

# TMD Studies in $e^+e^-$ Collisions — Week 9 Progress

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Simulation study using PYTHIA8, FastJet, ROOT

# Outline

- Recap & goals
- ancestry tracing
- New observables & plots

# Recap of Week 8 & Goals for Week 9

## Last week:

- Baseline jet shapes (thrust, sphericity) and jet multiplicity
- $\Delta\phi$  between leading jets and leading  $\pi/K$  spectra

## This week (requested tasks):

- Investigate leading pion origins using PYTHIA ancestry tracing
- Plot thrust for several jet radii  $R$  (radius scan)
- Study  $p_T$  differences:  $p_T(\text{jet}) - p_T(\pi)$  and  $p_T(\pi) - p_T(\text{parent})$

# Event setup: $e^+e^- \rightarrow d\bar{d}$

- The hard  $e^+e^-$  annihilation produces a down quark and an anti-down quark, seeding two back-to-back color strings.
- We show the early event record just after the hard process, before hadronization develops.

row	event	size	no	id	name	st	m1	m2	d1	d2	px	py	pz	E	
0	3	134	0	90	system	-11	0	0	0	0		0.000	0.000	0.000	91.200
1	3	134	1	-11	e+	-12	0	0	3	0		0.000	0.000	45.600	45.600
2	3	134	2	11	e-	-12	0	0	4	0		0.000	0.000	-45.600	45.600
3	3	134	3	-11	e+	-21	1	0	5	0		0.000	0.000	45.600	45.600
4	3	134	4	11	e-	-21	2	0	5	0		0.000	0.000	-45.600	45.600
5	3	134	5	23	z0	-22	3	4	6	7		0.000	0.000	0.000	91.200
6	3	134	6	1	d	-23	5	0	8	9		-44.829	7.850	2.821	45.600
7	3	134	7	-1	dbar	-23	5	0	10	10		44.829	-7.850	-2.821	45.600
8	3	134	8	1	d	-51	6	0	11	12		-41.505	0.505	4.102	41.711
9	3	134	9	21	g	-51	6	0	13	13		-0.289	6.813	-1.471	6.976

(showing rows 0 to 9 of 134 total)

More [Enter+=10, n=next event, q=quit]:

row	event	size	no	id	name	st	m1	m2	d1	d2	px	py	pz	E	
10	3	134	10	-1	dbar	-52	7	7	16	16		41.794	-7.318	-2.630	42.513
11	3	134	11	1	d	-51	8	0	28	28		-34.400	4.792	5.001	35.092
12	3	134	12	21	g	-51	8	0	26	27		-7.156	-3.064	-1.163	7.871
13	3	134	13	21	g	-52	9	9	14	15		-0.237	5.590	-1.287	5.724
14	3	134	14	21	g	-51	13	0	25	25		-1.159	0.632	-3.075	3.346
15	3	134	15	21	g	-51	13	0	17	18		5.687	4.137	1.573	7.143
16	3	134	16	-1	dbar	-52	10	10	19	19		37.109	-6.498	-2.336	37.747
17	3	134	17	21	g	-51	15	0	20	21		14.413	4.424	2.258	15.245
18	3	134	18	21	g	-51	15	0	22	22		4.413	-2.604	-1.518	5.345
19	3	134	19	-1	dbar	-52	16	16	37	37		23.889	-4.180	-1.502	24.301

(showing rows 10 to 19 of 134 total)

More [Enter+=10, n=next event, q=quit]:

# Most relevant PYTHIA8 status codes in this analysis

<b>Code</b>	<b>Meaning</b>
-11	Event record container ("system")
-12	Incoming beam particles ( $e^+$ , $e^-$ )
-21	Incoming particles of the hardest subprocess
-22	Intermediate state of the hardest subprocess (e.g. virtual $Z^0$ )
-23	Outgoing partons from the hardest subprocess (e.g. $d$ , $\bar{d}$ )
-51	Final-state shower products (FSR partons)
-52	Recoiler copies created by shower evolution
-71	Partons prepared for hadronization (pre-string state)
-83 / -84	Primary hadrons produced from string fragmentation

Reminder: negative code = particle already branched/decayed, positive = still present [1].

# Event record structure (id, m1, m2, d1, d2)

- $\text{id}$  = PDG particle ID,  $\text{m1}, \text{m2}$  = index of mother(s),  $\text{d1}, \text{d2}$  = index range of daughters in the event record [2].

QUARKS	DIQUARKS	LIGHT $I = 1$ MESONS	LIGHT $I = 0$ MESONS
$d$ 1	$(dd)_1$ 1103		
$u$ 2	$(ud)_0$ 2101		
$s$ 3	$(ud)_1$ 2103	$\pi^0$ 111	$(u\bar{u}, d\bar{d}, \text{and } s\bar{s} \text{ Admixtures})$
$c$ 4	$(uu)_1$ 2203	$\pi^+$ 211	
$b$ 5	$(sd)_0$ 3101	$a_0(980)^0$ 9000111	$\eta$ 221
$t$ 6	$(sd)_1$ 3103	$a_0(980)^+$ 9000211	$\eta'(958)$ 331
$b'$ 7	$(su)_0$ 3201		
$t'$ 8	$(su)_1$ 3203		
LEPTONS		$\pi(1300)^0$ 100111	$f_0(600)$ 9000221
$e^-$ 11	$(ss)_1$ 3303	$\pi(1300)^+$ 100211	$f_0(980)$ 9010221
$\nu_e$ 12	$(ed)_0$ 4101	$a_0(1450)^0$ 10111	$\eta(1295)$ 100221
$\mu^-$ 13	$(cd)_1$ 4103	$a_0(1450)^+$ 10211	$f_0(1370)$ 10221
$\nu_\mu$ 14	$(cu)_0$ 4201	$\pi(1800)^0$ 9010111	$\eta(1405)$ 9020221
$\tau^-$ 15	$(cu)_1$ 4203	$\pi(1800)^+$ 9010211	$\eta(1475)$ 100331
$\nu_\tau$ 16	$(es)_0$ 4301		
$\tau'^-$ 17	$(es)_1$ 4303		
$\nu_{\tau'}$ 18	$(ce)_1$ 4403		
EXCITED PARTICLES		$\rho(770)^0$ 113	$f_0(1500)$ 9030221
$d^*$ 4000001	$(bd)_0$ 5101	$\rho(770)^+$ 213	$f_0(1710)$ 10331
$u^*$ 4000002	$(bd)_1$ 5103	$b_1(1235)^0$ 10113	$\eta(1760)$ 9040221*
$e^*$ 4000011	$(bu)_0$ 5201	$b_1(1235)^+$ 10213	$f_0(2020)$ 9050221*
$\nu_e^*$ 4000012	$(bu)_1$ 5203	$a_1(1260)^0$ 20113	$f_0(2100)$ 9060221*
GAUGE AND HIGGS BOSONS		$a_1(1260)^+$ 20213	$f_0(2200)$ 9070221*
$g$ (9) 21	$(be)_0$ 5401	$a_1(1260)^+$ 20213	$\eta(2225)$ 9080221*
$\gamma$ 22	$(be)_1$ 5403	$\pi_1(1400)^0$ 9000113	
$Z^0$ 23	$(bb)_1$ 5503	$\pi_1(1400)^+$ 9000213	$\omega(782)$ 223
TECHNICOLOR PARTICLES		$\rho(1450)^0$ 100113	$\phi(1020)$ 333
$h^0/H_1^0$ 24	$\pi_{\text{tech}}^0$ 3000111	$\rho(1450)^+$ 100213	
$Z'/Z_2^0$ 25	$\pi_{\text{tech}}^+$ 3000211	$\rho(1450)^0$ 100113	$h_1(1170)$ 10223
$Z''/Z_3^0$ 32	$\pi_{\text{tech}}^{'+}$ 3000221	$\rho(1450)^+$ 100213	$f_1(1285)$ 20223
$W'/W_2^+$ 34	$\eta_{\text{tech}}^0$ 3100221	$\pi_1(1600)^0$ 9010113	$h_1(1380)$ 10333
$H^0/H_2^0$ 35	$\eta_{\text{tech}}^0$ 3100221		
$A^0/H_3^0$ 36	$\rho_{\text{tech}}^0$ 3000113		
$H^+$ 37	$\rho_{\text{tech}}^+$ 3000213		



# Onset of hadronization

- Color strings fragment into resonances and hadrons along each jet axis — we track mothers → daughters in the PYTHIA record.

row	event	size	no	id	name	st	m1	m2	d1	d2	px	py	pz	E
20	3	134	20	21	g	−51	17	0	23	24	10.608	3.998	2.510	11.611
21	3	134	21	21	g	−51	17	0	69	69	4.804	−0.163	−0.595	4.843
22	3	134	22	21	g	−52	18	18	35	36	3.415	−2.015	−1.175	4.136
23	3	134	23	21	g	−51	20	0	47	48	4.189	1.534	−0.805	4.459
24	3	134	24	21	g	−51	20	0	34	34	6.381	2.529	3.002	7.492
25	3	134	25	21	g	−52	14	14	32	33	−1.041	0.568	−2.762	3.086
26	3	134	26	21	g	−51	12	0	29	30	−10.199	−2.470	−1.629	10.620
27	3	134	27	21	g	−51	12	0	31	31	−1.436	0.031	1.118	1.820
28	3	134	28	1	d	−52	11	11	50	51	−29.921	4.167	4.349	30.523
29	3	134	29	21	g	−51	26	0	40	40	−7.940	−0.852	0.547	8.004

(showing rows 20 to 29 of 134 total)

More [Enter=+10, n=next event, q=quit]:

# Leading charged pions

- Identify the leading charged  $\pi^\pm$  in each jet and record its ancestry chain (resonance  $\rightarrow \pi$ ) for downstream  $\Delta p_T$  studies.

row	event	size	no	id	name	st	m1	m2	d1	d2	px	py	pz	E
70	3	134	70	21	g	−71	44	44	74	94	1.284	−0.840	−0.551	1.568
71	3	134	71	21	g	−71	45	45	74	94	7.446	−2.024	−0.585	7.727
72	3	134	72	21	g	−71	46	46	74	94	0.725	−0.188	−0.498	0.895
73	3	134	73	−1	dbar	−71	37	37	74	94	17.935	−3.143	−1.132	18.247
74	3	134	74	111	pi0	−83	57	73	107	108	−12.379	1.428	2.139	12.643
75	3	134	75	331	id331	−83	57	73	109	118	−6.873	1.072	0.685	6.279
76	3	134	76	111	pi0	−83	57	73	111	112	−5.161	0.835	0.887	5.305
77	3	134	77	−213	rho-	−83	57	73	95	96	−5.614	0.700	0.842	5.827
78	3	134	78	223	id223	−83	57	73	113	115	−4.959	−1.434	−0.383	5.235
79	3	134	79	2212	p+	83	57	73	0	0	−2.939	−0.420	0.067	3.116

(showing rows 70 to 79 of 134 total)

More [Enter=>10, n=next event, q=quit]:

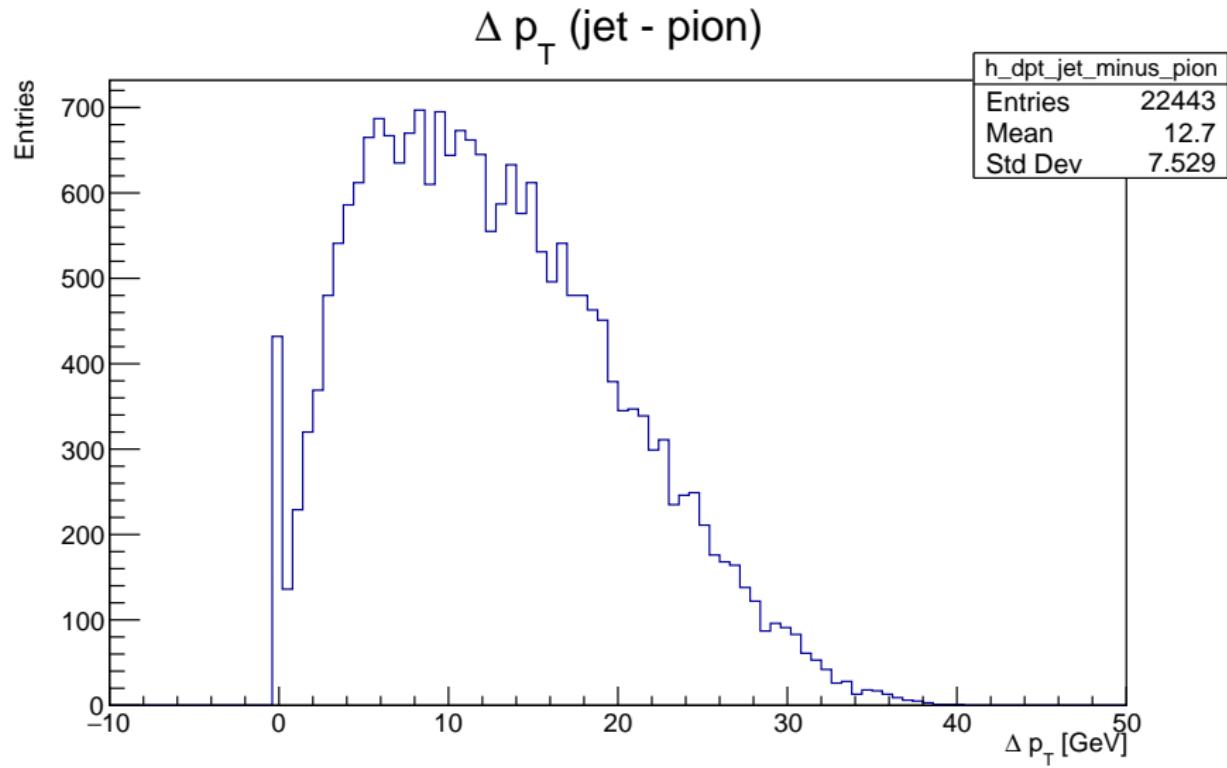
==== EVENT 3 ===

row	event	size	no	id	name	st	m1	m2	d1	d2	px	py	pz	E
80	3	134	80	−321	K-	83	57	73	0	0	−0.003	−0.112	−0.197	0.543
81	3	134	81	−3112	id-3112	−83	57	73	116	117	−3.258	0.221	−0.778	3.564
82	3	134	82	−211	pi-	83	57	73	0	0	−0.689	−0.776	0.336	1.051
83	3	134	83	−211	pi+	83	57	73	0	0	−0.643	0.377	0.396	0.856
84	3	134	84	−113	rho0	−84	57	73	97	98	0.238	0.721	−1.053	1.962
85	3	134	85	−111	pi0	−84	57	73	118	119	0.988	0.129	−0.747	1.191
86	3	134	86	−213	rho-	−84	57	73	99	100	0.512	0.385	0.484	1.136
87	3	134	87	−2212	p+	84	57	73	0	0	1.593	1.236	0.144	2.229
88	3	134	88	−211	pi-	84	57	73	0	0	0.647	−0.002	0.279	0.718
89	3	134	89	−2114	id-2114	−84	57	73	101	102	3.813	0.916	0.846	4.118

(showing rows 80 to 89 of 134 total)

More [Enter=>10, n=next event, q=quit]: |

$$\Delta p_T(\text{jet}) = p_T(\text{jet}) - p_T(\pi_{\text{lead}})$$



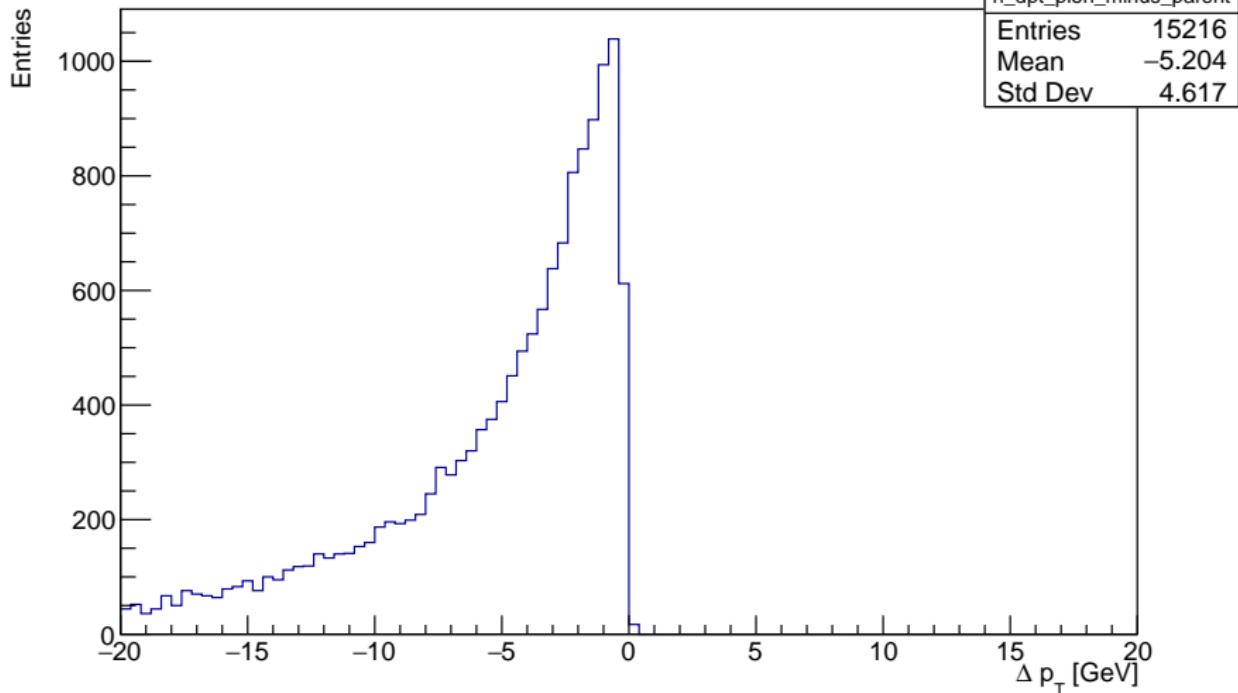
$$\Delta p_T, \text{jet} = p_T(\text{jet}) - p_T(\pi_{\text{lead}})$$

Implemented in code by looping over all reconstructed jets, locating the leading charged pion in each jet, and computing the  $p_T$  imbalance event-by-event.

- Identifies two highest-momentum pions per event
- Matches each pion to its parent jet via constituent tracking
- Calculates  $p_T$  difference: jet total minus leading pion
- Distribution shows momentum carried by other jet particles

$$\Delta p_T, \text{parent} = p_T(\pi_{\text{lead}}) - p_T(\text{parent})$$

$\Delta p_T$  (pion - parent)



Placeholder plot

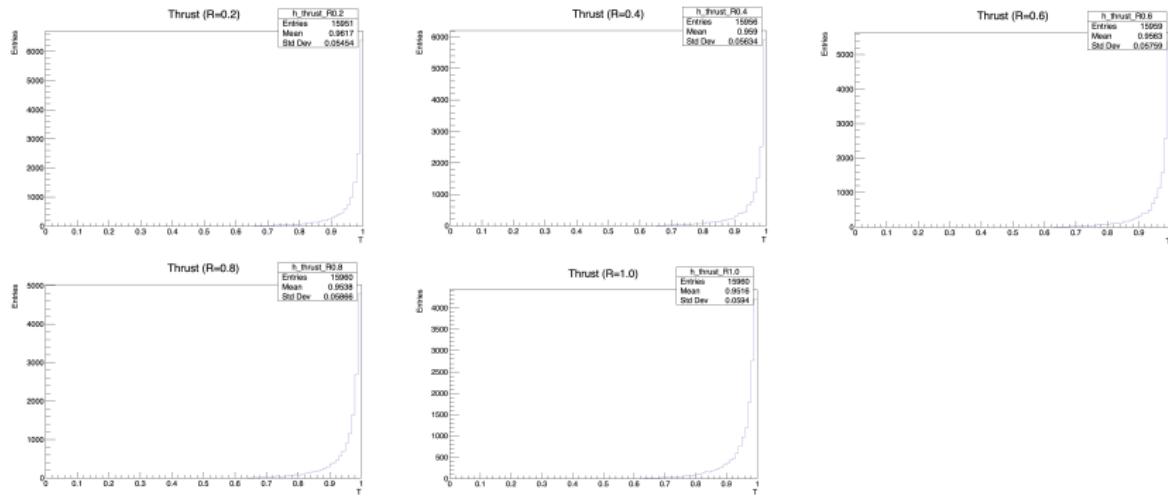
$$\Delta p_{T,\text{parent}} = p_T(\pi_{\text{lead}}) - p_T(\text{parent})$$

## Implementation:

- Traces ancestry of leading pions via mother indices
- Identifies first hadronic parent (PDG 100–10000, excluding pions)
- Measures  $p_T$  gained/lost during decay process

# Thrust vs jet radius $R$

- Compared thrust across jet radii  $R=0.2, 0.4, 0.6, 0.8, 1.0$  to assess radius dependence of global event shape.



# Thrust vs Jet Radius $R$

## Implementation:

- Scans over jet radii:  
 $R \in \{0.2, 0.4, 0.6, 0.8, 1.0\}$
- Clusters jets with anti- $k_T$  algorithm at each  $R$  value
- Collects all jet constituents (minimum  $p_T > 1$  GeV)
- Computes thrust from momentum tensor of jet particles
- Averages thrust over all events for each  $R$  setting

End

Questions?

# References

- 1 "Particle status codes in PYTHIA 8", PYTHIA 8 Manual — ParticleProperties section.  
<https://pythia.org/latest-manual/ParticleProperties.html>
- 2 Particle Data Group, "Review of Monte Carlo Particle Numbering Schemes",  
<https://pdg.lbl.gov/2007/reviews/montecarlорр.pdf>