

Introduction to Arrays

Array?

- ↳ contiguous list of homogeneous items
 - ↳ same type
- ↳ size is fixed → static size

A =

--	--	--	--	--

 → index to access a value in a array
0 1 2 3 4

For an array of size N : 0 to N-1 indices
↓
0, 1, 2, 3, ..., N-2, N-1

a[n] a[i] = ? TC = O(1)

To access all the elements it will take O(N) time.

A[0] → a[0], a[1], ..., a[n], ~~a[n+1]~~, ~~a[n+2]~~, ...

Traverse in Array

int a[n]

```
for (i=0; i<n; ++i) {  
    a[i] ...  
}
```

iterations = N

TC = O(N)

Question 1

Given an array of size N . find count of elements which has at least one greater element than itself.

eg 1 4 5 3 -1 5 4 ans = 5

eg 2 5 1 4 8 0 8 1 3 8 ans = 7

1. find the max element
2. count the occurrences of max element
3. ans = $N - \text{count}$

~~mx = 0~~ \rightarrow $mx = a[0]$

$N-1$ iteration $\left\{ \begin{array}{l} \text{for } (i=1; i < n; ++i) \{ \\ \quad \text{if } (a[i] > mx) \\ \quad \quad mx = a[i] \\ \} \end{array} \right.$
count = 0

N iteration $\left\{ \begin{array}{l} \text{for } (i=0; i < n; ++i) \{ \\ \quad \text{if } (a[i] == mx) \\ \quad \quad ++count \\ \} \end{array} \right.$
ans = $N - \text{count}$

iterations = $\frac{N-1 + N}{2} = N-1$

TC = $O(N)$

SC = $4 + 4 + 4 \text{ B}$
= $O(1)$

HW: Solve in one for loop.

eg -3 -1 -2 $mx=0$

In case of all -ive values, $mx=0$ will not work.

Question 2

Given an array of N elements. find count of pair (i, j) where i, j are indices such that

$$a[i] + a[j] = k \text{ (given)} \quad i < j$$

eg $a[6] = \{ 1 \ 5 \ 6 \ 2 \ 4 \ 3 \}$ $K=7$

0 1 2 3 4 5

$(0, 2) \quad (1, 3) \quad (4, 5)$

ans = 3

$a[10] = \{ 3 \ 5 \ 2 \ 1 \ -3 \ 7 \ 8 \ 15 \ 6 \ 13 \}$

0 1 2 3 4 5 6 7 8 9

$K=10$

$(0, 5) \quad (2, 6) \quad (4, 9)$

ans = 3

$a[4]$
↓
 $\{0, 1, 2, 3\}$
↓
 N^2 pairs

$i \quad j$			
$(0, 0)$	$(0, 1)$	$(0, 2)$	$(0, 3)$
$(1, 0)$	$(1, 1)$	$(1, 2)$	$(1, 3)$
$(2, 0)$	$(2, 1)$	$(2, 2)$	$(2, 3)$
$(3, 0)$	$(3, 1)$	$(3, 2)$	$(3, 3)$

```

count = 0
for (i = 0; i < n; ++i) {
    for (j = i + 1; j < n; ++j) {
        // (i, j) is valid
        if (a[i] + a[j] == k)
            ++count
    }
}

```

i	j = [i+1, n-1]	iterations
0	[1, n-1]	n-1
1	[2, n-1]	n-2
⋮	⋮	⋮
n-2	[n-1, n-1]	1
n-1	[]	0
		= 1 + 2 + ... + n-1

```

3
3
print(count)

```

TC: $O(N^2)$

$$\begin{aligned}
 \text{iterations} &= \frac{n(n-1)}{2} \\
 &= \frac{n^2}{2} - \frac{n}{2}
 \end{aligned}$$

```

count = 0
for (i = 0; i < n; ++i) {
    for (j = 0; j < n; ++j) {
        if (i < j && a[i] + a[j] == k)
            ++count
    }
}

```

iterations = n^2

TC: $O(N^2)$

```

3
3
print(count)

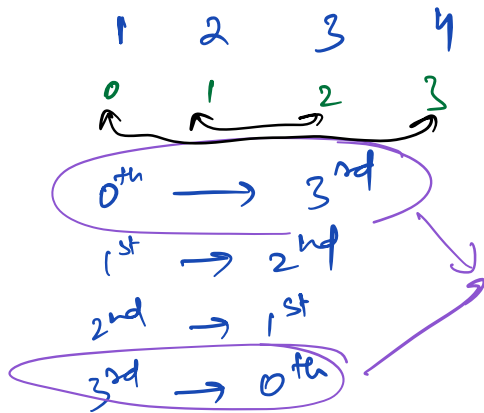
```

SC = $O(1)$

Question 3

Given an array of size N. Reverse the array without using extra space.

eg { 1 2 3 4 } $\xrightarrow{\text{reverse}}$ { 4 3 2 1 }



$$0^{th} \longleftrightarrow 3^{rd}$$

$$a[0] \longleftrightarrow a[n-1]$$

$$0 + n - 1 = n - 1$$

$$a[1] \longleftrightarrow a[n-2]$$

$$1 + n - 2 = n - 1$$

$$\vdots$$

$$a[i] \longleftrightarrow a[j]$$

\downarrow
 $n-i-1$

$$i + j = n - 1 \Rightarrow j = n - i - 1$$

```

for (i=0; i<n; ++i) {
    swap(a[i], a[n-i-1]);
}

```

NOT WORK

$$a[0] = 1 \quad 2 \quad 3 \quad 4$$

0 1 2 3

$$i=0 \quad j=4-0-1=3$$

4 2 3 1

$$i=1 \quad j=2$$

4 3 2 1

$$i=2 \quad j=1$$

4 2 3 1

$$i=3 \quad j=0$$

1 2 3 4

$$1 \quad 2 \quad 3 \quad 4 \quad 5$$

\Downarrow

5 4 3 2 1

```

i=0, j=n-1
while (i<j) {
    swap(a[i], a[j]);
    i++, j--;
}

```

WORKS

iterations = $n/2$

TC: $O(N)$

SC: $O(1)$

What if we have to reverse only some part of array. : [start, end]

1	2	3	4	5	6	7
0	1	2	3	4	5	6

↑ start ↓ ↑ end

1	5	4	3	2	6	7
---	---	---	---	---	---	---

```

i = start, j = end;
while (i < j) {
    swap(a[i], a[j]);
    i++, j--;
}

```

BREAK : 10:17 - 10:27

Question 4

Given an array of size N . Rotate your array K times clockwise. $K < N$

eg

	1	2	3	4	5
	0	1	2	3	4

$K=1$

5	1	2	3	4
---	---	---	---	---

$K=2$

4	5	1	2	3
---	---	---	---	---

$K=3$

3	4	5	1	2
0	1	2	3	4

$K=3$

$$a[0] = 1 \xrightarrow{+3} a[3] = 1$$

$$a[1] = 2 \xrightarrow{+3} a[4] = 2$$

$$a[2] = 3 \xrightarrow{-2} a[0] = 3$$

$$a[3] = 4 \xrightarrow{-2} a[1] = 4$$

$$a[4] = 5 \xrightarrow{-2} a[2] = 5$$

$$(0+3) \% 5 = 3$$

$$(1+3) \% 5 = 4$$

$$(2+3) \% 5 = 0$$

$$(3+3) \% 5 = 1$$

$$(4+3) \% 5 = 2$$

```
int temp[n]
for (i=0; i<n; ++i) {
    j = (i+K) % n
    temp[j] = a[i]
}
```

```
for (i=0; i<n; ++i) {
    a[i] = temp[i]
}
```

}

$[a[j] = a[i]]$
↪ ion of value

TC: $O(N)$

SC: $O(N)$

4	5	3	1	2
0	1	2	3	4

$K=3$

$i=0, j=3$
 $i=1, j=4$
 $i=2, j=0$

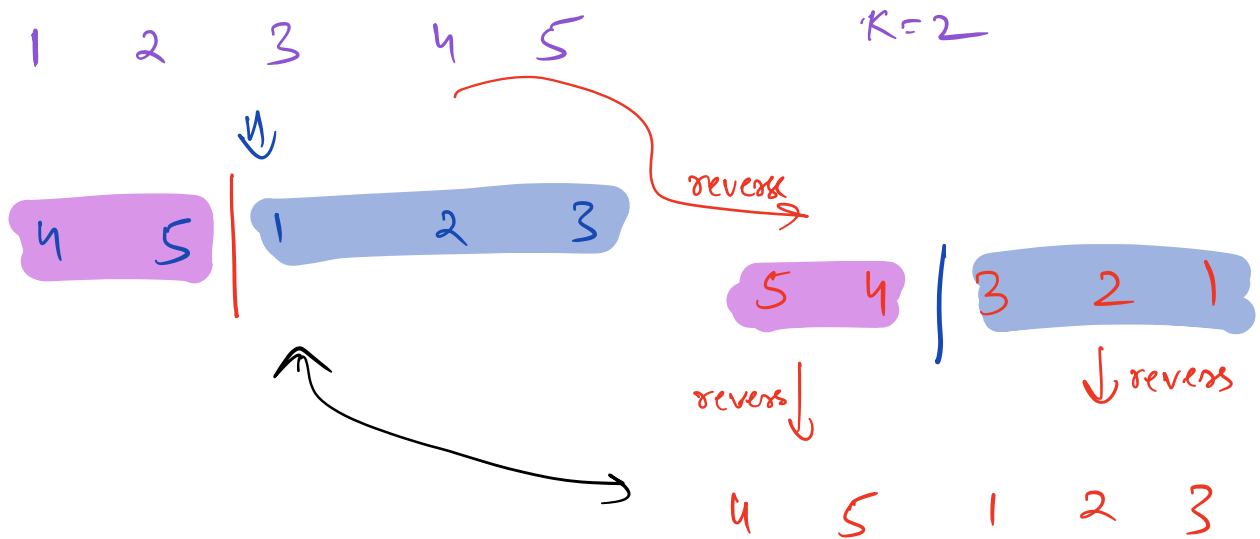
If we don't want extra space, we can shift one by one in K iterations.

```

for (i=0; i<K; ++i) {
    temp = a[n-1];
    for (j=1; j<n; ++j) {
        a[j] = a[j-1]
    }
    a[0] = temp
}

```

$TC: O(K \times N)$
 $SC: O(1)$



To shift element K times
clockwise \Rightarrow

reverse (0, N-1) \Rightarrow iterations

reverse (0, K-1) \Rightarrow K/2

reverse (K, N-1) \Rightarrow N-K/2

$$\text{total iterations} = \frac{N}{2} + \frac{K}{2} + \frac{N-K}{2} = \frac{N + K + N - K}{2} = \frac{2N}{2} = N$$

TC: $O(N)$

SC: $O(1)$

reverse(a, 0, n-1)
reverse(a, 0, k-1)
reverse(a, k, n-1)

```
void reverse(a[], start, end) {
    i = start, j = end
    while (i < j) {
        swap(a[i], a[j])
        ++i, --j
    }
}
```

Dynamic Array, Array with variable size

C++	Java	Python	JS/Ruby
vector	ArrayList	List	array

append() / add() / insert() / push-back()

HW: Understand dynamic array in your language.