

AI 1103 Assignment-1

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Download all python codes from here

<https://github.com/>

and latex-tikz codes from

<https://gi>

QUESTION-4.7

A bag consists of 10 balls each marked with one of the digits 0 to 9. If four balls are drawn successively with replacement from the bag, what is the probability that none is marked with the digit 0?

SOLUTION

Let X be number marked on ball drawn. Since the balls are drawn with replacement, the trials are Bernoulli trials.

So X has Binomial Distribution

$$P(X = x) = \binom{n}{x} q^{n-x} p^x \quad (1)$$

Here,

$$n = \text{number of times we pick the ball} = 4 \quad (2)$$

$$p = \text{Probability of getting 0} = \frac{1}{10} \quad (3)$$

$$q = 1 - p = 1 - \frac{1}{10} = \frac{9}{10} \quad (4)$$

Hence,

$$P(X = x) = \binom{4}{x} \left(\frac{9}{10}\right)^{(4-x)} \left(\frac{1}{10}\right)^{(x)} \quad (5)$$

We need to find probability that no ball is marked 0,
i.e.

$$P(X = 0) \quad (6)$$

Now,

$$P(X = 0) = \binom{4}{0} \left(\frac{9}{10}\right)^{(4-0)} \left(\frac{1}{10}\right)^{(0)} \quad (7)$$

$$\Rightarrow P(X = 0) = \frac{4!}{(4-0)!0!} \times 1 \times \left(\frac{9}{10}\right)^4 \quad (8)$$

$$\Rightarrow P(X = 0) = \left(\frac{9}{10}\right)^4 = 0.6561 \quad (9)$$

Therefore, The probability that none of ball is marked with 0 is **0.6561**