## EE5609 Assignment 1

## SHANTANU YADAV

The python solution code is available at

https://github.com/Shantanu2508/ assignment-1/blob/master/stline.py

and latex codes from

https://github.com/Shantanu2508/assignment-1/blob/master/assignment1.tex

## 1 Problem

Find the equations of the lines which intercepts on the both the axes and whose sum and product are 1 and -6 respectively.

## 2 Solution

The equation of line in terms of vector notations can be written as

$$\mathbf{n}^T \mathbf{x} = c \tag{2.0.1}$$

Let the intercepts be  $\begin{pmatrix} a \\ 0 \end{pmatrix}$  and  $\begin{pmatrix} 0 \\ b \end{pmatrix}$ , respectively. Given that: a+b=1, and ab=-6

The quadratic equation whose roots are the x and y intercepts can be written as:

$$x^2$$
 – (sum of roots) $x$  + (product of roots) = 0 (2.0.2)

$$\implies x^2 - x - 6 = 0 \tag{2.0.3}$$

$$\implies x = (3, -2) \tag{2.0.4}$$

and corresponding y intercepts are (-2,3).

The line L1 passes through  $\begin{pmatrix} 3 \\ 0 \end{pmatrix}$  and  $\begin{pmatrix} 0 \\ -2 \end{pmatrix}$ . Let direction vector of this line be **m**.

 $\begin{pmatrix} 0 \end{pmatrix} \begin{pmatrix} 3 \end{pmatrix} \begin{pmatrix} -3 \end{pmatrix}$ 

$$\mathbf{m} = \begin{pmatrix} 0 \\ -2 \end{pmatrix} - \begin{pmatrix} 3 \\ 0 \end{pmatrix} = \begin{pmatrix} -3 \\ -2 \end{pmatrix} \tag{2.0.5}$$

The normal vector, **n**:

$$\mathbf{n} = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \mathbf{m} = \begin{pmatrix} 2 \\ -3 \end{pmatrix} \tag{2.0.6}$$

The equation of line in terms of normal vector and passing through a point *A* is

$$\mathbf{n}^{\mathbf{T}}(\mathbf{x} - A) = 0 \implies \mathbf{n}^{\mathbf{T}}\mathbf{x} = \mathbf{n}^{\mathbf{T}}A \quad (2.0.7)$$

$$\implies \mathbf{n}^{\mathbf{T}}\mathbf{x} = (2 - 3) \begin{pmatrix} 3 \\ 0 \end{pmatrix} \quad (2.0.8)$$

$$\implies (2-3)\mathbf{x} = 6 \quad (2.0.9)$$

Similarly, the equation of second line L2, with x and y intercepts  $\begin{pmatrix} -2 \\ 0 \end{pmatrix}$  and  $\begin{pmatrix} 0 \\ 3 \end{pmatrix}$  and normal vector  $\begin{pmatrix} -3 \\ 2 \end{pmatrix}$  is

$$(-3 \ 2)\mathbf{x} = 6$$
 (2.0.10)

The equations of lines (2.0.9) and (2.0.10) can be represented collectively as

$$\begin{pmatrix} 2 & -3 \\ -3 & 2 \end{pmatrix} \mathbf{x} = \begin{pmatrix} 6 \\ 6 \end{pmatrix} \tag{2.0.11}$$

<i>x</i> -intercept	y-intercept	n
$\begin{pmatrix} 3 \\ 0 \end{pmatrix}$	$\begin{pmatrix} 0 \\ -2 \end{pmatrix}$	$\begin{pmatrix} 2 \\ -3 \end{pmatrix}$
$\begin{pmatrix} -2 \\ 0 \end{pmatrix}$	$\begin{pmatrix} 0 \\ 3 \end{pmatrix}$	$\begin{pmatrix} -3 \\ 2 \end{pmatrix}$

TABLE 0

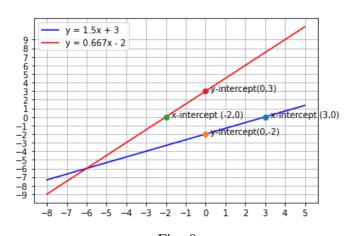


Fig. 0