

COMPUTER SCIENCE & IT

DIGITAL LOGIC



Lecture No. 08

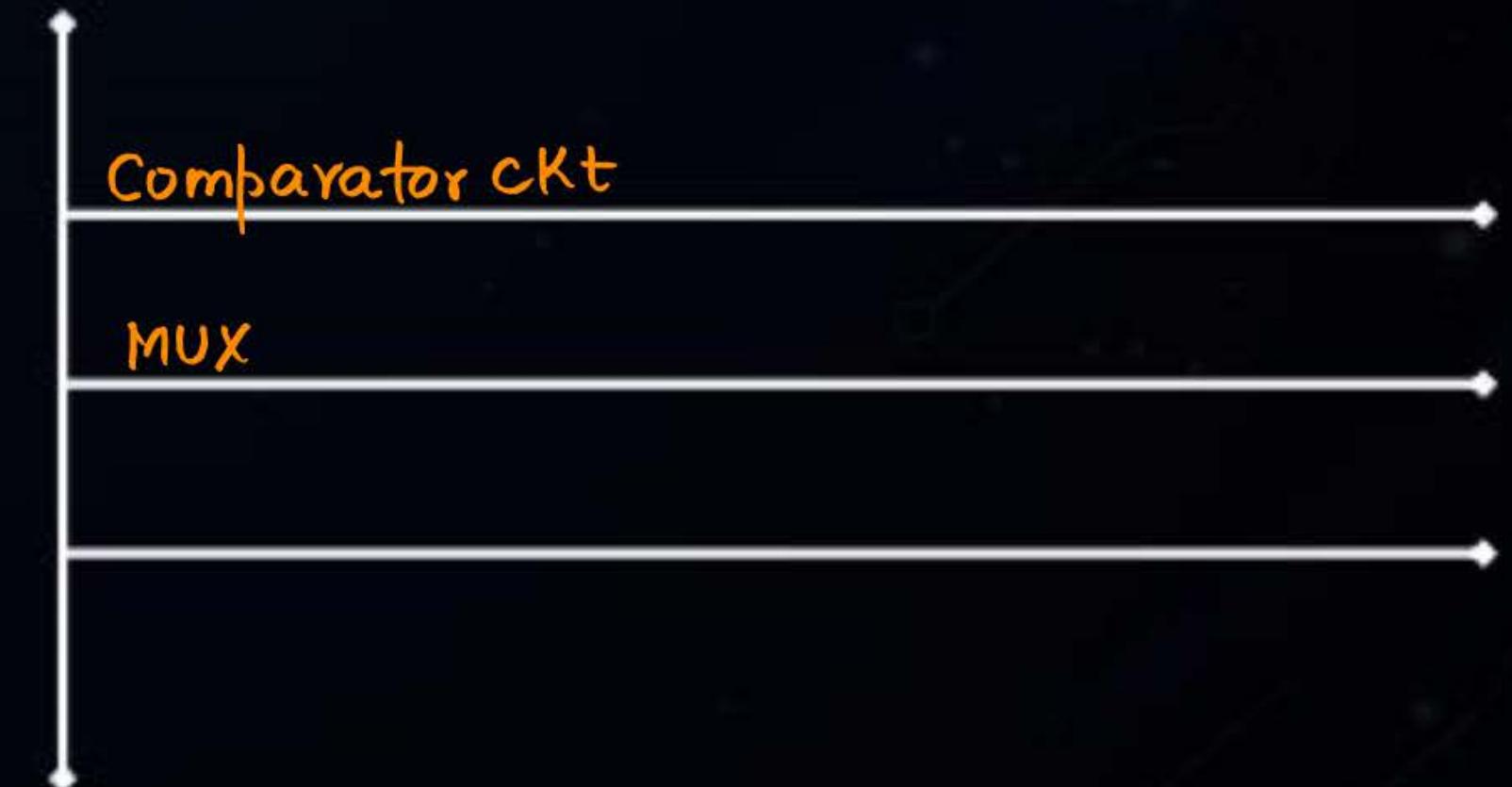
Combinational Circuit



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Recap of Previous Lecture





Topics to be Covered

MUX Cont.



(Higher order MUX using lower order MUX)

- $4:1 \xrightarrow{\text{Using } 2:1 \text{ MUX}} 2+1 = 3 = (2^2-1)$
 $2^2:1$
- $8:1 \text{ MUX} \xrightarrow{\text{Using } 2:1 \text{ MUX}} 4+2+1 = 7 = (2^3-1)$
 $2^3:1$
- $16:1 \text{ MUX} \xrightarrow{\text{Using } 2:1 \text{ MUX}} 8+4+2+1 = 15 = 2^4-1$
 $2^4:1$
- $2^n:1 \text{ MUX} \xrightarrow{\text{Using } 2:1 \text{ MUX}} (2^n-1)$

$$16:1 \xrightarrow{4:1} 4 + 1 = 5$$

$$256:1 \xrightarrow{4:1} 64 + 16 + 4 + 1 = 85$$

$$64:1 \xrightarrow{8:1} 8 + 1 = 9$$

$$32:1 \xrightarrow{4:1} 8 + 2 + 1(2:1)$$

\downarrow

$$10(4:1)$$

or
11 (4:1) MUX but one (4:1) MUX is
used as (2:1) MUX

$$256:1 \xrightarrow{8:1} 32 + 4$$

\downarrow

$$36(8:1) + 1(4:1) \text{ MUX}$$

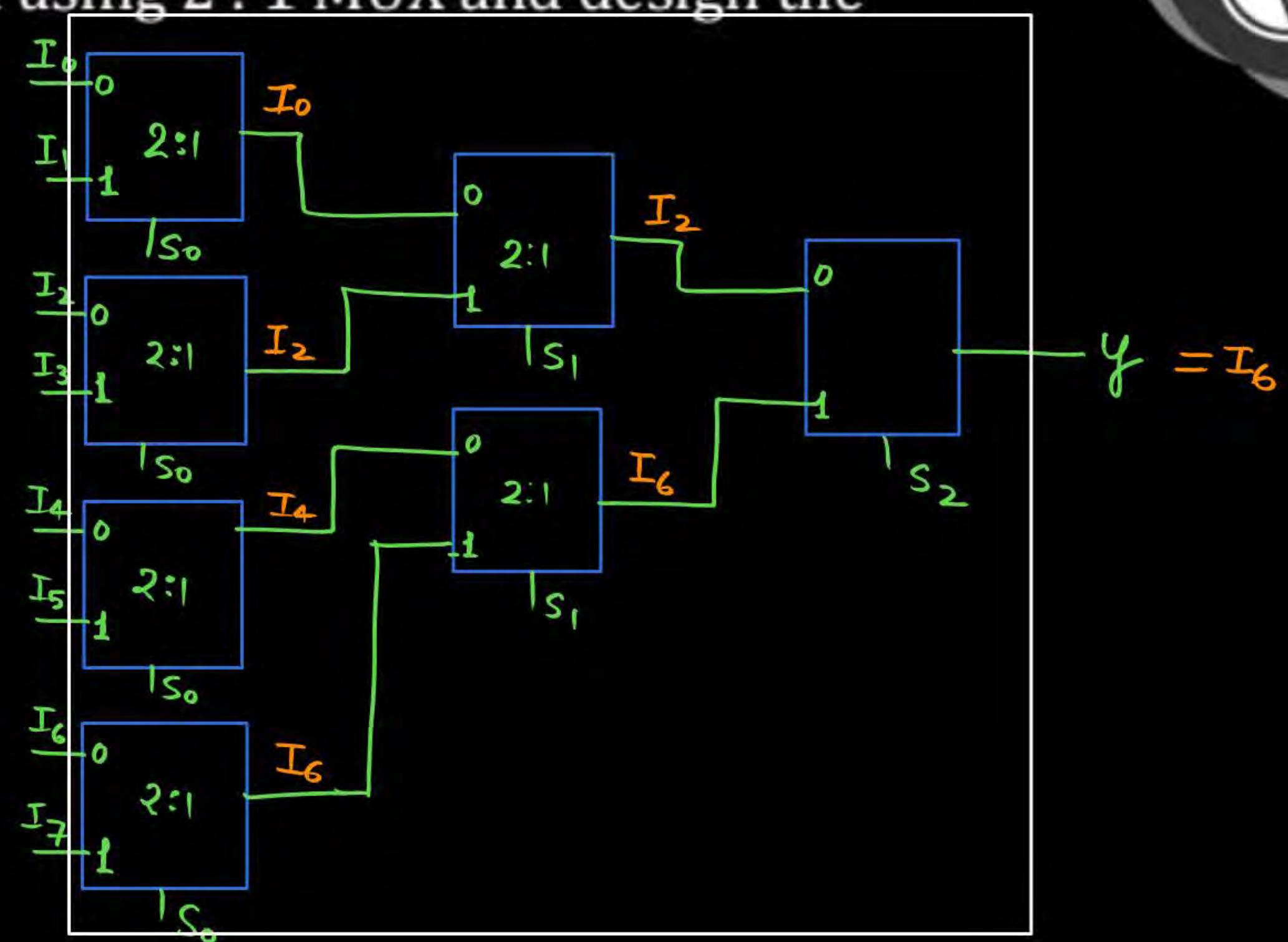
37 (8:1) or
but one (8:1) MUX is used as (4:1) MUX.

Implement 8 : 1 MUX using 2 : 1 MUX and design the complete circuit.

$I_0 - I_7$ → available
 S_2, S_1, S_0

8 : 1 $\xrightarrow{2:1}$ $4 + 2 + 1$

$S_2 S_1 S_0 = \underline{\underline{1}} \underline{\underline{1}} \underline{\underline{0}}$



$$16:1 \xrightarrow{4:1} 4+1$$

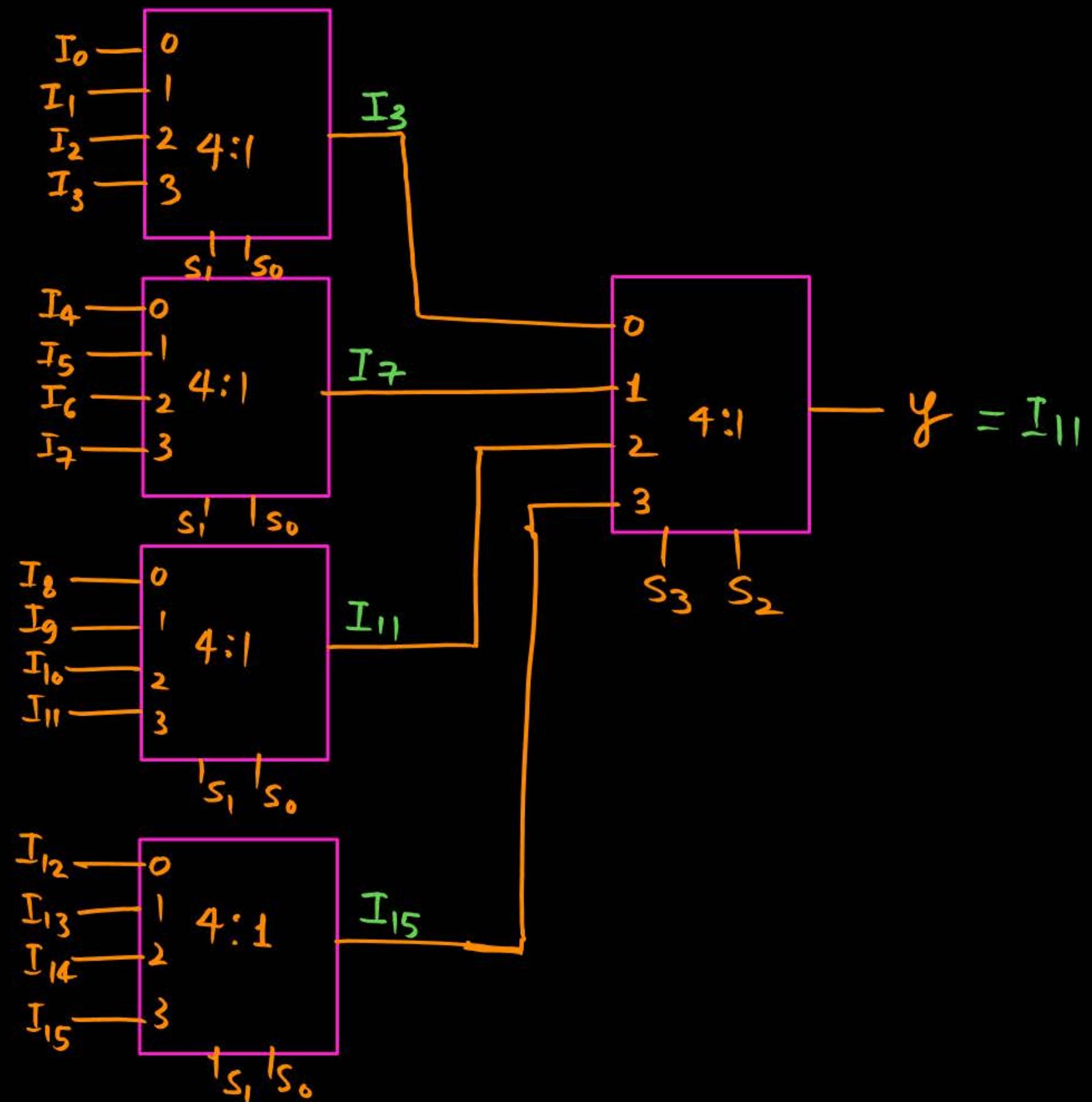
$(I_0 - I_{15})$

$S_3 S_2 S_1 S_0$

$$S_3 S_2 S_1 S_0 = (1011)$$

$$\downarrow$$

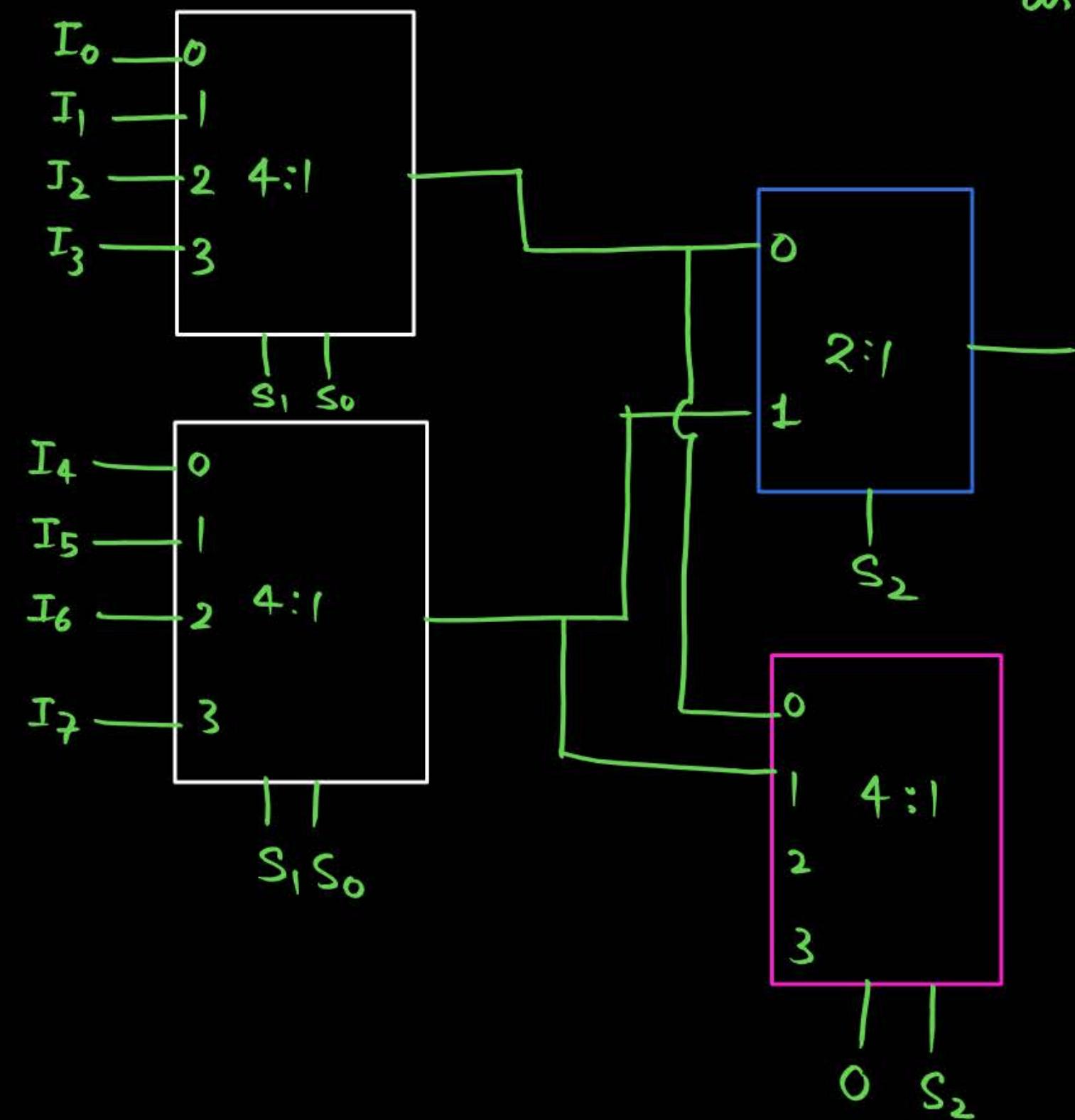
$$y = I_{11}$$



$8:1 \xrightarrow{4:1} 2(4:1) \text{ MUX} + 1(2:1)$ or $3(4:1)$ but one $4:1$ MUX will be used as $4:1$ MUX

$I_0 - I_7$

S_2, S_1, S_0



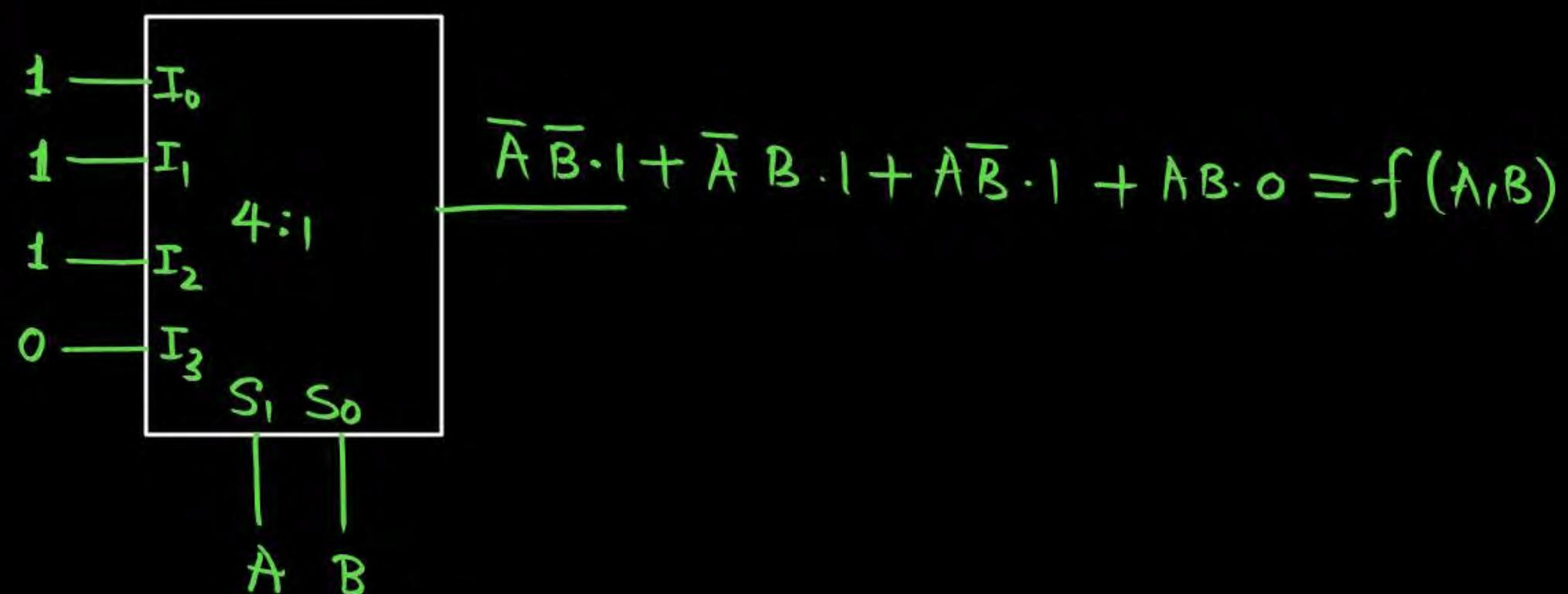
- $16 : 1 \text{ MUX} \xrightarrow{\text{Using } 8 : 1 \text{ MUX}} 2(8:1) + 1(2:1) \text{ MUX}$
 or
 $3(8:1)$
- $32 : 1 \text{ MUX} \xrightarrow{\text{Using } 4 : 1 \text{ MUX}} (8+2)$
 $10(4:1) \text{ MUX} + 1(2:1) \text{ MUX}$
 or
 $11(4:1) \text{ MUX}$

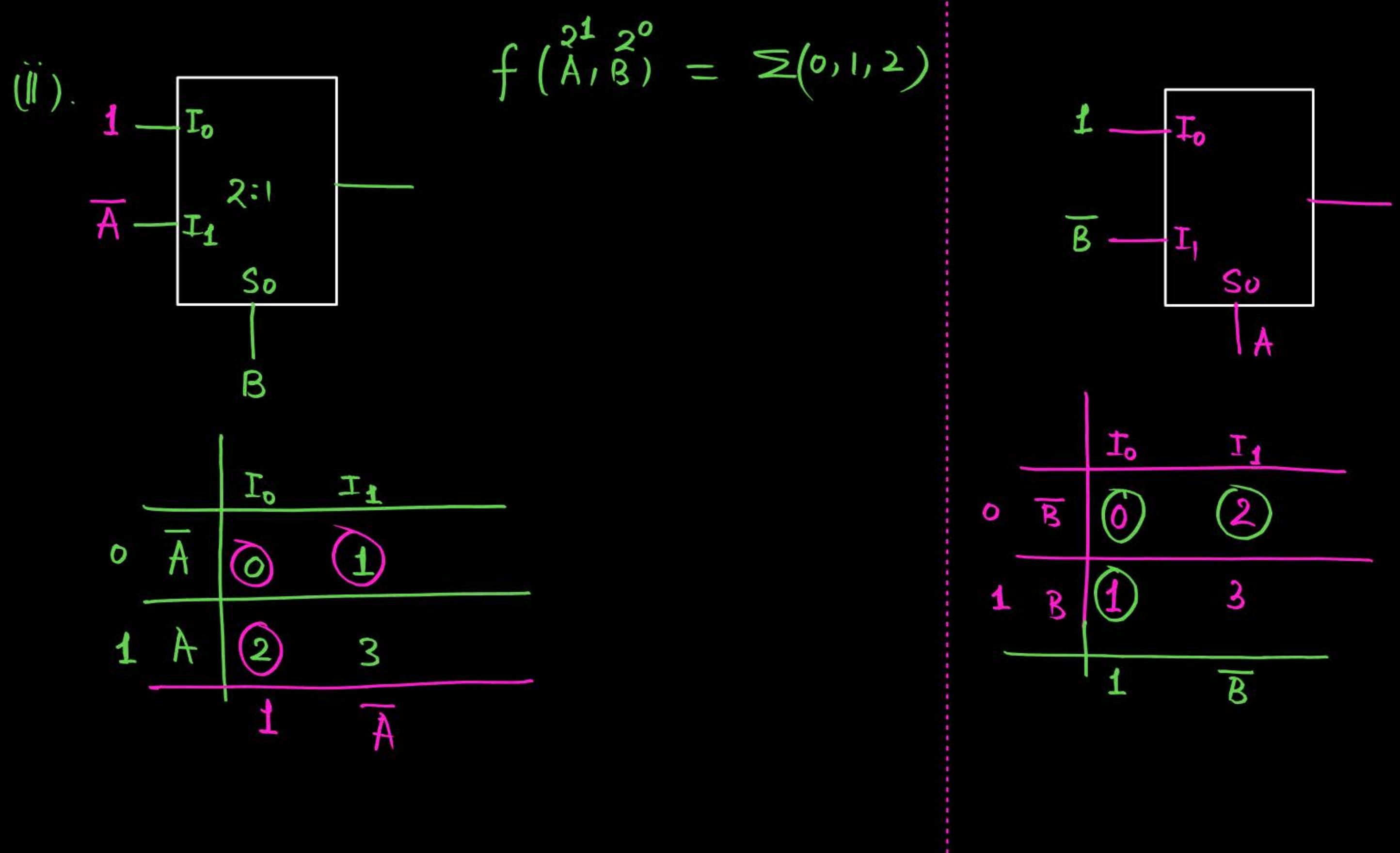
(Implementation of Boolean function using MUX)

Q. $f(A, B) = \Sigma(0, 1, 2) \rightarrow$ implement this logical function

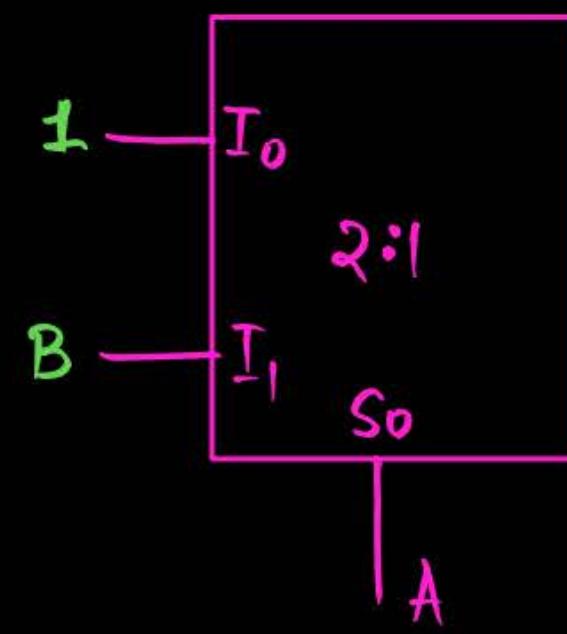
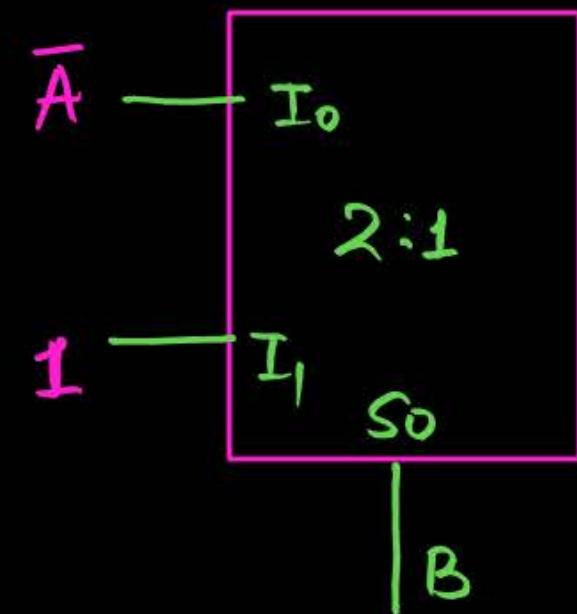
- (i) using 4 : 1 MUX
- (ii) using 2 : 1 MUX

(i).





$$\bullet f(\overset{2}{A}, B) = \sum(0, 1, 3)$$



	I_0	I_1
\bar{A}	0	1
A	2	3
\bar{A}		1

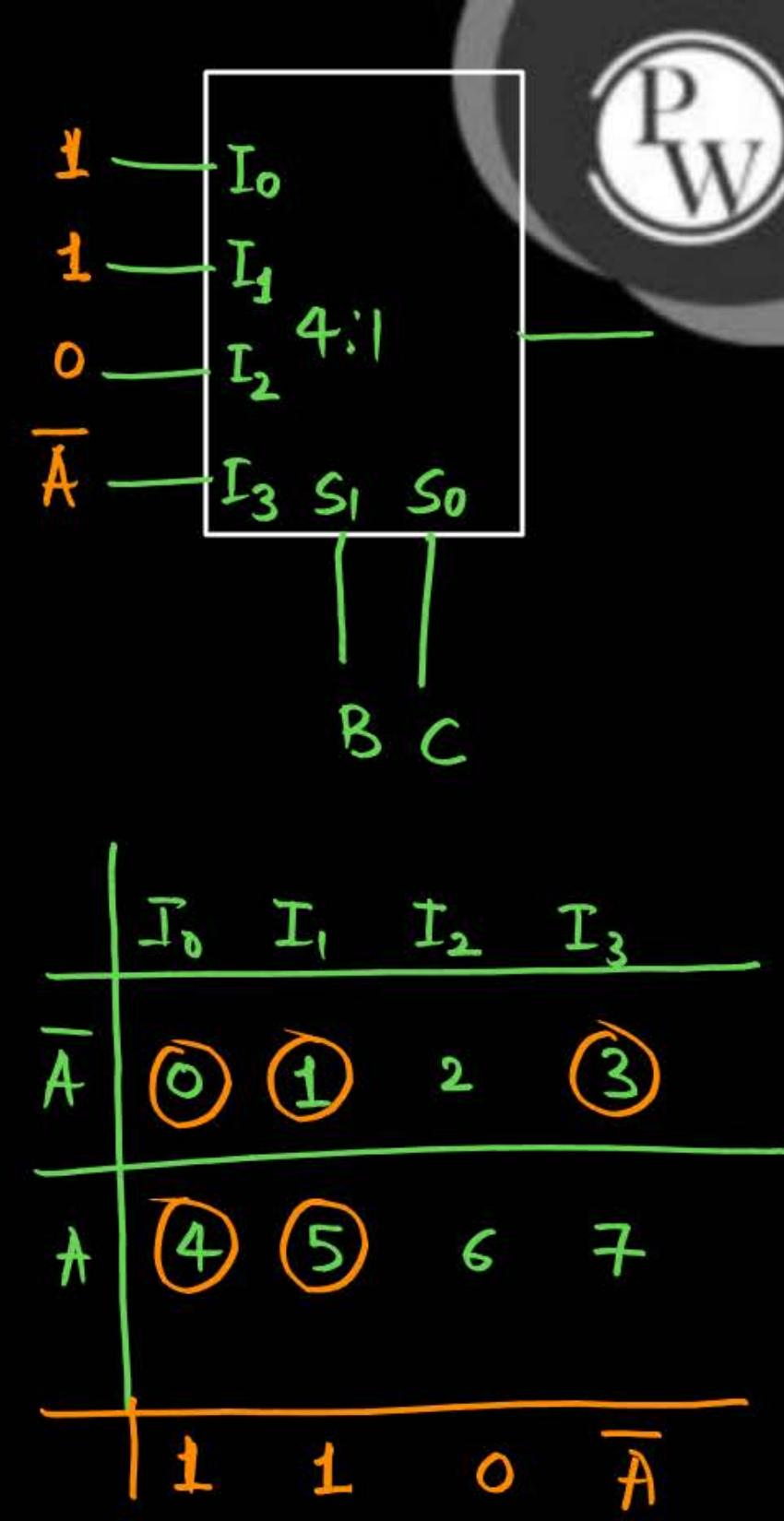
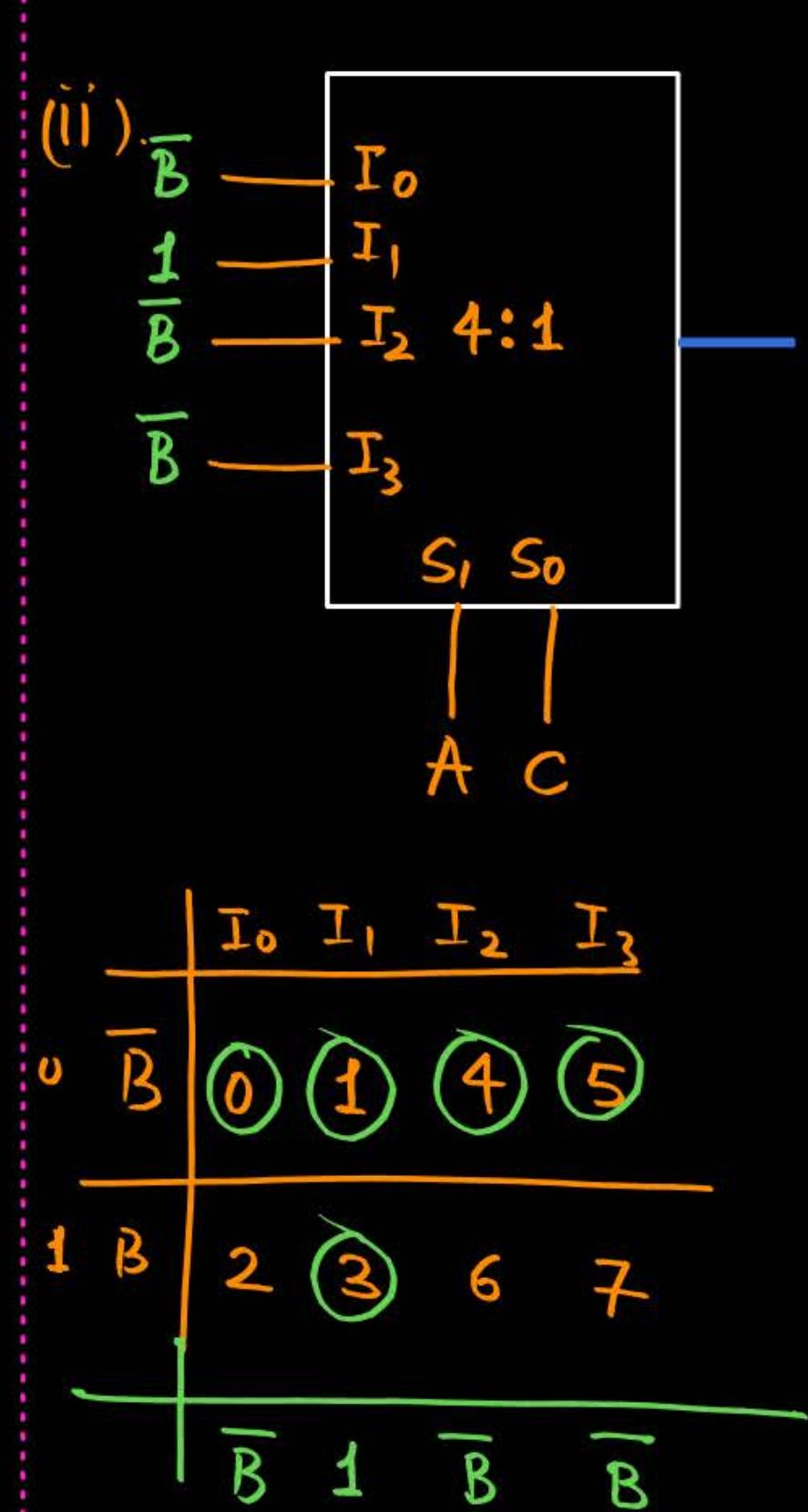
	I_0	I_1
\bar{B}	0	2
B	1	3
\bar{B}		1

$\bullet f(A, B, C) = \sum(0, 1, 3, 4, 5)$
 (i). 8:1
 (ii). 4:1
 (iii). 1:
 $f(0, B, 0) = \sum(0) = \overline{A} \overline{B} \overline{C}$
 $= \overline{B}$
 $I_0 = \overline{B}$

1	I_0
1	I_1
0	I_2
1	I_3
1	I_4
1	I_5
0	I_6
0	$I_7 S_2 S_1 S_0$

$f(A, B, C)$

$A \quad B \quad C$



$$f(A, B, C, D) = (A + \bar{C})(\bar{B} + \bar{D}) = \pi(2, 3, 5, 6, 7, 13, 15) = \sum_{(12, 14)} 0, 1, 4, 8, 9, 10, 11, P_W$$

to implement it using (4:1) MUX & A & D as select line.

$$A + \bar{C}$$

$$0 \ 0 \ 1 \ 0 \rightarrow 2$$

$$0 \ 0 \ 1 \ 1 \rightarrow 3$$

$$0 \ 1 \ 1 \ 0 \rightarrow 6$$

$$0 \ 1 \ 1 \ 1 \rightarrow 7$$

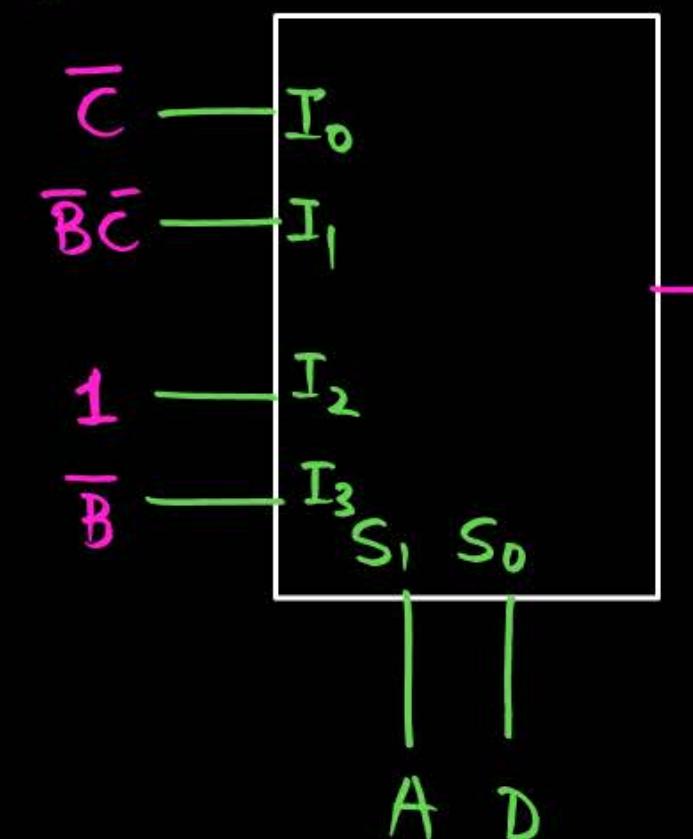
$$\bar{B} + \bar{D}$$

$$0 \ 1 \ 0 \ 1 \rightarrow 5$$

$$0 \ 1 \ 1 \ 1 \rightarrow 7$$

$$1 \ 1 \ 0 \ 1 \rightarrow 13$$

$$1 \ 1 \ 1 \ 1 \rightarrow 15$$



	I_0	I_1	I_2	I_3
$\bar{B}\bar{C}$	0	1	8	9
$\bar{B}C$	2	3	10	11
$B\bar{C}$	4	5	12	13
BC	6	7	14	15
	$\bar{B}\bar{C}$ + $B\bar{C}$	$\bar{B}\bar{C}$	1	\bar{B}
				$= \bar{C}$

$$f(0, B, C, 0) = \overline{C} , \quad I_0 = \overline{C}$$

$$f(0, B, C, 1) = \overline{B}\overline{C} , \quad I_1 = \overline{B}\overline{C}$$

$$f(1, B, C, 0) = 1 , \quad I_2 = 1$$

$$f(1, B, C, 1) = \overline{B} , \quad I_3 = \overline{B}$$



- H.W.
- Implement 16:1 MUX using 8:1 MUX
- Implement 32:1 MUX using 8:1 MUX.
- $f(A, B, C, D) = (\overline{A} + B + \overline{D})(A + \overline{C})$
 implement it using 4:1 MUX & B & C as select line.
- $f(A, B, C) = \overline{A}\overline{B} + BC$
 - (i) implement it using (2:1) MUX & A as select line
 - (ii) implement it using (4:1) MUX & A & C as select line.



2 Minute Summary

→ MUX

Thank you
GW
Soldiers!

