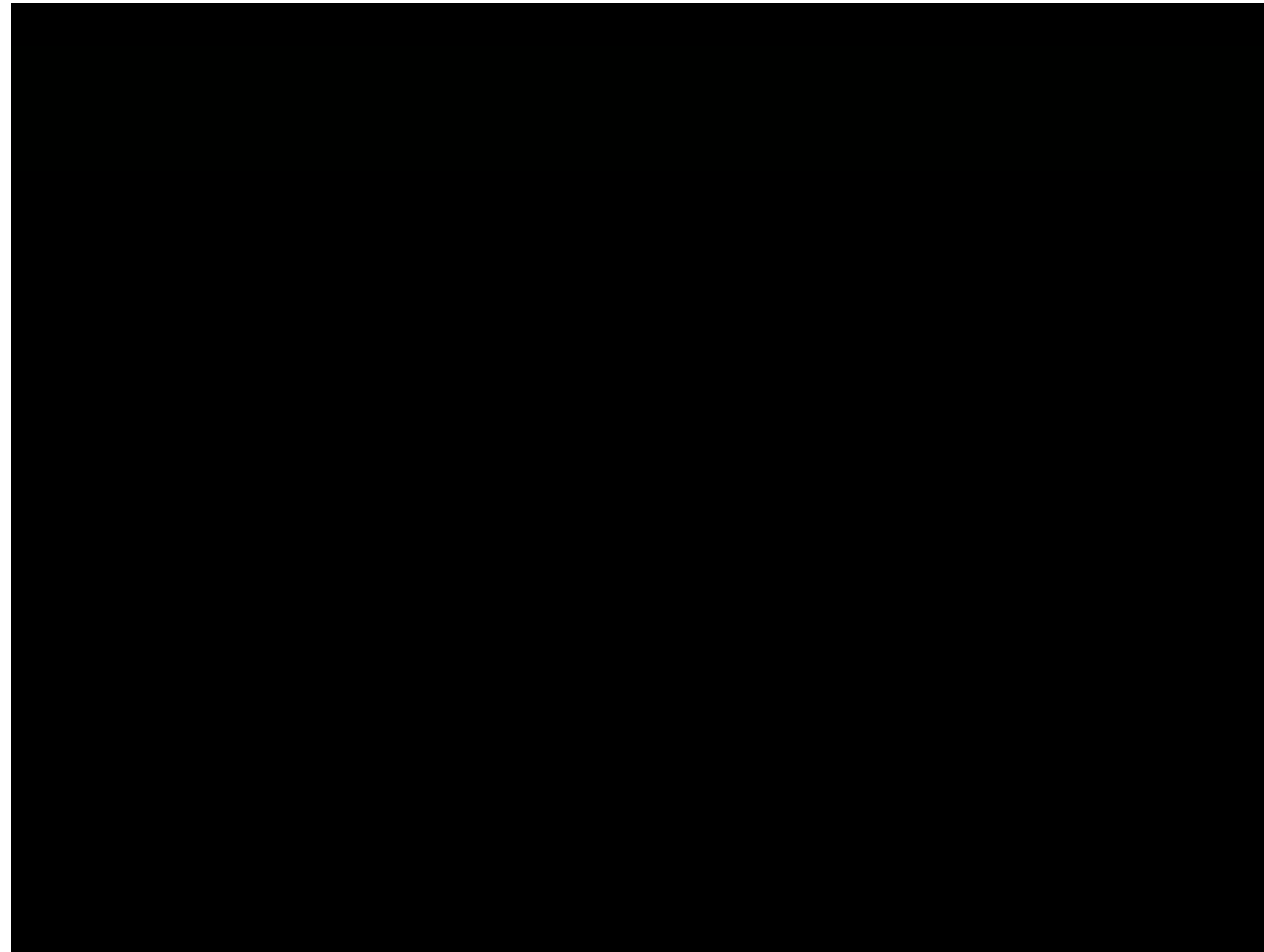
# Review

ECE 3710

No one knows what's next,  
but everybody does it.

- George Carlin

for what follows...



*Most Likely You Go Your Way (And I'll Go Mine)*  
- Bob Dylan

# binary

$2^n$	$n$
1	0
2	1
4	2
8	3

16	4
32	5
64	6
128	7

256	8
512	9
1 024	10
2 048	11

4 096	12
8 192	13
16 384	14
32 768	15

65 536	16
--------	----

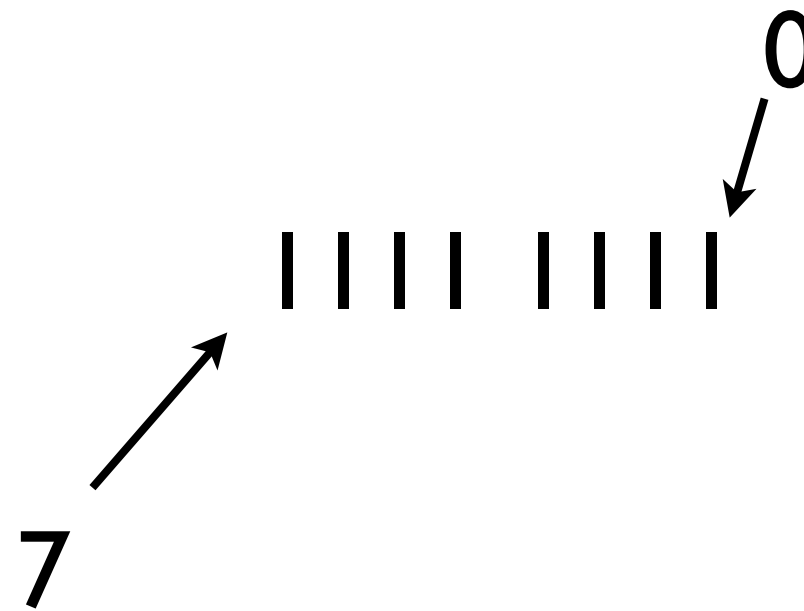
8 bits: 0000 0000



$2^8 = 256 \Rightarrow 256$  representations

# bin2dec

$2^n$	$n$
1	0
2	1
4	2
8	3
16	4
32	5
64	6
128	7
256	8
512	9
1 024	10
2 048	11
4 096	12
8 192	13
16 384	14
32 768	15
65 536	16



$$2^7 + 2^6 + 2^5 + 2^4 + 2^3 + 2^2 + 2^1 + 2^0 = 255$$

# bin2dec

Q: 0101 0101

# bin2dec

Q: 0101 0101

A:  $2^6 + 2^4 + 2^2 + 2^0 = 85$

never, ever use this:

"There are 10 types of people: those  
who understand binary and everyone  
else."

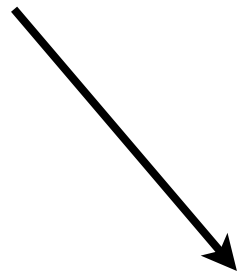


if you think it's funny...



# dec2bin

275 => 1 0001 0011



bits:

1. how many
2. which

# dec2bin

$2^n$	$n$
-------	-----

1	0
---	---

2	1
---	---

4	2
---	---

8	3
---	---

16	4
----	---

32	5
----	---

64	6
----	---

128	7
-----	---

256	8
-----	---

512	9
-----	---

1 024	10
-------	----

2 048	11
-------	----

4 096	12
-------	----

8 192	13
-------	----

16 384	14
--------	----

32 768	15
--------	----

65 536	16
--------	----

275 => 1 0001 0011

275 > 255 => more than 8

275 < 511 => less than 9

# dec2bin

$2^n$	n
1	0
2	1
4	2
8	3
16	4
32	5
64	6
128	7
256	8
512	9
1 024	10
2 048	11
4 096	12
8 192	13
16 384	14
32 768	15
65 536	16

275 => 1 0001 0011

$$2^8 + \underbrace{275 - 256}$$

tedious

19 = 1 0011

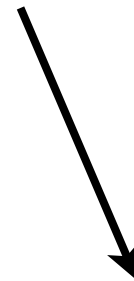
$$2^8 + 2^{(i-1)} \leq 275$$

fastest

# hex

Dec	Hex	Bin
00	0	0000
01	1	0001
02	2	0010
03	3	0011
04	4	0100
05	5	0101
06	6	0110
07	7	0111
08	8	1000
09	9	1001
10	A	1010
11	B	1011
12	C	1100
13	D	1101
14	E	1110
15	F	1111

hex2dec & dec2hex



use bin as intermediary

$2^n$	n
1	0
2	1
4	2
8	3
16	4
32	5
64	6
128	7
256	8
512	9
1 024	10
2 048	11
4 096	12
8 192	13
16 384	14
32 768	15
65 536	16

Q: dec2bin(34) & dec2hex(34)

Dec	Hex	Bin
00	0	0000
01	1	0001
02	2	0010
03	3	0011
04	4	0100
05	5	0101
06	6	0110
07	7	0111
08	8	1000
09	9	1001
10	A	1010
11	B	1011
12	C	1100
13	D	1101
14	E	1110
15	F	1111

Q: dec2bin(34) & dec2hex(34)

$2^5 = 32$  and  $2^6 = 64 \Rightarrow$  6 bits: 0010 0000

$2^n$	n
-------	---

1	0
---	---

2	1
---	---

4	2
---	---

8	3
---	---

16	4
----	---

32	5
----	---

64	6
----	---

128	7
-----	---

256	8
-----	---

512	9
-----	---

1 024	10
-------	----

2 048	11
-------	----

4 096	12
-------	----

8 192	13
-------	----

16 384	14
--------	----

32 768	15
--------	----

$32 + 2 = 34 \Rightarrow$  0010 0010



22H

Q: hex2dec(A5)

$2^n$	n
1	0
2	1
4	2
8	3
16	4
32	5
64	6
128	7
256	8
512	9
1 024	10
2 048	11
4 096	12
8 192	13
16 384	14
32 768	15
65 536	16

Dec	Hex	Bin
00	0	0000
01	1	0001
02	2	0010
03	3	0011
04	4	0100
05	5	0101
06	6	0110
07	7	0111
08	8	1000
09	9	1001
10	A	1010
11	B	1011
12	C	1100
13	D	1101
14	E	1110
15	F	1111



Q: hex2dec(A5)



10 5



shouldn't need table: 1010 0101

(memorise all 4-bit)



$$2^7 + 2^5 + 2^2 + 2^0 = 128 + 32 + 4 + 1 = 165$$

Q: 36BH+F6H

$2^n$	n
1	0
2	1
4	2
8	3
16	4
32	5
64	6
128	7
256	8
512	9
1 024	10
2 048	11
4 096	12
8 192	13
16 384	14
32 768	15
65 536	16

Dec	Hex	Bin
00	0	0000
01	1	0001
02	2	0010
03	3	0011
04	4	0100
05	5	0101
06	6	0110
07	7	0111
08	8	1000
09	9	1001
10	A	1010
11	B	1011
12	C	1100
13	D	1101
14	E	1110
15	F	1111

Q: 36BH+F6H

11  
36B  
+ F6  
=461

1: 11+6=17 (-16=1)  
2: 6+15+1=22 (-16=6)  
3: 3+1=4

	$2^n$	n
	1	0
	2	1
	4	2
	8	3
	16	4
	32	5
	64	6
	128	7
	256	8
	512	9
1	1 024	10
2	2 048	11
4	4 096	12
8	8 192	13
16	16 384	14
32	32 768	15
65	65 536	16

Q: 36BH-F6H

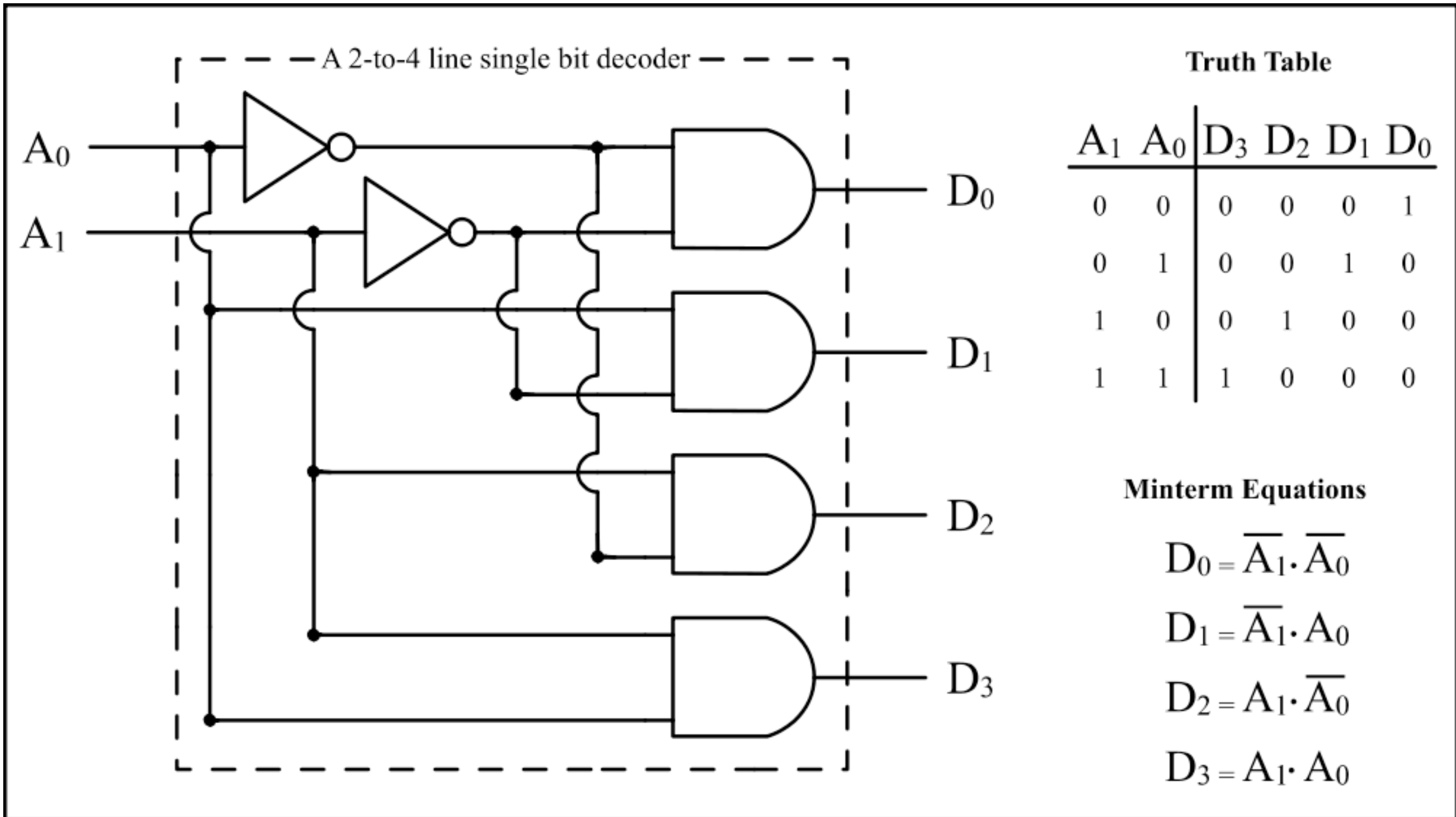
Dec	Hex	Bin
00	0	0000
01	1	0001
02	2	0010
03	3	0011
04	4	0100
05	5	0101
06	6	0110
07	7	0111
08	8	1000
09	9	1001
10	A	1010
11	B	1011
12	C	1100
13	D	1101
14	E	1110
15	F	1111

Q: 36BH-F6H

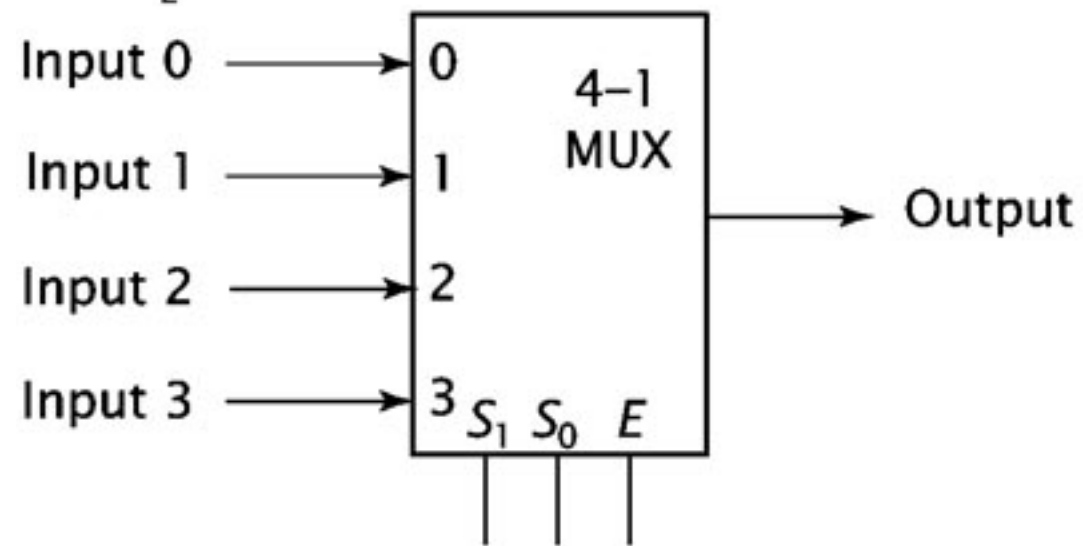
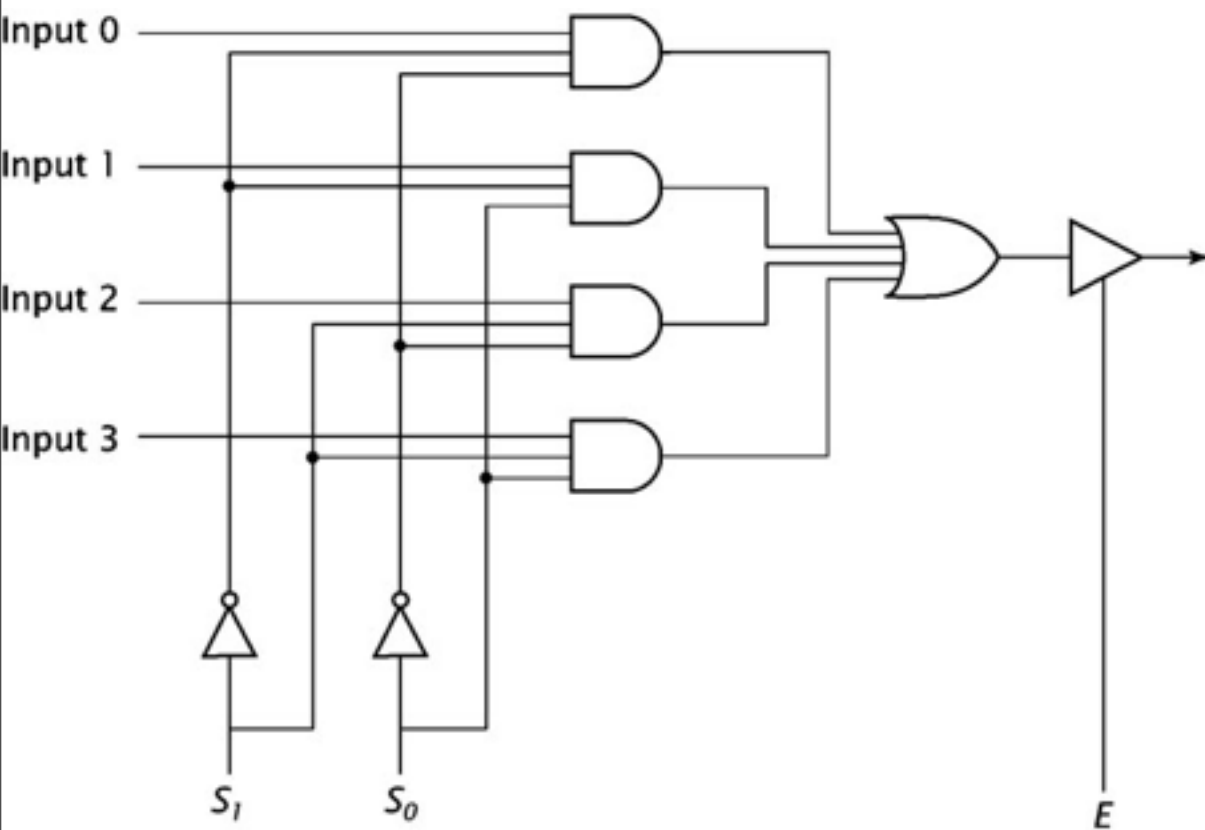
36B  
- F6  
=275

1: 11-6=5  
2: 6-15+16=7  
3: 2

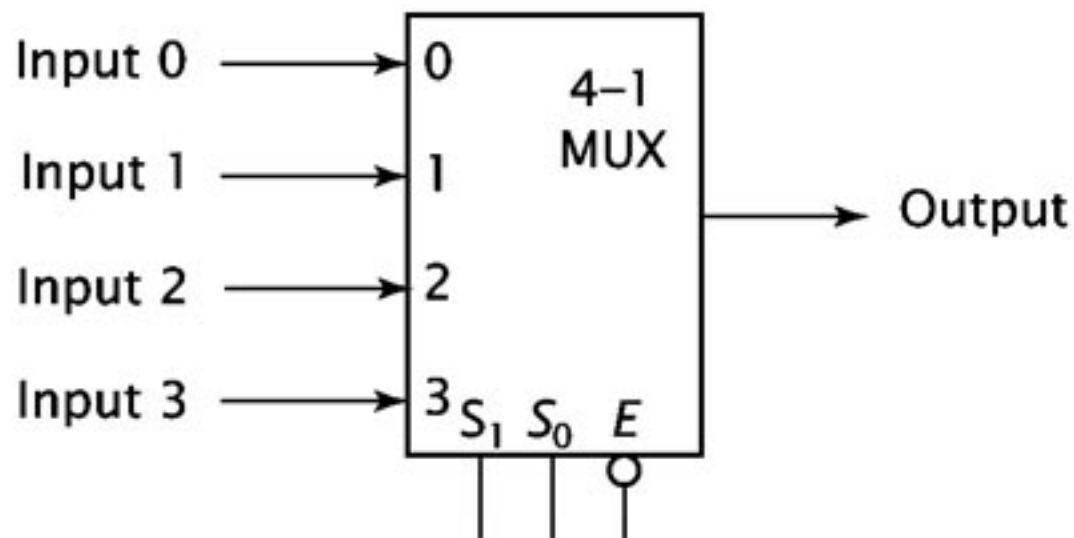
# decoder



# multiplexor



$S_1$	$S_0$	$E$	Output
X	X	0	Z
0	0	1	Input 0
0	1	1	Input 1
1	0	1	Input 2
1	1	1	Input 3



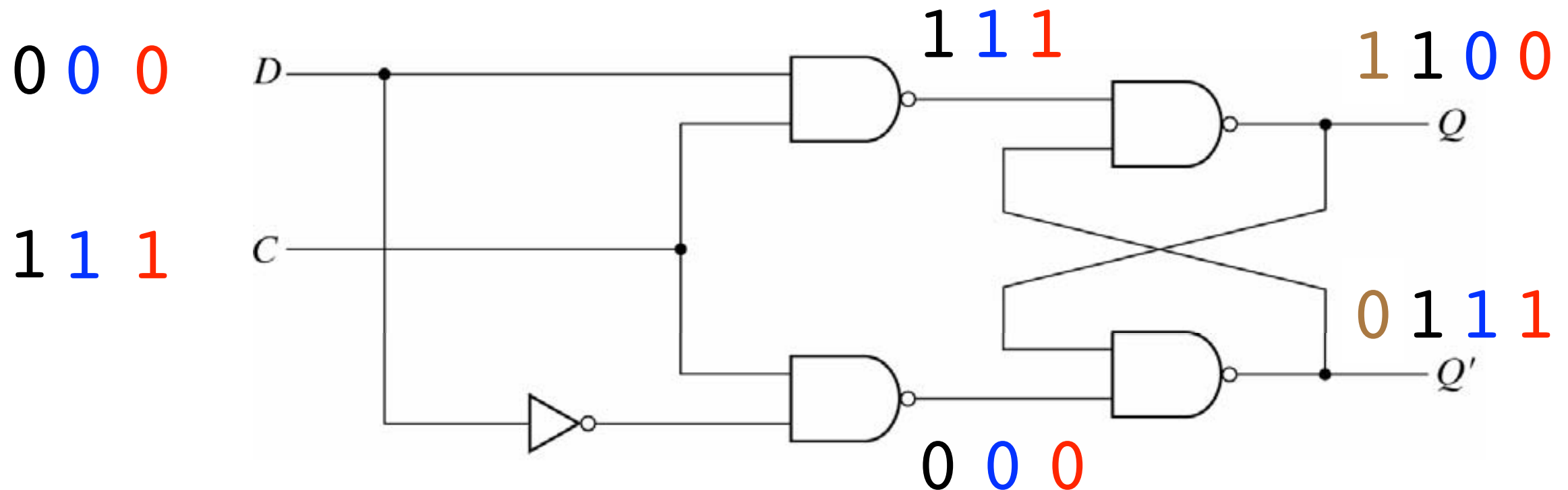
$S_1$	$S_0$	$E$	Output
X	X	1	Z
0	0	0	Input 0
0	1	0	Input 1
1	0	0	Input 2
1	1	0	Input 3

# flip-flop (d latch)

$C$	$D$	Next state of $Q$
0	X	No change
1	0	$Q = 0$ ; Reset state
1	1	$Q = 1$ ; Set state

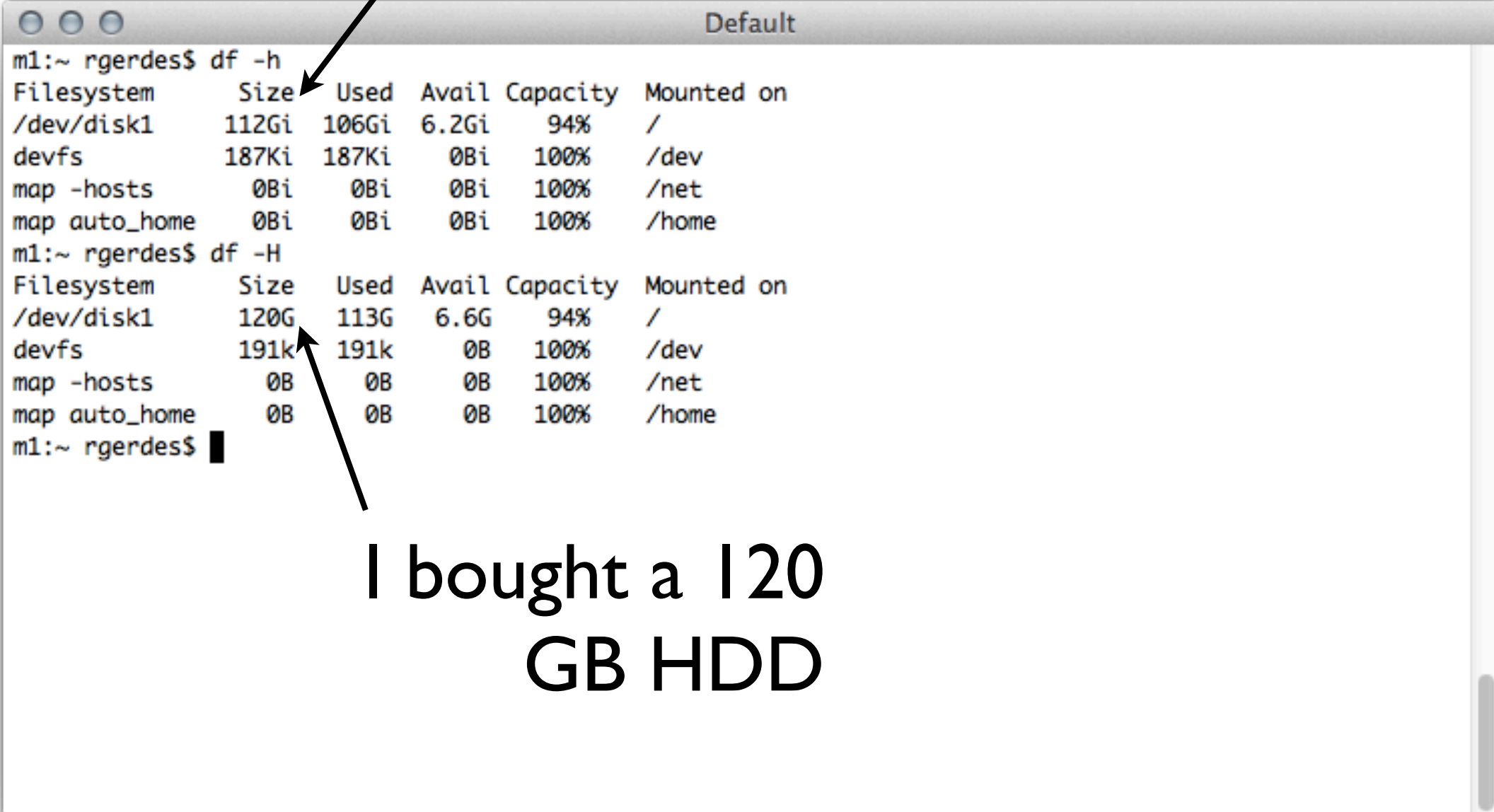
previous clock:  $Q = 1$   
 $Q' = 0$

want:  $Q = 0$





who makes a 112  
GB HDD?



A terminal window titled "Default" showing the output of the `df -h` and `df -H` commands. The window has a title bar with three window control buttons (red, yellow, green) on the left. The text inside the terminal is as follows:

```
m1:~ rgerdes$ df -h
Filesystem      Size  Used Avail Capacity  Mounted on
/dev/disk1      112Gi 106Gi   6.2Gi    94%      /
devfs           187Ki 187Ki    0Bi   100%    /dev
map -hosts       0Bi    0Bi    0Bi   100%    /net
map auto_home    0Bi    0Bi    0Bi   100%    /home
m1:~ rgerdes$ df -H
Filesystem      Size  Used Avail Capacity  Mounted on
/dev/disk1      120G  113G   6.6G    94%      /
devfs           191k  191k    0B   100%    /dev
map -hosts       0B     0B    0B   100%    /net
map auto_home    0B     0B    0B   100%    /home
m1:~ rgerdes$
```

Two arrows point from external text to the terminal output. The first arrow points from the text "who makes a 112 GB HDD?" to the "112Gi" value in the first row of the `df -h` output. The second arrow points from the text "I bought a 120 GB HDD" to the "120G" value in the first row of the `df -H` output.

I bought a 120  
GB HDD

## Why is 1 GB equal to $10^9$ bytes instead of $2^{30}$ ?

Because in 1960, the Bureau International des Poids et Mesures decided that the SI prefix G- meant  $10^9$ .

### But it means $2^{30}$ , really!

No it doesn't. Let's look at some examples:

A Gm is...  $10^9$  meters  
A GW is...  $10^9$  watts  
A GA is...  $10^9$  amperes  
A Gmol is...  $10^9$  moles

### But it's different in computing!

Let's look at some more examples:

A 2.2 GHz CPU operates at...	$2.2 \times 10^9$ cycles per second
1 Gbps Ethernet transmits data at...	$10^9$ bits per second
The 2.4GHz band which wireless ethernet operates within lies...	between $2.4 \times 10^9$ and $2.5 \times 10^9$ Hz
A 200 GB hard drive holds...	$200 \times 10^9$ bytes of data

## **But what about RAM?**

You're right: If you buy a "1GB" stick of RAM, it will hold  $2^{30}$  bytes of data.

However, this is a special case: Unlike everything else in the world of computing, RAM is addressed in hardware. When you're designing a piece of silicon, you want to have  $N$  address lines and have every combination of zeroes and ones map to a memory location — to do otherwise would make the logic far more complicated. *Nothing else* is addressed this way.

Finally, even for RAM calling  $2^{30}$  bytes "1GB" isn't really proper; instead, the IEC binary multiplier prefix "Gi-" should be used.

## **This is all a conspiracy by hard drive manufacturers who want to cheat us out of the disk space we're paying for!**

We all love good conspiracy theories... but really, this isn't about evil megacorporations trying to cheat you. Hard drive prices are determined almost entirely by competition between manufacturers, so if hard drives were labelled in GiB instead of being labelled in GB, we'd be paying the same number of dollars for the same number of bytes anyway — if this really was a global conspiracy, it would be one of the dumbest conspiracies ever.

<http://www.tarsnap.com/GB-why.html>