

**MATH 239 — Assignment 1, Question 2**

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a) I am mapping the vertices of graph  $G$  onto graph  $H$

$x$	$f(x)$
1	$P$
2	$R$
3	$O$
4	$D$
5	$U$
6	$C$
7	$T$
8	$I$
9	$V$
10	$E$
11	$L$
12	$Y$

b) We see that in graph  $H$ , there exist five vertices of degree 3. For these five vertices, we see that:

- Vertex  $O$  has neighbours with degree  $\{3, 3, 4\}$
- Vertex  $T$  has neighbours with degree  $\{3, 4, 5\}$
- Vertex  $E$  has neighbours with degree  $\{2, 3, 3\}$
- Vertex  $L$  has neighbours with degree  $\{3, 3, 5\}$
- Vertex  $Y$  has neighbours with degree  $\{2, 3, 4\}$

Now, in graph  $J$ , we see that vertex  $f$  is also degree 3; however, the respective degrees of its neighbours are  $\{2, 3, 5\}$ , which is not found for any third-degree vertex in graph  $H$ , thus  $H$  and  $J$  are non-isomorphic.