



*Islamic University – Gaza*  
*Engineering Faculty*  
*Department of Computer Engineering*  
*ECOM 5060: Compiler Design Discussion*



# Chapter 3

## Lexical Analysis

(Sections 3.6 and 3.7)



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Exercise 3.6.3: For the NFA of Fig. 3.29, indicate all the paths labeled  $aabb$ . Does the NFA accept  $aabb$ ?

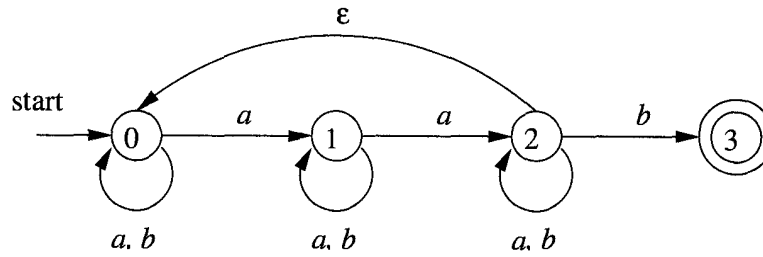


Figure 3.29: NFA for Exercise 3.6.3

$0 \xrightarrow{a} 1 \xrightarrow{a} 2 \xrightarrow{b} 2 \xrightarrow{b} 3$   
 $0 \xrightarrow{a} 0 \xrightarrow{a} 0 \xrightarrow{b} 0 \xrightarrow{b} 0$   
 $0 \xrightarrow{a} 0 \xrightarrow{a} 1 \xrightarrow{b} 1 \xrightarrow{b} 1$   
 $0 \xrightarrow{a} 1 \xrightarrow{a} 2 \xrightarrow{b} 2 \xrightarrow{b} 2$

Yes, accepted by the first path.

Exercise 3.6.4: Repeat Exercises 3.6.3 for the NFA of Fig. 3.30.

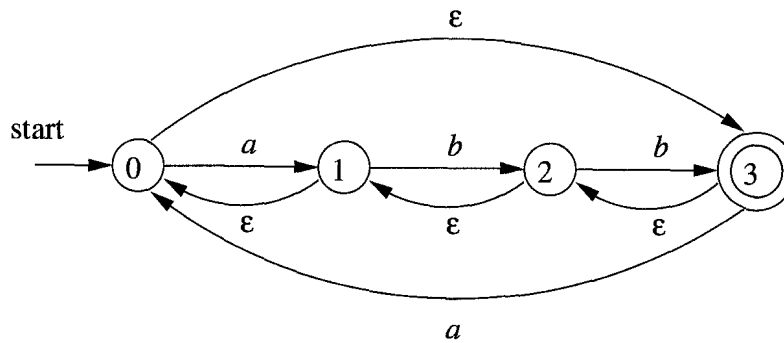


Figure 3.30: NFA for Exercise 3.6.4

$0 \xrightarrow{a} 1 \xrightarrow{\epsilon} 0 \xrightarrow{a} 1 \xrightarrow{b} 2 \xrightarrow{b} 3$   
 $0 \xrightarrow{\epsilon} 3 \xrightarrow{a} 0 \xrightarrow{a} 1 \xrightarrow{b} 2 \xrightarrow{b} 3$   
 $0 \xrightarrow{a} 1 \xrightarrow{\epsilon} 0 \xrightarrow{a} 1 \xrightarrow{b} 2 \xrightarrow{\epsilon} 1 \xrightarrow{b} 2$   
 $0 \xrightarrow{\epsilon} 3 \xrightarrow{a} 0 \xrightarrow{a} 1 \xrightarrow{b} 2 \xrightarrow{\epsilon} 1 \xrightarrow{b} 2$

Yes, accepted by the first or the second paths.

Exercise 3.6.5: Give the transition tables for the NFA of:  
a) Exercise 3.6.3

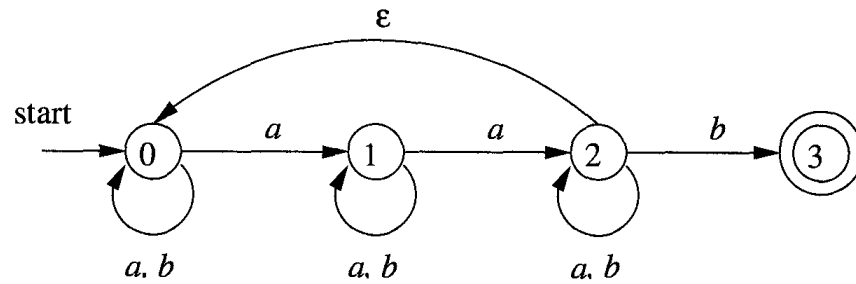


Figure 3.29: NFA for Exercise 3.6.3

state	a	b	$\epsilon$
0	{0, 1}	{0}	$\emptyset$
1	{1, 2}	{1}	$\emptyset$
2	{2}	{2, 3}	{0}
3	$\emptyset$	$\emptyset$	$\emptyset$

b) Exercise 3.6.4

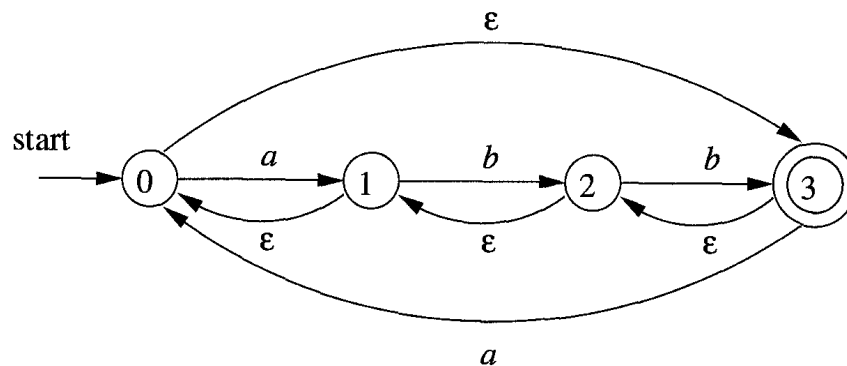
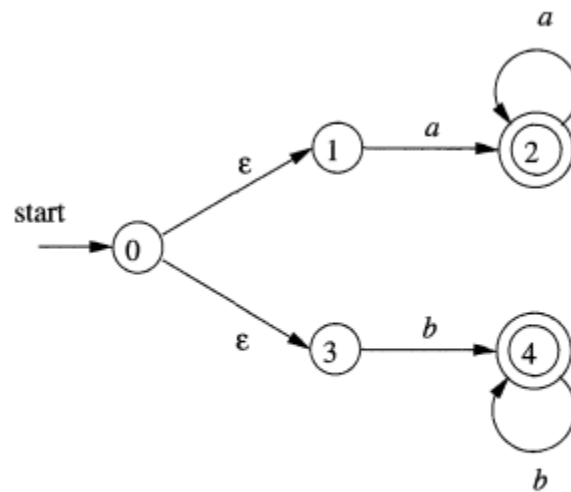


Figure 3.30: NFA for Exercise 3.6.4

state	a	b	$\epsilon$
0	{1}	$\emptyset$	{3}
1	$\emptyset$	{2}	{0}
2	$\emptyset$	{3}	{1}
3	{0}	$\emptyset$	{2}

c) Figure 3.26

Figure 3.26: NFA accepting  $aa^*|bb^*$ 

state	a	b	$\epsilon$
0	$\emptyset$	$\emptyset$	$\{1, 3\}$
1	$\{2\}$	$\emptyset$	$\emptyset$
2	$\{2\}$	$\emptyset$	$\emptyset$
3	$\emptyset$	$\{4\}$	$\emptyset$
4	$\emptyset$	$\{4\}$	$\emptyset$

Exercise 3.7.1: Convert to DFA's the NFA's of:

a) Fig. 3.26

$\epsilon$ -closure(0) = {0, 1, 3} = A

move(A, a) = {2}  $\rightarrow$   $\epsilon$ -closure(move(A, a)) = {2} = B

move(A, b) = {4}  $\rightarrow$   $\epsilon$ -closure(move(A, b)) = {4} = C

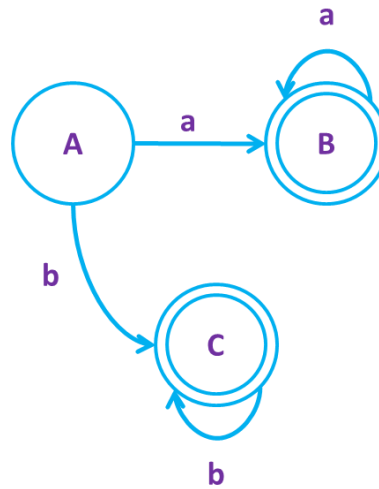
move(B, a) = {2}  $\rightarrow$   $\epsilon$ -closure(move(B, a)) = {2} = B

move(B, b) =  $\emptyset \rightarrow \epsilon$ -closure(move(B, b)) =  $\emptyset$

move(C, a) =  $\emptyset \rightarrow \epsilon$ -closure(move(C, a)) =  $\emptyset$

move(C, b) = {4}  $\rightarrow$   $\epsilon$ -closure(move(C, b)) = {4} = C

NFA state	DFA state	a	b
{0, 1, 3}	A	B	C
{2}	B	B	$\emptyset$
{4}	C	$\emptyset$	C



c) Fig. 3.30

$\epsilon\text{-closure}(0) = \{0, 1, 2, 3\} = A$

$\text{move}(A, a) = \{0, 1\} \rightarrow \epsilon\text{-closure}(\text{move}(A, a)) = \{0, 1, 2, 3\} = A$

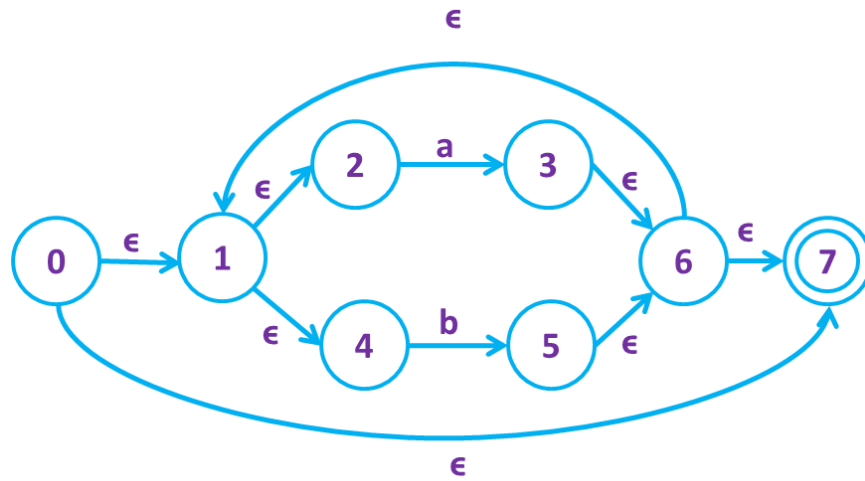
$\text{move}(A, b) = \{2, 3\} \rightarrow \epsilon\text{-closure}(\text{move}(A, b)) = \{0, 1, 2, 3\} = A$

NFA state	DFA state	a	b
$\{0, 1, 2, 3\}$	A	A	A



Exercise 3.7.3: Convert the following regular expressions to deterministic finite automata, using algorithms 3.23 and 3.20:

a)  $(a|b)^*$ .



$\epsilon$ -closure(0) = {0, 1, 2, 4, 7} = A

move(A, a) = {3}  $\rightarrow$   $\epsilon$ -closure(move(A, a)) = {1, 2, 3, 4, 6, 7} = B

move(A, b) = {5}  $\rightarrow$   $\epsilon$ -closure(move(A, b)) = {1, 2, 4, 5, 6, 7} = C

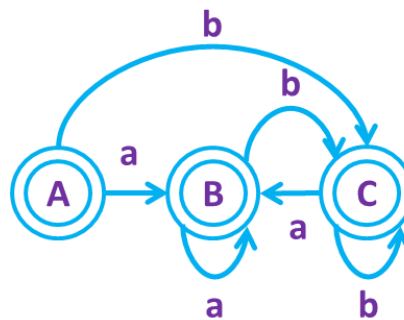
move(B, a) = {3}  $\rightarrow$   $\epsilon$ -closure(move(B, a)) = {1, 2, 3, 4, 6, 7} = B

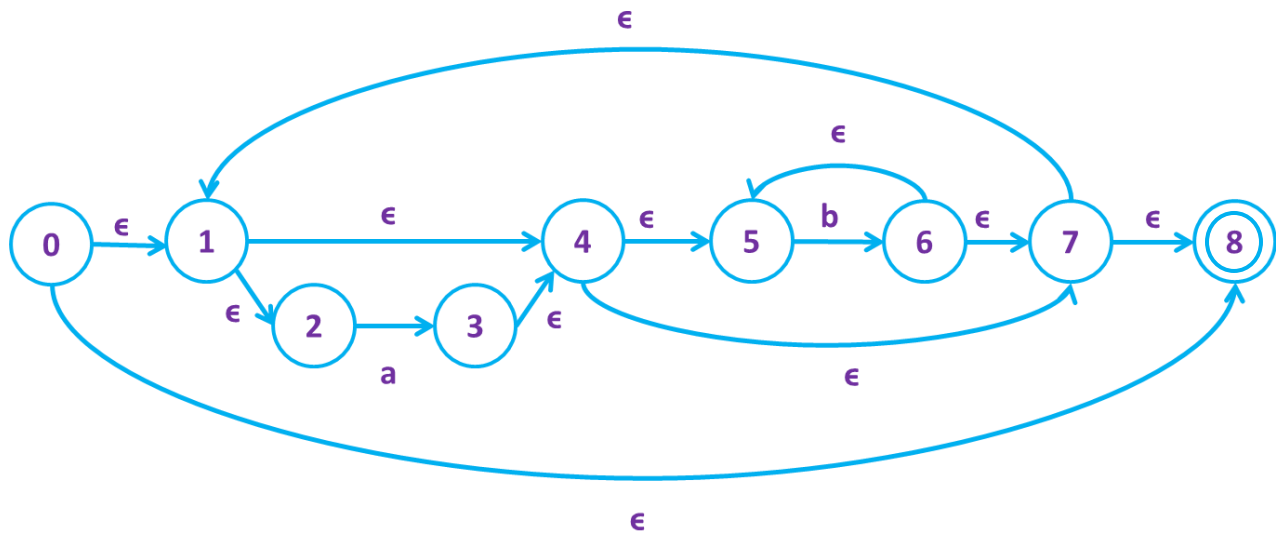
move(B, b) = {5}  $\rightarrow$   $\epsilon$ -closure(move(B, b)) = {1, 2, 4, 5, 6, 7} = C

move(C, a) = {3}  $\rightarrow$   $\epsilon$ -closure(move(C, a)) = {1, 2, 3, 4, 6, 7} = B

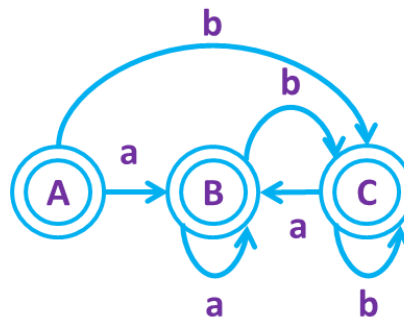
move(C, b) = {5}  $\rightarrow$   $\epsilon$ -closure(move(C, b)) = {1, 2, 4, 5, 6, 7} = C

NFA state	DFA state	a	b
{0, 1, 2, 4, 7}	A	B	C
{1, 2, 3, 4, 6, 7}	B	B	C
{1, 2, 4, 5, 6, 7}	C	B	C



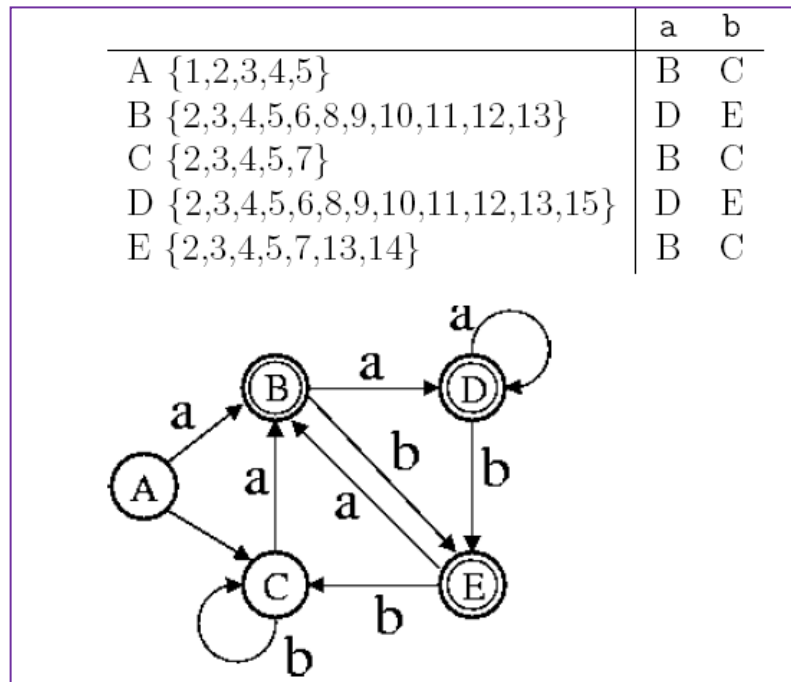
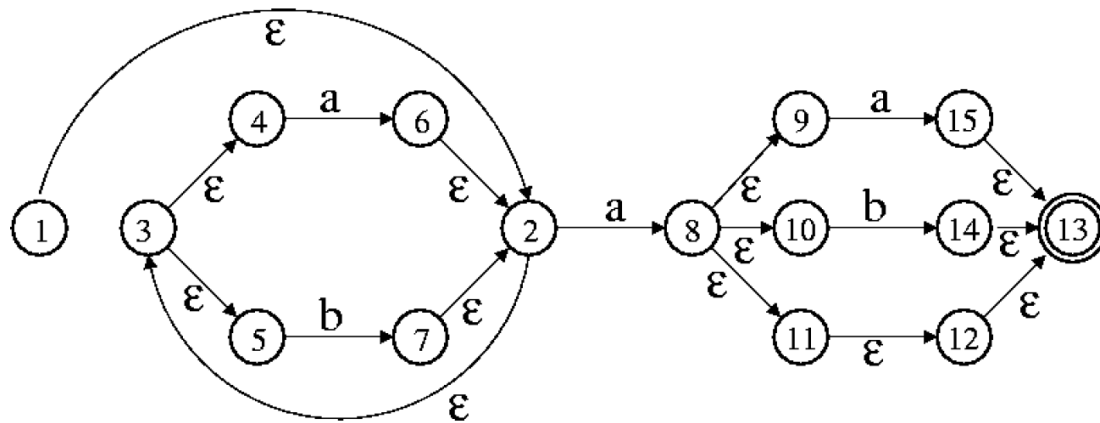
c)  $((\epsilon|a)b^*)^*$ .
 $\epsilon\text{-closure}(0) = \{0, 1, 2, 4, 5, 7, 8\} = A$ 
 $\text{move}(A, a) = \{3\} \rightarrow \epsilon\text{-closure}(\text{move}(A, a)) = \{1, 2, 3, 4, 5, 7, 8\} = B$ 
 $\text{move}(A, b) = \{6\} \rightarrow \epsilon\text{-closure}(\text{move}(A, b)) = \{1, 2, 4, 5, 6, 7, 8\} = C$ 
 $\text{move}(B, a) = \{3\} \rightarrow \epsilon\text{-closure}(\text{move}(B, a)) = \{1, 2, 3, 4, 5, 7, 8\} = B$ 
 $\text{move}(B, b) = \{6\} \rightarrow \epsilon\text{-closure}(\text{move}(B, b)) = \{1, 2, 4, 5, 6, 7, 8\} = C$ 
 $\text{move}(C, a) = \{3\} \rightarrow \epsilon\text{-closure}(\text{move}(C, a)) = \{1, 2, 3, 4, 5, 7, 8\} = B$ 
 $\text{move}(C, b) = \{6\} \rightarrow \epsilon\text{-closure}(\text{move}(C, b)) = \{1, 2, 4, 5, 6, 7, 8\} = C$ 

NFA state	DFA state	a	b
$\{0, 1, 2, 4, 5, 7, 8\}$	A	B	C
$\{1, 2, 3, 4, 5, 7, 8\}$	B	B	C
$\{1, 2, 4, 5, 6, 7, 8\}$	C	B	C



## Midterm Exam 2011-2012 - Problem 4:

Construct the DFA from the following NFA



☺ Best Wishes ☺