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Lines and Planes

Problem Statement

Find the equations of the lines which intercepts on the both the axes and whose sum and product are 1 and -6 respectively.

Solution

The intercept form of a straight line is given by

$$\begin{bmatrix} \frac{1}{a} & \frac{1}{b} \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = 1$$
: where a and b are x and y intercepts respectively (1)

Given data in problem statement : a + b = 1 and ab = -6

Upon solving for a and b we get the set of values as (3,-2) and (-2,3)

From (1) the equations of straight line are

$$-2x + 3y = -6$$
 and $3x - 2y = -6$

In matrix form it can be written as

$$\begin{bmatrix} -2 & 3 \\ 3 & -2 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -6 \\ -6 \end{bmatrix} \tag{2}$$