

Hashing-1

Content

- Hashmap intro
- freq. of each element
- first non-repeating element
- # of distinct elements
- exist a subarray with sum=0

Scenario 1: 1000 rooms labelled as : $[1, 1000]$

↳ occupied / not occupied

array \Rightarrow `bool room[1001]`

↓
since rooms are
labelled from $[1, 1000]$
NOT $[0, 999]$

\Rightarrow `room[i] = true`
[if i^{th} room is occupied]

\Rightarrow `room[i] = false`
[not occupied]

Scenario 2 1000 rooms labelled between $[1, 10^9]$

`bool room[$10^9 + 1$]`

↳ Issue: Huge space wastage

↳ Advantage: $T.C: O(1)$ to find any room's occupancy

Hashmap

It stores $\langle \text{key}, \text{value} \rangle$ pairs.

$\langle 10015, \text{occupied} \rangle$
 $\langle 123, \text{unoccupied} \rangle$
 \vdots
 $N \text{ entries}$

\Rightarrow check in 10015 ?
 \rightarrow occupied in TC: $O(1)$

TC: $O(1)$ to search
SC: $O(N)$ to store for N rooms

Note: Keys are unique. Value can be anything

Q1 Store population of every country

Key: country name \rightarrow string
value: population \rightarrow int/long

HashMap^{key}^{value} $\langle \text{string}, \text{long} \rangle$ hm \Rightarrow pseudo syntax
 \uparrow
variable name.

eg: India, US, UK

hm = $\langle \text{"India"}, 1.5 \times 10^9 \rangle$
 $\langle \text{"US"}, 10^8 \rangle$
 $\langle \text{"UK"}, 10^7 \rangle$

Q2 for every country we want to know all states.

Key: country name \rightarrow string

value: all state names \rightarrow array<string>

\hookrightarrow c++ : vector

\hookrightarrow py : list

\hookrightarrow java : ArrayList

HashMap<string, array<string>> hm

Q3 for every country, store population of each state.

Key: country name \rightarrow string

value: population of each state \rightarrow HashMap<string, long>

\downarrow
state
name

\downarrow
population

HashMap<string, HashMap<string, long>> hm

Observation 1: Value can be anything

Observation 2: Key can only be primitive datatype

\swarrow
int / long / float / double / string / char

HashSet<Key>

- \rightarrow we only store Keys
- \rightarrow Keys have to be unique
- \rightarrow only primitive datatypes

HashMap functionality

Size: {# of keys present}

insert (key, value)

search (key) → value
↳ NOT FOUND

delete (key)

update (key, newValue)

↳ HashMap

~~<India, 800>~~ *

<US, 200>

<India, 900>

All operations here are O(1)

HashSet functionality

Size: {# of keys present}

insert (key)

search (key) → true
false

delete (key)

→ Hashing Libraries name in diff. languages

Pseudocode	Java	C++	Python	JS	C#
HashMap	HashMap	unordered_map	dict	map	dictionary
HashSet	HashSet	unordered_set	set	set	HashSet

Question 1

Given N array elements & Q queries.

For each query find freq. of given element in array.

eg arr(10) = { 2 6 3 8 2 8 2 3 8 10 6 }

$Q=4$ freq

2 : 3

8 : 3

3 : 2

5 : 0

Constraints:

$1 \leq N \leq 10^5$ $1 \leq Q \leq 10^5$

$1 \leq arr(i) \leq 10^9$

Idea 1: for every query, iterate & get count

TC: $O(Q \cdot N)$ SC: $O(1)$

Idea 2: Store data in hashmap

key \rightarrow array element \rightarrow int

value \rightarrow freq. of element \rightarrow int

{ 2 6 3 8 2 8 2 3 8 10 6 }

$\langle 2, 3 \rangle$ $\langle 6, 2 \rangle$

$\langle 8, 3 \rangle$ $\langle 10, 1 \rangle$

$\langle 3, 2 \rangle$

Code

HashMap <int, int> hm // TODO

```
for (i=0; i<n; ++i) {  
    // key = a[i]  
    if (hm.containsKey(a[i]) == true) {  
        hm.put(a[i], hm.get(a[i]) + 1) // update  
    }  
    else {  
        hm.put(a[i], 1) // insert  
    }  
}
```

→ TC: $O(N)$

SC: $O(N)$

```
for (i=0; i<m; ++i) {  
    // key = b[i]  
    if (hm.containsKey(b[i]) == true) {  
        print(hm.get(b[i])) → access value of key  
    }  
    else {  
        print(0)  
    }  
}
```

→ M queries

TC: $O(M)$

TC: $O(N+M)$

SC: $O(N)$

Question 2

find the first non-repeating element.

↳ first element from start, non-repeating

eg $a[b] = \{ \underset{\text{freq}=2}{1} \underset{\text{freq}=2}{2} \underset{\text{freq}=1}{3} 1 2 5 \}$ ans = 3

$a[] = \{ 4 \underset{\text{freq}=2}{3} \underset{\text{freq}=2}{3} \underset{\text{freq}=1}{2} 5 4 \}$

Idea 1

1. Insert all elements in hashmap
2. Iterate hashmap to get first key with value = 1.

Note: Order of insertion of keys is not maintained in hashmap / hashset.

Idea 2 :

1. Insert all elements in hashmap $\rightarrow O(N)$
2. Iterate over array & get first element with $hm[a[i]] = 1 \rightarrow O(N)$

TC: $O(N)$ SC: $O(N)$

Code \rightarrow TODO

Question 3

Given an array elements, find no. of distinct elements?

eg $a[5] = \{ 3, 5, 6, 5, 4 \}$ ans = 4

$a[5] = \{ 1, 1, 1, 2, 2 \}$ ans = 2

Idea

Insert all elements in HashSet

$a[7] = \{ 6, 3, 7, 3, 8, 6, 9 \}$

HashSet<int> hs

$hs = \{ 6, 3, 7, 8, 9 \}$

hs.size = 5

Note: In HashSet, if same key is inserted multiple times, it will store only 1 occurrence.

Code

```
HashSet<int> hs
```

```
for (i=0; i<n; ++i) {
```

```
    hs.insert(a[i])
```

```
}
```

```
print(hs.size)
```

TC: $O(N)$

SC: $O(N)$

Question 4

Given $a(N)$ elements, check if there exists a subarray with $\text{sum} = 0$.

eg $a(10) =$

0	2	2	1	-3	4	3	1	-2	-3	2
	1	2	3	4	5	6	7	8	9	

Ans = true

Idea: for every subarray, calculate sum

↙
nested loops
 $O(N^3)$

↓
prefix sum
 $O(N^2), O(N)$

↘
array forward
 $O(N^2), O(1)$

TC: $O(N^2)$ SC: $O(1)$

	0	1	2	3	4	5	6	7	8	9
$a(10) =$	2	2	1	-3	4	3	1	-2	-3	2
$pf(1) =$	2	4	5	2	6	9	10	8	5	7

observation: In $pf()$, numbers are repeating.

$$pf(0) = 2 = \text{sum}(0,0]$$

$$pf(3) = 2 = \text{sum}(0,3] = \text{sum}(0,0] + \text{sum}(1,3]$$

$$2 = 2 + \text{sum}(1,3]$$

$$\boxed{\text{sum}(1,3] = 0}$$

$a[4] = \{ 2 \ -5 \ 3 \ 6 \}$

$pf[] = \{ 2 \ -3 \ 0 \ 6 \}$

↳ in $pf[]$ there is no repetition but subarray with sum=0 exist?

$$pf[2] = \text{sum}[0,2] = 0$$

Note: In $pf[]$ every if single 0 is present, there exists a subarray with sum=0

final Idea:

If ele repeat in $pf[]$
OR
If 0 is present in $pf[]$ } → there exist a subarray with sum=0

Code

```
bool subarrayZero(a[]) {  
    n = a.length  
    pf[n] // construct pf[] → TODO  
    HashSet<int> hs  
    for (i=0; i<n; i++) {  
        if (pf[i] == 0) { return true }  
    }
```

hs.insert(pf[i])

}

if (hs.size < N) { // repetition in pf[]

return true

}

return false

}

TC: $O(N)$

SC: $O(N)$