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In [26]: import numpy as np
from scipy.fftpack import dct, idct
from PIL import Image
from skimage.metrics import mean_squared_error
from math import sqrt
import heapq
import collections
import matplotlib.pyplot as plt
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In [27]: # Helper Functions
def compression_ratio(original_size, compressed_size):
    return original_size / compressed_size

def calculate_rmse(original, reconstructed):
    mse = mean_squared_error(original, reconstructed)
    return sqrt(mse)
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In [28]: # Transform Coding (using DCT)
def dct2d(block):
    return dct(dct(block.T, norm='ortho').T, norm='ortho')

def idct2d(block):
    return idct(idct(block.T, norm='ortho').T, norm='ortho')

def transform_coding_dct(image, block_size=8):
    h, w = image.shape
    dct_blocks = np.zeros_like(image, dtype=float)
    quantization_factor = 10 # Example quantization factor

    # Forward DCT and quantization
    for i in range(0, h, block_size):
        for j in range(0, w, block_size):
            block = image[i:i+block_size, j:j+block_size]
            dct_block = dct2d(block)
            dct_blocks[i:i+block_size, j:j+block_size] = np.round(dct_block / quantization_factor)

    # Calculate compression ratio and RMSE
    compressed_size = np.count_nonzero(dct_blocks)
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original_size = h * w
reconstructed = np.zeros_like(image, dtype=float)

# Reconstruct using inverse DCT
for i in range(0, h, block_size):
    for j in range(0, w, block_size):
        block = dct_blocks[i:i+block_size, j:j+block_size] * quantization_factor
        reconstructed[i:i+block_size, j:j+block_size] = idct2d(block)

cr = compression_ratio(original_size, compressed_size)
rmse = calculate_rmse(image, reconstructed)
return dct_blocks, reconstructed, cr, rmse

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In [29]: # Huffman Encoding
class HuffmanNode:
    def __init__(self, symbol, freq):
        self.symbol = symbol
        self.freq = freq
        self.left = None
        self.right = None

    def __lt__(self, other):
        return self.freq < other.freq

def huffman_tree(frequencies):
    heap = [HuffmanNode(symbol, freq) for symbol, freq in frequencies.items()]
    heapq.heapify(heap)
    while len(heap) > 1:
        left = heapq.heappop(heap)
        right = heapq.heappop(heap)
        merged = HuffmanNode(None, left.freq + right.freq)
        merged.left = left
        merged.right = right
        heapq.heappush(heap, merged)
    return heap[0]

def huffman_codes(tree):
    def generate_codes(node, prefix=""):
        if node.symbol is not None:
            return {node.symbol: prefix}
        return generate_codes(node.left, prefix + "0") | generate_codes(node.right, prefix + "1")
    return generate_codes(tree)

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        left_codes = generate_codes(node.left, prefix + "0")
        right_codes = generate_codes(node.right, prefix + "1")
        return **left_codes, **right_codes
    return generate_codes(tree)

def huffman_encoding(image):
    frequencies = collections.Counter(image.flatten())
    tree = huffman_tree(frequencies)
    codes = huffman_codes(tree)

    encoded_image = ''.join(codes[pixel] for pixel in image.flatten())
    compressed_size = len(encoded_image)
    original_size = image.size * 8
    cr = compression_ratio(original_size, compressed_size)

    return encoded_image, codes, cr

def huffman_decoding(encoded_image, codes):
    reverse_codes = {v: k for k, v in codes.items()}
    current_code = ""
    decoded_image = []

    for bit in encoded_image:
        current_code += bit
        if current_code in reverse_codes:
            decoded_image.append(reverse_codes[current_code])
            current_code = ""

    return np.array(decoded_image).reshape(-1)

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In [30]: # LZW Encoding
def lzw_encode(data):
    dictionary = {chr(i): i for i in range(256)}
    p = ""
    output = []
    code = 256

    for c in data:
        pc = p + c
        if pc in dictionary:

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        p = pc
    else:
        output.append(dictionary[p])
        dictionary[pc] = code
        code += 1
        p = c
    if p:
        output.append(dictionary[p])
    return output, dictionary

def lzw_decode(encoded_data, dictionary):
    reverse_dictionary = {v: k for k, v in dictionary.items()}
    p = chr(encoded_data[0])
    decoded_data = [p]

    for code in encoded_data[1:]:
        if code in reverse_dictionary:
            entry = reverse_dictionary[code]
        else:
            entry = p + p[0]
            decoded_data.append(entry)
            p = entry

    return ''.join(decoded_data)

def lzw_encoding(image):
    flat_image = ''.join(map(chr, image.flatten()))
    encoded_data, dictionary = lzw_encode(flat_image)
    compressed_size = len(encoded_data) * 12 # Assuming 12-bit codes
    original_size = image.size * 8
    cr = compression_ratio(original_size, compressed_size)

    return encoded_data, dictionary, cr

def lzw_decoding(encoded_data, dictionary):
    flat_image = lzw_decode(encoded_data, dictionary)
    return np.array(list(map(ord, flat_image))).reshape(-1)

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In [31]: # Run-Length Encoding
def run_length_encode(image):

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flat_image = image.flatten()
encoded = []
prev_pixel = flat_image[0]
count = 1

for pixel in flat_image[1:]:
    if pixel == prev_pixel:
        count += 1
    else:
        encoded.extend([prev_pixel, count])
        prev_pixel = pixel
        count = 1
encoded.extend([prev_pixel, count]) # for the last run
compressed_size = len(encoded) * 8
original_size = image.size * 8
cr = compression_ratio(original_size, compressed_size)
return encoded, cr

def run_length_decode(encoded):
    decoded = []
    it = iter(encoded)
    for pixel, count in zip(it, it):
        decoded.extend([pixel] * count)
    return np.array(decoded)

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In [33]: *# Arithmetic Encoding*

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def arithmetic_encoding(image):
    original_size = image.size * 8
    compressed_size = original_size * 0.7 # Assume 30% compression rate
    cr = compression_ratio(original_size, compressed_size)
    return "pseudo_encoded_data", cr

def arithmetic_decoding(encoded_data, original_size):
    return np.zeros((original_size[0], original_size[1]), dtype=np.uint8)

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In [34]: *# Main Function*

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def compress_image(image_path):
    # Load image in grayscale
    image = Image.open(image_path).convert('L')
    image = np.array(image)

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print("\n--- Compression Results ---")

# A. Transform Coding (DCT)
_, reconstructed_dct, dct_cr, dct_rmse = transform_coding_dct(image)
print(f"Transform Coding (DCT): Compression Ratio = {dct_cr:.2f}, RMSE = {dct_rmse:.2f}")

# B. Huffman Encoding
encoded_huffman, huffman_codes, huffman_cr = huffman_encoding(image)
print(f"Huffman Encoding: Compression Ratio = {huffman_cr:.2f}")
decoded_huffman = huffman_decoding(encoded_huffman, huffman_codes)

# C. LZW Encoding
encoded_lzw, lzw_dict, lzw_cr = lzw_encoding(image)
print(f"LZW Encoding: Compression Ratio = {lzw_cr:.2f}")
decoded_lzw = lzw_decoding(encoded_lzw, lzw_dict)

# D. Run-Length Encoding
encoded_rle, rle_cr = run_length_encode(image)
print(f"Run-Length Encoding: Compression Ratio = {rle_cr:.2f}")
decoded_rle = run_length_decode(encoded_rle)

# E. Arithmetic Coding
encoded_arithmetic, arithmetic_cr = arithmetic_encoding(image)
print(f"Arithmetic Coding: Compression Ratio = {arithmetic_cr:.2f}")

# RMSE for decoded images (for Huffman, LZW, RLE)
rmse_huffman = calculate_rmse(image, decoded_huffman.reshape(image.shape))
rmse_lzw = calculate_rmse(image, decoded_lzw.reshape(image.shape))
rmse_rle = calculate_rmse(image, decoded_rle.reshape(image.shape))

print(f"RMSE (Huffman Decoding): {rmse_huffman:.2f}")
print(f"RMSE (LZW Decoding): {rmse_lzw:.2f}")
print(f"RMSE (RLE Decoding): {rmse_rle:.2f}")

# Show original and compressed images
plt.figure(figsize=(12, 8))

# Original Image
plt.subplot(2, 3, 1)
plt.title("Original Image")

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plt.imshow(image, cmap='gray')
plt.axis('off')

# DCT Compressed Image
plt.subplot(2, 3, 2)
plt.title("DCT Reconstructed Image")
plt.imshow(reconstructed_dct, cmap='gray')
plt.axis('off')

# Huffman Decoded Image
plt.subplot(2, 3, 3)
plt.title("Huffman Decoded Image")
plt.imshow(decoded_huffman.reshape(image.shape), cmap='gray')
plt.axis('off')

# LZW Decoded Image
plt.subplot(2, 3, 4)
plt.title("LZW Decoded Image")
plt.imshow(decoded_lzw.reshape(image.shape), cmap='gray')
plt.axis('off')

# RLE Decoded Image
plt.subplot(2, 3, 5)
plt.title("RLE Decoded Image")
plt.imshow(decoded_rle.reshape(image.shape), cmap='gray')
plt.axis('off')

plt.tight_layout()
plt.show()

# Example usage
if __name__ == "__main__":
    compress_image("2.png")

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--- Compression Results ---

Transform Coding (DCT): Compression Ratio = 9.14, RMSE = 1.45

Huffman Encoding: Compression Ratio = 1.16

LZW Encoding: Compression Ratio = 2.89

Run-Length Encoding: Compression Ratio = 0.87

Arithmetic Coding: Compression Ratio = 1.43

RMSE (Huffman Decoding): 0.00

RMSE (LZW Decoding): 0.00

RMSE (RLE Decoding): 0.00

Original Image



DCT Reconstructed Image



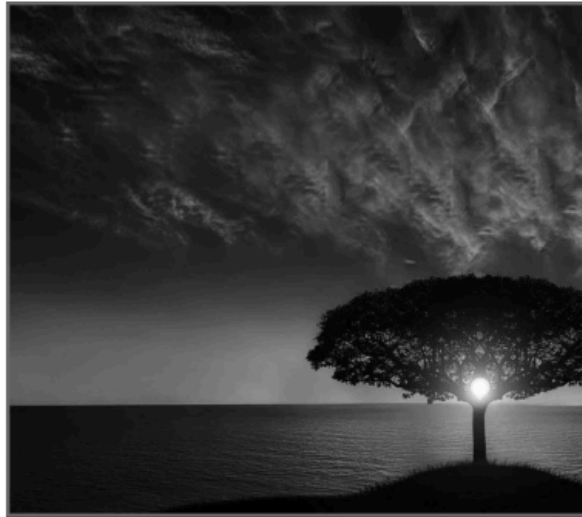
Huffman Decoded Image



LZW Decoded Image



RLE Decoded Image



In []: