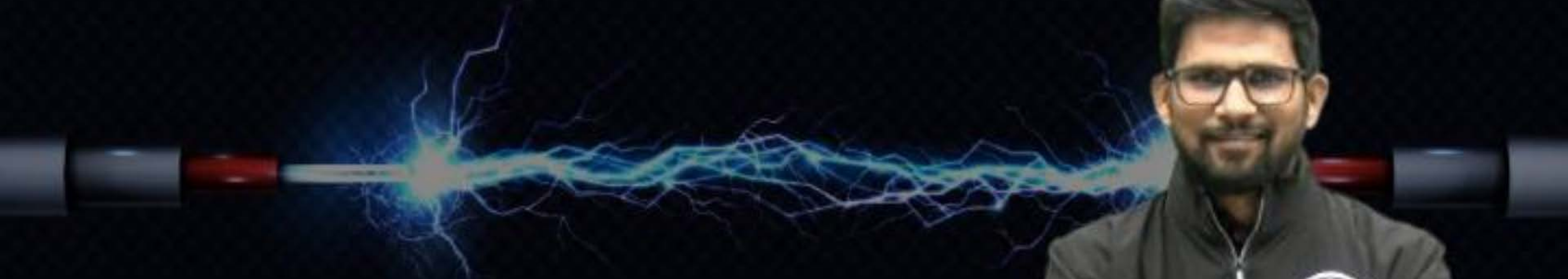


COMPUTER SCIENCE & IT

DIGITAL LOGIC



Lecture No. 08

Combinational Circuit



By- Chandan Gupta Sir



Recap of Previous Lecture

Comparator CKt

MUX



Topics to be Covered

MUX Cont.



[Higher order MUX using lower order MUX]

- $4 : 1$ $\xrightarrow{\text{Using } 2 : 1 \text{ MUX}}$ $2 + 1 = 3 = (2^2 - 1)$
 $2^2 : 1$
- $8 : 1 \text{ MUX}$ $\xrightarrow{\text{Using } 2 : 1 \text{ MUX}}$ $4 + 2 + 1 = 7 = (2^3 - 1)$
 $2^3 : 1$
- $16 : 1 \text{ MUX}$ $\xrightarrow{\text{Using } 2 : 1 \text{ MUX}}$ $8 + 4 + 2 + 1 = 15 = 2^4 - 1$
 $2^4 : 1$
- $2^n : 1 \text{ MUX}$ $\xrightarrow{\text{Using } 2 : 1 \text{ MUX}}$ $(2^n - 1)$

$$16:1 \xrightarrow{4:1} 4 + 1 = 5$$

$$256:1 \xrightarrow{4:1} 64 + 16 + 4 + 1 = 85$$

$$64:1 \xrightarrow{8:1} 8 + 1 = 9$$

$$32:1 \xrightarrow{4:1} \underbrace{8 + 2 + 1}_{10(4:1)} (2:1)$$

or

11(4:1) MUX but one(4:1) MUX is used as (2:1) MUX

$$256:1 \xrightarrow{8:1} \underbrace{32 + 4}_{36(8:1) + 1(4:1) \text{ MUX}}$$

or

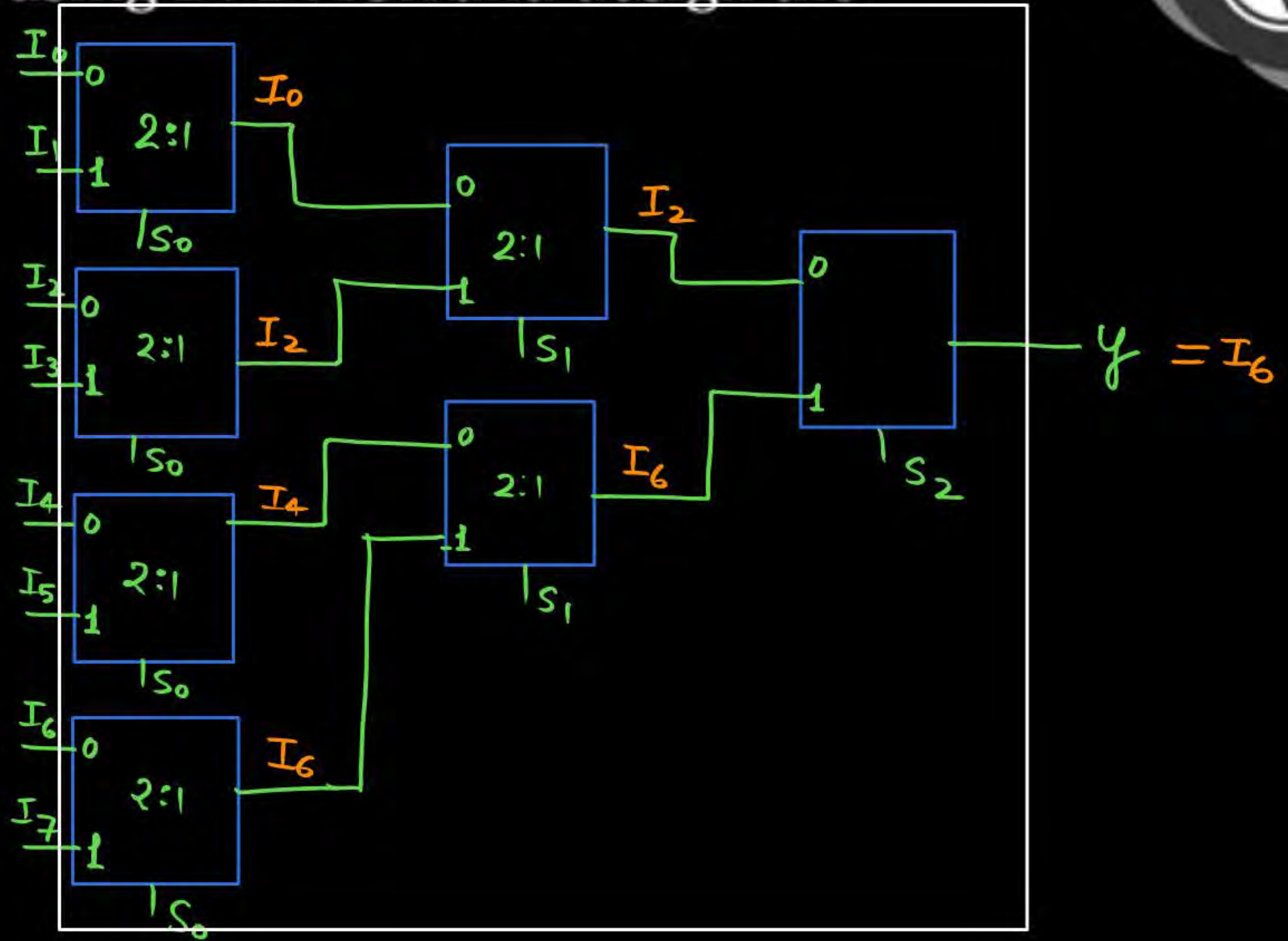
37(8:1) but one(8:1) MUX is used as (4:1) MUX.

Implement 8 : 1 MUX using 2 : 1 MUX and design the complete circuit.

$I_0 - I_7$ → available
 S_2, S_1, S_0

$8:1 \xrightarrow{2:1} 4+2+1$

S_2 S_1 S_0 = 1 1 0

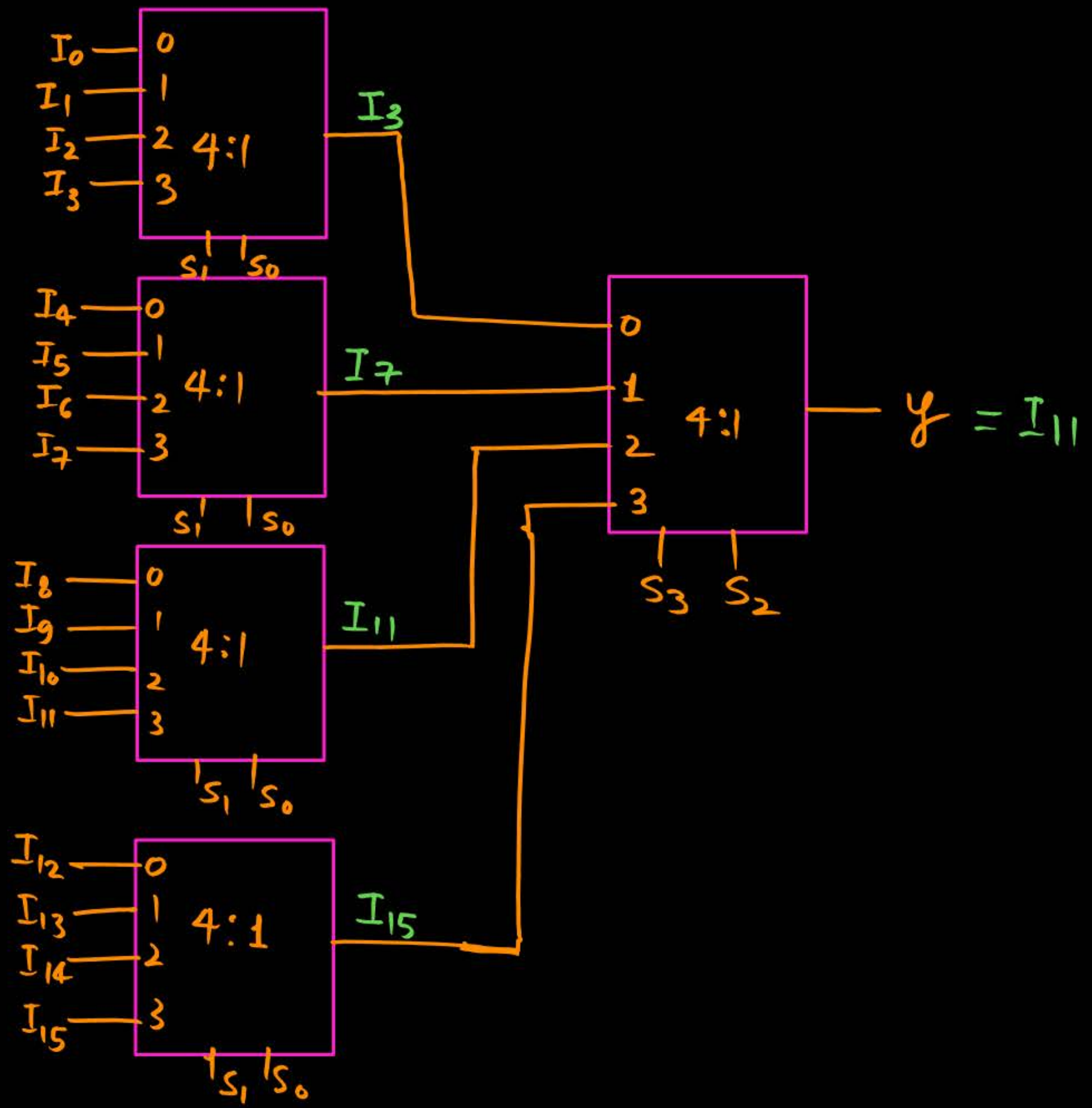




$16:1 \xrightarrow{4:1} 4+1$

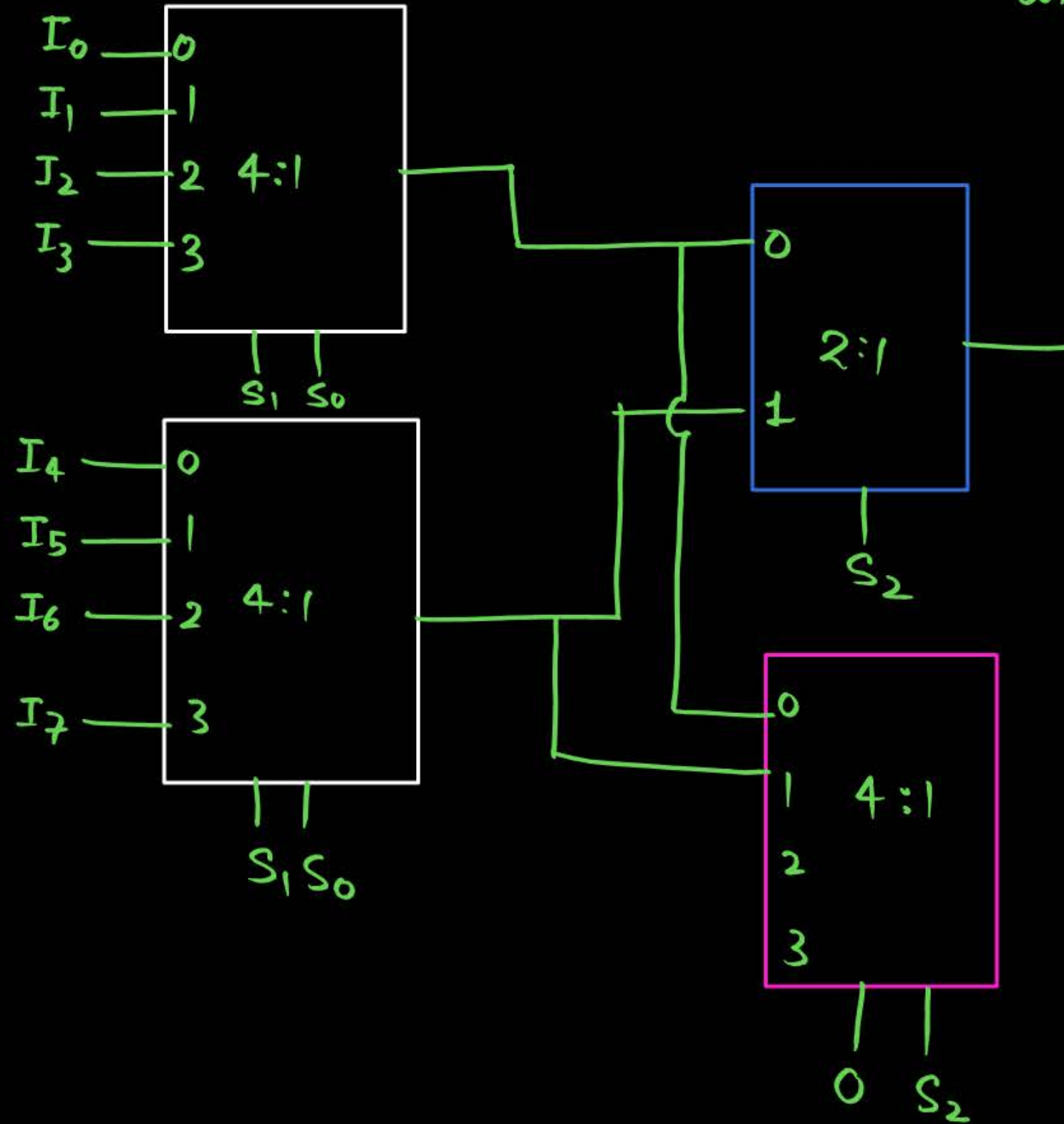
$(I_0 - I_{15})$
 $S_3 S_2 S_1 S_0$ } available
←

$S_3 S_2 S_1 S_0 = (1011)$
↓
 $y = I_{11}$



$8:1 \xrightarrow{4:1} 2(4:1) \text{ MUX} + 1(2:1) \text{ or } 3(4:1) \text{ but one } 4:1 \text{ MUX will be used as } 4:1 \text{ MUX}$

$I_0 - I_7$
 S_2, S_1, S_0



- 16 : 1 MUX $\xrightarrow{\text{Using 8 : 1 MUX}}$ $2(8:1) + 1(2:1)\text{MUX}$
 or
 $3(8:1)$

- 32 : 1 MUX $\xrightarrow{\text{Using 4 : 1 MUX}}$ $(8+2)$
 $10(4:1)\text{MUX} + 1(2:1)\text{MUX}$
 or
 $11(4:1)\text{MUX}$

Implementation of Boolean function using MUX

Q. $f(A, B) = \Sigma(0, 1, 2) \rightarrow$ implement this logical function

(i) using 4 : 1 MUX

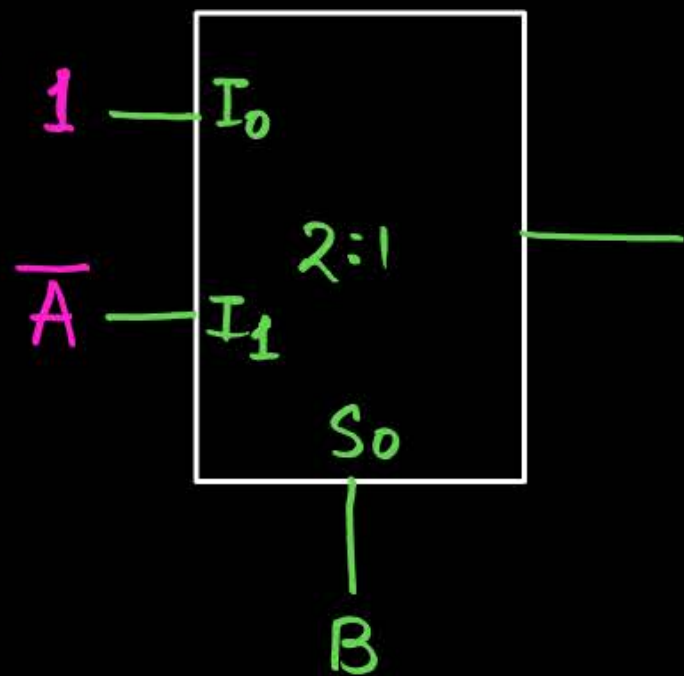
(ii) using 2 : 1 MUX

(i).

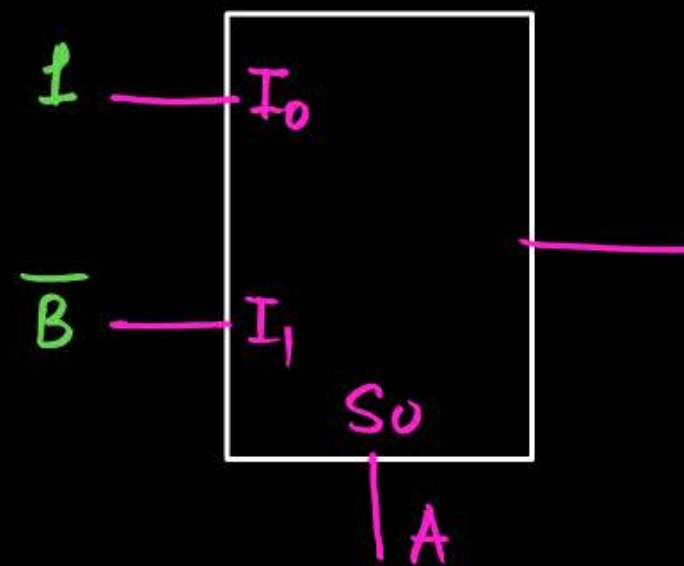


$$\bar{A}\bar{B}.1 + \bar{A}B.1 + A\bar{B}.1 + AB.0 = f(A, B)$$

(ii). $f(A, B) = \Sigma(0, 1, 2)$

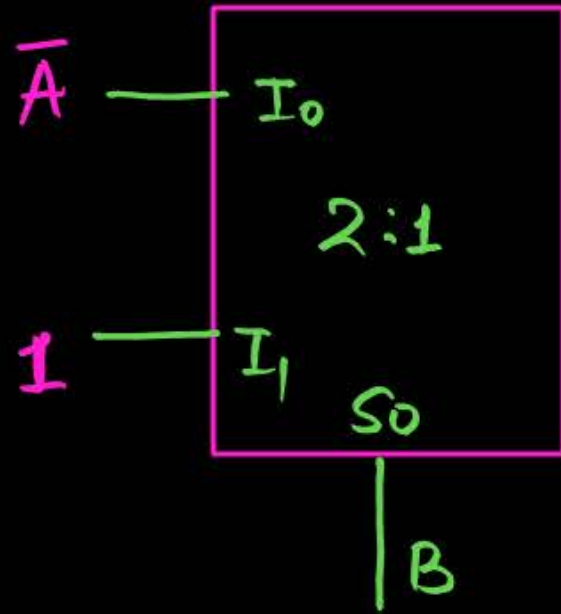


		I_0	I_1
0	\bar{A}	0	1
1	A	2	3
		1	\bar{A}

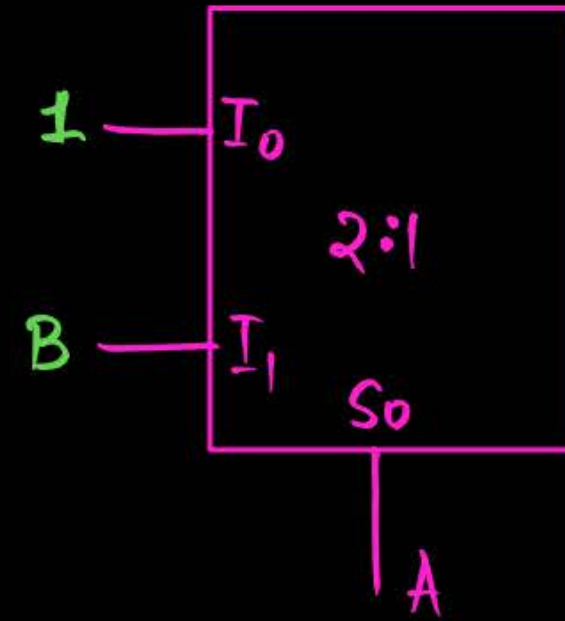


		I_0	I_1
0	\bar{B}	0	2
1	B	1	3
		1	\bar{B}

- $f(\overset{2'}{\bar{A}}, B) = \Sigma(0, 1, 3)$



	I_0	I_1
\bar{A}	(0)	(1)
A	2	(3)
	\bar{A}	1



	I_0	I_1
\bar{B}	(0)	2
B	(1)	(3)
	1	B



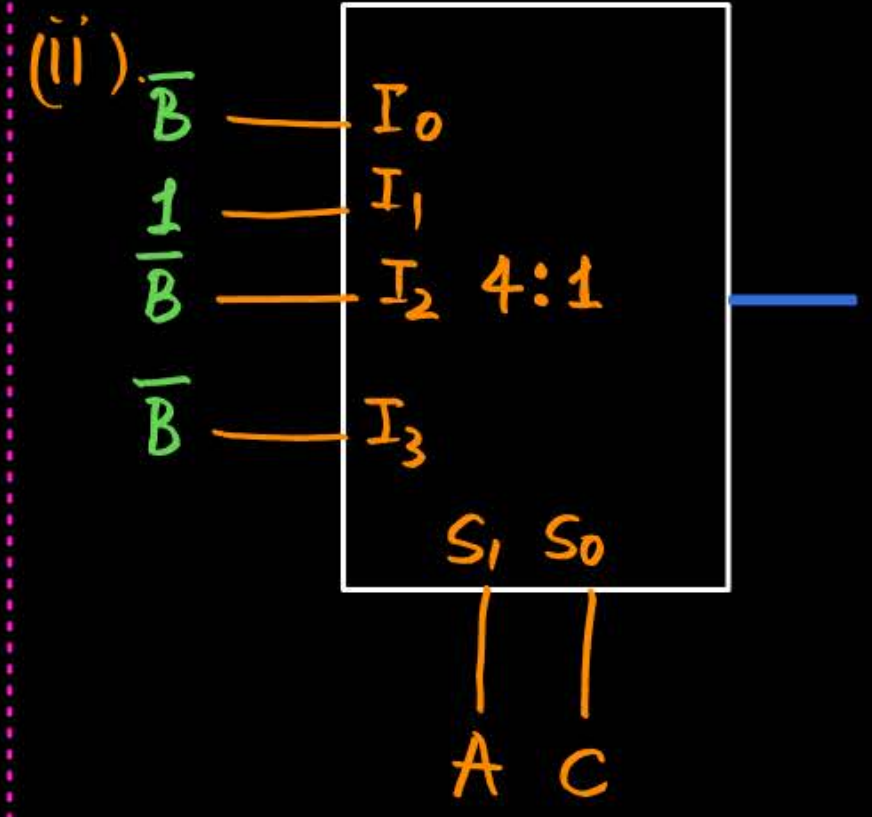
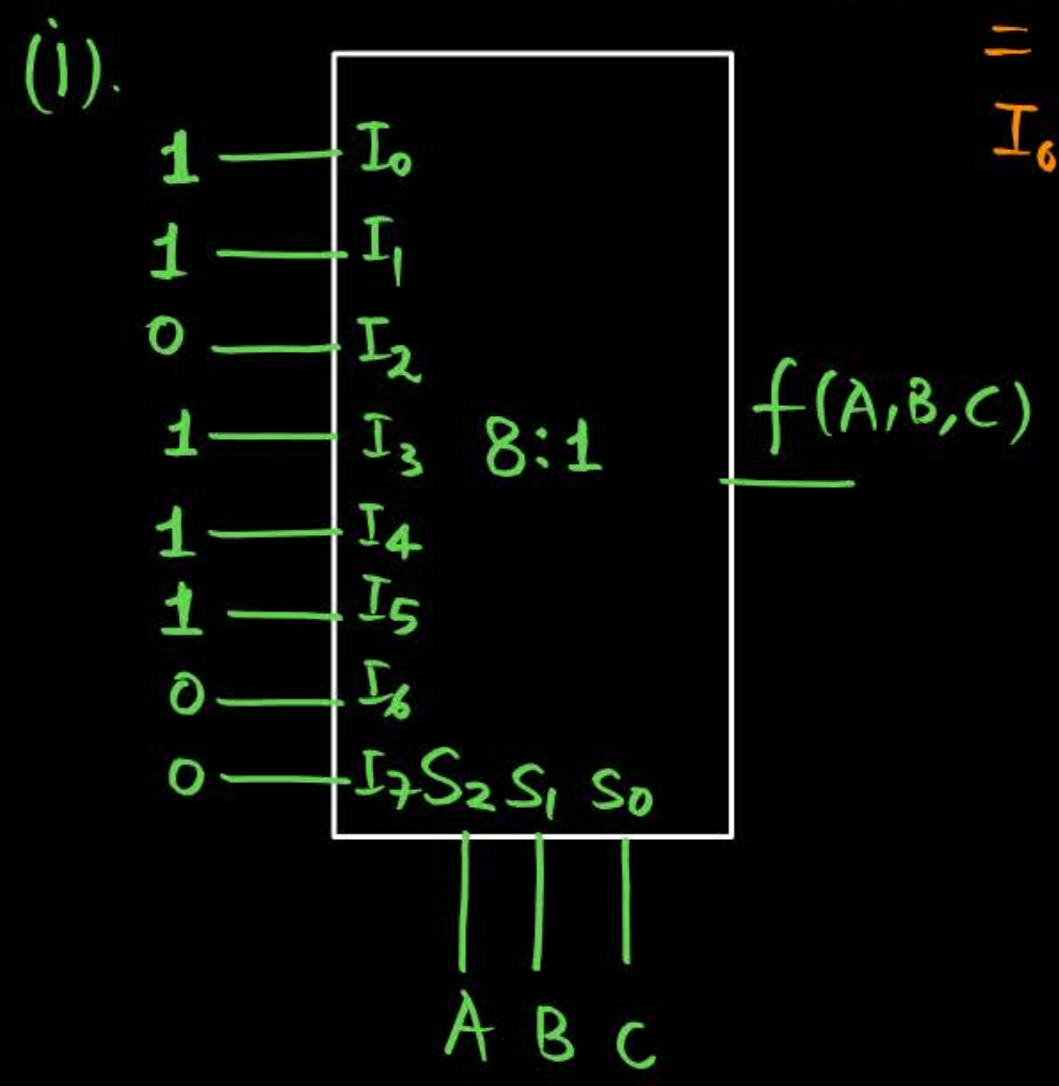
• $f(A, B, C) = \sum(0, 1, 3, 4, 5)$

(i). 8:1

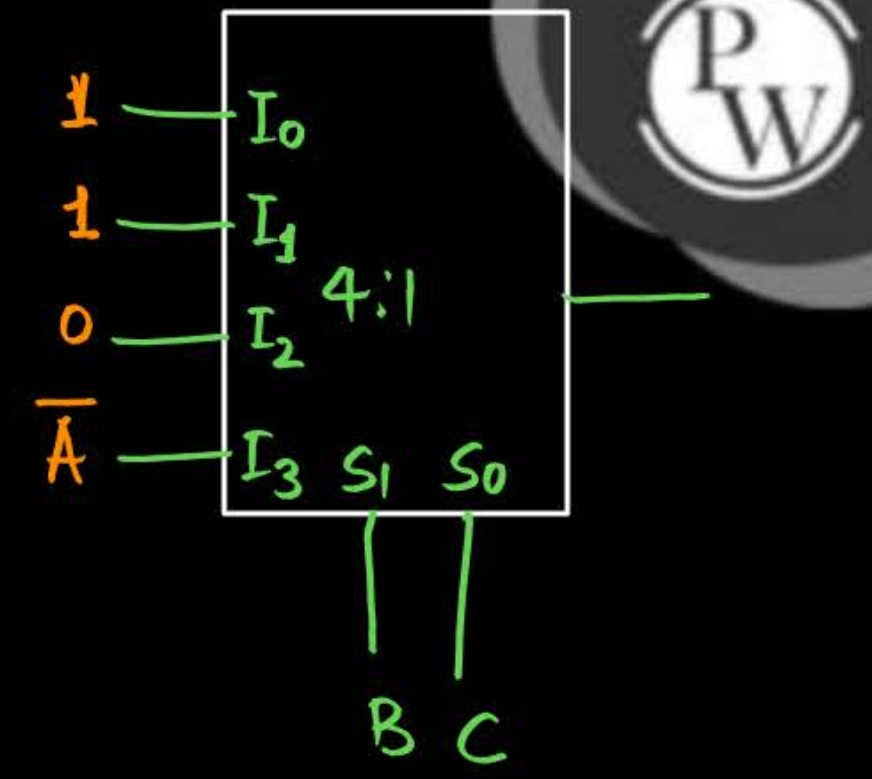
(ii). 4:1

$f(0, B, 0)$

$= \sum(0) = \overline{A} \overline{B} \overline{C}$
 $= \overline{B}$
 $I_0 = \overline{B}$



		I_0	I_1	I_2	I_3
0	\overline{B}	0	1	4	5
1	B	2	3	6	7
		\overline{B}	1	\overline{B}	\overline{B}



		I_0	I_1	I_2	I_3
\overline{A}		0	1	2	3
A		4	5	6	7
		1	1	0	\overline{A}



• $f(A, B, C, D) = (A + \bar{C})(\bar{B} + \bar{D}) = \pi(2, 3, 5, 6, 7, 13, 15) = \sum(0, 1, 4, 8, 9, 10, 11, 12, 14)$

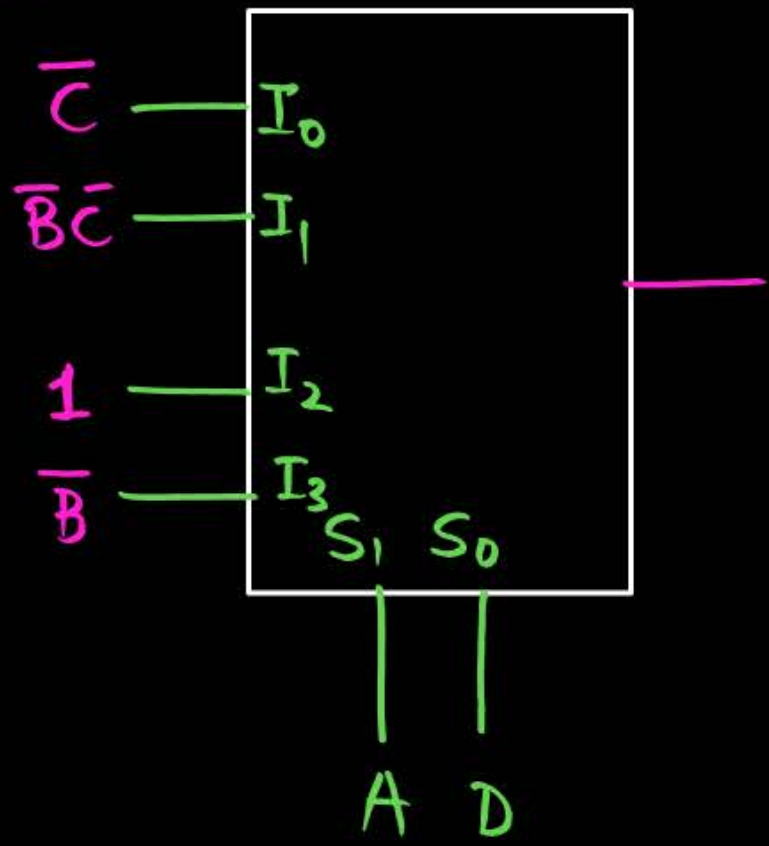
to implement it using (4:1) MUX & A & D as select line.

$A + \bar{C}$

0	0	1	0	→ 2
0	0	1	1	→ 3
0	1	1	0	→ 6
0	1	1	1	→ 7

$\bar{B} + \bar{D}$

0	1	0	1	→ 5
0	1	1	1	→ 7
1	1	0	1	→ 13
1	1	1	1	→ 15



	I ₀	I ₁	I ₂	I ₃
$\bar{B}\bar{C}$	0	1	8	9
$\bar{B}C$	2	3	10	11
$B\bar{C}$	4	5	12	13
BC	6	7	14	15
<hr/>				
	$\bar{B}\bar{C} + B\bar{C} = \bar{C}$	$\bar{B}\bar{C}$	1	\bar{B}

$$f(0, B, C, 0) = \overline{C} , \quad I_0 = \overline{C}$$

$$f(0, B, C, 1) = \overline{B} \overline{C} , \quad I_1 = \overline{B} \overline{C}$$

$$f(1, B, C, 0) = 1, \quad I_2 = 1$$

$$f(1, B, C, 1) = \overline{B} , \quad I_3 = \overline{B}$$

• H.W.

• Implement 16:1 MUX using 8:1 MUX

• Implement 32:1 MUX using 8:1 MUX.

• $f(A, B, C, D) = (\bar{A} + B + \bar{D})(A + \bar{C})$

Implement it using 4:1 MUX & B & C as select line.

• $f(A, B, C) = \bar{A}\bar{B} + BC$

(i) Implement it using (2:1) MUX & A as select line

(ii) Implement it using (4:1) MUX & A & C as select line.



2 Minute Summary

→ MUX

Thank you

GW
Soldiers !

