

Today's content

1. Smallest element on left side
2. max area in a histogram
3. design stack with getMin functionality.

class content starts at 7:05
from next class.

Q. Given $ar[N]$, for every index calculate 1st smaller element on left side.

Ex 1:

	0	1	2	3	4	5
$ar[6]$:	4	5	2	10	3	2
ans :	-1	4	-1	2	2	-1

Ex 2:

	0	1	2	3	4	5	6	7
$ar[8]$:	4	6	10	11	7	8	3	5
ans :	-1	4	6	10	6	7	-1	3

Idea 1: For every $ar[i]$, iterate on left and get 1st smallest element.

```
int() smallerOnleft (int() ar)
{
    int() ans = -1;
    for (i = 1; i < n; i++)
    {
        // find 1st smaller on left.
        for (j = i - 1; j >= 0; j--)
        {
            if (ar[j] < ar[i])
            {
                ans[i] = ar[j];
                break;
            }
        }
    }
    return ans;
}
```

Tc: $O(N^2)$.
Sc: $O(1)$

idea: Let's try using some DS, which one? --

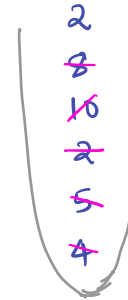
ex1:

ar[6] : 0 1 2 3 4 5
 5 2 8 10 6 1



ex2:

ar[6] : 0 1 2 3 4 5
 4 5 2 10 8 2



while inserting new element,

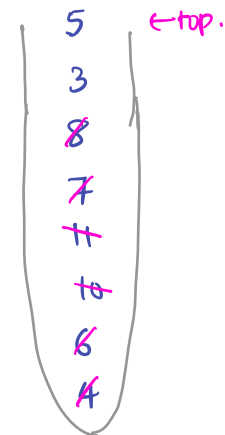
while top of stack is greater than or equal^{to} new element, remove it.

top of stack is smaller ele on left.

If stack is empty \Rightarrow ans = -1.

ex3:

ar[8] : 0 1 2 3 4 5 6 7
 4 6 10 11 7 8 3 5
 -1 4 6 10 6 7 -1 3



int() smallerOnleft (int() ar)

int[] ans = -1.

Stack<int> st

i=0; i<n; i++

while (st.size() > 0 && st.top() > ar[i])

st.pop()

if (st.size() > 0)

ans[i] = st.top()

st.push(ar[i])

return ans.

push pop.

TC: $N + N \Rightarrow O(N)$.

SC: $O(N)$.

Variations of 1st smaller ele on left.

(i) 1st smaller ele on right. \Rightarrow Traverse from right.

(ii) 1st smaller index on left and right.

changes \begin{cases} instead of pushing $ar[i]$, push 'i'.
instead of $st.top() \geq ar[i]$, $ar[st.top()] \geq ar[i]$.

(iii) 1st greater ele on left and right.

changes for left \Rightarrow instead of $st.top() \geq ar[i] \Rightarrow st.top() \leq ar[i]$

histogram area

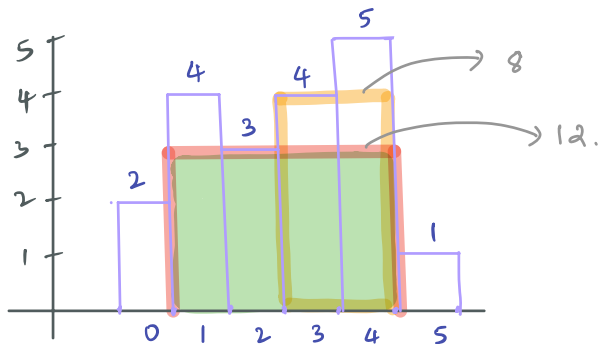
Given continuous blocks of histograms, find max rectangular area.

Note: Every histogram has a width of 1.

max rectangle that you can keep inside histograms.

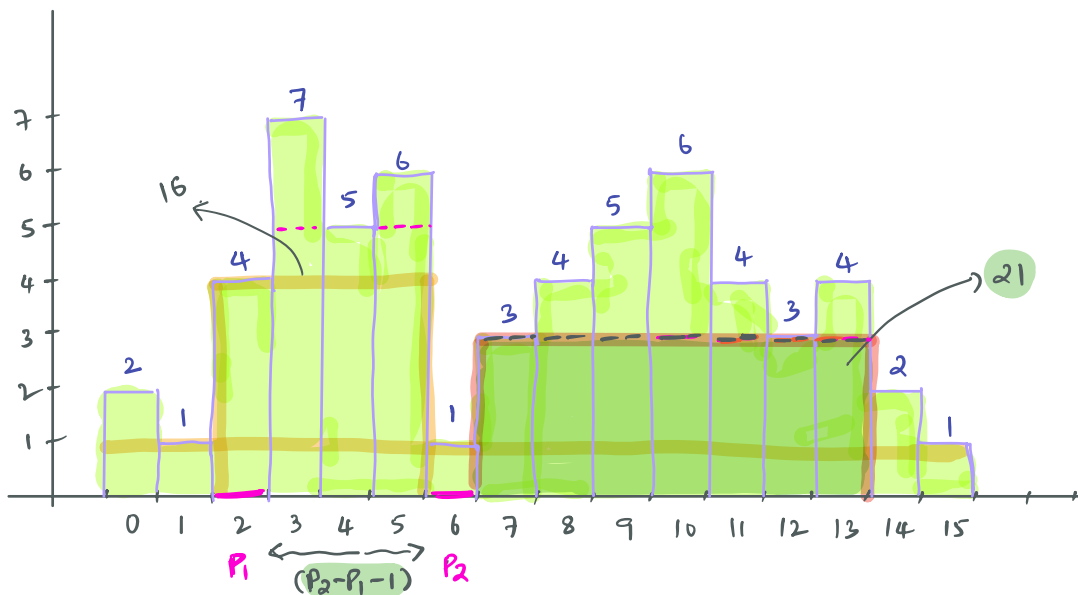
Ex1:

0 1 2 3 4 5
ar[6] : [2 4 3 4 5 1]



Ex2:

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15
ar : [2 1 4 7 5 6 1 3 4 5 6 4 3 4 2 1]



$[P_1 \ P_2] \rightarrow P_2 - P_1 + 1$
excluding P_1 & $P_2 \Rightarrow P_2 - P_1 - 1$

Observations:

- (i) Height of any rectangle will have to match with height of any one histogram.
- (ii) Take every histogram height as height of rectangle and try to extend the rectangle on both the sides.

How to extend?

- a) keep extending to left until we find height < rectangle height = P_1
- b) keep extending to right until we find height < rectangle height = P_2 .

$P_1 \rightarrow$ 1st smaller element on left.

$P_2 \rightarrow$ 1st smaller element on right.

(iii) Rectangle Area = $(P_2 - P_1 - 1) * \text{height}$.

Code:

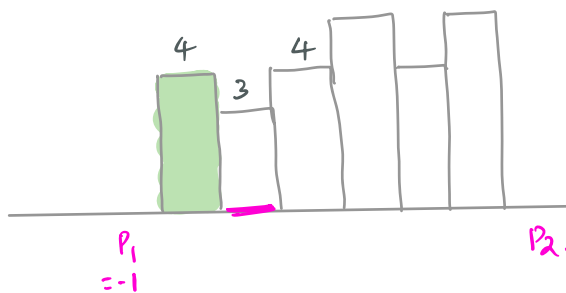
```
int rectangleArea(int[] hist, int n)
// for every histogram, find smallest on left & right
int[] left = smallestIndexLeft(hist)
int[] right = smallestIndexOnRight(hist)
// edge case.
// set default value for right as n
ans = 0;
for (i = 0; i < n; i++)
    // consider every hist, hist[i] as height of rectangle.
    P1 = left[i], P2 = right[i]
    ans = max(ans, (P2 - P1 - 1) * hist[i])
return ans
```

3n iterations

↑

Tc: O(n)

Sc: O(n)



arr[3]: 4 3 4

	P1		P2	
left	-1	-1	1	
right	1	-1	-1	
(r-l-1)	1	-1	-3	

[Setting default value as (-1) for left will work, but not for right]

Q3: Design a stack that supports push, pop, top, getMin methods.

Note: The time complexity for all the methods should be $O(1)$ in TC.

ex: push(5), push(6), push(3), push(8), getMin(), push(1), getMin(),
pop(), pop(), pop(), getMin().



hint: Try using another stack to keep track of min.

(i) push(ele)

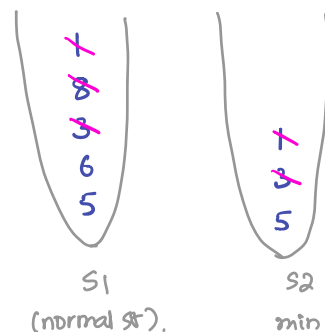
* Always push the ele to S1.

* Push the ele to S2 if $ele \leq S2.top$.

(ii) pop()

* Pop out from S2 if $S1.top = S2.top$.

* Always pop out from S1.



(iii) getMin()

* Simply read S2.top.

Note: Equal elements must also be pushed to both S1 & S2 if the condⁿ is satisfied.

class SpecialStack

Stack s1 // normal stack

Stack s2 // for min ele.

void push(int ele)

if (s1.size() == 0)
s1.push(ele), s2.push(ele)

else

s1.push(ele)

if (s2.size > 0 && ele ≤ s2.top())
s2.push(ele)

void pop()

if (s1.top == s2.top)
s2.pop()

s1.pop()

int getMin()

return s2.top.

[Possible to implement with O(1) space, TODO] → Optional.