

# ASSIGNMENT A6

Shantnu Kakkar

CS 6320, Spring 2016

March 09, 2016

## Section 1: Intro:

This assignment is based on the edge tracking and feature detection (corners) techniques learnt in the lecture. I will be implementing various method, for example **Harris corner detector**, **orientation histogram**, **algorithm 5.2 and 5.3 from text**. The basic idea behind my approach is that as the light gets brighter or darker, the image will get brighter or darker. This means that the gradient scales with the image. This creates a problem for edge detectors since they rely on image gradient magnitude. To overcome that problem, we use orientation of the image gradient, which is unaffected by scaling. The following figure 1 from the text proves this. Orientation histogram is a good technique that will be used for this.

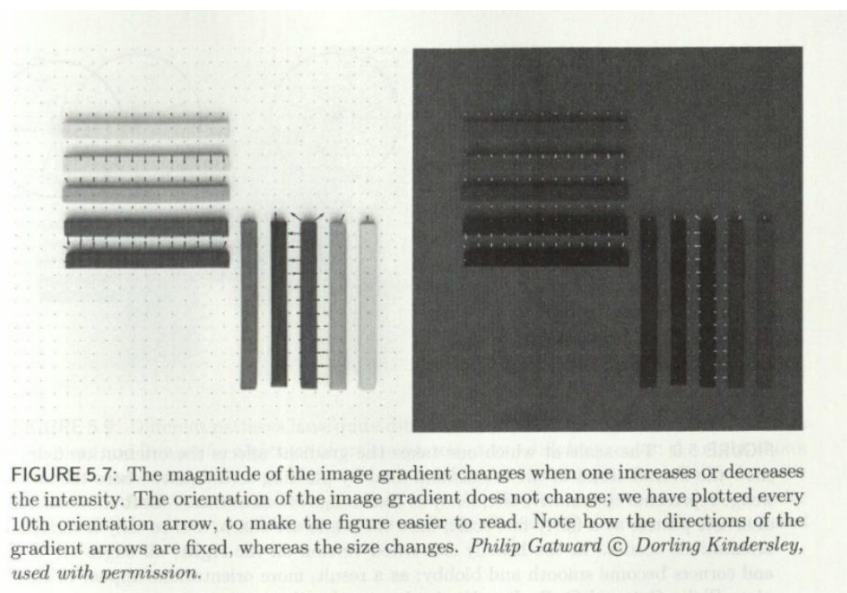


Figure 1 This figure forms the motivation for me to using image orientation for corner detection.

Another motivation is to use Laplacian of Gaussian since we need to estimate the radius (scale) of the circular patch. The radius estimate should get larger proportionally when the image gets bigger. We could center a blob of fixed appearance on the corner and then choose the scale to be the radius of the best fitting blob. An efficient way to do that us Laplacian of Gaussian.

For this problem, we are given two images and we need to find corners in them. We are required to implement algorithm 5.2 and 5.3 and compare them as feature detectors by implementing on the two given images. After the implementation, I will be answering the following question

- Are the two algorithms stable with respect to image rotation, translation and scaling?

## **Section 2: Method:**

- Matlab is used to carry out the experiments.
- For the interest points I will try to shoot between 20-40 points.
- I will be doing the translation, rotation and scaling part as follows:

### **Translation:**

If the image is  $m \times n$ , then shift it right (with wraparound):

```
imt = [im(:,51:n),im(:,1:50)];
```

### **Rotation:**

```
im45 = imrotate(im,45);
```

### **Scaling:**

```
im2 = imresize(im,2);
```

- I will be using the combo function provided by professor to analyse my results for Harris.
- I will be using `imregionalmax` function instead of defining my own function since it worked better for me compared to my function. I was able to get stable rotation and translation by using this function. There were some problems when I tried with my own `local_max` function. My own local max function will go into the critique section.

Following functions are implemented

- `CS5320_Harris` – This function detects the corners(interest points). It takes input as the gray image and the desired window size, and the output is the response matrix defined as:  
R ( $m \times n$  array): corner response  $\leq 0$ : homogeneous ,  $> 0$  and small: edge, large: corner
- `CS5320_Log_interest` – It finds the interest points as well as the radius (maxima sigma scale) at those points. Its input is the gray image and a value  $p$  which helps us to set the threshold to reduce the number of threshold points. It outputs the interest points as 1 and other points as 0. It also outputs the corresponding max sigma scale at that location.
- `CS5320_gradient_histogram` – It gets the histogram of gradient orientations. Its input is the gray image, the row of center of patch, column of center of patch, radius of pixels to consider, minimum gradient magnitude to consider, and a Boolean which tells which tells whether to use magnitude of gradient as weight in histogram. It outputs orientation counts in 20-degree bins
- `CS5320_corner_patches` – It produces patches using Harris ( Alg. 5.2 from text). See below for detailed description if this function.
- `CS5320_Log_patches` – It produces patches using `LogInterest` (Alg. 5.3 text). ). See below for detailed description if this function. It takes 30-40 seconds to run, but could be somewhat faster sometimes.

In addition to the above functions there is a script named verification which contains how I call every function. Please note that I have divided this script into various cells (sections). Please run individual section for every function. I have commented out imshow in this script everywhere. Please uncomment that to see the answers. For translation, rotation and scaling, uncomment from the corner patches and loG patches section to see the stability analysis. **Press ctrl + enter to run section wise.**

**The following algorithm has been used for Harris:**

- *Initialize  $R = \text{zeros}(\text{size}(im,1), \text{size}(im,2));$*
- *Find  $\text{gradient}[dx,dy] = \text{gradient}(\text{double}(im));$*
- *Loop for  $r = 1+k:\text{size}(im,1)-k$* 
  - *Loop for  $c = 1+k:\text{size}(im,2)-k$* 
    - *$a = dx(r-k:r+k, c-k:c+k);$*
    - *$b = dy(r-k:r+k, c-k:c+k);$*
    - *$a = a(:);$*
    - *$b = b(:);$*
    - *$pts = [a,b];$*
    - *$M = pts'*pts;$*

**The following algorithm has been used for log interest**

- *Make sigma vector  $\sigma = 0.3:0.01:6;$*
- *Initializations*

```

scale = zeros(nr,nc);

C = zeros(nr,nc,num_sigmas);

interest_pts = zeros(nr,nc);

maxResponses = zeros(nr,nc);

temp1_scale = zeros(nr,nc);

temp2_scale = zeros(nr,nc);

```
- *Loop for  $s\_index = 1:\text{num\_sigmas}$* 

```

Make template  $T = \text{fspecial}('log', 21, \sigma(s\_index));$ 

Find response  $C(:, :, s\_index) = \text{abs}(\text{filter2}(T, im));$ 

```

- Loop for  $r = 1:nr$ 
  - loop for  $c = 1:nc$ 

```

temp1 = C(r,c,:);
temp1 = temp1(:);
[temp2(r,c),idx] = max(temp1);
if idx ~= 1 && idx ~= num_sigmas
    temp1_scale(r,c) = sigma(idx);
    maxResponses(r,c) = temp2(r,c);

```
- Find points above threshold

```

maxvalues = p*max(max(maxResponses));
for r = 1:nr
    for c = 1:nc
        if maxResponses(r,c) < maxvalues
            maxResponses(r,c) = 0;

```
- Find local maxima  $interest\_pts = imregionalmax(maxResponses);$
- Update scale =  $interest\_pts.*temp1\_scale;$

The following method is used for finding hands in CS5320\_gradient\_histogram function:

- Initialize  $H = [0;0;0;0;0;0;0;0;0;0];$
- Find window/patch =  $im(r-ceil(radius):r+ceil(radius),c-ceil(radius):c+ceil(radius));$
- Gradient  $[dx,dy] = gradient(double(patch));$
- Loop for  $r = 1:size(patch,1)$ 
  - for  $c = 1:size(patch,2)$ 

```

magnitude = sqrt( dx(r,c)^2 + dy(r,c)^2);
if magnitude > thresh
    orientation = (atan2d(dy(r,c),dx(r,c)));
    if orientation < 0
        orientation = orientation + 180;
    end
    bin = ceil(orientation/20);
    if bin > 0
        if w==0
            H(bin) = H(bin) + 1;
        else

```

$H(\text{bin}) = H(\text{bin}) + \text{magnitude};$

**The following method is used in CS5320\_corner\_patches:**

```
Initialize sigma = 0.3:0.01:6;
num_sigmas = length(sigma);
call R = CS5320_Harris(im,w);
call RregionalMax = imregionalmax(R);
R = RregionalMax.*R;
[nr,nc] = size(im);
Find threshold = max(max(R/2));
Make interest point vector x = R > threshold;
initialize patches = [];
loop for s_index = 1:num_sigmas
    T = fspecial('log', 7, sigma(s_index));
    C(:,s_index) = abs(filter2(T,im));

loop for r = 1:nr
    loop for c = 1:nc
        if x(r,c) == 1
            Xc = r;
            Yc = c;
            temp1 = C(r,c,:);
            temp1 = temp1(:);
            [temp2(r,c),idx] = max(temp1);
            radius = sigma(idx);
            H = CS5320_gradient_histogram(im,Xc,Yc,radius*k,0,0);
            [thetaP,index] = max(H);
            allThetaP = find(H==thetaP);
            for i = 1:length(allThetaP)
                tp(1) = Xc;
                tp(2) = Yc;
                tp(3) = r;
                tp(4) = 20 * allThetaP(i);
                patches = [patches;tp];
            end
        end
    end
end
```

**The following method is used in CS5320\_loG\_patches:**

```
Initialize patches = [];

Find interest point and radius [x,A_scale] = CS5320_LoG_interest(im,0.7);

[nr,nc] = size(im);

Loop for r = 1:nr

    Loop for c = 1:nc

        if x(r,c) == 1

            row of corner point Xc = r;

            column of corner point Yc = c;
```

```

radius = A_scale(r,c);
call H = CS5320_gradient_histogram(im,Xc,Yc,radius*k,0,0);
[thetaP,index] = max(H);
allThetaP = find(H==thetaP);
loop for i = 1:length(allThetaP)
    tp(1) = Xc;
    tp(2) = Yc;
    tp(3) = r;
    tp(4) = 20 * allThetaP(i);
    patches = [patches;tp];

```

### **Section 3: Verification:**

#### **Testing cs5320\_Harris**

- In testing for Harris, there IS A PROBLEM THAT gradient needs to be computed, which is difficult by hand. Hence, to find the gradient, I will be using matlab. Other calculations will be done by hand. Following figure shows hand calculations

For pixel (2,2),

The window is

$$w = im(1:3, 1:3) = \begin{bmatrix} 151 & 151 & 151 \\ 151 & 151 & 151 \\ 152 & 152 & 152 \end{bmatrix}$$

Gradient of these pixels in x

$$dx = \begin{bmatrix} 0 & 0 & 0.5 \\ 0 & 0.5 & 0.5 \\ 0 & 0 & 0 \end{bmatrix}$$

Gradient in y

$$dy = \begin{bmatrix} 0.5 & 0 & 1 \\ 0.5 & 0.5 & 0.5 \\ 0.5 & 1 & 0.5 \end{bmatrix}$$

$$pfs = \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 0.5 & 1 \\ 0 & 0.5 \\ 0.5 & 0.5 \\ 0.5 & 0.5 \\ 0 & 0.5 \\ 0 & 1 \\ 0 & 0.5 \end{bmatrix}$$

$$M = pfs' * pfs = \begin{bmatrix} 0.75 & 1 \\ 1 & 3.5 \end{bmatrix}$$

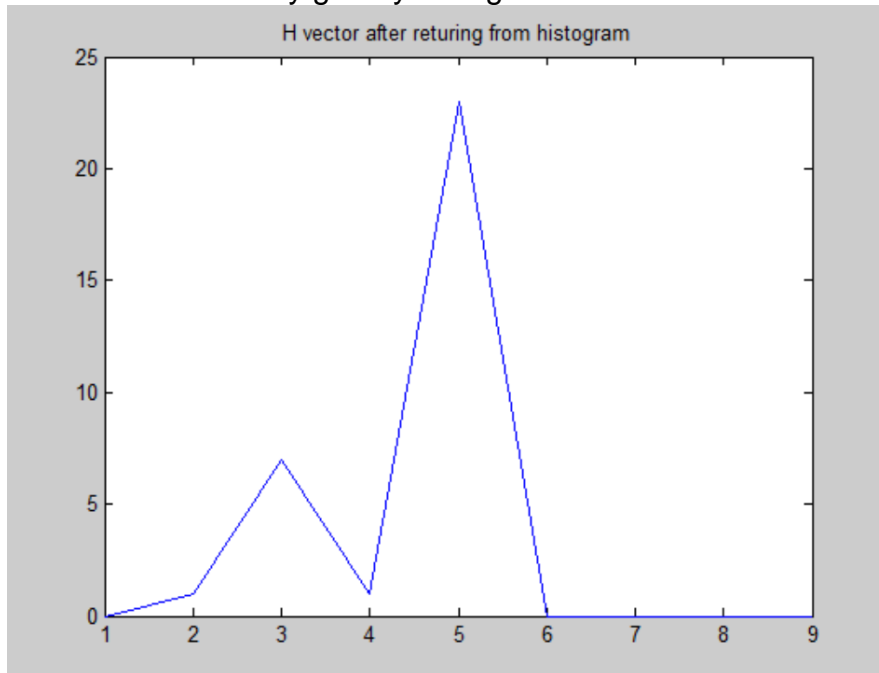
$$\begin{aligned} R(2,2) &= \det(M) - 0.05 * (\text{trace}(M)/2)^2 \\ &= (2.65 - 1) - 0.05 * \left(\frac{4.25}{2}\right)^2 \\ &= 1.65 - 0.05 * (2.125)^2 \\ &= 1.23 \end{aligned}$$

- From the above two images we can see that  $R(2,2)$  is 1,23. I am getting same in the matlab window:

R <288x466 double>				
	1	2	3	
1	0	0	0	
2	0	1.2375	0	
3	0	0	0	
4	0	0	0	
5	0	0	0	
6	0	0	0	
7	0	0	0	

## Testing CS5320\_gradient\_histogram

I am able to correctly get my histogram as follows



## Testing log\_interest function

- This function should output 20-40 interest points. The following command window shows that I am able to get interest points in this range.



```
Command Window
K>> clear
K>> im = imread('glass-box.jpg');
im = rgb2gray(im);
[A_IP,A_scale] = CS5320_Log_interest(im,0.7);
K>> NumofInterestpts = sum(sum(A_IP))

NumofInterestpts =

    38
```

### **Testing corner patches function**

I am getting good results for this function as follows:

```
Command Window
K>> im = imread('glass-box.jpg');
im = rgb2gray(im);
p = CS5320_corner_patches(im,2,2);
imshow(im);
hold on;
quiver(p(:,2),p(:,1),-1*cosd(p(:,4)),-1*sind(p(:,4)));
```

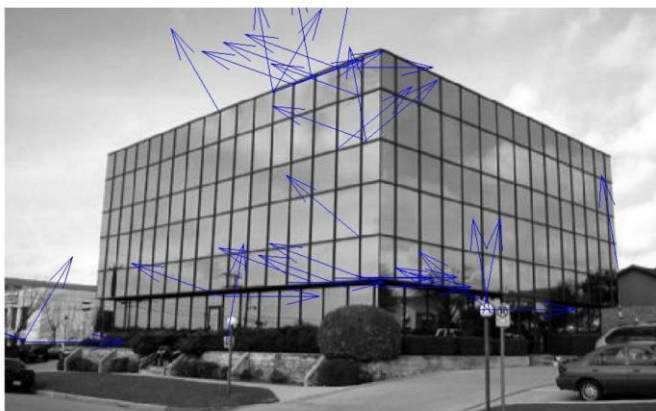


Figure 2 result for algo5.2

### **Testing loG patches function**

I am getting good results for this function as follows:

```

Command Window
K>> clear
K>> im = imread('glass-box.jpg');
im = rgb2gray(im);
K>> p = CS5320_LoG_patches(im,2,2);
imshow(im);
hold on;
quiver(p(:,2),p(:,1),-1*cosd(p(:,4)),-1*sind(p(:,4)));

```



Figure 3 result for algo 5.3

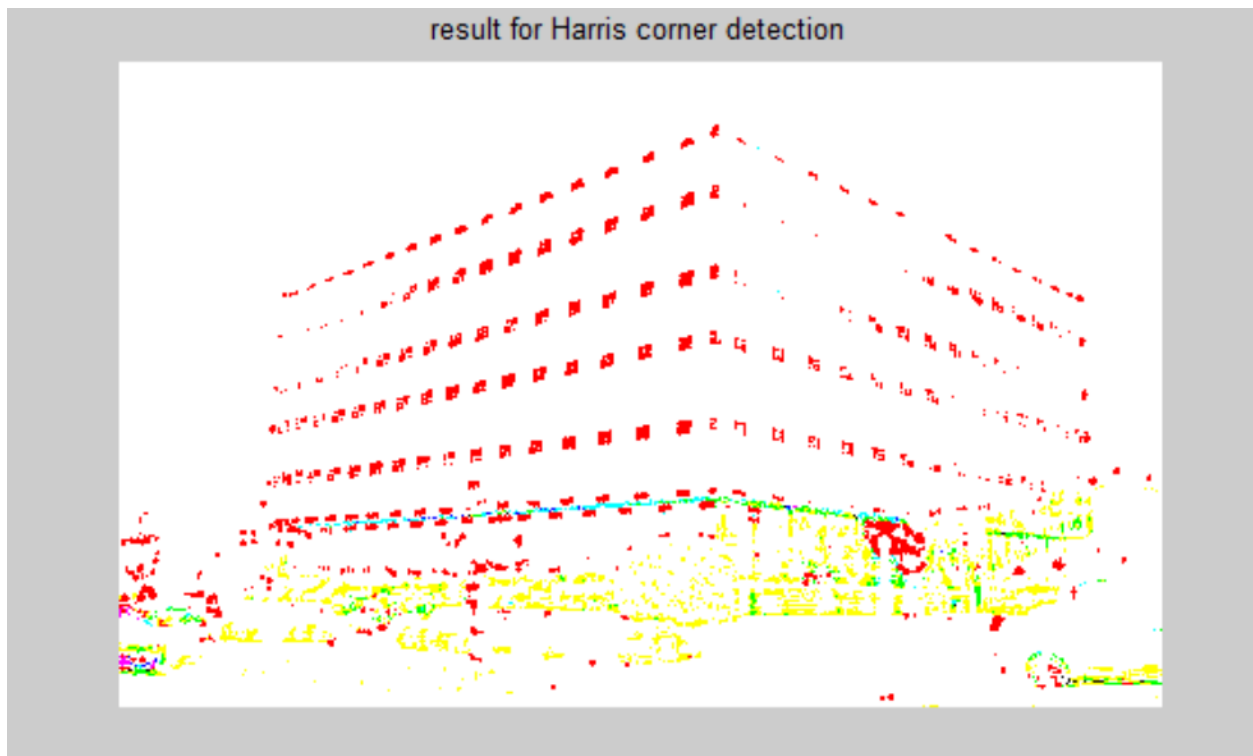
## **Section 4: Data:**

The following two images are being used:



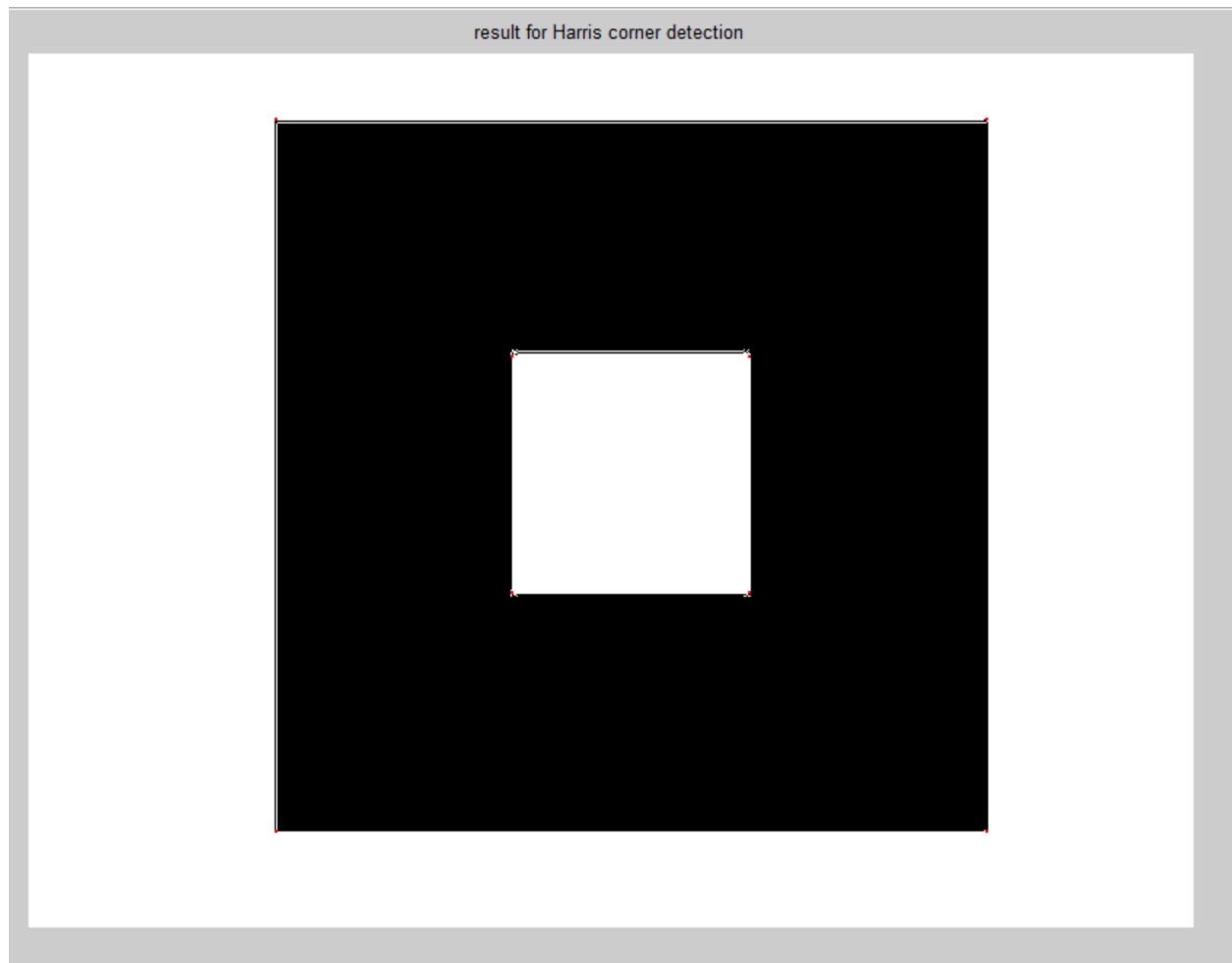
The histogram being formed has been shown in the verification dection

The following images show the result for Harris:



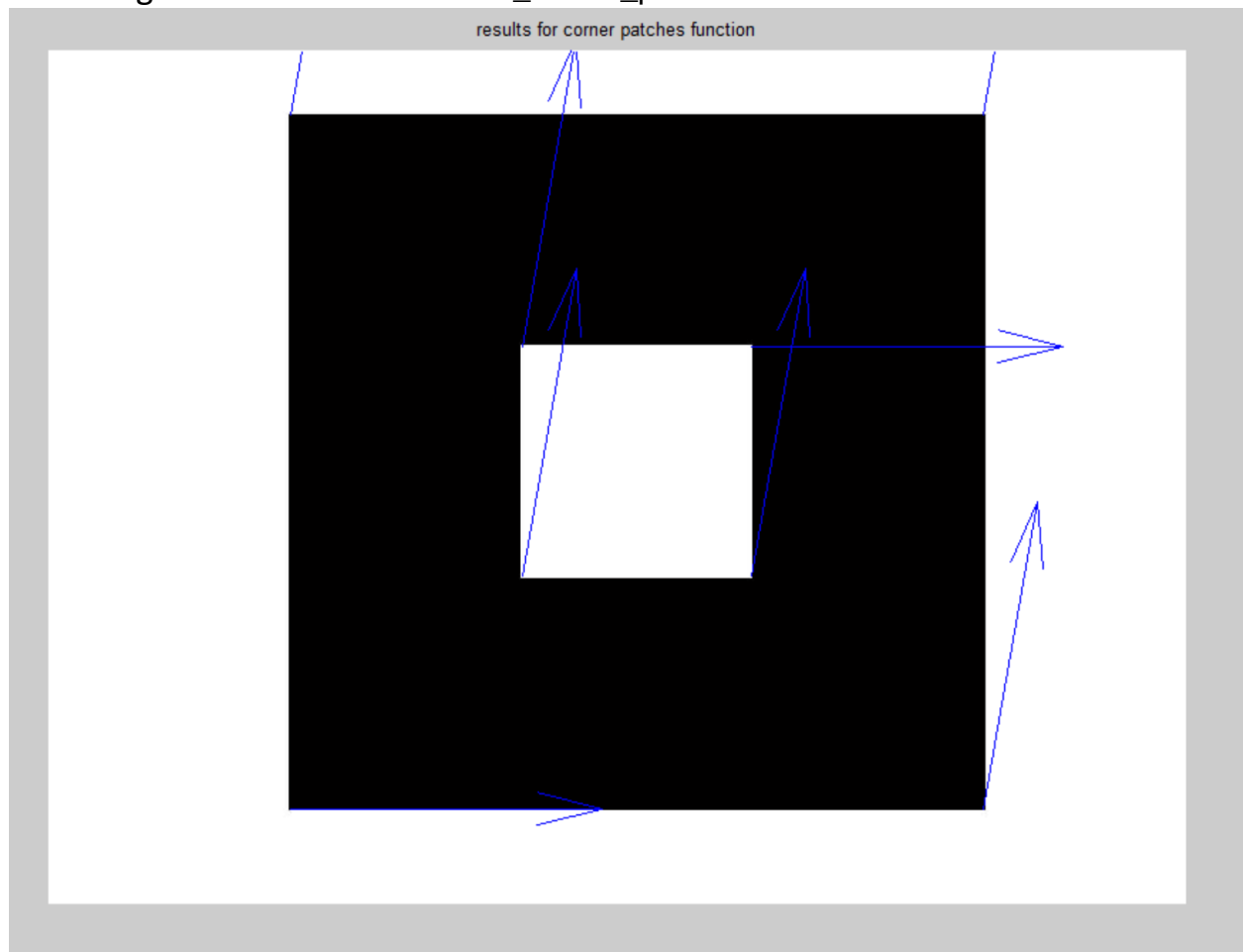
Please note that the combo function is not working fine for me since my matlab version is old. I ran this in matlab version 2015 and got the building correctly. Please run my Harris and you will know what I am talking about. I am calling it like this:

```
imoriginal = imread('glass-box.jpg');  
im = imread('glass-box.jpg');  
% imshow(im);  
im = rgb2gray(im);  
R = CS5320_Harris(im,1);  
combo(double(imoriginal), R>max(max(R/25)));  
title('result for Harris corner detection');
```



*Figure 4 Please try to see the red dots on the corner. They there*

Following is the result for CS5320\_corner\_patches:



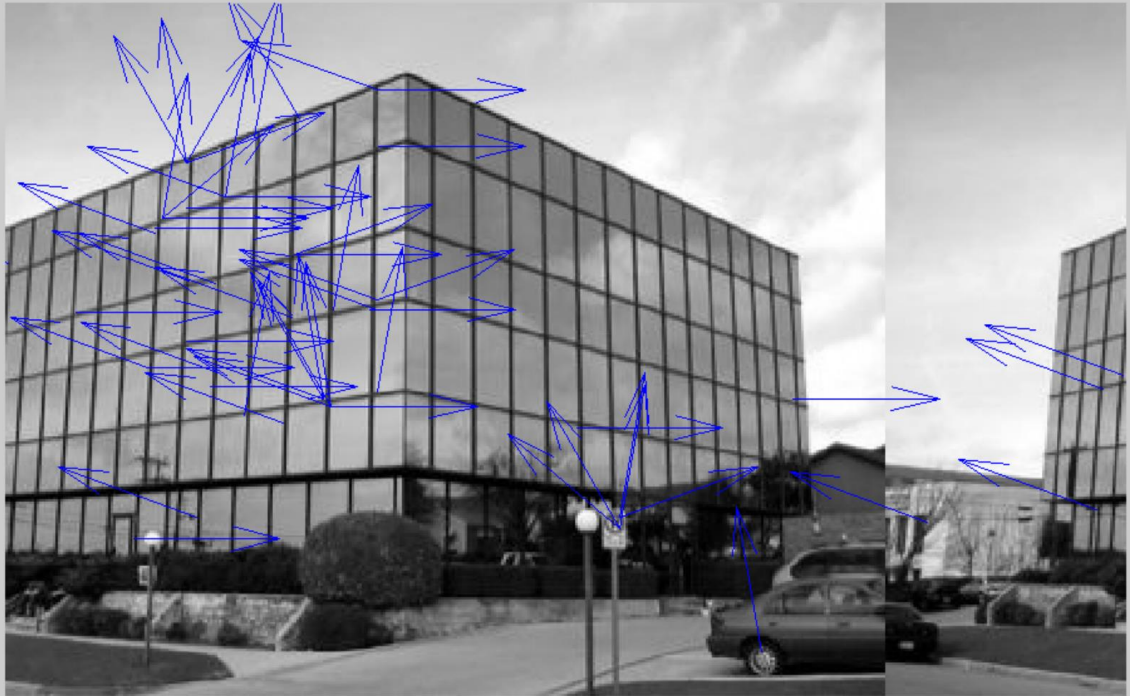
## Section 5: Analysis:

Now we will see the results for translation, rotation and scaling for CS5320\_corner\_patches function

1) Translation

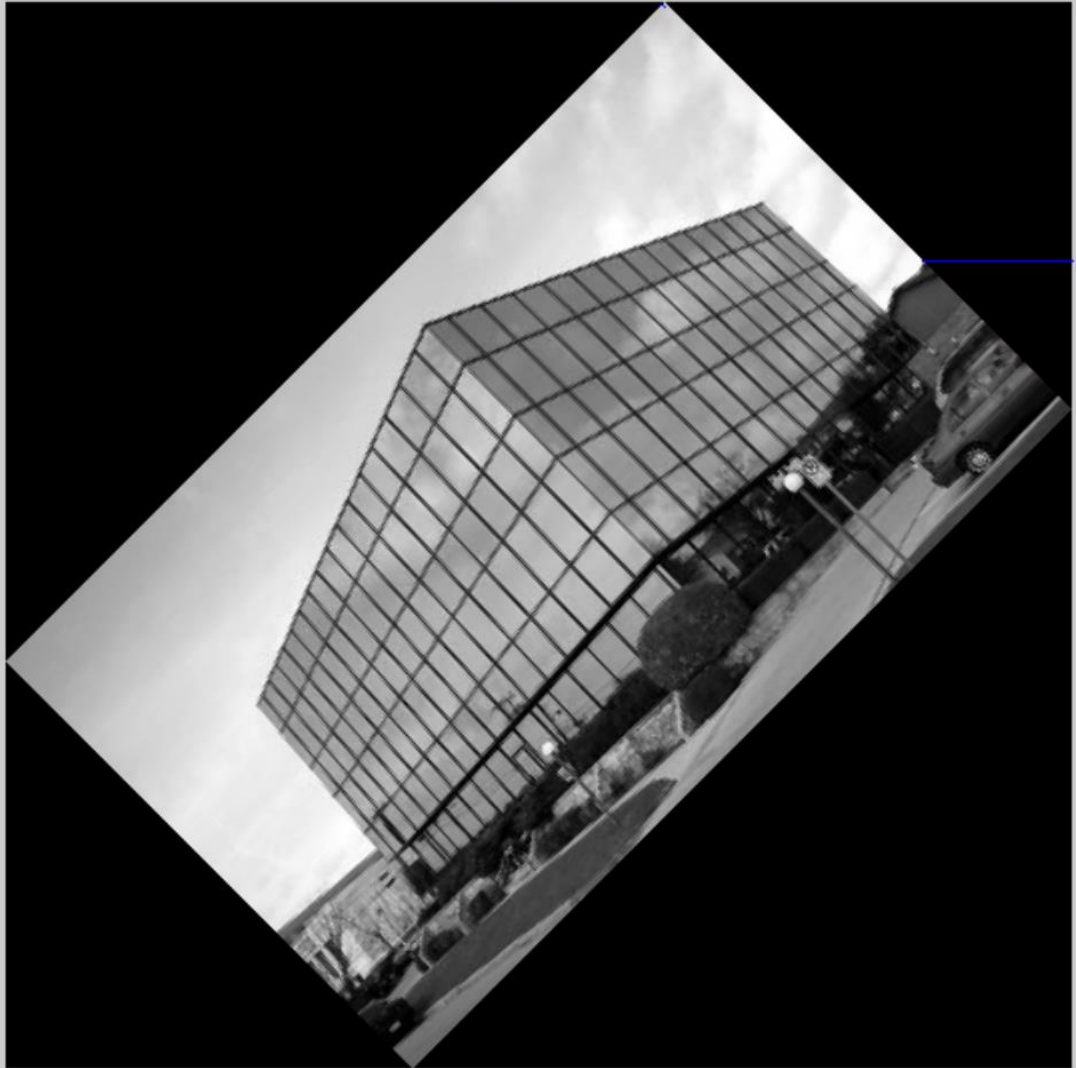


Results for algo 5.3 after translation



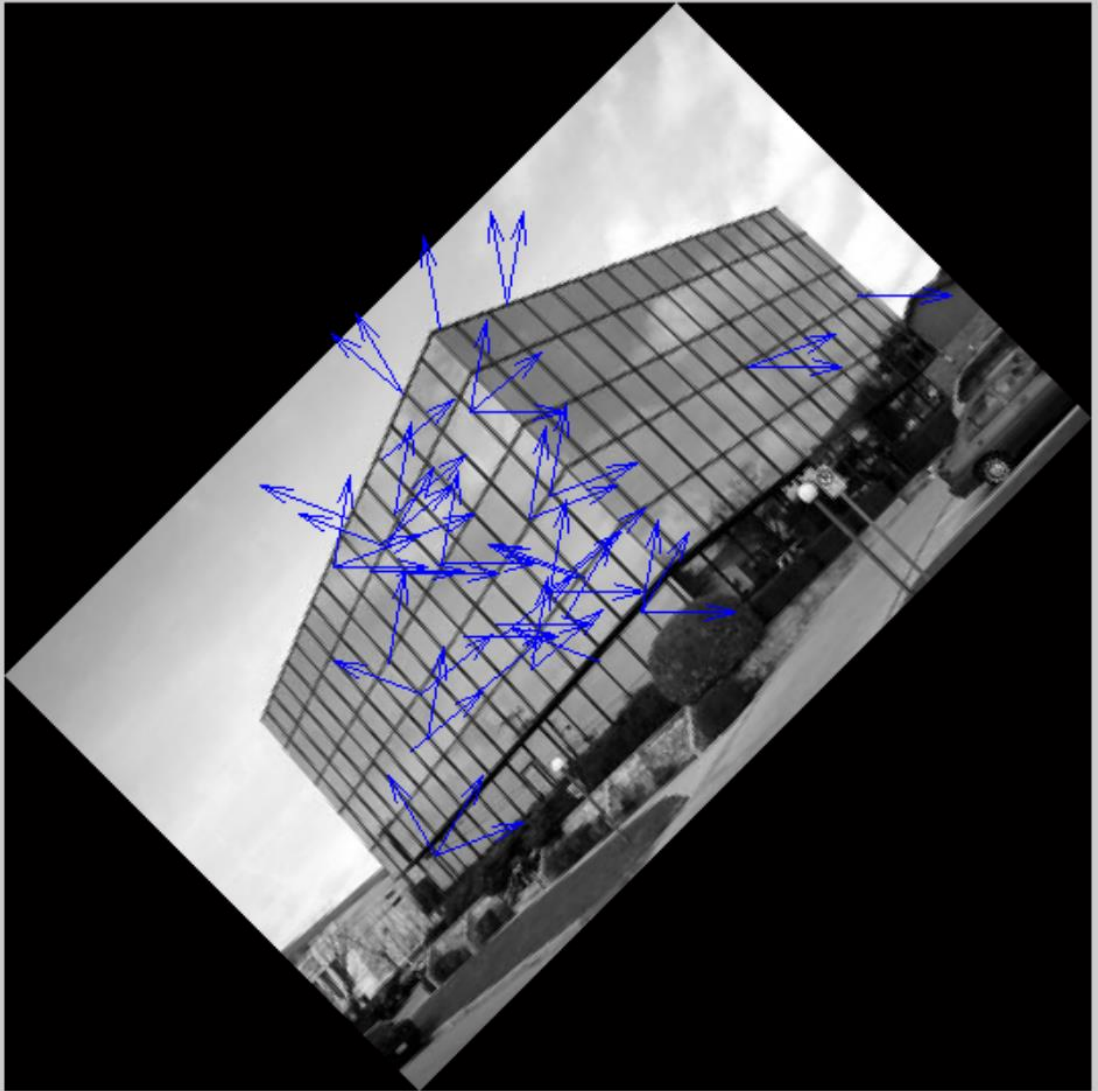
## 2) Rotation

Results for algo 5.2 after rotation

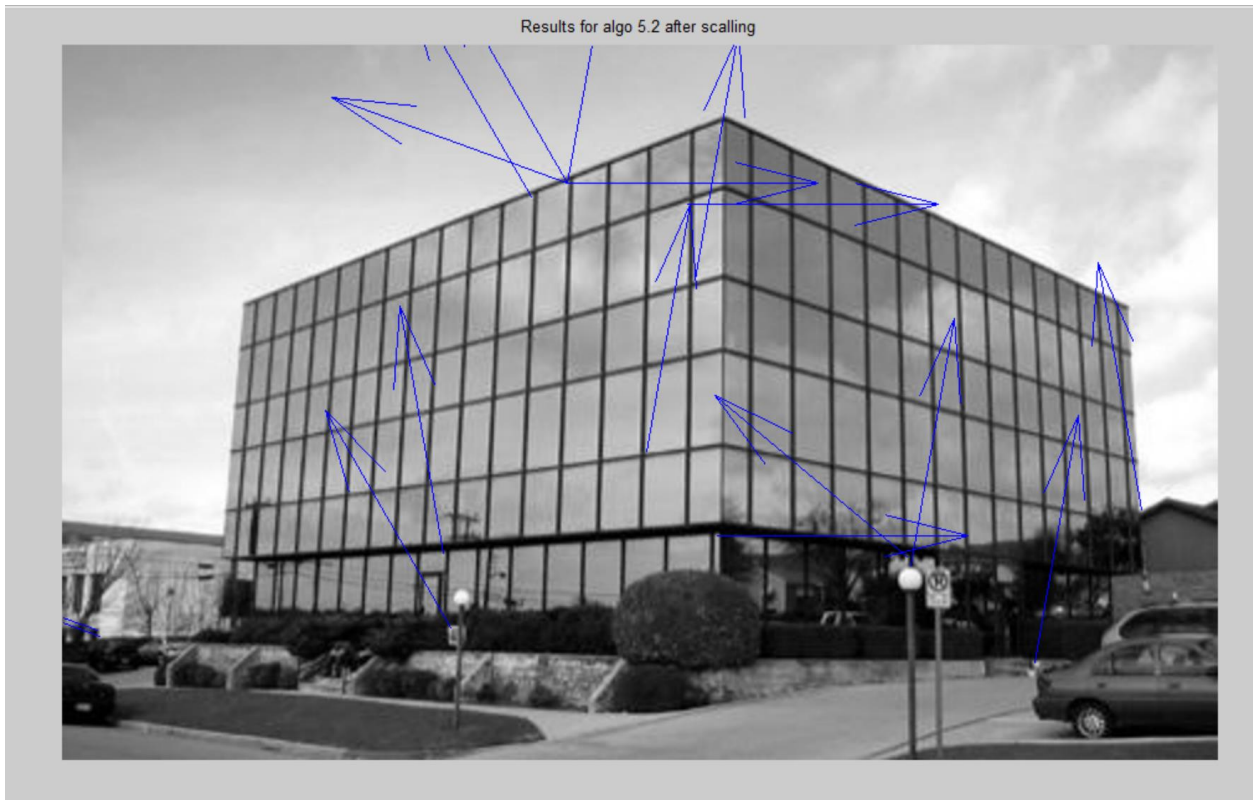




Results for algo 5.3 after rotation



### 3) Scaling



### Section 6: Interpretation:

The following are my observations:

- Orientation proved to be a powerful method for corner recognition
- Harris detection, although powerful, solely cannot be used for corner detection and getting orientation
- Both algo 5.2 and 5.3 are able to give me good number of corner points. But what I observed is that in algo 5.3, I can more flexibly choose the number of points that I want by playing around with  $p$ .
- **However, Algo 5.3 took more time to run.**
- Square image takes more time to run.
- **Translation and rotation are stable with algorithm 5.3**
- **Scaling is stable with algo 5.2. Scaling for algo 5.3 is giving not so good results**(infact it is causing dynamic runtime problems). This makes me sceptical whether algo 5.3 actually is stable with a scaled image or not. This question is still unanswered from my observations.

## **Section 7: Critique:**

The experiment could be improved by following ways:

- Implement my own local maxima function
- Couldn't get my algo 5.3 to properly work for a scaled image.

## **Section 8: log**

18 hours total